Pollard

```
const int max_step = 4e5;
   unsigned long long gcd(unsigned long
   → long a, unsigned long long b){
       if (!a) return 1;
       while (a) swap(a, b\%=a);
       return b;
   }
   unsigned long long get(unsigned long
       long a, unsigned long long b){
       if (a > b)
10
           return a-b;
11
       else
12
           return b-a;
13
   }
14
15
   unsigned long long pollard(unsigned long
       long n){
       unsigned long long x = (rand() + 1)
17
        \rightarrow % n, y = 1, g;
       int stage = 2, i = 0;
18
       g = gcd(get(x, y), n);
19
       while (g == 1){
20
           if (i == max_step)
                break;
            if (i == stage){
23
                y = x;
24
                stage <<= 1;
26
           x = (x * (_int128)x + 1) \% n;
27
           i++;
           g = gcd(get(x, y), n);
       }
       return g;
31
32
   }
```

Team Reference

pragma

#pragma GCC optimize("'03, no-stack-protecto") #pragma GCC target(''sse,sse2,sse4,ssse3,popcnt,abm,mmx,avx,tune=native'')

Алгебра Pick

$$B + \Gamma / 2 - 1 = AREA$$
,

где В — количество целочисленных точек внутри многоугольника, а Γ — количество целочисленных точек на границе многоугольника.

Newton
$$x_{i+1} = x_i - \frac{f(x_i)}{f'(x_i)}$$

$$C_n = \sum_{k=0}^{n-1} C_k C_{n-1-k}$$

$$C_i = \frac{1}{n+1} {2n \choose n}$$

Кол-во графов

$$G_N := 2^{n(n-1)/2}$$

Количество связных помеченных графов

$$Conn_N = G_N - \frac{1}{N} \sum_{K=1}^{N-1} K\binom{N}{K} Conn_K G_{N-K}$$

Количество помеченных графов с К понентами связности

$$D[N][K] = \sum_{S=1}^{N} {N-1 \choose S-1} Conn_S D[N-S][K-1]$$

Miller-Rabbin

return a==1 ? PRIME : NOT PRIME

Интегрирование по формуле Симпсона $\int_a^b f(x)dx$?

$$\begin{aligned}
y_a f(x) & \text{div.} \\
x_i &:= a + ih, i = 0 \dots 2n \\
h &= \frac{b-a}{2n}
\end{aligned}$$

$$\int = (f(x_0) + 4f(x_1) + 2f(x_2) + 4f(x_3) + 2f(x_4) + \dots + 4f(x_{2n-1}) + f(x_{2n})) \frac{h}{3}$$

 $O(n^4)$.

Простые числа

1009,1013;10007,10009;100003,100019

1000003,1000033;10000019,10000079

1,00000007,100000037 10000000019,10000000033

100000000000031,10000000000067

10000000000000061,10000000000000069

100000000000000003,100000000000000000

Числа для Фурье

- prime: $7340033 = 7 \cdot 2^{20} + 1$; $w : 5(w^{2^{20}} = 1)$
- prime: $13631489 = 13 \cdot 2^{20} + 1$; $w: 3(w^{2^{20}} = 1)$
- prime: $23068673 = 11 \cdot 2^{21} + 1$; $w: 38(w^{2^{21}} = 1)$
- prime: $69206017 = 33 \cdot 2^{21} + 1$; $w: 45(w^{2^{21}} = 1)$
- prime: $81788929 = 39 \cdot 2^{21} + 1$; $w: 94(w^{2^{21}} = 1)$
- prime: $104857601 = 25 \cdot 2^{22} + 1$; $w : 21(w^{2^{22}}) = 25 \cdot 2^{22} + 1$
- prime: $113246209 = 27 \cdot 2^{22} + 1$; $w : 66(w^{2^{22}}) = 66(w^{2^{22}})$ 1)
- prime: $138412033 = 33 \cdot 2^{22} + 1$; $w: 30(w^{2^{22}}) = 33 \cdot 2^{22} + 1$ 1)
- prime: $167772161 = 5 \cdot 2^{25} + 1$; $w : 17(w^{2^{25}} = 1)$
- prime: $469762049 = 7 \cdot 2^{26} + 1$; $w : 30(w^{2^{26}} = 1)$
- prime: $998244353 = 7.17.2^{23} + 1$; $w: 3^{7*17}$.

