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1 Basic

1.1 vimrc

```
colo ron
svn on
se ai ar nu rnu
se mouse=a bs=2 ts=4 sw=4 ttm=100
se makeprg=g++\ -Wall\ -Wshadow\ -O2\ -std=c++0x\ -o\
    %<\ %
au BufNewFile *.cpp 0r ~/default.cpp | :1,$-7 fo
filetype indent on
map <F7> <ESC>:wa<CR>:make!<CR>
imap <F7> <ESC>:wa<CR>:make!<CR>
map <F8> :cope <CR>
map <S-F8> :ccl <CR>
map <F9> :!./%< <CR>
map <C-F9> :!./%< < %<.in <CR>>
map <C-F7> <ESC>:tabe %<.in<CR>
```

1.2 Default Code

```
#include < bits / stdc++.h>
#define F first
#define S second
#define PB push_back
#define MP make_pair
#define ALL(x) begin(x),end(x)
#define SZ(x) ((int)(x).size())
#define FZ(n) memset((n),0,sizeof(n))
using namespace std;
typedef long long LL;
typedef double D;
typedef long double LDB;
typedef pair<int, int> PII;
typedef pair<LL, LL> PLL;
#define IOS ios_base::sync_with_stdio(0); cin.tie(0)
int main(){
}
```

Data Structure

2.1 Bigint

```
struct Bigint{
  static const int LEN = 60;
  static const int BIGMOD = 10000;
  int s;
  int v1, v[LEN];
  // vector<int> v;
  Bigint() : s(1) { vl = 0; }
  Bigint(long long a) {
    s = 1; v1 = 0;
if (a < 0) { s = -1; a = -a; }
     while (a) {
      push_back(a % BIGMOD);
       a /= BIGMOD;
    }
  Bigint(string str) {
    s = 1; v1 = 0;
     int stPos = 0, num = 0;
    if (!str.empty() && str[0] == '-') {
      stPos = 1;
       s = -1;
    for (int i=SZ(str)-1, q=1; i>=stPos; i--) {
  num += (str[i] - '0') * q;
  if ((q *= 10) >= BIGMOD) {
         push_back(num);
         num = 0; q = 1;
       }
     if (num) push_back(num);
```

2

```
r.v[i+1] += r.v[i] / BIGMOD;
r.v[i] %= BIGMOD;
  n();
                                                                      }
int len() const {
                                                                    }
  return v1;
                                                                    r.n();
      return SZ(v);
                                                                    return r;
bool empty() const { return len() == 0; }
                                                                  Bigint operator - (const Bigint &b) const {
void push_back(int x) {
                                                                    if (s == -1) return -(-(*this)-(-b));
  v[vl++] = x;
                                                                    if (b.s == -1) return (*this)+(-b);
      v.PB(x);
                                                                    if ((*this) < b) return -(b-(*this));</pre>
                                                                    Bigint r;
void pop_back() {
                                                                    r.resize(len());
for (int i=0; i<len(); i++) {</pre>
 vl--;
       v.pop_back();
                                                                      r.v[i] += v[i];
                                                                      if (i < b.len()) r.v[i] -= b.v[i];</pre>
                                                                      if (r.v[i] < 0) {
   r.v[i] += BIGMOD;</pre>
int back() const {
  return v[vl-1];
        return v.back();
                                                                         r.v[i+1]--;
                                                                      }
void n() {
                                                                    }
  while (!empty() && !back()) pop_back();
                                                                    r.n();
                                                                    return r;
void resize(int nl) {
  v1 = n1;
                                                                  Bigint operator * (const Bigint &b) {
  fill(v, v+vl, 0);
                                                                    Bigint r;
         v.resize(nl);
                                                                    r.resize(len() + b.len() + 1);
                                                                    r.s = s * b.s;
         fill(ALL(v), 0);
                                                                    for (int i=0; i<len(); i++) {</pre>
                                                                      for (int j=0; j<b.len(); j++) {
  r.v[i+j] += v[i] * b.v[j];</pre>
void print() const {
                                                                         if(r.v[i+j] >= BIGMOD) {
  if (empty()) { putchar('0'); return; }
  if (s == -1) putchar('-');
printf("%d", back());
                                                                           r.v[i+j+1] += r.v[i+j] / BIGMOD;
                                                                           r.v[i+j] %= BIGMOD;
  for (int i=len()-2; i>=0; i--) printf("%.4d",v[i]);
                                                                      }
friend std::ostream& operator << (std::ostream& out,</pre>
                                                                    }
    const Bigint &a) {
                                                                    r.n();
  if (a.empty()) { out << "0"; return out; }
if (a.s == -1) out << "-";</pre>
                                                                    return r;
  out << a.back();</pre>
                                                                  Bigint operator / (const Bigint &b) {
  for (int i=a.len()-2; i>=0; i--) {
                                                                    Bigint r:
    char str[10];
                                                                    r.resize(max(1, len()-b.len()+1));
    snprintf(str, 5, "%.4d", a.v[i]);
                                                                    int oriS = s;
    out << str;
                                                                    Bigint b2 = b; // b2 = abs(b)
                                                                    s = b2.s = r.s = 1;
                                                                    for (int i=r.len()-1; i>=0; i--) {
  return out;
                                                                      int d=0, u=BIGMOD-1;
                                                                       while(d<u) {</pre>
int cp3(const Bigint &b)const {
                                                                         int m = (d+u+1)>>1;
  if (s != b.s) return s - b.s;
if (s == -1) return -(-*this).cp3(-b);
                                                                         r.v[i] = m;
                                                                         if((r*b2) > (*this)) u = m-1;
  if (len() != b.len()) return len()-b.len();//int
                                                                         else d = m;
  for (int i=len()-1; i>=0; i--)
                                                                      }
    if (v[i]!=b.v[i]) return v[i]-b.v[i];
                                                                      r.v[i] = d;
  return 0;
                                                                    }
}
                                                                    s = oriS;
                                                                    r.s = s * b.s;
bool operator < (const Bigint &b)const{ return cp3(b)</pre>
                                                                    r.n();
     <0; }
                                                                    return r;
bool operator <= (const Bigint &b)const{ return cp3(b</pre>
                                                                  Bigint operator % (const Bigint &b) {
    )<=0; }
                                                                    return (*this)-(*this)/b*b;
bool operator == (const Bigint &b)const{ return cp3(b
    )==0; }
bool operator != (const Bigint &b)const{ return cp3(b
    )!=0; }
bool operator > (const Bigint &b)const{ return cp3(b)
    >0; }
                                                                2.2
                                                                      unordered map
bool operator >= (const Bigint &b)const{ return cp3(b
    )>=0: }
                                                                struct Key {
Bigint operator - () const {
                                                                  int first, second;
  Bigint r = (*this);
                                                                  Key () {}
  r.s = -r.s:
                                                                  Key (int _x, int _y) : first(_x), second(_y) {}
bool operator == (const Key &b) const {
  return r;
                                                                    return tie(F,S) == tie(b.F,b.S);
Bigint operator + (const Bigint &b) const {
                                                                  }
  if (s == -1) return -(-(*this)+(-b));
if (b.s == -1) return (*this)-(-b);
                                                               };
                                                                struct KeyHasher {
  Bigint r;
                                                                  size_t operator()(const Key& k) const {
  int nl = max(len(), b.len());
                                                                    return k.first + k.second*100000;
  r.resize(nl + 1);

for (int i=0; i<nl; i++) {
                                                               };
    if (i < len()) r.v[i] += v[i];</pre>
    if (i < b.len()) r.v[i] += b.v[i];</pre>
                                                                typedef unordered_map<Key,int,KeyHasher> map_t;
    if(r.v[i] >= BIGMOD) {
```

```
int main(int argc, char** argv){
   map_t mp;
   for (int i=0; i<10; i++)
        mp[Key(i,0)] = i+1;
   for (int i=0; i<10; i++)
        printf("%d\n", mp[Key(i,0)]);
   return 0;
}</pre>
2.3 extc_heap
```

```
#include <bits/extc++.h>
         _gnu_pbds::priority_queue<<mark>int</mark>> heap_t;
heap_t a,b;
int main() {
  a.clear();
  b.clear();
  a.push(1);
  a.push(3);
  b.push(2);
  b.push(4);
  assert(a.top() == 3);
 assert(b.top() == 4);
 // merge two heap
 a.join(b);
  assert(a.top() == 4);
  assert(b.empty());
  return 0;
```

