

# TO CATCH A THIEF: ENDOGENOUS POLICING AND CHOICE OF LOCATION BY CRIMINALS

Siddhartha Bandyopadhyay <sup>1</sup>   Antonio Cabrales <sup>2</sup>   Kaustav Das <sup>3</sup>

<sup>1</sup>University of Birmingham

<sup>2</sup>Universidad Carlos III de Madrid

<sup>3</sup>University of Leicester

# MOTIVATION AND INTRODUCTION

- Hotspot policing where one patrols areas with high concentrations of crime is celebrated as a success story of policing.
- This has led to police being deployed in some high crime areas.
- Yet while there is moderate evidence on its effectiveness, there are no studies that look at longer term impacts.
- Given that criminals can move, one needs to consider optimal responses to changes in policing on criminal location choice in that area and other neighbouring areas.
- Indeed, some empirical studies actually do find displacement
- For example, 'Operation Menas' in London involved a double patrol team of uniformed officers patrolling bus stops three times a day, for 15 minutes → 37 percent reduction in incident reports by bus drivers but a 25 percent increase in victims reporting incidents in nearby areas.

# RESEARCH QUESTIONS

- How should police allocate resources optimally across regions given people can choose where to locate?
- Given rational policing and criminal location decision making, what does the equilibrium distribution of policing resources and location choice look like?

# THIS PAPER

- Characterise this optimal location and spending allocation in a model with multiple regions with both a fixed and optimally chosen police budget
- Account for the social (negative) externality of having more potential criminals in a region
- Understand how the relative value of crime opportunities across areas determine the solution to the problem i.e. optimal location choice and distribution of police resources

# RELATED LITERATURE

- Hotspot policing (Sherman and Weisburd 1995)
- Theoretical modelling limited
- Zenou (2003)-social interaction and distance to work affect crime rates
- Verdier and Zenou (2004)-beliefs, endogenous location and opportunity to commit crime → self-fulfilling equilibrium with different ex post crime rates between two groups with same ex ante propensities
- Bandyopadhyay and Chatterjee (2010)-self fulfilling equilibrium through biased citizen reporting and rational policing
- Mathieson et. al (2023) and Gao and Vasquez (2024) have a spatial search model of criminal activity
- Our model has both endogenous location choice and policing

# THE ENVIRONMENT

- Consider a region  $R$  which has a continuum of population with measure  $N > 0$ .
- $R$  comprises of two areas  $A$  and  $B$ .
- Any member in the population is free to locate in any of the areas.
- Relocation from one area to another is costless.
- In each of the areas, a member of the population can choose to get involved in crime activities.
- If a positive measure of individuals (say  $n_j > 0$ ) get involved in crime activities in area  $j = A, B$ , then this mass of *criminals* jointly get a payoff of  $v_j > 0$ .

# THE ENVIRONMENT

- For any  $i$  belonging to the set  $n_j$ , the expected gain from getting involved in criminal activity in city  $j$  is  $\frac{v_j}{n_j}$ .
- Let  $P_j$  be level of policing in city  $j$ .  $P = P_A + P_B$ .
- For any  $i$  belonging to the set  $n_j$ , the probability of getting caught is  $\frac{P_j}{n_j} \Rightarrow$   $i$ 's expected cost of getting caught is  $c_i \frac{P_j}{n_j}$ .
- $c_i$ : cost type of individual  $i$ .  $c_i$  is uniformly distributed over the population from 0 to  $C$ ,  $C > 0$ .
- Net expected payoff to  $i$  from getting involved in criminal activities in city  $j$  is

$$U_{ij} = \frac{v_j - c_i P_j}{n_j}$$

- W.L.O.G, we normalise the expected payoff of a non-criminal to 0. Also assume  $v_j - CP_j < 0$  for  $j = A, B$ .

# EQUILIBRIUM

- We conjecture an equilibrium as follows:
  - There exist two thresholds  $c_1$  and  $c_2$  such that  $0 < c_1 < c_2 < C$ .
  - All individuals with  $c_i \in (0, c_2)$  get involved in criminal activities.
  - $c_i \in (0, c_1)$  locate in  $A$  and  $c_i \in (c_1, c_2)$  locate in  $B$ .
  - $c_i > c_2$  remains as non-criminals and they are indifferent between locating either in  $A$  or  $B$ .
- We will show that the conjectured equilibrium exists iff we have

$$\frac{P_A}{v_A} \geq \frac{P_B}{v_B}$$



# EXISTENCE OF EQUILIBRIUM

- For given values of  $c_1$  and  $c_2$ , we have  $n_A = \frac{c_1}{C}N$  and  $n_B = \frac{c_2 - c_1}{C}N$
- First we compute the thresholds  $c_1$  and  $c_2$ :
  - $c_2$  computed from the following indifference condition:

$$\frac{v_B - c_2 P_B}{c_2 - c_1} = 0 \Rightarrow c_2 = \frac{v_B}{P_B}$$

- $c_1$  computed from the following indifference condition:

$$\frac{v_A - c_1 P_A}{c_1} = \frac{v_B - c_1 P_B}{c_2 - c_1} \Rightarrow c_1 = \frac{v_A}{P_A + P_B}$$

- Mass of non-criminal is  $\frac{C - c_2}{C}N$ .
- Need to show:
  - For any  $c < c_1 (\in (c_1, c_2))$ ,  $\frac{v_A - c P_A}{c_1} \geq (\leq) \frac{v_B - c P_B}{c_2 - c_1}$ .
  - For any  $c > c_2$ ,  $v_A - c P_A < 0$  and  $v_B - c P_B < 0$ .

