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In [1]: import numpy as np
import matplotlib.pyplot as plt
import scipy.stats as sps
import math
%matplotlib inline
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In [4]: z = sps.norm.ppf(0.5 + 0.95/2.0)
sigm2 = 1 / (4 * z**2)
```

$\theta \sim \mathcal{N}(a, \sigma^2)$

положим $a = 0$, найдем σ

$P(\frac{-0.5}{\sigma} < \frac{\theta}{\sigma} < \frac{0.5}{\sigma}) = 0.95$

$P(-z < \frac{\theta}{\sigma} < z) = 0.95$, где z - квантиль уровня $0.5 + \frac{0.95}{2}$

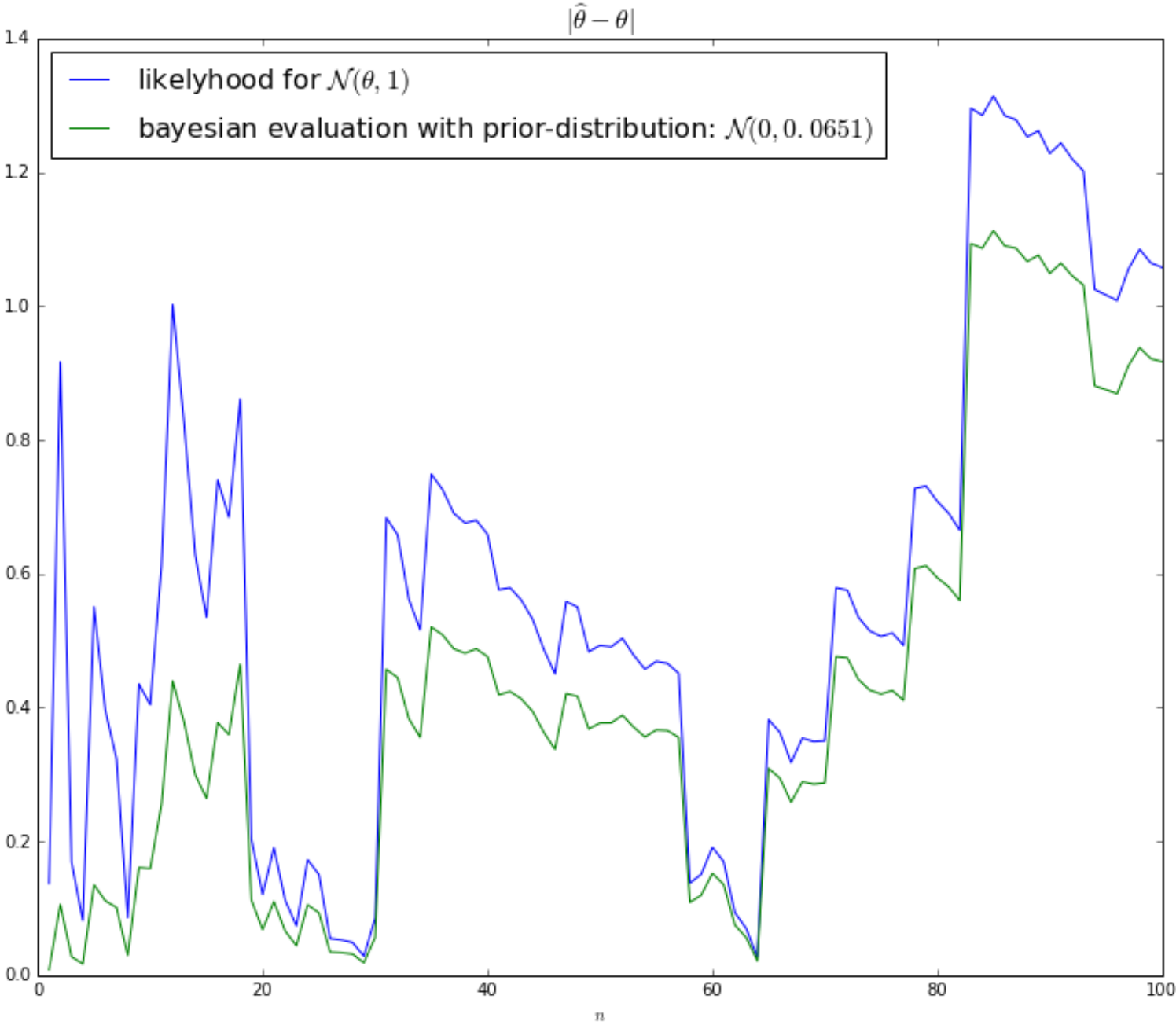
Получим $\frac{0.5}{\sigma} = z \implies \sigma = \frac{1}{2z} \implies \sigma^2 = \frac{1}{4z^2}$

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In [6]: N = 100
smp_cov = 1
sample = sps.cauchy.rvs(size=N)
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In [9]: def get_bayesian_mean_evaluation(X, prior_params) :
    pr_mean,pr_cov = prior_params
    return (pr_mean/pr_cov + np.sum(X)/smp_cov)/(1/pr_cov + len(X)/smp_cov)
```

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In [36]: n = np.arange(1,101,1)
likelihood_mean_evl = [abs(sample[0:k].mean()) for k in n]
bayesian_mean_evl = [abs(get_bayesian_mean_evaluation(
    sample[0:k],(0,sigm2)))
    for k in n]
```

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In [37]: bayes_label = 'bayesian evaluation with prior-distribution: '\
    + r'\mathcal{N}(0,' + str(round(sigm2,4)) + r')$'
likelihood_label = r'likelihood for $\mathcal{N}(\theta,1)$'
plt.figure(figsize=(12,10))
plt.title(r'$|\widehat{\theta} - \theta|$', fontsize=16)
plt.xlabel(r'$n$')
plt.plot(n,likelihood_mean_evl,label = likelihood_label)
plt.plot(n,bayesian_mean_evl, label = bayes_label)
plt.legend(loc = 'best',fontsize=16)
plt.show()
```



По графику видно, что байесовская оценка немного лучше оценки максимального правдоподобия, но ни одна из оценок не сходится.