2.4 extc balance tree

```
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
using namespace std;
using namespace __gnu_pbds;
typedef tree<int,null_type,less<int>,rb_tree_tag,
    tree_order_statistics_node_update> set_t;
typedef cc_hash_table<int,int> umap_t;
int main()
 // Insert some entries into s.
 set t s:
 s.insert(12):
 s.insert(505);
 // The order of the keys should be: 12, 505.
 assert(*s.find_by_order(0) == 12);
 assert(s.find_by_order(2) == end(s));
 // The order of the keys should be: 12, 505.
 assert(s.order_of_key(12) == 0);
 assert(s.order_of_key(505) == 1);
 // Erase an entry.
 s.erase(12);
 // The order of the keys should be: 505.
 assert(*s.find_by_order(0) == 505);
  // The order of the keys should be: 505.
 assert(s.order_of_key(505) == 0);
```

2.5 Disjoint Set

```
struct DisjointSet {
   // save() is like recursive
   // undo() is like return
   int n, fa[MXN], sz[MXN];
   vector<pair<int*,int>> h;
   vector<int> sp;
   void init(int tn) {
     n=tn;
     for (int i=0; i<n; i++) {</pre>
```

```
fa[i]=i:
        sz[i]=1;
     sp.clear(); h.clear();
   void assign(int *k, int v) {
     h.PB({k, *k});
     *k=v;
   void save() { sp.PB(SZ(h)); }
   void undo() {
     assert(!sp.empty());
     int last=sp.back(); sp.pop_back();
while (SZ(h)!=last) {
        auto x=h.back(); h.pop_back();
        *x.F=x.S;
     }
   int f(int x) {
     while (fa[x]!=x) x=fa[x];
     return x;
   void uni(int x, int y) {
     x=f(x); y=f(y);
     if (x==y) return
     if (sz[x]<sz[y]) swap(x, y);
assign(&sz[x], sz[x]+sz[y]);</pre>
     assign(&fa[y], x);
}djs;
```

2.6 Treap

cout << t->val;

```
const int MEM = 16000004;
struct Treap {
  static Treap nil, mem[MEM], *pmem;
  Treap *1, *r;
  char val;
  int size;
Treap (): 1(&nil), r(&nil), size(0) {}
Treap (char _val):
    1(&nil), r(&nil), val(_val), size(1) {}
} Treap::nil, Treap::mem[MEM], *Treap::pmem = Treap::
int size(const Treap *t) { return t->size; }
void pull(Treap *t) {
  if (!size(t)) return;
  t\rightarrow size = size(t\rightarrow l) + size(t\rightarrow r) + 1;
Treap* merge(Treap *a, Treap *b) {
  if (!size(a)) return b;
  if (!size(b)) return a;
  Treap *t;
  if (rand() % (size(a) + size(b)) < size(a)) {</pre>
     t = new (Treap::pmem++) Treap(*a);
     t->r = merge(a->r, b);
  } else {
     t = new (Treap::pmem++) Treap(*b);
     t->l = merge(a, b->l);
  pull(t);
  return t;
void split(Treap *t, int k, Treap *&a, Treap *&b) {
  if (!size(t)) a = b = &Treap::nil;
  else if (size(t->1) + 1 <= k) {
     a = new (Treap::pmem++) Treap(*t);
     split(t->r, k - size(t->l) - 1, a->r, b);
     pull(a);
  } else {
     b = new (Treap::pmem++) Treap(*t);
     split(t->1, k, a, b->1);
     pull(b);
}
int nv;
Treap *rt[50005];
void print(const Treap *t) {
  if (!size(t)) return;
  print(t->1);
```

```
print(t->r);
int main(int argc, char** argv) {
  rt[nv=0] = &Treap::nil;
  Treap::pmem = Treap::mem;
  int Q, cmd, p, c, v;
  string s;
  cin >> Q;
  while (Q--) {
   cin >> cmd;
    if (cmd == 1) {
       // insert string s after position p
       cin >> p >> s;
Treap *tl, *tr;
       split(rt[nv], p, tl, tr);
       for (int i=0; i<SZ(s); i++)</pre>
         tl = merge(tl, new (Treap::pmem++) Treap(s[i]))
    rt[++nv] = merge(tl, tr);
} else if (cmd == 2) {
      // remove c characters starting at position
Treap *tl, *tm, *tr;
       cin >> p >> c;
       split(rt[nv], p-1, tl, tm);
split(tm, c, tm, tr);
       rt[++nv] = merge(tl, tr);
    } else if (cmd == 3) {
       // print c characters starting at position p, in
            version v
       Treap *tl, *tm, *tr;
       cin >> v >> p >> c;
       split(rt[v], p-1, tl, tm);
       split(tm, c, tm, tr);
      print(tm);
cout << "\n";</pre>
    }
  return 0;
```

