

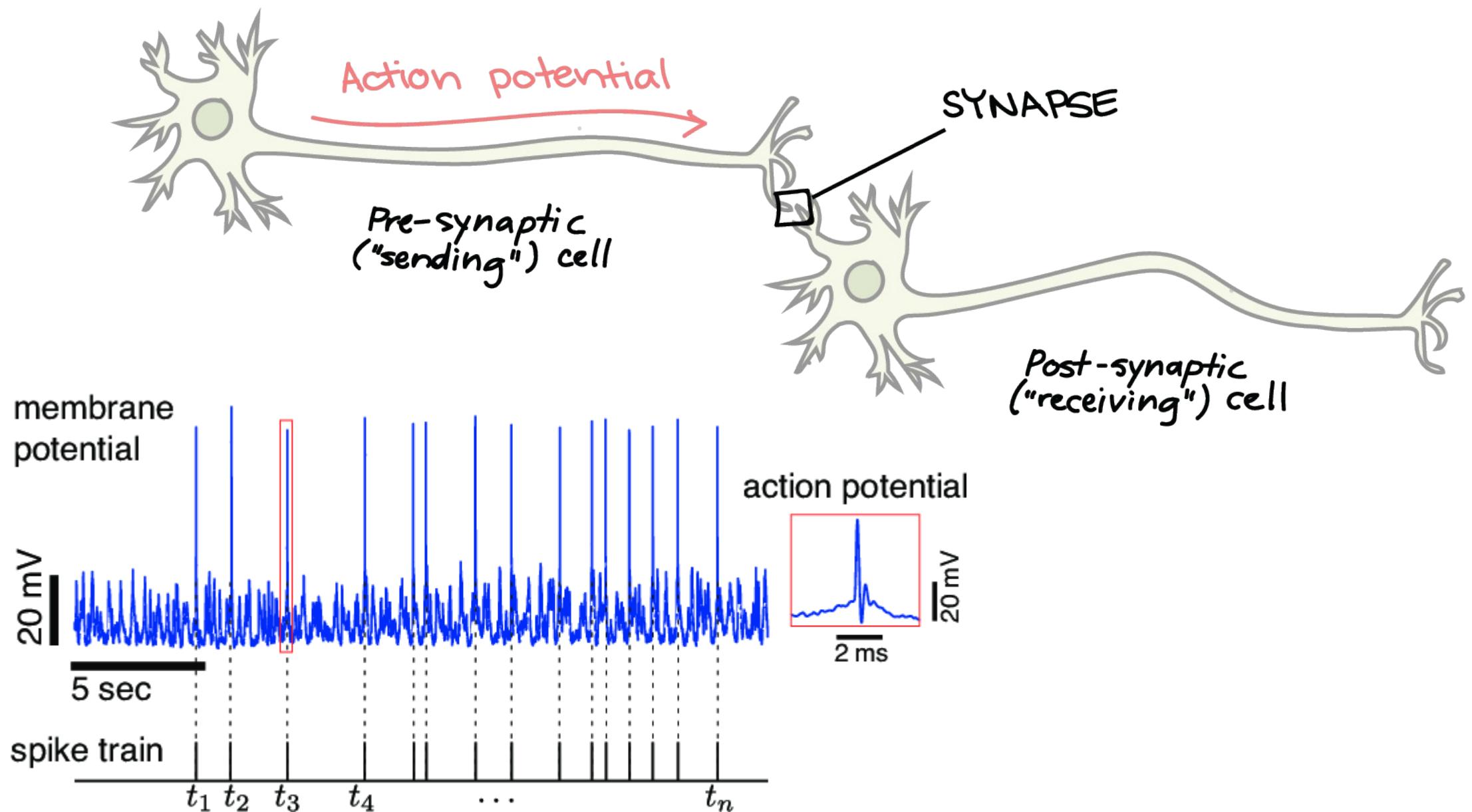
# Machine Learning for Neuroimaging and Neuroscience