Erdős-Gallai theorem

A sequence of non-negative integers $d_1 \ge \cdots \ge d_n$ can be represented as the degree sequence of a finite simple graph on n vertices if and only if $d_1 + \cdots + d_n \ d_1 + \cdots + d_n$ is even and

 $\sum_{i=1}^{k} d_i \le k(k-1) + \sum_{i=k+1}^{n} \min(d_i, k) \text{ holds for }$ every k in $1 \le k \le n$.

```
/** Begin fast allocation */
   const int MAX_MEM = 5e8;
                                                  inline int readWord(char * buffer) {
                                               45
   int mpos = 0;
                                                      int c = getChar();
                                               46
                                                      while (c <= 32) {
   char mem[MAX_MEM];
                                               47
   inline void * operator new ( size_t n ) 48
                                                           c = getChar();
                                                      }
       {
       assert((mpos += n) <= MAX_MEM);</pre>
                                               50
       return (void *) (mem + mpos - n);
                                                      int len = 0;
                                               51
                                                      while (c > 32) {
                                               52
                                                           *buffer = (char) c;
   inline void operator delete ( void * )
                                               53
   → noexcept { } // must have!
                                                           c = getChar();
                                                           buffer++;
                                               55
10
   /** End fast allocation */
                                                           len++;
11
                                               56
                                                      }
12
                                               57
                                                      return len;
13
                                               58
   #define pb push_back
                                                  }
                                               59
14
   #define mp make_pair
15
                                               60
   #define fst first
                                                  inline int readChar() {
                                               61
                                                      int c = getChar();
   #define snd second
                                               62
   #define ll long long
                                                      while (c \leq 32)
                                               63
18
   \#define\ forn(i,\ n)\ for\ (int\ i=0;\ i<
                                                           c = getChar();
   \rightarrow (int) (n); i++)
                                                      return c;
                                               65
   #define forlr(i, l, r) for (int i =
                                                  }
                                               66
   \rightarrow (int) l; i <= (int) (r); i++)
                                               67
   \#define\ forrl(i,\ r,\ l)\ for\ (int\ i=
                                                  template <class T>
      (int) r; i >= (int) (l); i--)
                                                  inline T readInt() {
                                                      int s = 1, c = readChar();
                                               70
   /** Interface */
                                                      T x = 0;
23
                                               71
                                                      if (c == '-')
                                               72
   inline int readChar();
                                                           s = -1, c = getChar();
                                               73
   template <class T = int> inline T
                                                      while ('0' \le c \&\& c \le '9')
                                               74
                                                           x = x * 10 + c - 0, c =
   → readInt();
   template <class T> inline void writeInt(

    getChar();

   \rightarrow T x, char end = 0);
                                                      return s == 1 ? x : -x;
   inline void writeChar( int x );
                                               77
   inline void writeWord( const char *s ); 78
                                                  /** Write */
                                               79
30
   /** Read */
                                                  static int write_pos = 0;
                                                  static char write_buf[buf_size];
   static const int buf_size = 2048;
                                               82
33
                                               83
34
   inline int getChar() {
                                                  inline void writeChar( int x ) {
35
                                               84
       static char buf[buf_size];
                                                      if (write_pos == buf_size)
                                               85
       static int len = 0, pos = 0;
                                                           fwrite(write_buf, 1, buf_size,
37
                                               86

    stdout), write_pos = 0;

       if (pos == len)
            pos = 0, len = fread(buf, 1,
                                                      write_buf[write_pos++] = x;
                                                  }
            → buf_size, stdin);
                                               88
       if (pos == len)
40
                                               89
            return -1;
                                                  template <class T>
41
                                               90
       return buf[pos++];
                                                  inline void writeInt( T x, char end ) {
                                               91
   }
                                                      if (x < 0)
43
                                               92
```

```
writeChar('-'), x = -x;
                                                   struct line {
93
                                                        ll k, b;
94
        char s[24];
                                                        11 at(ll x) const {
        int n = 0;
                                                            return k * x + b;
        while (x \mid | !n)
                                                        }
            s[n++] = '0' + x \% 10, x /= 10; 6
                                                   };
        while (n--)
                                                    double intersec(line a, line b) {
99
            writeChar(s[n]);
                                                        return 1.0 * (b.b - a.b) / (a.k -
100
        if (end)
                                                            b.k);
101
            writeChar(end);
                                                   }
102
                                                Q