3 Graph

3.1 BCC Edge

```
struct BccEdge {
  static const int MXN = 100005;
  struct Edge { int v,eid; };
  int n,m,step,par[MXN],dfn[MXN],low[MXN];
  vector<Edge> E[MXN];
  DisjointSet djs;
  void init(int _n) {
   n = _n; m = 0;
for (int i=0; i<n; i++) E[i].clear();</pre>
    djs.init(n);
  void add_edge(int u, int v) {
   E[u].PB({v, m});
E[v].PB({u, m});
    m++;
  void DFS(int u, int f, int f_eid) {
    par[u] = f;
    dfn[u] = low[u] = step++;
    for (auto it:E[u]) {
      if (it.eid == f_eid) continue;
      int v = it.v;
      if (dfn[v] == -1) {
        DFS(v, u, it.eid);
        low[u] = min(low[u], low[v]);
      } else
        low[u] = min(low[u], dfn[v]);
      }
   }
  void solve() {
    step = 0;
    memset(dfn, -1, sizeof(int)*n);
    for (int i=0; i<n; i++) {</pre>
      if (dfn[i] == -1) DFS(i, i, -1);
```

```
djs.init(n);
  for (int i=0; i<n; i++) {
    if (low[i] < dfn[i]) djs.uni(i, par[i]);
  }
}
graph;</pre>
```

3.2 BCC Vertex

```
struct BccVertex {
   int n,nBcc,step,root,dfn[MXN],low[MXN];
   vector<int> E[MXN], ap;
   vector<pii> bcc[MXN];
   int top;
   pii stk[MXN];
   void init(int _n) {
    n = _n;
nBcc = step = 0;
     for (int i=0; i<n; i++) E[i].clear();</pre>
   void add_edge(int u, int v) {
     E[u].PB(v);
     E[v].PB(u);
   void DFS(int u, int f) {
     dfn[u] = low[u] = step++;
     int son = 0;
     for (auto v:E[u]) {
       if (v == f) continue;
if (dfn[v] == -1) {
         son++
         stk[top++] = \{u,v\};
         DFS(v,u);
         if (low[v] >= dfn[u]) {
            if(v != root) ap.PB(v);
            do {
              assert(top > 0);
              bcc[nBcc].PB(stk[--top]);
            } while (stk[top] != pii(u,v));
            nBcc++;
         low[u] = min(low[u], low[v]);
         if (dfn[v] < dfn[u]) stk[top++] = pii(u,v);</pre>
         low[u] = min(low[u],dfn[v]);
     if (u == root && son > 1) ap.PB(u);
   // return the edges of each bcc;
   vector<vector<pii>>> solve() {
     vector<vector<pii>>> res;
for (int i=0; i<n; i++) {</pre>
       dfn[i] = low[i] = -1;
     ap.clear();
     for (int i=0; i<n; i++) {</pre>
       if (dfn[i] == -1) {
         top = 0;
         root = i;
         DFS(i,i);
     REP(i,nBcc) res.PB(bcc[i]);
     return res;
  }
}graph;
```

3.3 Strongly Connected Components

```
struct Scc{
  int n, nScc, vst[MXN], bln[MXN];
  vector<int> E[MXN], rE[MXN], vec;
  void init(int _n){
    n = _n;
    for (int i=0; i<n; i++){
        E[i].clear();
        rE[i].clear();
    }
}
void add_edge(int u, int v){
    E[u].PB(v);</pre>
```

nWa.

```
rE[v].PB(u);
   void DFS(int u){
     vst[u]=1;
     for (auto v : E[u])
       if (!vst[v]) DFS(v);
     vec.PB(u);
   void rDFS(int u){
     vst[u] = 1;
     bln[u] = nScc;
     for (auto v : rE[u])
        if (!vst[v]) rDFS(v);
   void solve(){
     nScc = 0;
     vec.clear();
     for (int i=0; i<n; i++) vst[i] = 0;
for (int i=0; i<n; i++)</pre>
       if (!vst[i]) DFS(i);
     reverse(vec.begin(),vec.end());

for (int i=0; i<n; i++) vst[i] = 0;

for (auto v : vec){
       if (!vst[v]){
          rDFS(v);
          nScc++;
       }
     }
  }
};
```

Maximum Clique

```
class MaxClique {
public:
    static const int MV = 210;
    int V;
    int el[MV][MV/30+1];
    int dp[MV];
    int ans;
    int s[MV][MV/30+1];
    vector<int> sol;
    void init(int v) {
         V = v; ans = 0;
         FZ(el); FZ(dp);
    }
    /* Zero Base */
    void addEdge(int u, int v) {
         if(u > v) swap(u, v);
         if(u == v) return;
         el[u][v/32] = (1<<(v%32));
    bool dfs(int v, int k) {
   int c = 0, d = 0;
   for(int i=0; i<(V+31)/32; i++) {</pre>
             s[k][i] = el[v][i];
             if(k != 1) s[k][i] &= s[k-1][i];
             c += __builtin_popcount(s[k][i]);
         if(c == 0) {
             if(k > ans) {
                  ans = \hat{k};
                  sol.clear();
                  sol.push_back(v);
                  return 1;
             return 0;
         for(int i=0; i<(V+31)/32; i++) {</pre>
             for(int a = s[k][i]; a; d++) {
                  if(k + (c-d) <= ans) return 0;</pre>
                  int lb = a&(-a), lg = 0;
                  a ^= 1b;
                  while(lb!=1) {
                      lb = (unsigned int)(lb) >> 1;
                  int u = i*32 + 1g;
                  if(k + dp[u] <= ans) return 0;</pre>
                  if(dfs(u, k+1)) {
```

```
sol.push_back(v);
                        return 1;
                   }
              }
          return 0;
     int solve() {
          for(int i=V-1; i>=0; i--) {
              `dfs(i, 1);
dp[i] = ans;
          return ans;
     }
};
```