## Spiking Neural Networks



AGH UNIVERSITY OF SCIENCE  
AND TECHNOLOGY

# What is a spiking neural network?



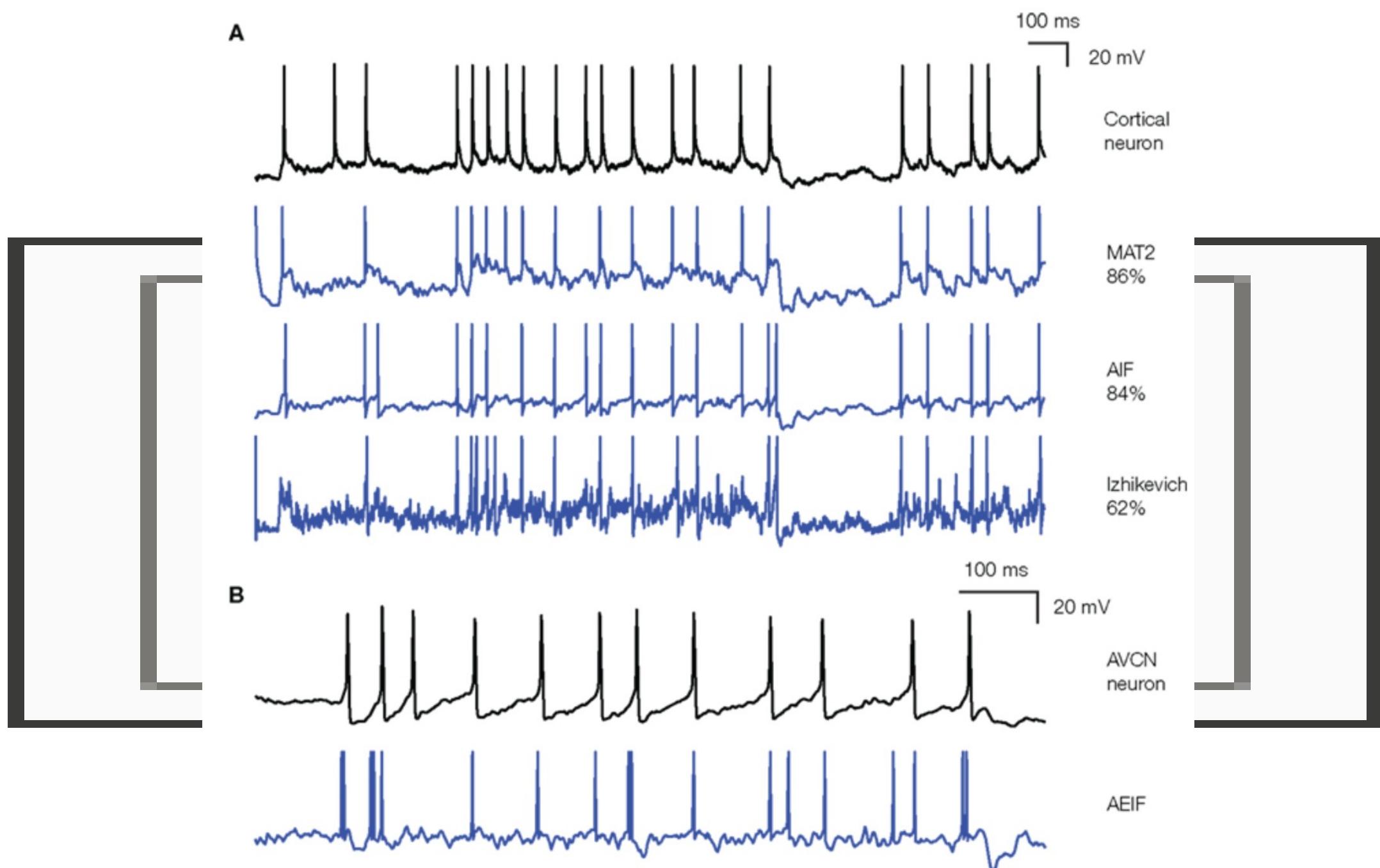


Fig. 5.21 Spike trains. Source: [Rossant et al., 2011].

The leaky integrate-and-fire (LIF; Lapicque, 1907) neuron has a **membrane potential**  $v(t)$  that integrates its input current  $I(t)$ :

$$C \frac{dv(t)}{dt} = -g_L (v(t) - V_L) + I(t)$$

$C$  is the membrane capacitance,  $g_L$  the leak conductance and  $V_L$  the resting potential. In the absence of input current ( $I = 0$ ), the membrane potential is equal to the resting potential.

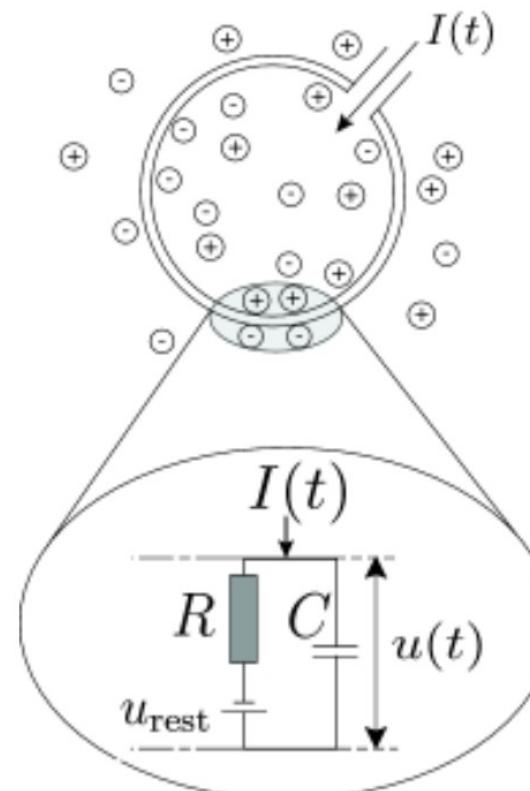


Fig. 5.22 Membrane potential of a leaky integrate-and-fire neuron. Source:  
<https://neuronaldynamics.epfl.ch/online/Ch1.S3.html>.

