

Algorithm 1:

The algorithm runs in  $O(n \log n)$  time because each recursive splits the list of buildings in half. It produces the recurrence of  $T(n) = 2T(n/2) + O(n)$ . The merge requires culling the visible buildings from each half, which causes the worst case to be  $O(n)$ . By applying the Master Theorem, it gives an overall running time of  $O(n \log n)$ . The recursion depth is  $\log_2(n)$ , so the algorithm uses  $O(\log n)$  by using extra space on the call stack.

Algorithm 2:

The greedy activity-selection algorithm runs in  $O(n \log n)$  time because sorting the activities by their finish time is expensive, taking  $n \log n$  time. After the sorting, the algorithm performs a single linear scan through the list, in which it selects each activity whose start time is compatible, which is  $O(n)$ . The total running time is dominated by the sort where  $n + n \log n$  is equal to  $O(n \log n)$ . The algorithm uses  $O(1)$  extra space because it only stores a few variables and it appends compatible activities directly to the output list.