5

3.5MinimumMeanCycle

```
/* minimum mean cycle */
const int MAXE = 1805;
const int MAXN = 35;
const double inf = 1029384756;
const double eps = 1e-6;
struct Edge {
 int v,u;
  double c;
int n,m,prv[MAXN][MAXN], prve[MAXN][MAXN], vst[MAXN];
Edge e[MAXE];
vector<int> edgeID, cycle, rho;
double d[MAXN][MAXN];
inline void bellman_ford()
 d[i+1][u] = d[i][v]+e[j].c;
        prv[i+1][u] = v;
        prve[i+1][u] = j;
      }
  }
double karp_mmc() {
   // returns inf if no cycle, mmc otherwise
  double mmc=inf;
  int st = -1;
  bellman_ford();
  for(int i=0; i<n; i++) {</pre>
    double avg=-inf;
    for(int k=0; k<n; k++) {</pre>
      if(d[n][i]<inf-eps) avg=max(avg,(d[n][i]-d[k][i])</pre>
          /(n-k));
      else avg=max(avg,inf);
    if (avg < mmc) tie(mmc, st) = tie(avg, i);</pre>
  for(int i=0; i<n; i++) vst[i] = 0;</pre>
  edgeID.clear(); cycle.clear(); rho.clear();
  for (int i=n; !vst[st]; st=prv[i--][st]) {
    vst[st]++;
    edgeID.PB(prve[i][st]);
    rho.PB(st);
  while (vst[st] != 2) {
    int v = rho.back(); rho.pop_back();
    cycle.PB(v);
    vst[v]++;
  reverse(ALL(edgeID));
  edgeID.resize(SZ(cycle));
  return mmc;
```

Flow

Dinic 4.1

```
struct Dinic{
  static const int MXN = 10000;
  struct Edge{ int v,f,re; };
  int n,s,t,level[MXN];
  vector<Edge> E[MXN];
  void init(int _n, int _s, int _t){
    n = _n;    s = _s;    t = _t;
    for (int i=0; i<n; i++) E[i].clear();</pre>
  void add_edge(int u, int v, int f){
    E[u].PB((v,f,SZ(E[v]));
    E[v].PB({u,0,SZ(E[u])-1});
  bool BFS(){
    for (int i=0; i<n; i++) level[i] = -1;</pre>
    queue<int> que;
    que.push(s);
    level[s] = 0;
    while (!que.empty()){
      int u = que.front(); que.pop();
       for (auto it : E[u]){
         if (it.f > 0 && level[it.v] == -1){
   level[it.v] = level[u]+1;
           que.push(it.v);
         }
      }
    }
    return level[t] != -1;
  int DFS(int u, int nf){
    if (u == t) return nf;
    int res = 0;
    for (auto &it : E[u]){
       if (it.f > 0 && level[it.v] == level[u]+1){
         int tf = DFS(it.v, min(nf,it.f));
         res += tf; nf -= tf; it.f -= tf;
         E[it.v][it.re].f += tf;
         if (nf == 0) return res;
    if (!res) level[u] = -1;
    return res:
  int flow(int res=0){
    while ( BFS() )
      res += DFS(s,2147483647);
    return res:
}flow;
```

4.2 Cost Flow

```
typedef pair<long long, long long> pll;
struct CostFlow +
  static const int MXN = 205;
  static const long long INF = 102938475610293847LL;
  struct Edge {
    int v, r;
    long long f, c;
  int n, s, t, prv[MXN], prvL[MXN], inq[MXN];
  long long dis[MXN], fl, cost;
  vector<Edge> E[MXN];
  void init(int _n, int _s, int _t) {
    n = _n; s = _s; t = _t;
    for (int i=0; i<n; i++) E[i].clear();</pre>
    fl = cost = 0;
  void add_edge(int u, int v, long long f, long long c)
    E[u].PB({v, SZ(E[v]) , f, c});
E[v].PB({u, SZ(E[u])-1, 0, -c});
  pll flow() {
    while (true) {
  for (int i=0; i<n; i++) {</pre>
         dis[i] = INF;
         inq[i] = 0;
       dis[s] = 0;
       queue<int> que;
       que.push(s);
       while (!que.empty()) {
         int u = que.front(); que.pop();
```

```
inq[u] = 0;
for (int i=0; i<SZ(E[u]); i++) {</pre>
            int v = E[u][i].v;
            long long w = E[u][i].c;
if (E[u][i].f > 0 && dis[v] > dis[u] + w) {
              prv[v] = u; prvL[v] = i;
dis[v] = dis[u] + w;
               if (!inq[v]) {
                 inq[v] = 1;
                 que.push(v);
              }
            }
         }
       if (dis[t] == INF) break;
       long long tf = INF;
       for (int v=t, u, 1; v!=s; v=u) {
         u=prv[v]; l=prvL[v];
          tf = min(tf, E[u][1].f);
       for (int v=t, u, 1; v!=s; v=u) {
         u=prv[v]; l=prvL[v];
E[u][l].f -= tf;
         E[v][E[u][1].r].f += tf;
       cost += tf * dis[t];
       fl += tf;
     return {fl, cost};
}flow;
```

