Team Reference

#### Pollard

}

```
const int max_step = 4e5;
   unsigned long long gcd(unsigned long long a, unsigned long long b){
       if (!a) return 1;
       while (a) swap(a, b\%=a);
       return b;
   }
   unsigned long long get(unsigned long long a, unsigned long long b){
9
       if (a > b)
10
           return a-b;
11
       else
12
           return b-a;
13
   }
14
15
   unsigned long long pollard(unsigned long long n) {
16
       unsigned long long x = (rand() + 1) \% n, y = 1, g;
       int stage = 2, i = 0;
       g = gcd(get(x, y), n);
19
       while (g == 1){
20
           if (i == max_step)
21
               break;
           if (i == stage){
23
                y = x;
                stage <<= 1;
           }
           x = (x * (__int128)x + 1) \% n;
27
           i++;
28
           g = gcd(get(x, y), n);
29
       }
30
       return g;
31
```

#### pragma

#pragma GCC optimize(''03,no-stack-protector'') #pragma GCC target(''sse,sse2,sse4,ssse3,popcnt,abm,mmx,avx,tune=native'')

# Алгебра Pick

$$B + \Gamma / 2 - 1 = AREA,$$

где B — количество целочисленных точек внутри многоугольника, а  $\Gamma$  — количество целочисленных точек на границе многоугольника.

#### Newton

$$x_{i+1} = x_i - \frac{f(x_i)}{f'(x_i)}$$

Catalan
$$C_n = \sum_{k=0}^{n-1} C_k C_{n-1-k}$$

$$C_i = \frac{1}{n+1} {2n \choose n}$$

#### Кол-во графов

$$G_N := 2^{n(n-1)/2}$$

Количество связных помеченных графов

$$Conn_N = G_N - \frac{1}{N} \sum_{K=1}^{N-1} K\binom{N}{K} Conn_K G_{N-K}$$

Количество помеченных графов с К компонентами связности

$$D[N][K] = \sum_{S=1}^{N} {N-1 \choose S-1} Conn_S D[N-S][K-1]$$

#### Miller-Rabbin

# Интегрирование по формуле Симпсона

$$\int_{a}^{b} f(x)dx?$$

$$x_{i} := a + ih, i = 0 \dots 2n$$

$$h = \frac{b-a}{2n}$$

$$\int_{O(n^4)} \left( f(x_0) + 4f(x_1) + 2f(x_2) + 4f(x_3) + 2f(x_4) + \dots + 4f(x_{2n-1}) + f(x_{2n}) \right) \frac{h}{3}$$

# Простые числа

1009,1013;10007,10009;100003,100019 1000003,1000033;10000019,10000079 100000007,100000037 10000000019,10000000033 100000000039,100000000061

 $10000000000031, 10000000000067 \\ 1000000000000061, 100000000000069 \\ 1000000000000000003, 100000000000000009$ 

#### Числа для Фурье

- prime:  $7340033 = 7 \cdot 2^{20} + 1; w : 5(w^{2^{20}} = 1)$
- prime:  $13631489 = 13 \cdot 2^{20} + 1$ ;  $w : 3(w^{2^{20}} = 1)$
- prime:  $23068673 = 11 \cdot 2^{21} + 1$ ;  $w: 38(w^{2^{21}} = 1)$
- prime:  $69206017 = 33 \cdot 2^{21} + 1$ ;  $w: 45(w^{2^{21}} = 1)$
- prime:  $81788929 = 39 \cdot 2^{21} + 1$ ;  $w: 94(w^{2^{21}} = 1)$
- prime:  $104857601 = 25 \cdot 2^{22} + 1$ ;  $w : 21(w^{2^{22}} = 1)$
- prime:  $113246209 = 27 \cdot 2^{22} + 1$ ;  $w : 66(w^{2^{22}} = 1)$
- prime:  $138412033 = 33 \cdot 2^{22} + 1$ ;  $w : 30(w^{2^{22}} = 1)$
- prime:  $167772161 = 5 \cdot 2^{25} + 1$ ;  $w: 17(w^{2^{25}} = 1)$
- prime:  $469762049 = 7 \cdot 2^{26} + 1$ ;  $w: 30(w^{2^{26}} = 1)$
- prime:  $998244353 = 7 \cdot 17 \cdot 2^{23} + 1$ ;  $w: 3^{7*17}$ .