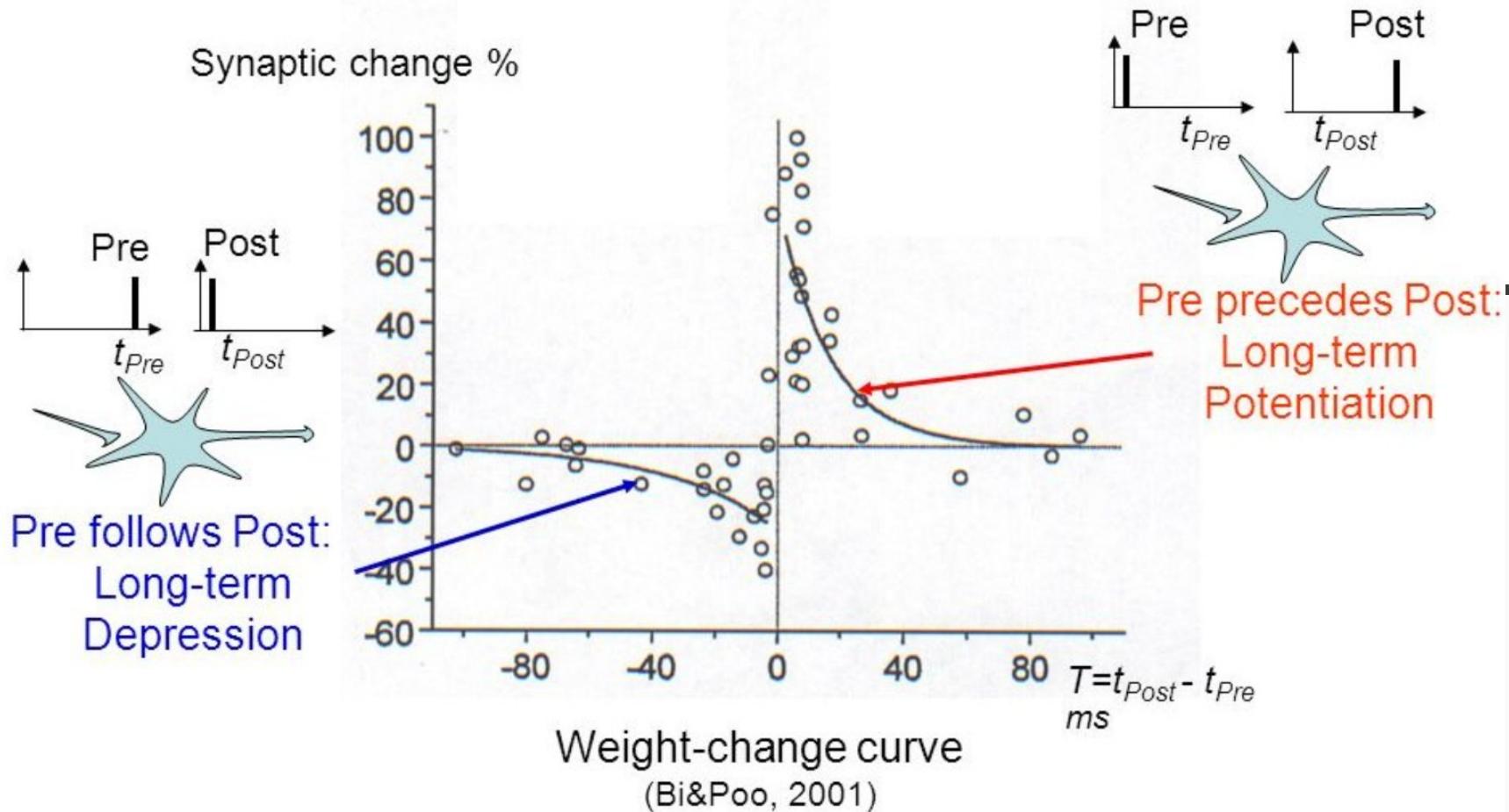
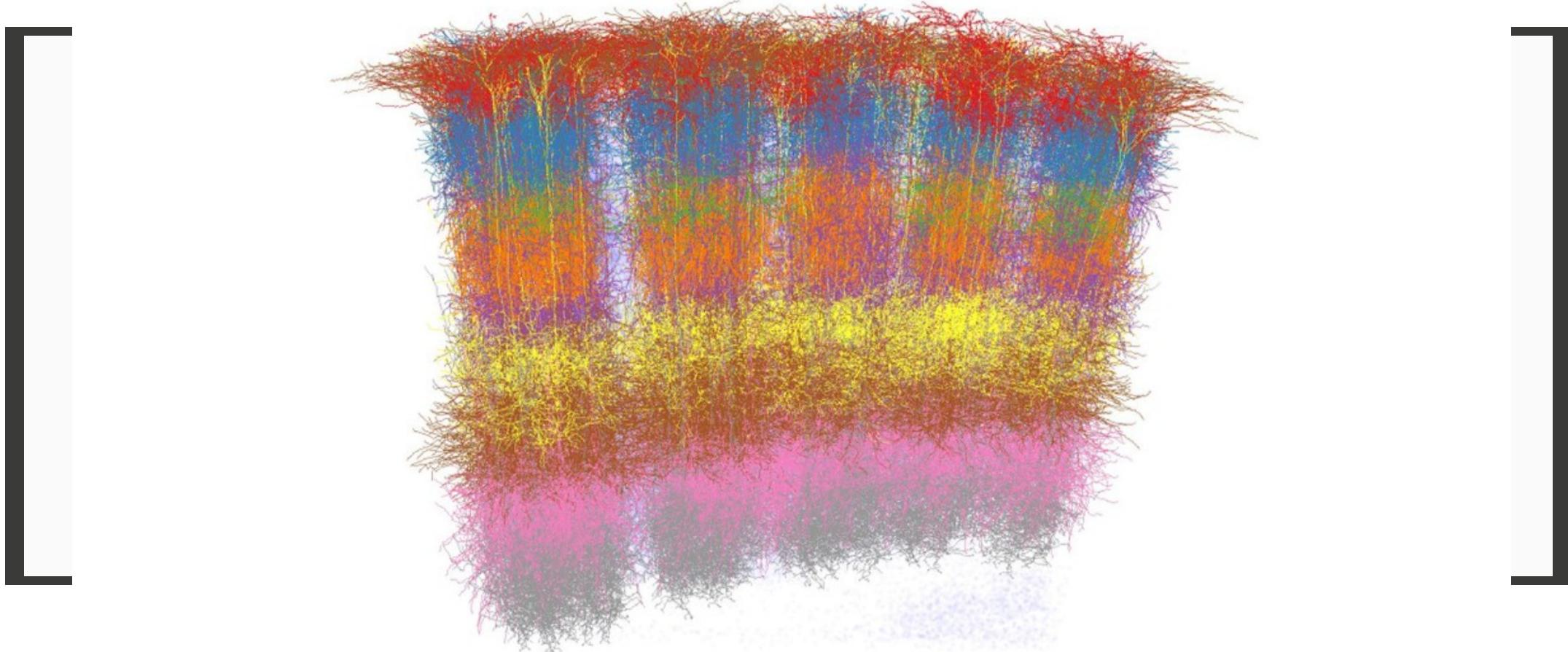