                                                    struct convex_hull_trick {
   }
103
                                                10
                                                        vector<double> x = {-1e18};
                                                11
104
   inline void writeWord( const char *s )
                                                        vector<line> lines;
105
        while (*s)
                                                         void add(line 1) {
106
            writeChar(*s++);
                                                            // l.k increasing
                                                14
107
   }
                                                            if (lines.empty()) {
108
                                                15
                                                                 lines.pb(1);
109
                                                16
   struct Flusher {
                                                            } else {
110
                                                17
        ~Flusher() {
                                                                 while (lines.size() > 1 &&
            if (write_pos)
                                                                     intersec(1,
112
                                                                     lines[lines.size() - 2])
                 fwrite(write_buf, 1,
113
                    write_pos, stdout),
                                                                     < x.back()) {
                     write_pos = 0;
                                                                     lines.pop_back();
                                                19
        }
                                                                     x.pop_back();
114
                                                20
   } flusher;
                                                                 }
                                                21
                                                                 x.push_back(intersec(1,
                                                22

→ lines.back()));
                                                                 lines.push_back(1);
                                                23
                                                            }
                                                24
                                                        }
                                                25
                                                   };
                                                26
                                                    struct cht_forward_iterator {
                                                27
                                                        int ci = 0;
                                                28
                                                         ll promote(const convex_hull_trick&
                                                29
                                                             cht, ll value) {
                                                            while (ci < (int)cht.x.size() -</pre>
                                                30
                                                                 1 && cht.x[ci + 1] < value)
                                                                 ci++;
                                                31
                                                            return cht.lines[ci].at(value);
                                                        }
                                                33
                                                   };
                                                34
                                                    const int g = 275;
                                                35
                                                    struct sqrt_dec {
                                                36
                                                        struct block {
                                                37
                                                            vector<int> bs;
                                                38
                                                            convex_hull_trick cht;
                                                            cht_forward_iterator it;
                                                40
                                                             block(vector<int> b) {
                                                41
                                                                 bs = b;
                                                42
                                                                 int k = b.size();
                                                43
                                                                 forn(i, k) {
                                                44
```

```
cht.add({ b[i], 111 *
                                                   struct treap{
                                                1
45
                      \rightarrow b[i] * (k - i) });
                                                       map<char, int> go;
                                                2
                }
                                                        int len, suff;
46
            }
                                                        long long sum_in;
                                                4
47
             11 value(11 x) {
                                                       treap(){}
                if (cht.lines.empty())
                                                   };
                     return 0;
50
                return it.promote(cht, x);
                                                   treap v[max_n * 4];
            }
                                                   int last = 0;
52
       };
                                                10
                                                   int add_treap(int max_len){
        void insert(block& bl, int b) {
                                                11
            auto v = std::move(bl.bs);
                                                        v[number].sum_in = 0;
            v.insert(lower_bound(all(v), b),13
                                                        v[number].len = max_len;
                                                        v[number].suff = -1;
             \rightarrow b);
            bl = block(std::move(v));
                                                       number++;
                                                15
       }
                                                        return number - 1;
                                                16
58
        vector<block> blocks;
                                                   }
                                                17
         sqrt_dec(int n) {
            blocks.resize((n + g - 1) / g,
                                                   void add_char(char c){
                                                19
               block({}));
                                                        int cur = last;
                                                20
                                                        int new_treap = add_treap(v[cur].len
62
                                                21