#### Erdős-Gallai theorem

A sequence of non-negative integers  $d_1 \ge \cdots \ge d_n$  can be represented as the degree sequence of a finite simple graph on n vertices if and only if  $d_1 + \cdots + d_n$   $d_1 + \cdots + d_n$  is even and

 $\sum_{i=1}^k d_i \le k(k-1) + \sum_{i=k+1}^n \min(d_i, k) \text{ holds for every } k \text{ in } 1 \le k \le n.$ 

```
/** Begin fast allocation */
  const int MAX_MEM = 5e8;
   int mpos = 0;
   char mem[MAX_MEM];
   inline void * operator new ( size_t n ) {
       assert((mpos += n) <= MAX_MEM);</pre>
       return (void *) (mem + mpos - n);
   inline void operator delete ( void * ) noexcept { } // must have!
   /** End fast allocation */
12
13
   #define pb push_back
14
  #define mp make_pair
  #define fst first
  #define snd second
  #define ll long long
  #define form(i, n) for (int i = 0; i < (int) (n); i++)
   #define for lr(i, l, r) for (int i = (int) l; i \leq (int) (r); i++)
20
   #define forrl(i, r, l) for (int i = (int) r; i \ge (int) (l); i--)
21
22
   /** Interface */
23
   inline int readChar();
   template <class T = int> inline T readInt();
   template <class T> inline void writeInt( T x, char end = 0 );
27
   inline void writeChar( int x );
   inline void writeWord( const char *s );
30
   /** Read */
31
   static const int buf_size = 2048;
33
34
   inline int getChar() {
35
       static char buf[buf_size];
       static int len = 0, pos = 0;
37
       if (pos == len)
           pos = 0, len = fread(buf, 1, buf_size, stdin);
       if (pos == len)
           return -1;
41
       return buf[pos++];
42
   }
43
44
   inline int readWord(char * buffer) {
45
       int c = getChar();
       while (c <= 32) {
           c = getChar();
49
       int len = 0;
```

```
while (c > 32) {
52
            *buffer = (char) c;
53
            c = getChar();
            buffer++;
            len++;
        }
        return len;
   }
59
60
   inline int readChar() {
61
        int c = getChar();
62
        while (c <= 32)
63
            c = getChar();
64
        return c;
65
   }
66
67
   template <class T>
   inline T readInt() {
        int s = 1, c = readChar();
        T x = 0;
        if (c == '-')
72
            s = -1, c = getChar();
        while ('0' <= c && c <= '9')
            x = x * 10 + c - '0', c = getChar();
        return s == 1 ? x : -x;
   }
78
   /** Write */
79
   static int write_pos = 0;
81
   static char write_buf[buf_size];
   inline void writeChar( int x ) {
        if (write_pos == buf_size)
85
            fwrite(write_buf, 1, buf_size, stdout), write_pos = 0;
86
        write_buf[write_pos++] = x;
   }
   template <class T>
   inline void writeInt( T x, char end ) {
91
        if (x < 0)
92
            writeChar('-'), x = -x;
93
        char s[24];
        int n = 0;
        while (x \mid \mid !n)
            s[n++] = '0' + x \% 10, x /= 10;
        while (n--)
99
            writeChar(s[n]);
100
        if (end)
101
            writeChar(end);
102
```

```
}
103
104
   inline void writeWord( const char *s ) {
105
        while (*s)
106
            writeChar(*s++);
107
108
109
   struct Flusher {
110
        ~Flusher() {
111
            if (write_pos)
112
                 fwrite(write_buf, 1, write_pos, stdout), write_pos = 0;
113
        }
114
   } flusher;
```

```
struct line {
       ll k, b;
       11 at(ll x) const {
           return k * x + b;
       }
   };
    double intersec(line a, line b) {
       return 1.0 * (b.b - a.b) / (a.k - b.k);
    struct convex_hull_trick {
10
       vector < double > x = {-1e18};
       vector<line> lines;
        void add(line 1) {
           // l.k increasing
           if (lines.empty()) {
                lines.pb(1);
           } else {