Fig. 5.29 Spike-timing dependent plasticity. Source: [Bi & Poo, 2001].

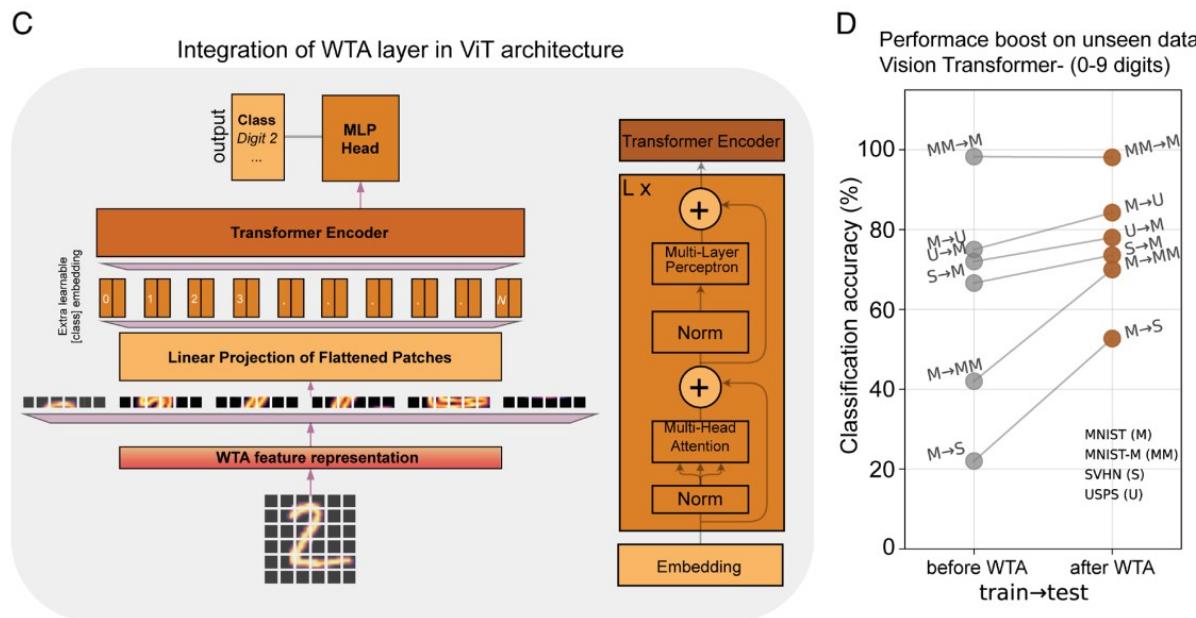
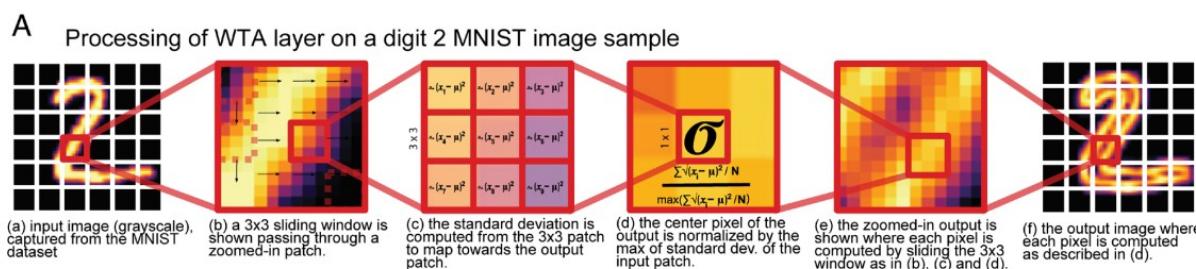
The STDP (**spike-timing dependent plasticity**) plasticity rule describes how the weight of a synapse evolves when the pre-synaptic neuron fires at  $t_{pre}$  and the post-synaptic one fires at  $t_{post}$ .

$$\Delta w = \begin{cases} A^+ \exp -\frac{t_{pre}-t_{post}}{\tau^+} & \text{if } t_{post} > t_{pre} \\ A^- \exp -\frac{t_{pre}-t_{post}}{\tau^-} & \text{if } t_{pre} > t_{post} \end{cases}$$

Recurrent networks of spiking neurons exhibit various dynamics. They can fire randomly, or tend to fire synchronously, depending on their inputs and the strength of the connections. **Liquid State Machines** are the spiking equivalent of echo-state networks.



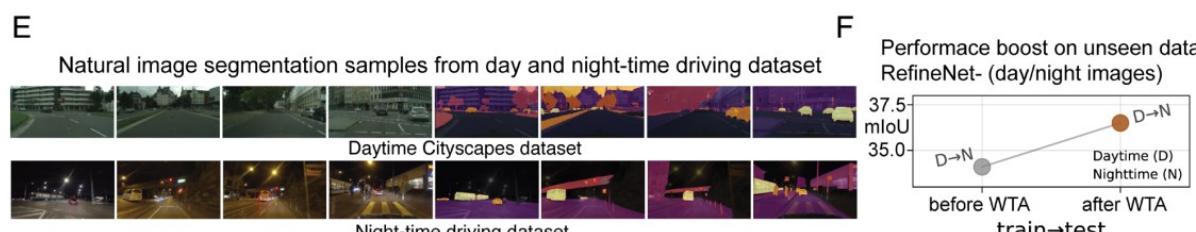
*Fig. 5.28* Cortical column of the rat's vibrissal cortex. Source:  
<https://www.pnas.org/content/110/47/19113>.