         void add(int i, int b) {
                                                        \rightarrow + 1):
            insert(blocks[i / g], b);
                                                        last = new_treap;
                                                22
64
       }
                                                        while (\operatorname{cur} != -1){
                                                23
                                                            if (v[cur].go.count(c) == 0){
        11 get_max() {
            int sm = 0;
                                                                 v[cur].go[c] = new_treap;
                                                                 v[new_treap].sum_in +=
            11 \text{ ans} = 0;
                                                26

    v[cur].sum_in;

            for (int i = blocks.size() - 1;
69
                i >= 0; i--) {
                                                                 cur = v[cur].suff;
                                                27
                ans = max(ans,
                                                                 if (cur == -1)
70
                 → blocks[i].value(sm));
                                                                     v[new_treap].suff = 0;
                                                29
                sm += blocks[i].bs.size();
                                                            }else{
            }
                                                                 int a = v[cur].go[c];
                                                31
                                                                 if (v[a].len == v[cur].len +
            return ans;
                                                32
       }
74
   };
                                                                     v[new_treap].suff = a;
75
                                                33
                                                                 }else{
                                                34
                                                                     int b =
                                                35
                                                                      → add_treap(v[cur].len
                                                                      \rightarrow + 1);
                                                                     v[b].go = v[a].go;
                                                36
                                                                     v[b].suff = v[a].suff;
                                                37
                                                                     v[new_treap].suff = b;
                                                38
                                                                     while (cur != -1 &&
                                                39

    v[cur].go.count(c)

                                                                         != 0 && v[cur].go[c]
                                                                         == a){
                                                                          v[cur].go[c] = b;
                                                40
                                                                          v[a].sum_in =
                                                41

    v[cur].sum_in;
```

```
v[b].sum_in +=
                                                int k = sqrt((double)p) + 2;
42

    v[cur].sum_in;

                          cur = v[cur].suff;
                                                   for (int i = k; i >= 1; i--)
43
                                                        mp[bin(b, (i * 111 * k) \% (p-1), p)]
                     v[a].suff = b;
                                                        \hookrightarrow = i;
                }
                return;
                                                   bool answered = false;
47
            }
                                                   int ans = INT32_MAX;
       }
                                                   for (int i = 0; i <= k; i++){
49
   }
                                                        int sum = (n * 111 * bin(b, i, p)) %
50
                                                        \hookrightarrow p;
                                                        if (mp.count(sum) != 0){
                                                10
                                                            int an = mp[sum] * 111 * k - i;
                                                11
                                                            if (an < p)
                                                12
                                                                 ans = min(an, ans);
                                                13
                                                        }
                                                14
                                                   }
                                                15
```

```
int gcd (int a, int b, int & x, int & y)11
                                                      memset(prev, 0, sizeof(prev));
       {
   \hookrightarrow
                                                      int pos;
            if (a == 0) {
                                                      while (true){
                                              13
                                                          pair<pair<int, int>, int> p =
                    x = 0; y = 1;

→ make_pair(make_pair(1e9,
                    return b;
            }
                                                           → 1e9), 1e9);
                                                           for (int i = 0; i < n; i++)
            int x1, y1;
                                              15
            int d = gcd (b\%a, a, x1, y1);
                                                               if (!usedb[i])
                                              16
            x = y1 - (b / a) * x1;
                                                                   p = min(p,
                                              17
            y = x1;

→ make_pair(w[i], i));
                                                           for (int i = 0; i < n; i++)
            return d;
   }
                                                               if (!useda[i])
11
                                              19
                                                                   row[i] += p.first.first;
                                              20
     linear sieve
                                                           for (int i = 0; i < n; i++)
                                              21
                                                               if (!usedb[i]){
                                              22
                                                                   col[i] -= p.first.first;
   const int N = 1000000;
                                              23
                                                                   w[i].first -=
                                              24
2
   int pr[N + 1], sz = 0;
                                                                    → p.first.first;
                                                               }