                while (lines.size() > 1 && intersec(l, lines[lines.size() - 2]) <</pre>
                \rightarrow x.back()) {
                    lines.pop_back();
19
                    x.pop_back();
20
                }
                x.push_back(intersec(1, lines.back()));
22
                lines.push_back(1);
           }
       }
   };
26
    struct cht_forward_iterator {
27
       int ci = 0;
        11 promote(const convex_hull_trick& cht, ll value) {
29
           while (ci < (int)cht.x.size() - 1 && cht.x[ci + 1] < value)</pre>
                ci++;
           return cht.lines[ci].at(value);
       }
   };
34
    const int g = 275;
35
    struct sqrt_dec {
36
       struct block {
           vector<int> bs;
           convex_hull_trick cht;
           cht_forward_iterator it;
            block(vector<int> b) {
                bs = b;
                int k = b.size();
                forn(i, k) {
                    cht.add({ b[i], 111 * b[i] * (k - i) });
                }
           }
            11 value(11 x) {
48
                if (cht.lines.empty())
                    return 0;
50
```

```
return it.promote(cht, x);
51
           }
52
       };
        void insert(block& bl, int b) {
           auto v = std::move(bl.bs);
           v.insert(lower_bound(all(v), b), b);
           bl = block(std::move(v));
       }
        vector<block> blocks;
59
        sqrt_dec(int n) {
           blocks.resize((n + g - 1) / g, block({}));
        void add(int i, int b) {
           insert(blocks[i / g], b);
        11 get_max() {
           int sm = 0;
           11 \text{ ans} = 0;
           for (int i = blocks.size() - 1; i >= 0; i--) {
               ans = max(ans, blocks[i].value(sm));
               sm += blocks[i].bs.size();
           }
           return ans;
73
       }
74
   };
```

```
struct treap{
       map<char, int> go;
       int len, suff;
       long long sum_in;
       treap(){}
   };
   treap v[max_n * 4];
   int last = 0;
   int add_treap(int max_len){
11
       v[number].sum_in = 0;
       v[number].len = max_len;
13
       v[number].suff = -1;
14
       number++;
       return number - 1;
16
   }
17
   void add_char(char c){
       int cur = last;
20
       int new_treap = add_treap(v[cur].len + 1);
21
       last = new_treap;
22
       while (\operatorname{cur} != -1){
23
           if (v[cur].go.count(c) == 0){
                v[cur].go[c] = new_treap;
                v[new_treap].sum_in += v[cur].sum_in;
                cur = v[cur].suff;
                if (cur == -1)
                    v[new_treap].suff = 0;
           }else{
                int a = v[cur].go[c];
                if (v[a].len == v[cur].len + 1){
                    v[new_treap].suff = a;
                }else{
                    int b = add_treap(v[cur].len + 1);
35
                    v[b].go = v[a].go;
                    v[b].suff = v[a].suff;
                    v[new_treap].suff = b;
                    while (cur != -1 && v[cur].go.count(c) != 0 && v[cur].go[c] == a){
                        v[cur].go[c] = b;
                        v[a].sum_in -= v[cur].sum_in;
                        v[b].sum_in += v[cur].sum_in;
42
                        cur = v[cur].suff;
                    v[a].suff = b;
                }
                return;
           }
48
       }
49
  }
50
```

```
int k = sqrt((double)p) + 2;
   for (int i = k; i >= 1; i--)
       mp[bin(b, (i * 111 * k) \% (p-1), p)] = i;
  bool answered = false;
   int ans = INT32_MAX;
   for (int i = 0; i \le k; i++){
       int sum = (n * 111 * bin(b, i, p)) % p;
       if (mp.count(sum) != 0){
10
           int an = mp[sum] * 111 * k - i;
           if (an < p)
12
               ans = min(an, ans);
13
       }
15 }
```

```
int gcd (int a, int b, int & x, int & y) {