# EXISTENCE OF EQUILIBRIUM

- Define the function  $\Gamma(c)$ :

$$\Gamma(c) = \frac{v_A - cP_A}{c_1} - \frac{v_B - cP_B}{c_2 - c_1}$$

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$$\frac{P_A}{v_A} \geq \frac{P_B}{v_B} \Leftrightarrow \Gamma'(c) \leq 0$$

- Since  $\Gamma(c_1) = 0$ ,  $\Gamma'(c) \leq 0$  ensures the first equilibrium condition.
- Also,  $\frac{P_A}{v_A} \geq \frac{P_B}{v_B} \Leftrightarrow$  for all  $c > c_2$

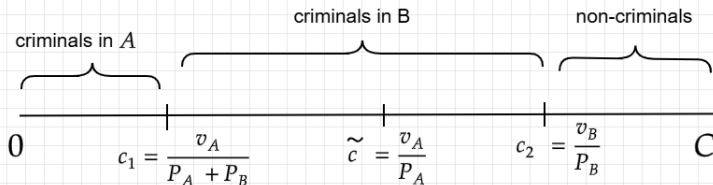
$$v_j - cP_j < 0$$

# ILLUSTRATION OF EQUILIBRIUM

$$\frac{P_A}{P_B} \geq \frac{P_B}{V_B} \Leftrightarrow \Gamma'(c) \leq 0$$

$$\frac{P_A}{v_A} \geq \frac{P_B}{B} \Leftrightarrow v_j - cP_j < 0 \text{ for } c > c_2$$

$$\frac{P_A}{v_A} \geq \frac{P_B}{v_B} \text{ sufficient (not necessary) to guarantee } c_2 > c_1$$



# OPTIMAL CHOICE OF POLICING: FIXED P

- Define the payoff off the society as

$$U_P(n_A, n_B) = -\frac{1}{2}(n_A^2 + n_B^2) - \frac{1}{\beta}(P_A + P_B)^\beta$$

such that  $\beta > 1$

- Using the equilibrium values of  $c_1$  and  $c_2$  we get

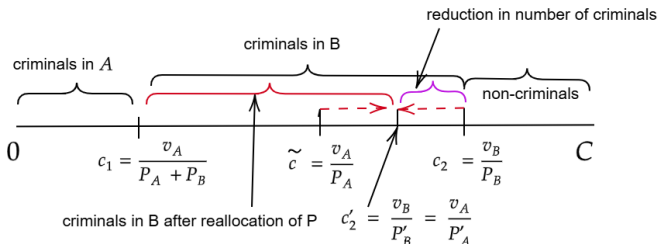
$$U_P(n_A, n_B) = -\frac{1}{2P^2}[v_A^2 + \{\frac{Pv_B}{P_B} - v_A\}^2] - \frac{1}{\beta}P^\beta$$

- Fixed  $P \Rightarrow$  number of criminals can be reduced only through allocating more to  $B$  at the expense of  $A$ .
- $c_1$  only depends on  $P \Rightarrow$  no effect on  $c_1$  because of reallocation
- Optimal action entails increase  $P_B$  up to the point when  $\frac{P_A}{v_A} = \frac{P_B}{v_B}$

# ILLUSTRATION OF POLICING REALLOCATION

Reallocation of  $P$  when it is fixed

$$P_A + P_B = P'_A + P'_B$$



# OPTIMAL POLICING: VARIABLE P

- Two stage process:
  - Given value of  $P \rightarrow$  adjust  $P_A$  and  $P_B$  such that

$$\frac{P_A}{v_A} = \frac{P_B}{v_B} \Rightarrow P_B = \frac{P v_B}{v_A + v_B}$$

- Substituting  $P_B = \frac{P v_B}{v_A + v_B}$  in  $U_P(n_A, n_B)$  to obtain the optimal level of  $P$ .

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$$U_P(n_A, n_B) = \frac{1}{2P^2} [v_A^2 + v_B^2] - \frac{1}{\beta} P^\beta$$

- $U_P$  is strictly concave  $\Rightarrow$  optimal  $P$  is given by the F.O.C:

$$P = (v_A + v_B)^{\frac{1}{\beta+2}}$$

- Optimal value  $P_B = \frac{v_B}{(v_A + v_B)^{1 - \frac{1}{\beta+2}}}$
- Optimal value of  $P_A = \frac{v_A}{(v_A + v_B)^{1 - \frac{1}{\beta+2}}}$

# CONCLUDING REMARKS

- Developed a model of optimal criminal location and policing/allocation
- Generalise the structure of equilibrium (ongoing)
- Understand how a dynamic hotspot model of policing will work
- Generate cycles or persistence?
- Develop testable predictions