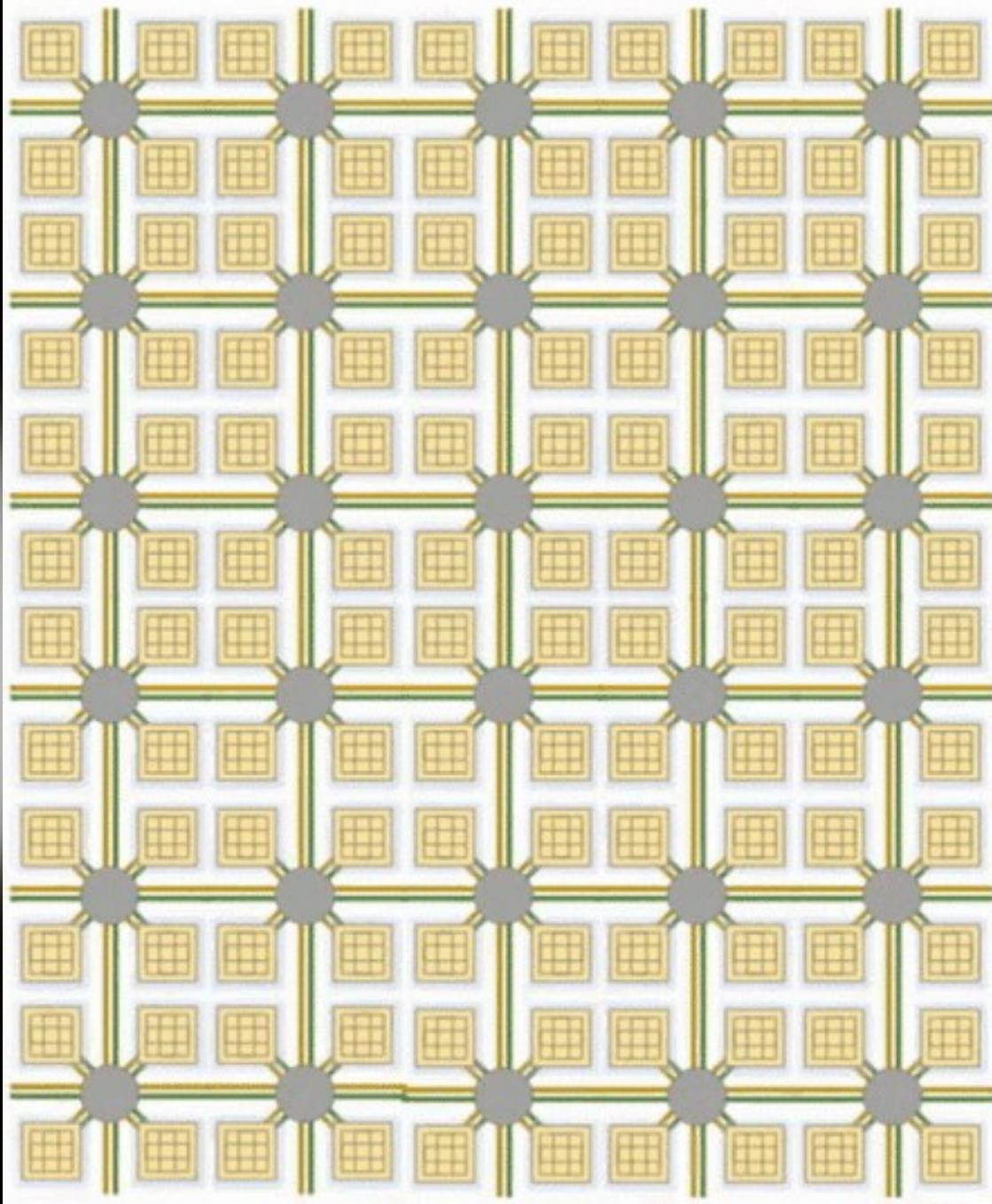