           if (a == 0) {
                   x = 0; y = 1;
                   return b;
           }
           int x1, y1;
           int d = gcd (b%a, a, x1, y1);
           x = y1 - (b / a) * x1;
           y = x1;
           return d;
10
  }
11
      linear sieve
   const int N = 1000000;
   int pr[N + 1], sz = 0;
   /* minimal prime, mobius function, euler function */
   int lp[N + 1], mu[N + 1], phi[N + 1];
   lp[1] = mu[1] = phi[1] = 1;
   for (int i = 2; i <= N; ++i) {
           if (lp[i] == 0)
                   lp[i] = pr[sz++] = i;
           for (int j = 0; j < sz && pr[j] <= lp[i] && i * pr[j] <= N; ++j)
                   lp[i * pr[j]] = pr[j];
       mu[i] = lp[i] == lp[i / lp[i]] ? 0 : -1 * mu[i / lp[i]];
14
       phi[i] = phi[i / lp[i]] * (lp[i] == lp[i / lp[i]] ? lp[i] : lp[i] - 1);
15
   }
16
      kasai
   //p[i] -- prefix (id of first symbol) on i-th position of suff array (from 0)
   for (int i = 0; i < n; i++)
       r[p[i]] = i;
   int k = 0;
   for (int j = 0; j < n; j++){
       int i = r[j];
       k--;
       if (k < 0 | | i == n - 1)
           k = 0;
       if (i != n - 1)
10
           while (s[p[i] + k] == s[p[i + 1] + k])
11
               k++;
       lcp[i] = k;
   }
14
   for (int i = 0; i + 1 < n; i++)
15
       cout << lcp[i] << " ";
```

```
fill(par, par + 301, -1);
   fill(par2, par2 + 301, -1);
   int ans = 0;
   for (int v = 0; v < n; v++){
       memset(useda, false, sizeof(useda));
       memset(usedb, false, sizeof(usedb));
       useda[v] = true;
       for (int i = 0; i < n; i++)
           w[i] = make_pair(a[v][i] + row[v] + col[i], v);
       memset(prev, 0, sizeof(prev));
       int pos;
       while (true){
13
           pair<pair<int, int>, int> p = make_pair(make_pair(1e9, 1e9), 1e9);
14
           for (int i = 0; i < n; i++)
               if (!usedb[i])
16
                   p = min(p, make_pair(w[i], i));
           for (int i = 0; i < n; i++)
               if (!useda[i])
                   row[i] += p.first.first;
           for (int i = 0; i < n; i++)
21
               if (!usedb[i]){
22
                    col[i] -= p.first.first;
23
                   w[i].first -= p.first.first;
           ans += p.first.first;
           usedb[p.second] = true;
           prev[p.second] = p.first.second; //из второй в первую
28
           int x = par[p.second];
           if (x == -1){
30
               pos = p.second;
               break;
           }
           useda[x] = true;
           for (int j = 0; j < n; j++)
35
               w[j] = min(w[j], \{a[x][j] + row[x] + col[j], x\});
37
       while (pos != -1){
           int nxt = par2[prev[pos]];
           par[pos] = prev[pos];
41
           par2[prev[pos]] = pos;
42
           pos = nxt;
       }
44
   }
45
   cout << ans << ''\n'';
   for (int i = 0; i < n; i++)
47
       cout << par[i] + 1 << "" << i + 1 << "\n";
48
```

```
struct edge{
       int from, to;
       int c, f, num;
       edge(int from, int to, int c, int num):from(from), to(to), c(c), f(0),
        \rightarrow num(num){}
       edge(){}
   };
   const int max_n = 600;
   edge eds[150000];
   int num = 0;
   int it[max_n];
   vector<int> gr[max_n];
   int s, t;
   vector<int> d(max_n);
   bool bfs(int k) {
       queue<int> q;
       q.push(s);
19
       fill(d.begin(), d.end(), -1);
20
       d[s] = 0;
       while (!q.empty()) {
22
           int v = q.front();
           q.pop();
           for (int x : gr[v])
                if (d[eds[x].to] == -1 \&\& eds[x].c - eds[x].f >= (1 << k)){
                    d[eds[x].to] = d[v] + 1;
27
                    q.push(eds[x].to);
                }
29
       }
       return (d[t] != -1);
   }
33
34
   int dfs(int v, int flow, int k) {
35
       if (flow < (1 << k))
