Your title goes here

Your name goes here

School of Mathematics and Statistics University of Sheffield



Dissertation submitted as part of the requirements for the award of MSc in Statistics, University of Sheffield, 2021–2022

Contents

A	cknowledgements	i
La	ay Summary of the Dissertation	iii
1	Introduction	1
2	Some reminders 2.1 A key theorem	3 3 4
\mathbf{A}	Review of probability calculus A.1 Functions of random variables	7 7 7
В	Some technical proofs B.1 Proof 1	9
\mathbf{C}	Research Ethics Approval	11

Acknowledgements

I would like to thank \dots

Lay Summary of the Dissertation

Please provide here a summary of your dissertation aimed at a lay reader i.e. someone with a good general education, but no university level training in mathematics or statistics. It should summarise the content, method and results and be one to two pages in length. If in doubt about the content or style of this chapter, please consult your Dissertation Support Worker.

Chapter 1

Introduction

You can call your first chapter (and all the others) whatever you wish, but it is usual to start with an introduction to your project and, perhaps, a discussion of some background literature.

When you are discussing other people's work, you might find the following snippets of LaTeX helpful. You might make references like these if you want to discuss the work of Lambert et al. (2005) and Dellaportas et al. (2000) within a sentence. Then, later, you might also want to make some parenthetic references to support an argument that you are making, like this (Lambert et al., 2005). Alternatively, we might want to say that in 2005 a key paper was published by Lambert et al. in which they demonstrated that ...

In the next chapter, we provide some more snippets that you might find useful. We do not give advice about the structure of the dissertation here, since that is covered in the separate document on Dissertation Expectations (on Blackboard), but do remember the very strict page limit of 70 pages in the \mainmatter of your dissertation. Those working on theoretical topics, with little need for figures and tables in their dissertation, should aim for considerably fewer than 70 pages (typically 30–50). If you do submit something longer, examiners will read only the first 70 pages (or 50 pages of more theoretical material). Note too that, regardless of length, any material in appendices will only be inspected cursorily by examiners. You should thus use appendices judiciously.

Chapter 2

Some reminders

For all the basics of typesetting, that you are likely to need in your dissertation, please use the handouts on LaTeX that you were given earlier in the MSc or consult or the single document on LaTeX provided on the dissertation Blackboard page. Below we provide further snippets of code, inspired by the Wikipedia entry on Lévy's continuity theorem, to remind you of some key typesetting concepts that you should be aware of.

Before we do that, however, just a quick note on editing and commenting on your writing. First, you might find the online LaTeX editor called Overleaf helpful for working on your dissertation and sharing it with your Support Worker. Instructions for using Overleaf in this way are provided on Blackboard. Second, note that we have defined some extra LaTeX commands within this template to help when discussing your writing with others. You are not required to use these commands, but we hope that you (and the staff working with you) might find them useful.

SUPERVISOR: This is a comment on the student's work by the supervisor.

DSW: This is a comment on the student's work by the DSW.

YOUR NAME GOES HERE: This is a query related to the above comment.

2.1 A key theorem

Later we will find it useful to remember Lévy's continuity theorem (Theorem 2.1.1), which we do not prove since it is fairly well known, but complete proofs are available in Williams (1991, section 18.1) and Fristedt and Gray (1996, Theorems 14.15 and 18.21).

Theorem 2.1.1 Suppose we have

- a sequence of random variables $\{X_n\}_{n=1}^{\infty}$, not necessarily sharing a common probability space,
- the sequence of corresponding characteristic functions $\{\varphi_n\}_{n=1}^{\infty}$, which by definition are:

$$\varphi_n(t) = \mathbf{E} e^{itX_n} \quad \forall t \in \mathbb{R}, \ \forall n \in \mathbb{N},$$

where E is the expected value operator.