   /* minimal prime, mobius function, euler<sup>25</sup>
                                                           ans += p.first.first;
       function */
                                                          usedb[p.second] = true;
   int lp[N + 1], mu[N + 1], phi[N + 1];
                                              27
                                                          prev[p.second] = p.first.second;
                                              28
                                                           → //из второй в первую
   lp[1] = mu[1] = phi[1] = 1;
                                                           int x = par[p.second];
   for (int i = 2; i <= N; ++i) {
                                                           if (x == -1){
            if (lp[i] == 0)
                                                               pos = p.second;
                    lp[i] = pr[sz++] = i;
10
            for (int j = 0; j < sz && pr[j] 32
                                                               break;
11
            \rightarrow <= lp[i] && i * pr[j] <= N; ^{33}
                                                          useda[x] = true;
               ++j)
                                                           for (int j = 0; j < n; j++)
                    lp[i * pr[j]] = pr[j];
12
                                                               w[j] = min(w[j], \{a[x][j] +
13
                                                               \rightarrow row[x] + col[j], x});
       mu[i] = lp[i] == lp[i / lp[i]] ? 0 :
        \rightarrow -1 * mu[i / lp[i]];
       phi[i] = phi[i / lp[i]] * (lp[i] == 38
15
                                                      while (pos != -1){
        \rightarrow lp[i / lp[i]] ? lp[i] : lp[i] - 39
                                                           int nxt = par2[prev[pos]];
           1);
                                                          par[pos] = prev[pos];
   }
                                              41
16
                                                          par2[prev[pos]] = pos;
                                               42
     kasai
                                                          pos = nxt;
                                                      }
                                              44
                                              45
   fill(par, par + 301, -1);
                                                  cout << ans << ''\n'';
                                              46
   fill(par2, par2 + 301, -1);
                                                  for (int i = 0; i < n; i++)
                                              47
                                                      cout << par[i] + 1 << "" << i + 1
   int ans = 0;
                                                       < ''\n'';
   for (int v = 0; v < n; v++){
       memset(useda, false, sizeof(useda));
       memset(usedb, false, sizeof(usedb));
       useda[v] = true;
       for (int i = 0; i < n; i++)
            w[i] = make_pair(a[v][i] +
10
            \rightarrow row[v] + col[i], v);
```

```
struct edge{
                                                            if (res){
                                               45
                                                                 eds[num].f += res;
       int from, to;
2
                                               46
                                                                eds[num ^ 1].f -= res;
       int c, f, num;
                                                47
       edge(int from, int to, int c, int
                                                                return res;
            num):from(from), to(to), c(c),
                                                            }
            f(0), num(num){}
                                                       }
       edge(){}
                                                       return 0;
                                               51
   };
                                                   }
                                               52
                                               53
   const int max_n = 600;
                                                   void add(int fr, int to, int c, int nm)
                                               54
                                                       {
                                                       gr[fr].push_back(num);
   edge eds[150000];
                                               55
10
                                                       eds[num++] = edge(fr, to, c, nm);
   int num = 0;
11
                                               56
   int it[max_n];
                                                       gr[to].push_back(num);
                                               57
12
                                                       eds[num++] = edge(to, fr, 0, nm);
   vector<int> gr[max_n];
                                               58
   int s, t;
                                                           //corrected c
   vector<int> d(max_n);
                                                   }
                                               59
15
                                                60
   bool bfs(int k) {
                                                   int ans = 0;
                                               61
       queue<int> q;
                                                       for (int k = 30; k \ge 0; k--)
                                               62
18
                                                            while (bfs(k)) {
       q.push(s);
19
                                               63
       fill(d.begin(), d.end(), -1);
                                                                memset(it, 0, sizeof(it));
20
                                               64
       d[s] = 0;
                                                                while (int res = dfs(s, 1e9
21
                                                65
       while (!q.empty()) {
                                                                 \rightarrow + 500, k))
            int v = q.front();
                                                                     ans += res;
                                                            }
            q.pop();
                                               67
            for (int x : gr[v])
                                               68
25
                if (d[eds[x].to] == -1 \&\&
                                                69
26
                     eds[x].c - eds[x].f >=
                                                   // decomposition
                                               70
                     (1 << k)){}
                     d[eds[x].to] = d[v] + 1;_{72}
                                                   int path_num = 0;
27
                     q.push(eds[x].to);
                                                   vector<int> paths[550];
                }
                                                   int flows[550];
                                               74
       }
                                               75
30
                                                   int decomp(int v, int flow) {
31
                                               76
       return (d[t] != -1);