36
           return 0;
       if (v == t)
           return flow;
       for (; it[v] < gr[v].size(); it[v]++) {</pre>
40
           if (d[v] + 1 != d[eds[gr[v][it[v]]].to])
                continue;
           int num = gr[v][it[v]];
43
           int res = dfs(eds[gr[v][it[v]]].to, min(flow, eds[gr[v][it[v]]].c -
               eds[gr[v][it[v]]].f), k);
           if (res){
45
                eds[num].f += res;
                eds[num ^1].f -= res;
47
                return res;
           }
49
```

```
}
50
       return 0;
51
   }
52
53
   void add(int fr, int to, int c, int nm) {
54
       gr[fr].push_back(num);
55
       eds[num++] = edge(fr, to, c, nm);
56
       gr[to].push_back(num);
       eds[num++] = edge(to, fr, 0, nm); //corrected c
   }
59
60
   int ans = 0;
61
       for (int k = 30; k >= 0; k--)
62
           while (bfs(k)) {
63
                memset(it, 0, sizeof(it));
                while (int res = dfs(s, 1e9 + 500, k))
                    ans += res;
           }
   // decomposition
70
   int path_num = 0;
   vector<int> paths[550];
73
   int flows[550];
   int decomp(int v, int flow) {
76
       if (flow < 1)
77
           return 0;
       if (v == t) {
79
           path_num++;
           flows[path_num - 1] = flow;
           return flow;
       }
       for (int i = 0; i < gr[v].size(); i++) {</pre>
           int num = gr[v][i];
           int res = decomp(eds[num].to, min(flow, eds[num].f));
                      {
           if (res)
                eds[num].f -= res;
                paths[path_num - 1].push_back(eds[num].num);
                return res;
90
           }
91
       }
       return 0;
93
   }
94
   while (decomp(s, 1e9 + 5));
```

```
long long ans = 0;
   int mx = 2 * n + 2;
  memset(upd, 0, sizeof(upd));
   for (int i = 0; i < mx; i++)
       dist[i] = inf;
  dist[st] = 0;
   queue<int> q;
  q.push(st);
   upd[st] = 1;
10
   while (!q.empty()){
       int v = q.front();
       q.pop();
13
       if (upd[v]){
14
                                         {
           for (int x : gr[v])
                edge &e = edges[x];
16
                if (e.c - e.f > 0 \&\& dist[v] != inf \&\& dist[e.to] > dist[v] + e.w) {
                    dist[e.to] = dist[v] + e.w;
                    if (!upd[e.to])
                        q.push(e.to);
                    upd[e.to] = true;
21
                    p[e.to] = x;
22
                }
23
           }
           upd[v] = false;
       }
   }
27
28
   for (int i = 0; i < k; i++){
29
       for (int i = 0; i < mx; i++)</pre>
30
           d[i] = inf;
       d[st] = 0;
       memset(used, false, sizeof(used));
       set<pair<int, int> > s;
       s.insert(make_pair(0, st));
35
       for (int i = 0; i < mx; i++){
           int x;
37
           while (!s.empty() && used[(s.begin() -> second)]){
                s.erase(s.begin());
           }
           if (s.empty())
41
                break;
42
           x = s.begin() -> second;
           used[x] = true;
44
           s.erase(s.begin());
           for (int i = 0; i < gr[x].size(); i++){
                edge &e = edges[gr[x][i]];
                if (!used[e.to] \&\& e.c - e.f > 0){
                    if (d[e.to] > d[x] + (e.c - e.f) * e.w + dist[x] - dist[e.to]){}
49
                        d[e.to] = d[x] + (e.c - e.f) * e.w + dist[x] - dist[e.to];
                        p[e.to] = gr[x][i];
51
```

```
s.insert(make_pair(d[e.to], e.to));
52
                    }
53
                }
           }
           dist[x] += d[x];
       }
       int pos = t;
       while (pos != st){
                int id = p[pos];
60
                edges[id].f += 1;
           edges[id ^ 1].f -= 1;
           pos = edges[id].from;
       }
64
  }
65
```