If the sequence of characteristic functions converges pointwise to some function φ where

$$\varphi_n(t) \to \varphi(t) \quad \forall t \in \mathbb{R},$$

then the following statements become equivalent:

• X_n converges in distribution to some random variable X:

$$X_n \xrightarrow{\mathcal{D}} X$$

i.e. the cumulative distribution functions corresponding to random variables converge at every continuity point of the c.d.f. of X;

• $\{X_n\}_{n=1}^{\infty}$ is tight:

$$\lim_{x \to \infty} \left(\sup_{n} P[|X_n| > x] \right) = 0;$$

- $\varphi(t)$ is a characteristic function of some random variable X;
- $\varphi(t)$ is a continuous function of t;
- $\varphi(t)$ is continuous at t=0.

2.2 Another section

It is often useful to refer the reader to a figure, such as Figure 2.1, and you could use a similar \label and \ref technique for refering to chapters (such as Chapter 1), sections (such as Section 2.1), Appendices (like Appendices A, B and C), as well as for tables.

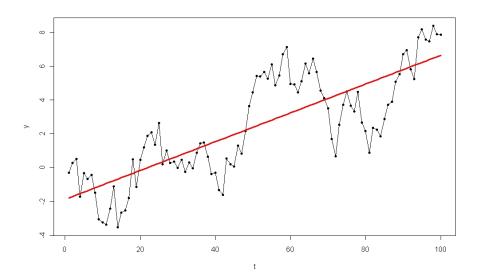


Figure 2.1: Here is a horrible figure. Note the variable names in the axis labels and the rather small tick mark labels. You must not make these mistakes in the plots for your own dissertation. Remember too the Caption Test from the EDA with R lecture notes.

Appendix A

Review of probability calculus

Use appendicies only for material that is directly relevant to the contents of your dissertation and is referenced from within it. Never use it for code or for things that you found interesting, but did not in the end use for your own work. If you and your supervisor agree that providing examiners with code is essential then please deposit it online (via a service such as GitHub).

A.1 Functions of random variables

A.2 Schwarz Inequality

Appendix B

Some technical proofs

B.1 Proof 1

10 B.1. PROOF 1

Appendix C

Research Ethics Approval

The last appendix of the dissertation must contain evidence that you complied with the University of Sheffield research ethics approval process. Like all other appendices, it should be cross-referenced from the main text of the dissertation so that readers are alerted to its presence. The appendix should start with a paragraph of text, in your own words, that summarises the approval process as it applied to your dissertation. Here is an example to get you started.

The research ethics approval process for the work described in this dissertation was completed in March 2019, before any work using data commenced. Due to the use of data arising from <summarise the data collection process here>, formal research ethics approval was deemed to be necessary and, when submitted, the application was allocated reference number: 000094. Formal approval is evidenced here by inclusion of the final approval letter in Figure C.1.



Downloaded: 17/03/2021 Approved: 04/03/2019

Student User

Registration number: 123456789

Example Department Programme: TEST

Dear Student

PROJECT TITLE: Test UG student application **APPLICATION:** Reference Number 000094

On behalf of the University ethics reviewers who reviewed your project, I am pleased to inform you that on 04/03/2019 the above-named project was **approved** on ethics grounds, on the basis that you will adhere to the following documentation that you submitted for ethics review:

• University research ethics application form 000094 (dated 04/03/2019).

If during the course of the project you need to <u>deviate significantly from the above-approved documentation</u> please inform me since written approval will be required.

Yours sincerely

Ethics Admin Ethics Administrator Example Department

Figure C.1: The research ethics approval letter provided for the work outlined in this dissertation, following compliance with the University of Sheffield offical research ethics processes.

References

- Dellaportas, P., Foster, J. J., and Ntzoufras, I. (2000). Bayesian variable selection using the Gibbs sampling. In D. K. Dey, S. K. G. and Mallick, B. K., editors, *Generalized linear models: a Bayesian perspective*, pages 273–286. Marcel Dekker, New York.
- Fristedt, B. E. and Gray, L. F. (1996). A modern approach to probability theory. Birkhäuser Boston.
- Lambert, P. C., Sutton, A. J., Burton, P. R., Abrams, K. R., and Jones, D. R. (2005). How vague is vague? A simulation study of the impact of the use of vague prior distributions in MCMC using WinBUGS. *Statistics in Medicine*, 24:2401–2428.
- Williams, D. (1991). Probability with Martingales. Cambridge University Press.