4.3 Maximum Simple Graph Matching

```
struct GenMatch { // 1-base
  static const int MAXN = 514;
  int V;
  bool el[MAXN][MAXN];
  int pr[MAXN];
  bool inq[MAXN],inp[MAXN],inb[MAXN];
  queue<int> qe;
  int st,ed;
  int nb;
  int bk[MAXN],djs[MAXN];
  int ans;
  void init(int _V) {
    V =
    for(int i = 0; i <= V; i++) {
  for(int j = 0; j <= V; j++) el[i][j] = 0;
  pr[i] = bk[i] = djs[i] = 0;
  pr[i] = 0;</pre>
       inq[i] = inp[i] = inb[i] = 0;
    ans = 0;
  void add_edge(int u, int v) {
    el[u][v] = el[v][u] = 1;
  int lca(int u,int v) {
     for(int i = 0; i <= V; i++) inp[i] = 0;</pre>
     while(1) {
       u = djs[u];
       inp[u] = true;
if(u == st) break;
       u = bk[pr[u]];
     while(1) {
      v = djs[v];
       if(inp[v]) return v;
       v = bk[pr[v]];
     return v;
  void upd(int u) {
     while(djs[u] != nb) {
       v = pr[u]
       inb[djs[u]] = inb[djs[v]] = true;
       u = bk[v];
       if(djs[u] != nb) bk[u] = v;
    }
  void blo(int u,int v) {
    nb = lca(u,v);
     for (int i=0; i<=V; i++) inb[i] = 0;</pre>
```

```
upd(u); upd(v);
if(djs[u] != nb) bk[u] = v;
if(djs[v] != nb) bk[v] = u;
                                                                    // Minimum General Weighted Matching (Perfect Match)
                                                                         0-base
                                                                    static const int MXN = 105;
    for(int tu = 1; tu <= V; tu++)</pre>
      if(inb[djs[tu]]) {
                                                                    int n, edge[MXN][MXN];
                                                                    int match[MXN],dis[MXN],onstk[MXN];
         djs[tu] = nb;
         if(!inq[tu]){
                                                                    vector<int> stk;
           qe.push(tu);
           inq[tu] = 1;
                                                                    void init(int _n) {
        }
                                                                       n = _n;
      }
                                                                       for (int i=0; i<n; i++)</pre>
                                                                         for (int j=0; j<n; j++)</pre>
  void flow() {
  for(int i = 1; i <= V; i++) {</pre>
                                                                           edge[i][j] = 0;
      inq[i] = 0;
                                                                    void add_edge(int u, int v, int w) {
      bk[i] = 0;
djs[i] = i;
                                                                       edge[u][v] = edge[v][u] = w;
                                                                    bool SPFA(int u){
                                                                       if (onstk[u]) return true;
                                                                       stk.PB(u);
    while(qe.size()) qe.pop();
                                                                       onstk[u] = 1;
    qe.push(st);
                                                                       for (int v=0; v<n; v++){</pre>
    inq[st] = 1;
                                                                         if (u != v && match[u] != v && !onstk[v]){
    ed = 0;
    while(qe.size()) {
                                                                            int m = match[v];
      int u = qe.front(); qe.pop();
for(int v = 1; v <= V; v++)</pre>
                                                                            if (dis[m] > dis[u] - edge[v][m] + edge[u][v]){
                                                                              dis[m] = dis[u] - edge[v][m] + edge[u][v];
         if(el[u][v] && (djs[u] != djs[v]) && (pr[u] !=
                                                                              onstk[v] = 1;
             v)) {
                                                                              stk.PB(v);
                                                                              if (SPFA(m)) return true;
           if((v == st) || ((pr[v] > 0) && bk[pr[v]] >
                                                                              stk.pop_back();
                0))
             blo(u,v);
                                                                              onstk[v] = 0;
                                                                           }
           else if(bk[v] == 0) {
             bk[v] = u;
                                                                         }
             if(pr[v] > 0) {
               if(!inq[pr[v]]) qe.push(pr[v]);
                                                                       onstk[u] = 0;
                                                                       stk.pop_back();
return false;
             } else {
               ed = v;
                return;
             }
                                                                    int solve() {
          }
        }
                                                                       // find a match
                                                                       for (int i=0; i<n; i+=2){
  match[i] = i+1;</pre>
    }
  void aug() {
                                                                         match[i+1] = i;
    int u,v,w;
                                                                       while (true){
    u = ed;
                                                                         int found = 0;
    while (u > 0) {
                                                                         for (int i=0; i<n; i++)</pre>
      v = bk[u];
      w = pr[v];
                                                                           dis[i] = onstk[i] = 0;
                                                                         for (int i=0; i<n; i++){</pre>
      pr[v] = u;
      pr[u] = v;
                                                                            stk.clear();
                                                                            if (!onstk[i] && SPFA(i)){
      u = w;
                                                                              found = 1:
    }
                                                                              while (SZ(stk)>=2){
  int solve() {
                                                                                int u = stk.back(); stk.pop_back();
    for(int i = 0; i <= V; i++) pr[i] = 0;
for(int u = 1; u <= V; u++)</pre>
                                                                                int v = stk.back(); stk.pop_back();
                                                                                match[u] = v;
                                                                                match[v] = u;
       if(pr[u] == 0) {
         st = u;
         flow();
                                                                           }
         if(ed > 0) {
                                                                         if (!found) break;
           aug();
           ans ++;
                                                                       int ret = 0;
                                                                       for (int i=0; i<n; i++)</pre>
                                                                        ret += edge[i][match[i]];
    return ans;
                                                                       ret /= 2;
                                                                       return ret:
}G;
                                                                    }
                                                                 }graph;
int main() {
 G.init(V);
  for(int i=0; i<E; i++) {</pre>
    int u, v;
    cin >> u >> v;
                                                                  5
                                                                        Math
    G.add_edge(u, v);
  cout << G.solve() << endl;</pre>
                                                                         ax+by=gcd
                                                                  typedef pair<int, int> pii;
```

4.4 Minimum Weight Matching (Clique version)

| struct Graph {

```
pii gcd(int a, int b){
  if(b == 0) return make_pair(1, 0);
  else{
    int p = a / b;
    pii q = gcd(b, a % b);
```

```
return make_pair(q.second, q.first - q.second * p);
}
}
```

5.2 Fast Fourier Transform

struct cp{

```
double _a,_b;
      cp operator +(const cp &o)const {return (cp){_a+o.
             _a,_b+o._b};}
      cp operator -(const cp &o)const {return (cp){_a-o.
      _a,_b-o._b};}
cp operator *(const cp &o)const {return (cp){_a*o.}
      _a-_b*o._b,_b*o._a+_a*o._b};}
cp operator *(const double &o)const {return (cp){_a}
             *o,_b*o};}
      cp operator !() const{return (cp){_a,-_b};}
}w[MAX];
int pos[MAX];
void fft_init(int len){
   int j = 0;
   while((1<<j) < len) j++;</pre>
       for(int i=0;i<len;i++)</pre>
            pos[i] = pos[i>>1]>>1 | ((i&1)<<j);
void fft(cp *_x, int len, int sta){
    for(int i = 0; i < len; i++)</pre>
            if(i < pos[i]) swap(_x[i], _x[pos[i]]);</pre>
      w[0] = (cp){1,0};
for(unsigned i = 2; i <= len; i <<= 1){
    cp g=(cp){cos(2*PI/i),sin(2*PI/i)*sta};
    cos(2*PI/i);</pre>
            for(int j = i>>1; j >= 0; j -= 2) w[j] = w[j
                   >>1];
            for(int j = 1; j < (i>>1); j += 2)w[j] = w[j]
            -1]*g;

for(int j = 0; j < len; j += i){

    cp *_a = _x+j, *_b = _a+(i>>1);

    for(int l = 0; l < (i>>1); l++){
                        cp o = _b[1]*w[1];
_b[1] = _a[1]-o;
_a[1] = _a[1]+o;
                  }
      if(sta == -1) for(int i = 0; i < len; i++) _x[i]._a</pre>
              /= len, _x[i]._b /= len;
     _x[MAX],_y[MAX],_z[MAX];
void FFT(int _a, int _b, int 11, int 12, int _c){
   int len = 1;
      while(len <= (l1+l2)>>1)len <<= 1;</pre>
       fft_init(len);
       for(int i = l1>>1; i<len; i++) _x[i]._a = _x[i]._b</pre>
      for(int i = 12>>1; i<len; i++) _y[i]._a = _y[i]._b</pre>
             = 0;
       for(int i = 0; i < 11; i++) (i&1 ? _x[i>>1]._b : _x
      [i>>1]._a) = st[_a][i];
for(int i = 0; i < 12; i++) (i&1 ? _y[i>>1]._b : _y
             [i>>1]._a) = st[_b][i];
      fft(_x, len, 1), fft(_y, len, 1);
for(int i = 0; i < len>1; i++){
   int j = len - 1&len - i;
   _z[i] = _x[i]*_y[i] - (_x[i]-!_x[j])*(_y[i]-!_y
                  [j])*(w[i]+(cp){1,0})*0.25;
      for(int i = len>>1; i < len; i++){</pre>
            int j = len - 1&len -i;

_z[i] = _x[i]*_y[i] - (_x[i]-!_x[j])*(_y[i]-!_y
                  [j])*((cp){1,0}-w[i^len>>1])*0.25;
      fft(_z, len, -1);
for(int i = 0; i < l1 + l2 - 1;i++)
    if(i&1) st[_c][i] = (LL)(_z[i>>1]._b+0.5);
    else st[_c][i] = (LL)(_z[i>>1]._a+0.5);
}
```