}

```
string min_cyclic_shift (string s) {
           s += s;
           int n = (int) s.length();
           int i=0, ans=0;
           while (i < n/2) {
                    ans = i;
                    int j=i+1, k=i;
                    while (j < n \&\& s[k] <= s[j]) {
                            if (s[k] < s[j])
                                     k = i;
                             else
                                     ++k;
                            ++j;
14
                    while (i <= k)
                                     i += j - k;
           }
16
           return s.substr (ans, n/2);
17
  }
      Sum over subsets
  for(int i = 0; i<(1<<N); ++i)</pre>
           F[i] = A[i];
  for(int i = 0; i < N; ++i) for(int mask = 0; mask < (1<<N); ++mask){
           if(mask & (1<<i))</pre>
                    F[mask] += F[mask^(1<< i)];
```

```
vector<int> getZ(string s){
       vector<int> z;
       z.resize(s.size(), 0);
       int 1 = 0, r = 0;
       for (int i = 1; i < s.size(); i++){</pre>
            if (i <= r)
                z[i] = min(r - i + 1, z[i - 1]);
            while (i + z[i] < s.size() \&\& s[z[i]] == s[i + z[i]])
                z[i]++;
            if (i + z[i] - 1 > r){
                r = i + z[i] - 1;
                1 = i;
            }
13
       }
14
       return z;
15
   }
16
17
   vector<int> getP(string s){
       vector<int> p;
       p.resize(s.size(), 0);
20
       int k = 0;
21
       for (int i = 1; i < s.size(); i++){</pre>
22
            while (k > 0 \&\& s[i] == s[k])
23
                k = p[k - 1];
            if (s[i] == s[k])
                k++;
            p[i] = k;
28
       return p;
29
   }
30
   vector<int> getH(string s){
32
       vector<int> h;
33
       h.resize(s.size() + 1, 0);
34
       for (int i = 0; i < s.size(); i++)</pre>
35
            h[i + 1] = ((h[i] * 111 * pow) + s[i] - 'a' + 1) \% mod;
       return h;
37
   }
38
   int getHash(vector<int> &h, int 1, int r){
40
       int res = (h[r + 1] - h[1] * p[r - 1 + 1]) \% mod;
41
       if (res < 0)
42
            res += mod;
43
       return res;
44
   }
45
```