                                                       if (flow < 1)
32
                                               77
   }
                                                            return 0;
33
                                               78
                                                       if (v == t) {
                                                79
   int dfs(int v, int flow, int k) {
                                                            path_num++;
35
       if (flow < (1 << k))
                                                            flows[path_num - 1] = flow;
                                               81
36
            return 0;
                                                            return flow;
                                               82
37
                                                       }
       if (v == t)
38
                                               83
            return flow;
                                                       for (int i = 0; i < gr[v].size();</pre>
                                               84
       for (; it[v] < gr[v].size();</pre>
                                                            i++) {
40
        \rightarrow it[v]++) {
                                                            int num = gr[v][i];
            int num = gr[v][it[v]];
                                                            int res = decomp(eds[num].to,
            if (d[v] + 1 != d[num].to])

→ min(flow, eds[num].f));
                continue;
                                                            if (res)
                                                                       {
43
                                               87
            int res = dfs(eds[num].to,
                                                                eds[num].f -= res;
44
                                               88
               min(flow, eds[num].c -
                                                                paths[path_num -
                                                89
                eds[num].f), k);
                                                                     1].push_back(eds[num].num);
```

```
return res;
                                                  long long ans = 0;
90
            }
                                                  int mx = 2 * n + 2;
91
       }
92
                                                  memset(upd, 0, sizeof(upd));
       return 0;
93
   }
                                                  for (int i = 0; i < mx; i++)
94
                                                       dist[i] = inf;
95
   while (decomp(s, 1e9 + 5));
                                                  dist[st] = 0;
                                                  queue<int> q;
                                                  q.push(st);
                                                  upd[st] = 1;
                                               10
                                                  while (!q.empty()){
                                                       int v = q.front();
                                               12
                                                       q.pop();
                                               13
                                                       if (upd[v]){
                                               14
                                                            for (int x : gr[v])
                                                                                          {
                                               15
                                                                edge &e = edges[x];
                                               16
                                                                if (e.c - e.f > 0 && dist[v]
                                               17
                                                                     != inf && dist[e.to] >
                                                                     dist[v] + e.w) {
                                                                     dist[e.to] = dist[v] +
                                               18
                                                                     → e.w;
                                                                     if (!upd[e.to])
                                               19
                                                                         q.push(e.to);
                                               20
                                                                     upd[e.to] = true;
                                               21
                                                                     p[e.to] = x;
                                                                }
                                               23
                                                           }
                                               24
                                                           upd[v] = false;
                                               25
                                                       }
                                               26
                                                  }
                                               27
                                               28
                                                  for (int i = 0; i < k; i++){
                                                       for (int i = 0; i < mx; i++)</pre>
                                               30
                                                           d[i] = inf;
                                               31
                                                       d[st] = 0;
                                               32
                                                       memset(used, false, sizeof(used));
                                               33
                                                       set<pair<int, int> > s;
                                               34
                                                       s.insert(make_pair(0, st));
                                               35
                                                       for (int i = 0; i < mx; i++){
                                                            int x;
                                               37
                                                           while (!s.empty() &&
                                               38

    used[(s.begin() ->

                                                                second)]){
                                                                s.erase(s.begin());
                                               39
                                                            }
                                               40
                                                            if (s.empty())
                                               41
                                                                break;
                                               42
                                                           x = s.begin() -> second;
                                               43
                                                           used[x] = true;
                                               44
```