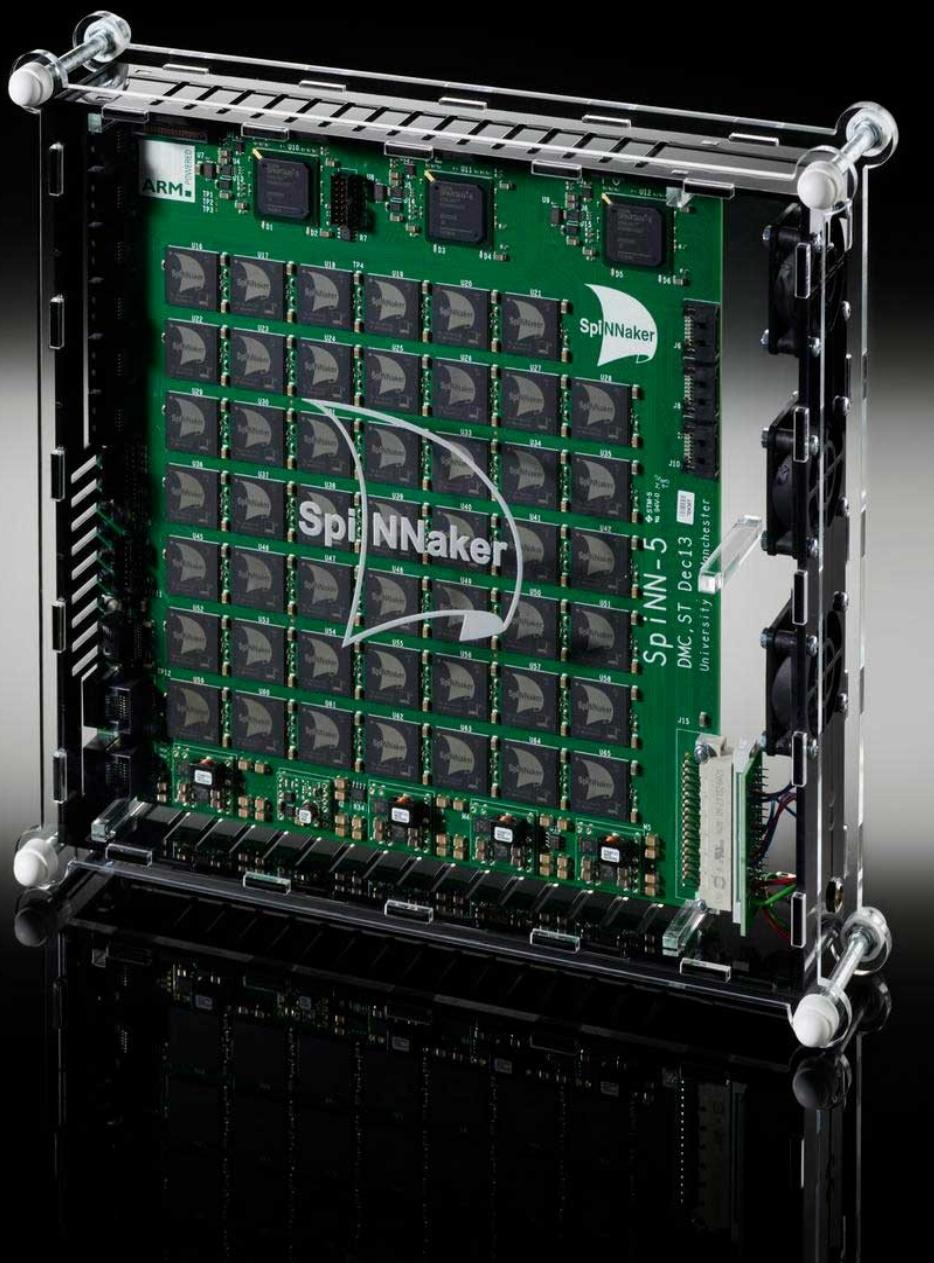