#### suf array + lcp

43 }

```
char *s; // входная строка
   int n; // длина строки
   const int maxlen = ...; // максимальная длина строки
   const int alphabet = 256; // pasmep andaeuma, <= maxlen
   int p[maxlen], cnt[maxlen], c[maxlen];
   memset (cnt, 0, alphabet * sizeof(int));
   for (int i=0; i<n; ++i)
           ++cnt[s[i]];
   for (int i=1; i<alphabet; ++i)</pre>
           cnt[i] += cnt[i-1];
   for (int i=0; i<n; ++i)</pre>
12
           p[--cnt[s[i]]] = i;
   c[p[0]] = 0;
14
   int classes = 1;
   for (int i=1; i<n; ++i) {
           if (s[p[i]] != s[p[i-1]]) ++classes;
           c[p[i]] = classes-1;
   }
19
   //
20
   int pn[maxlen], cn[maxlen];
21
   for (int h=0; (1<<h)<n; ++h) {
22
           for (int i=0; i<n; ++i) {</pre>
23
                    pn[i] = p[i] - (1 << h);
                    if (pn[i] < 0) pn[i] += n;
           }
           memset (cnt, 0, classes * sizeof(int));
           for (int i=0; i<n; ++i)</pre>
28
                    ++cnt[c[pn[i]]];
           for (int i=1; i < classes; ++i)</pre>
                    cnt[i] += cnt[i-1];
           for (int i=n-1; i>=0; --i)
                    p[--cnt[c[pn[i]]]] = pn[i];
           cn[p[0]] = 0;
           classes = 1;
           for (int i=1; i<n; ++i) {
                    int mid1 = (p[i] + (1 << h)) \% n, mid2 = (p[i-1] + (1 << h)) \% n;
                    if (c[p[i]] != c[p[i-1]] || c[mid1] != c[mid2])
                             ++classes;
                    cn[p[i]] = classes-1;
40
41
           memcpy (c, cn, n * sizeof(int));
42
```

```
int num = 0;
   long long phi = n, nn = n;
   for (long long x:primes){
       if (x*x>nn)
           break;
       if (nn \% x == 0){
           while (nn \% x == 0)
                nn /= x;
           phi -= phi/x;
           num++;
       }
   }
   if (nn != 1){
13
       phi -= phi/nn;
14
       num++;
15
   }
16
   if (!((num == 1 && n % 2 != 0) || n == 4 || n == 2 || (num == 2 && n % 2 == 0 && n
       % 4 != 0))){
       cout << "-1\n";
       continue;
19
20
   vector<long long> v;
21
   long long pp = phi;
   for (long long x:primes){
       if (x*x>pp)
           break;
       if (pp \% x == 0){
26
           while (pp \% x == 0)
27
                pp /= x;
           v.push_back(x);
       }
   }
31
   if (pp != 1){
       v.push_back(pp);
33
34
   while (true){
35
       long long a = primes[rand()%5000]%n;
36
       if (gcd(a, n) != 1)
           continue;
       bool bb = false;
       for (long long x:v)
           if (pow(a, phi/x) == 1){
                bb = true;
                break;
           }
       if (!bb){
           cout << a << ''\n'';
46
           break;
47
       }
48
   }
49
```

```
const int LOG = 19;
  const int N = (1 \ll LOG);
   typedef std::complex<double> cd;
   int rev[N];
   cd W[N];
   void precalc() {
       const double pi = std::acos(-1);
10
       for (int i = 0; i != N; ++i)
           W[i] = cd(std::cos(2 * pi * i / N), std::sin(2 * pi * i / N));
       int last = 0;
       for (int i = 1; i != N; ++i) {
           if (i == (2 << last))</pre>
               ++last;
           rev[i] = rev[i ^ (1 << last)] | (1 << (LOG - 1 - last));
       }
20
   }
21
22
   void fft(vector<cd>& a) {
23
       for (int i = 0; i != N; ++i)
24
           if (i < rev[i])</pre>
                std::swap(a[i], a[rev[i]]);
       for (int lvl = 0; lvl != LOG; ++lvl)
           for (int start = 0; start != N; start += (2 << lvl))</pre>
               for (int pos = 0; pos != (1 << lvl); ++pos) {</pre>
30
                    cd x = a[start + pos];
                    cd y = a[start + pos + (1 << lvl)];
                    y *= W[pos << (LOG - 1 - lvl)];
35
                    a[start + pos] = x + y;
                    a[start + pos + (1 << lvl)] = x - y;
37
               }
   }
40
   void inv_fft(vector<cd>& a) {
41
       fft(a);
42
       std::reverse(a.begin() + 1, a.end());
43
44
       for (cd& elem: a)
           elem /= N;
   }
   void fast_fourier(vector<int>& a) { // AND-FFT.
       for (int k = 1; k < SZ(a); k *= 2)
           for (int start = 0; start < (1 << K); start += 2 * k) {
```

```
for (int off = 0; off < k; ++off) {</pre>
                    int a_val = a[start + off];
                    int b_val = a[start + k + off];
                    a[start + off] = b_val;
                    a[start + k + off] = add(a_val, b_val);
                }
10
           }
11
   }
12
13
   void inverse_fast_fourier(vector<int>& a) {
       for (int k = 1; k < SZ(a); k *= 2)
15
            for (int start = 0; start < (1 << K); start += 2 * k) {</pre>
16
                for (int off = 0; off < k; ++off) {</pre>
17
                    int a_val = a[start + off];
                    int b_val = a[start + k + off];
19
                    a[start + off] = sub(b_val, a_val);
                    a[start + k + off] = a_val;
                }
23
           }
24
  }
25
```

```
struct Edge {
       int a;