5.3 Theorem

5.3.1 Lucas' Theorem

For non-negative integer n,m and prime p, $\binom{m}{n} \equiv \prod_{i=0}^k \binom{m_i}{n_i} \pmod{p}$ where m_i is the i-th digit of m in base p.

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5.3.2 Sum of Two Squares Thm (Legendre)

```
For a given positive integer n, let D_1=(\# \text{ of positive integers } d \text{ dividing } N \text{ that } 1\equiv d \pmod 4) D_3=(\# \text{ of positive integers } d \text{ dividing } N \text{ that } 3\equiv d \pmod 4) then n can be written as a sum of two squares in exactly R(n)=4(D_1-D_3) ways.
```

5.3.3 Difference of D1-D3 Thm

```
\begin{array}{l} \text{let } n=2^t\cdot (p_1^{e_1}\cdot\ldots\cdot p_r^{e_r})\cdots (q_1^{f_1}\cdot\ldots\cdot q_s^{f_s})\\ \text{where } p_i,q_i \text{ are primes and } 1\equiv p_i\pmod 4, 3\equiv q_i\pmod 4\\ \text{then } D_1-D_3=\begin{cases} (e_1+1)(e_2+1)...(e_r+1), & \text{if } f_i \text{ all even}\\ 0, & \text{if any } f_i \text{ is odd} \end{cases}
```

5.3.4 Krush-Kuhn-Tucker Conditions

```
Stationarity For maximizing f(x): \nabla f(x^*) = \sum_{i=1}^m \mu_i \nabla g_i(x^*) + \sum_{j=1}^l \lambda_j \nabla h_j(x^*) For minimizing f(x): -\nabla f(x^*) = \sum_{i=1}^m \mu_i \nabla g_i(x^*) + \sum_{j=1}^l \lambda_j \nabla h_j(x^*) Primal feasibility
```

```
g_i(x^*) \le 0, for all i = 1, ..., m

h_j(x^*) = 0, for all j = 1, ..., l
```

 $\mu_i \geq 0$, for all $i = 1, \ldots, m$ Complementary slackness

 $\mu_i g_i(x^*) = 0$, for all i = 1, ..., m

Dual feasibility

5.3.5 Chinese remainder theorem

```
\begin{split} x &\equiv r_i \mod p_i \\ N &= \prod p_i \\ N_i &= N/p_i \\ x &\equiv \sum r_i N_i (N_i)_{p_i}^{-1} \mod N \end{split}
```

6 Geometry

6.1 Point operators

```
#define x first
#define y second
#define cpdd const pdd
struct pdd : pair<double, double> {
   using pair<double, double>::pair;
   pdd operator + (cpdd &p) const {
       return {x+p.x, y+p.y};
   pdd operator - () const {
       return {-x, -y};
   }
   pdd operator - (cpdd &p) const {
       return (*this) + (-p);
   pdd operator * (double f) const {
       return {f*x, f*y};
   double operator * (cpdd &p) const {
       return x*p.x + y*p.y;
};
double abs(cpdd &p) { return hypot(p.x, p.y);
double arg(cpdd &p) { return atan2(p.y, p.x); }
.x; }
```

```
double cross(cpdd &p, cpdd &q, cpdd &o) { return cross(
   p-o, q-o); }
pdd operator * (double f, cpdd &p) { return p*f; } //
   !! Not f*p !!
```

6.2 Intersection of two circles

6.3 Intersection of two lines

```
const double EPS = 1e-9;
pdd interPnt(pdd p1, pdd p2, pdd q1, pdd q2, bool &res)
    {
    double f1 = cross(p2, q1, p1);
    double f2 = -cross(p2, q2, p1);
    double f = (f1 + f2);

if(fabs(f) < EPS) {
    res = false;
    return {};
    }

res = true;
    return (f2 / f) * q1 + (f1 / f) * q2;
}</pre>
```