**Table 1. Comparison of classification accuracy between WTA-based DNN architectures (Vision Transformer, EfficientNet, CapsuleNet, MobileNet, and ResNet) and source-only models trained on the MNIST (M), MNIST-M (MM), SVHN (S), and USPS (U) datasets**

Source-only Models	M→U	U→M	S→M	M→S	M→MM	MM→M
ViT	75.0	72.0	66.6	22.0	42.0	98.3
EfficientNet	77.9	50.7	61.4	18.6	18.8	95.0
CapsuleNet	<b>96.4</b>	<b>87.2</b>	58.1	11.8	22.5	<b>98.4</b>
MobileNet	84.4	60.0	72.2	22.4	33.9	97.3
ResNet	82.5	58.5	63.4	27.2	38.2	97.4
ViT+WTA	84.26	78.0	<b>73.6</b>	<b>52.7</b>	<b>70.0</b>	98.1
EfficientNet+WTA	83.5	74.2	69.1	19.6	48.8	96.3
CapsuleNet+WTA	<b>94.1</b>	<b>87.8</b>	<b>75.9</b>	32.1	57.2	<b>98.6</b>
MobileNet+WTA	82.5	70.9	73.5	<b>40.5</b>	<b>73.4</b>	97.8
ResNet+WTA	82.8	66.0	71.2	27.7	<b>70.2</b>	97.8

Biologically grounded neocortex computational primitives implemented on neuromorphic hardware improve vision transformer performance