       int b;
       int cost;
   };
   vector<int> negative_cycle(int n, vector<Edge> &edges) {
       // O(nm), return ids of edges in negative cycle
       vector<int> d(n);
10
       vector<int> p(n, -1); // last edge ids
       const int inf = 1e9;
       int x = -1;
       for (int i = 0; i < n; i++) {
16
           x = -1;
           for (int j = 0; j < edges.size(); j++) {</pre>
               Edge &e = edges[j];
20
               if (d[e.b] > d[e.a] + e.cost) {
21
                    d[e.b] = max(-inf, d[e.a] + e.cost);
22
                    p[e.b] = j;
23
                    x = e.b;
               }
           }
       }
28
       if (x == -1)
           return vector<int>(); // no negative cycle
30
       for (int i = 0; i < n; i++)
           x = edges[p[x]].a;
       vector<int> result;
       for (int cur = x; ; cur = edges[p[cur]].a) {
           if (cur == x && result.size() > 0) break;
37
           result.push_back(p[cur]);
       reverse(result.begin(), result.end());
41
       return result;
42
   }
43
44
   vector<int> min_avg_cycle(int n, vector<Edge> &edges) {
45
       const int inf = 1e3;
       for (auto &e : edges)
           e.cost *= n * n;
49
       int 1 = -inf;
```

```
int r = inf;
52
       while (l + 1 < r) {
53
            int m = (1 + r) / 2;
            for (auto &e : edges)
                e.cost -= m;
            if (negative_cycle(n, edges).empty())
            else
60
                r = m;
            for (auto &e : edges)
                e.cost += m;
       }
65
       if (r >= 0) // if only negative needed
            return vector<int>();
       for (auto &e : edges)
            e.cost -= r;
       vector<int> result = negative_cycle(n, edges);
       for (auto &e : edges)
            e.cost += r;
       for (auto &e : edges)
            e.cost /= n * n;
81
       return result;
   }
83
84
   struct edge {
85
       int from, to;
86
       int c, f, cost;
   };
   const int max_n = 200;
91
   vector<int> gr[max_n];
92
   vector<edge> edges;
93
   void add(int fr, int to, int c, int cost) {
95
       gr[fr].push_back(edges.size());
       edges.push_back({fr, to, c, 0, cost});
       gr[to].push_back(edges.size());
       edges.push_back({to, fr, 0, 0, -cost}); // single
99
100
101
   void calc_min_circulation(int n) {
```

```
while (true) {
103
             vector<Edge> eds;
104
             vector<int> origin;
105
106
             for (int i = 0; i < edges.size(); i++) {</pre>
107
                 edge &e = edges[i];
108
                 if (e.c - e.f > 0) {
109
                      eds.push_back({e.from, e.to, e.cost});
110
                      origin.push_back(i);
111
                 }
112
             }
113
114
             vector<int> cycle = negative_cycle(n, eds);
115
116
             if (cycle.empty())
117
                 break;
118
119
             for (auto id : cycle) {
120
                 int x = origin[id];
                 edges[x].f += 1;
122
                 edges[x ^1].f = 1;
123
             }
124
        }
125
   }
126
```

```
Добавим к нашему графу вершину ѕ и рёбра из неё во все остальные вершины.
        Запустим алгоритм Форда-Беллмана и попросим его построить нам квадратную
        матрицу со следующим условием: d[i][u] - длина минимального пути от s до u
        ровно из і ребер. Тогда длина оптимального цикла и* минимального среднего
    \hookrightarrow
        веса вычисляется как minumaxkd[n][u]-d[k][u]n-k.
  Достаточно будет доказать это правило для \mu *=0, так как для других \mu * можно
       просто отнять эту величину от всех ребер и получить снова случай с и*=0.
  Чтобы найти цикл после построения матрицы d[k][u], запомним, при каких u и k
       достигается оптимальное значение \mu *, и, используя d[n][u], поднимемся по
       указателям предков. Как только мы попадем в уже посещенную вершину - мы нашли
       цикл минимального среднего веса.
  Этот алгоритм работает за O(VE)
   func findMinCycle(Graph G)
        // вводим мнимую вершину s, от которой проведём рёбра нулевого веса в каждую
10
            вершину графа
        \hookrightarrow
        Node s
11
        Edge[] e
12
        insert(s)
        i = 0
        for u in G
            e[i].begin = s
            e[i].end = u
17
            e[i].weight = 0
19
        // строим матрицу кратчайших расстояний, запустив алгоритм Форда-Беллмана из
            вершины ѕ
        fordBellman(s)
        // т - длина оптимального цикла
```

m = minumaxk((d[n][u] - d[k][u]) / (n - k))

23

 $\mathbf{D}M$ 

# Кол-во корневых деревьев:

$$t(G) = \frac{1}{n}\lambda_2 \dots \lambda_n \ (\lambda_1 = 0)$$

# Кол-во эйлеровых циклов:

$$e(D) = t^-(D,x) \cdot \prod_{y \in D} (outdeg(y) - 1)!$$

# Наличие совершенного паросочетания:

T — матрица с нулями на диагонали. Если есть ребро (i,j), то  $a_{i,j}:=x_{i,j},\ a_{j,i}=-x_{i,j}$   $\det(T)=0\Leftrightarrow$  нет совершенного паросочетания.

# Whitespace code FFT