6.4 Circle cover

```
typedef double type;
typedef pair<type,type> Pt;
typedef pair<Pt,Pt> Line;
typedef pair<Pt,type> Circle;
#define X first
#define Y second
#define O first
#define R second
Pt operator+( const Pt& p1 , const Pt& p2 ){
 return { p1.X + p2.X , p1.Y + p2.Y };
Pt operator-( const Pt& p1 , const Pt& p2 ){
  return { p1.X - p2.X , p1.Y - p2.Y };
Pt operator*( const Pt& tp , const type& tk ){
  return { tp.X * tk , tp.Y * tk };
Pt operator/( const Pt& tp , const type& tk ){
  return { tp.X / tk , tp.Y / tk };
type operator*( const Pt% p1 , const Pt% p2 ){
  return p1.X * p2.X + p1.Y * p2.Y;
type operator^( const Pt& p1 , const Pt& p2 ){
  return p1.X * p2.Y - p1.Y * p2.X;
type norm2( const Pt& tp ){
  return tp * tp;
double norm( const Pt& tp ){
  return sqrt( norm2( tp ) );
Pt perp( const Pt& tp ){
  return { tp.Y , -tp.X };
#define N 1021
```

```
struct CircleCover{
   int C; Circ c[ N ];
   bool g[ N ][ N ], overlap[ N ][ N ];
   // Area[i] : area covered by at least i circles
   D Area[ N ];
   void init( int _C ){ C = _C; }
bool CCinter( Circ& a , Circ& b , Pt& p1 , Pt& p2 ){
     Pt o1 = a.0, o2 = b.0;
     D r1 = a.R , r2 = b.R;
     if( norm( o1 - o2 ) > r1 + r2 ) return {};
     if( norm( o1 - o2 ) < max(r1, r2) - min(r1, r2) )</pre>
          return {};
     D d2 = (o1 -
                    02 ) * ( 01 - 02 );
     D d = sqrt(d2);
     if( d > r1 + r2 ) return false;
     Pt u=(o1+o2)*0.5 + (o1-o2)*((r2*r2-r1*r1)/(2*d2));
     D A=sqrt((r1+r2+d)*(r1-r2+d)*(r1+r2-d)*(-r1+r2+d));
     Pt v=Pt( o1.Y-o2.Y , -o1.X + o2.X ) * A / (2*d2);
p1 = u + v; p2 = u - v;
     return true:
   struct Teve {
     Pt p; D ang; int add;
     Teve() {}
      Teve(Pt _a, D _b, int _c):p(_a), ang(_b), add(_c){}
     bool operator < (const Teve &a) const
     {return ang < a.ang;}
   }eve[ N * 2 ];
   // strict: x = 0, otherwise x = -1
   bool disjuct( Circ& a, Circ &b, int x )
   {return sign( norm( a.O - b.O ) - a.R - b.R ) > x;}
   bool contain( Circ& a, Circ &b, int x )
   {return sign( a.R - b.R - norm( a.O - b.O ) ) > x;}
   bool contain(int i, int j){
     /* c[j] is non-strictly in c[i]. */
     contain(c[i], c[j], -1);
   void solve(){
     for( int i = 0 ; i <= C + 1 ; i ++ )</pre>
       Area[ i ] = 0;
      for( int i = 0 ; i < C ; i ++ )</pre>
       for( int j = 0 ; j < C ; j ++ )
  overlap[i][j] = contain(i, j);</pre>
     for( int i = 0 ; i < C ; i ++ )
  for( int j = 0 ; j < C ; j ++ )</pre>
          g[i][j] = !(overlap[i][j] || overlap[j][i] ||
                       disjuct(c[i], c[j], -1));
     for( int i = 0 ; i < C ; i ++ ){</pre>
       int E = 0, cnt = 1;
        for( int j = 0 ; j < C ;</pre>
          if( j != i && overlap[j][i] )
            cnt ++;
        for( int j = 0 ; j < C ; j ++ )</pre>
          if( i != j && g[i][j] ){
            Pt aa, bb;
            CCinter(c[i], c[j], aa, bb);
D A=atan2(aa.Y - c[i].0.Y, aa.X - c[i].0.X);
D B=atan2(bb.Y - c[i].0.Y, bb.X - c[i].0.X);
            eve[E ++] = Teve(bb, B, 1);
            eve[E ++] = Teve(aa, A, -1);
            if(B > A) cnt ++;
       if( E == 0 ) Area[ cnt ] += pi * c[i].R * c[i].R;
        else{
          sort( eve , eve + E );
          eve[E] = eve[0];
          for( int j = 0 ; j < E ; j ++ ){</pre>
            cnt += eve[j].add;
            Area[cnt] += (eve[j].p ^{\circ} eve[j + 1].p) * .5;
            D theta = eve[j + 1].ang - eve[j].ang;
            if (theta < 0) theta += 2. * pi;</pre>
            Area[cnt] +=
              (theta - sin(theta)) * c[i].R*c[i].R * .5;
       }
     }
   }
};
```

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6.5 Half Plane Intersection

```
const double EPS = 1e-9;
```

```
struct Point{
pdd interPnt(Line l1, Line l2, bool &res){
                                                               Type x, y;
                                                               Point(){};
    pdd p1, p2, q1, q2;
    tie(p1, p2) = 11;
                                                               Point(Type _x, Type _y){
    tie(q1, q2) = 12;
                                                                 x = _x, y = _y;
  double f1 = cross(p2, q1, p1);
    double f2 = -cross(p2, q2, p1);
                                                               void read(){
                                                                 scanf("%lf %lf", &x, &y);
  double f = (f1 + f2);
    if(fabs(f) < EPS) {</pre>
                                                               Point operator +(const Point & P2){
                                                                 return Point(x + P2.x, y + P2.y);
        res = false;
        return {0, 0};
                                                               Point operator -(const Point & P2){
                                                                 return Point(x - P2.x, y - P2.y);
    res = true;
  return (f2 / f) * q1 + (f1 / f) * q2;
                                                               Point operator *(const Type & Len){
                                                                 return Point(x*Len, y*Len);
bool isin(Line 10, Line 11, Line 12) {
                                                               Type operator *(const Point & P2){
    // Check inter(l1, l2) in l0
                                                                 return x*P2.x + y*P2.y;
    bool res;
    pdd p = interPnt(l1, l2, res);
                                                               Type operator ^(const Point & P2){
    return cross(10.S, p, 10.F) > EPS;
                                                                 return x*P2.y - y*P2.x;
                                                               Type dis(){
/* If no solution, check: 1. ret.size() < 3</pre>
                                                                 return x*x+y*y;
 * Or more precisely, 2. interPnt(ret[0], ret[1])
 * in all the lines. (use (l.5 - l.F).cross(p - l.F) >
                                                             };
                                                             struct Line{
                                                               Point s, e;
vector<Line> halfPlaneInter(vector<Line> lines) {
                                                               Line(){};
                                                               Line(Point _s, Point _e){
    int sz = lines.size();
    vector<double> ata(sz), ord(sz);
                                                                 s = _s, e = _e;
    for (int i=0; i<sz; i++) {</pre>
                                                               void read(){
        ord[i] = i;
        pdd d = lines[i].S - lines[i].F;
ata[i] = atan2(d.y, d.x);
                                                                 s.read(); e.read();
                                                            };
    sort(ALL(ord), [&](int i, int j) {
    if (abs(ata[i] - ata[j]) < EPS) {</pre>
             return cross(lines[i].S, lines[j].S, lines[
                 i].F) < 0;
                                                             6.7
                                                                  dao inter
        return ata[i] < ata[j];</pre>
                                                             Point(Line 11, Line 12){
                                                               Type v1 = (11.s - 11.e) ^ (12.s - 11.e);
    vector<Line> fin;
                                                               Type v2 = (11.s - 11.e) ^ (11.e - 12.e);
    for (int i=0; i<sz; i++) {</pre>
        if (!i or fabs(ata[ord[i]] - ata[ord[i-1]]) >
                                                               Type v3 = (v1 + v2);
             EPS) {
                                                               return 12.s*(v2/v3) + 12.e*(v1/v3);
             fin.PB(lines[ord[i]]);
                                                            }
    deque<Line> dq;
                                                                  dao 2D convex hull
    for (int i=0; i<SZ(fin); i++) {</pre>
        while(SZ(dq) >= 2 and
               not isin(fin[i], dq[SZ(dq)-2], dq[SZ(dq)
                                                             int ori(Point s, Point e, Point P){
                   -1])) {
                                                               Type val = (s - e)^(P - e);
             dq.pop_back();
                                                               if(fabs(val) < eps) return 0;</pre>
                                                               else if(val > 0) return 1;
        while(SZ(dq) >= 2 and
                                                               else return -1;
               not isin(fin[i], dq[0], dq[1])) {
             dq.pop_front();
                                                             vector<Point> convex_hull(vector<Point> pt){
                                                               sort(pt.begin(), pt.end());
        dq.push_back(fin[i]);
                                                               int top=0;
                                                               vector<Point> stk(2*pt.size());
                                                               for (int i=0; i<(int)pt.size(); i++){</pre>
    while (SZ(dq) >= 3 \text{ and}
                                                                 while (top >= 2 && ori(stk[top-2],stk[top-1],pt[i])
           top--;
        dq.pop_back();
                                                                 stk[top++] = pt[i];
                                                               for (int i=pt.size()-2, t=top+1; i>=0; i--){
    while (SZ(dq) >= 3 \text{ and}
                                                                 while (top >= t && ori(stk[top-2],stk[top-1],pt[i])
           not isin(dq[SZ(dq)-1], dq[0], dq[1])) {
        dq.pop_front();
                                                                   top--;
                                                                 stk[top++] = pt[i];
    vector<Line> res(ALL(dq));
    return res;
                                                               stk.resize(top-1);
|}
                                                               return stk;
                                                             }
```