# A simple model: the leaky integrate-and-fire (LIF)

Membrane potential  $V$  evolves according to a differential equation

$$\tau \frac{dV}{dt} = -V$$

Leak

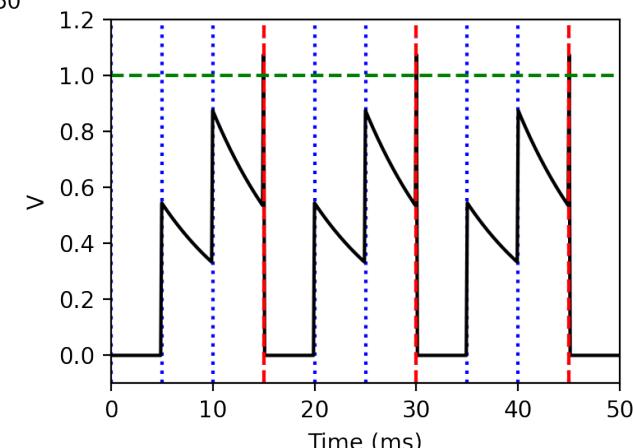
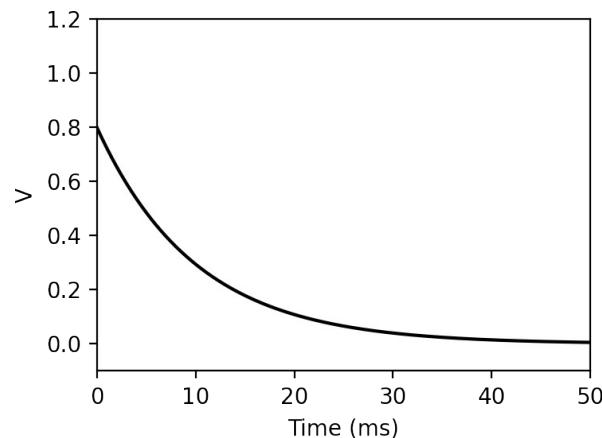
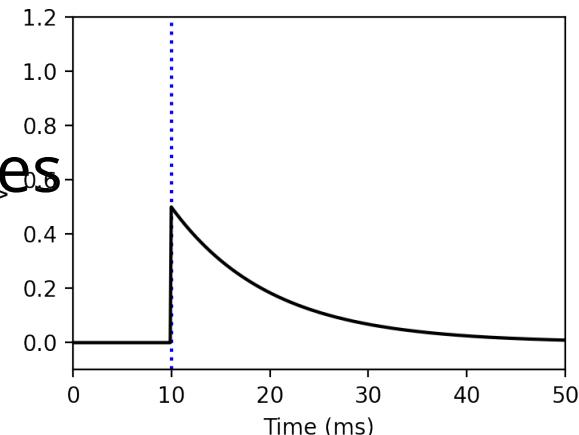
When a neuron receives a spike,  $V$  increases synaptic weight  $w$ :

$$V \leftarrow V + w$$

Integrate

When  $V > V_t$  the neuron “fires a spike” and Resets:  $V \leftarrow 0$

**Nonlinear, discontinuous dynamics!**



# Spiking NN deep learning

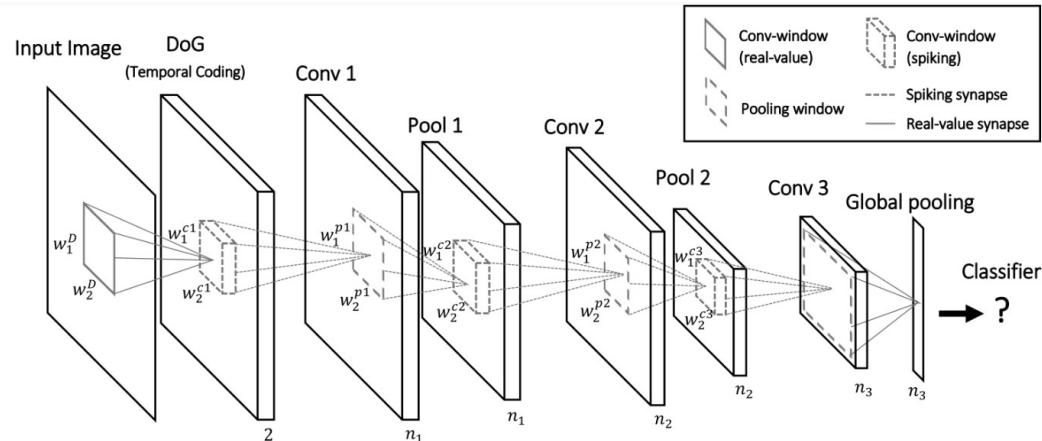
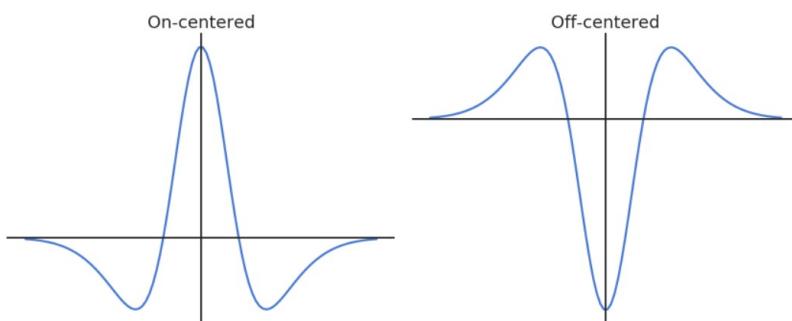


Fig. 5.30 Deep convolutional spiking network of [Kheradpisheh et al., 2018].

The image is first transformed into a spiking population using **difference-of-Gaussian (DoG)** filters.

- **On-center** neurons fire when a bright area at the corresponding location is surrounded by a darker area.
- **Off-centered** cells do the opposite.



Snn-Torch  
SpikeJelly  
Etc

Neuron  
Nest  
PyNN

# Questions?



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