6.6 dao point

```
struct Mcc{
  // return pair of center and r^2
  static const int MAXN = 1000100;
  pdd p[MAXN],cen;
  double r2;
  void init(int _n, pdd _p[]){
    memcpy(p,_p,sizeof(pdd)*n);
  double sqr(double a){ return a*a; }
  double abs2(pdd a){ return a*a;
  pdd center(pdd p0, pdd p1, pdd p2) {
    pdd a = p1-p0;
    pdd b = p2-p0;
    double c1=abs2(a)*0.5;
    double c2=abs2(b)*0.5;
    double d = a % b;
    double x = p0.x + (c1 * b.y - c2 * a.y) / d;
    double y = p0.y + (a.x * c2 - b.x * c1) / d;
    return pdd(x,y);
  pair<pdd,double> solve(){
    random_shuffle(p,p+n);
    r2=0;
    for (int i=0; i<n; i++){</pre>
      if (abs2(cen-p[i]) <= r2) continue;</pre>
      cen = p[i];
      r2 = 0;
      for (int j=0; j<i; j++){</pre>
        if (abs2(cen-p[j]) <= r2) continue;
cen = 0.5 * (p[i]+p[j]);</pre>
        r2 = abs2(cen-p[j]);
        for (int k=0; k<j; k++){</pre>
          if (abs2(cen-p[k]) <= r2) continue;</pre>
           cen = center(p[i],p[j],p[k]);
           r2 = abs2(cen-p[k]);
      }
    }
    return {cen,r2};
  }
}mcc;
```

7 Stringology

7.1 Suffix Array

```
const int MAX = 1020304;
int ct[MAX], he[MAX], rk[MAX], sa[MAX], tsa[MAX], tp[
    MAX][2];
void suffix arrav(char *ip){
  int len = strlen(ip);
  int alp = 256;
  memset(ct, 0, sizeof(ct));
  for(int i=0;i<len;i++) ct[ip[i]+1]++;</pre>
  for(int i=1;i<alp;i++) ct[i]+=ct[i-1]</pre>
  for(int i=0;i<len;i++) rk[i]=ct[ip[i]];</pre>
  for(int i=1;i<len;i*=2){</pre>
    for(int j=0;j<len;j++){</pre>
      if(j+i>=len) tp[j][1]=0;
       else tp[j][1]=rk[j+i]+1;
      tp[j][0]=rk[j];
    memset(ct, 0, sizeof(ct));
    for(int j=0;j<len;j++) ct[tp[j][1]+1]++;</pre>
    for(int j=1;j<len+2;j++) ct[j]+=ct[j-1];
for(int j=0;j<len;j++) tsa[ct[tp[j][1]]++]=j;</pre>
    memset(ct, 0, sizeof(ct));
    for(int j=0;j<len;j++) ct[tp[j][0]+1]++;</pre>
    for(int j=1;j<len+1;j++) ct[j]+=ct[j-1];</pre>
    for(int j=0;j<len;j++) sa[ct[tp[tsa[j]][0]]++]=tsa[</pre>
         j];
```

```
rk[sa[0]]=0;
     for(int j=1;j<len;j++){</pre>
       if( tp[sa[j]][0] == tp[sa[j-1]][0] &&
  tp[sa[j]][1] == tp[sa[j-1]][1] )
          rk[sa[j]] = rk[sa[j-1]];
       else
          rk[sa[j]] = j;
     }
   }
   for(int i=0,h=0;i<len;i++){</pre>
     if(rk[i]==0) h=0;
     else{
       int j=sa[rk[i]-1];
       h=max(0,h-1);
       for(;ip[i+h]==ip[j+h];h++);
     he[rk[i]]=h;
}
```

7.2 KMP

```
#include<bits/stdc++.h>
using namespace std;
void build_fail_function(string B, int *fail) {
    int len = B.length(), pos;
    pos = fail[0] = -1;

for (int i = 1; i < len; i ++) {

   while (pos != -1 and B[pos + 1] != B[i])
              pos = fail[pos];
          if (B[pos + 1] == B[i]) pos ++;
          fail[i] = pos;
    }
}
void match(string A, string B, int *fail) {
     int lenA = A.length(), lenB = B.length();
     int pos = -1;
    for (int i = 0; i < lenA; i ++) {
    while (pos != -1 and B[pos + 1] != A[i])</pre>
              pos = fail[pos];
          if (B[pos + 1] == A[i]) pos ++;
          if (pos == lenB - 1) {
              // Match ! A[i - LenB + 1, i] = B
              pos = fail[pos];
         }
    }
}
```

7.3 Z value

```
void Zval(const char *s, int len, int *z) {
   z[0] = 0;
   for (int b=0, i=1; i<len; i++) {
        z[i] = max(min(z[i-b], z[b] + b - i), 0);
        while (s[i + z[i]] == s[z[i]]) z[i] ++;
        if (i+z[i] > b+z[b]) b=i;
    }
}
```

7.4 Lexicographically Smallest Rotation

```
string mcp(string s){
  int n = s.length();
  s += s;
  int i=0, j=1;
  while (i<n && j<n){
    int k = 0;
    while (k < n && s[i+k] == s[j+k]) k++;
    if (s[i+k] <= s[j+k]) j += k+1;
    else i += k+1;
    if (i == j) j++;
  }
  int ans = i < n ? i : j;
  return s.substr(ans, n);
}</pre>
```