45

s.erase(s.begin());

```
for (int i = 0; i <
                                                   string min_cyclic_shift (string s) {
                                                1
46
                gr[x].size(); i++){
                                                            s += s;
                edge &e = edges[gr[x][i]];
                                                            int n = (int) s.length();
47
                 if (!used[e.to] && e.c - e.f4
                                                            int i=0, ans=0;
                 \rightarrow > 0){
                                                            while (i < n/2) {
                     if (d[e.to] > d[x] +
                                                                     ans = i;
                         (e.c - e.f) * e.w +
                                                                     int j=i+1, k=i;
                         dist[x] -
                                                                     while (j < n \&\& s[k] <=
                         dist[e.to]){
                                                                      → s[j]) {
                         d[e.to] = d[x] +
                                                                               if (s[k] < s[j])
50
                          \hookrightarrow (e.c - e.f) *
                                                                                       k = i;
                          \rightarrow e.w + dist[x] - 11
                                                                              else

→ dist[e.to];

                                                                                        ++k;
                         p[e.to] = gr[x][i];_{13}
                                                                              ++j;
51
                                                                     }
52
                              s.insert(make_pair(d[e.to],
                                                                     while (i <= k)
                                                                                       i += j -
                              e.to));
                                                                      \hookrightarrow k;
                     }
                }
                                                            return s.substr (ans, n/2);
            }
                                                   }
                                                18
            dist[x] += d[x];
56
       }
       int pos = t;
       while (pos != st){
                int id = p[pos];
                edges[id].f += 1;
            edges[id ^ 1].f -= 1;
62
            pos = edges[id].from;
63
       }
64
  }
                                                     Sum over subsets
65
```

```
for(int i = 0; i<(1<<N); ++i)
    F[i] = A[i];
for(int i = 0; i < N; ++i) for(int mask =
    O; mask < (1<<N); ++mask){
    if(mask & (1<<i))
        F[mask] +=
        F[mask^(1<<i)];
}</pre>
```

```
suf array + lcp
   vector<int> getZ(string s){
       vector<int> z;
       z.resize(s.size(), 0);
                                                 1 // O(n)
       int 1 = 0, r = 0;
                                                   #define forn(i, n) for (int i = 0; i <
       for (int i = 1; i < s.size(); i++){</pre>
                                                    \rightarrow (int)(n); i++)
            if (i <= r)
                 z[i] = min(r - i + 1, z[i - 4])
                                                   typedef vector<char> bits;
                 → 1]);
            while (i + z[i] < s.size() &&
                                                   template < const int end>
             \rightarrow s[z[i]] == s[i + z[i]])
                                                   void getBuckets(int *s, int *bkt, int n,
                z[i]++;
                                                        int K) {
            if (i + z[i] - 1 > r){
                                                        fill(bkt, bkt + K + 1, 0);
                r = i + z[i] - 1;
                                                        forn(i, n) bkt[s[i] + !end]++;
                                                9
                 1 = i;
                                                        forn(i, K) bkt[i + 1] += bkt[i];
12
                                                10
            }
                                                   }
                                                11
       }
                                                   void induceSAl(bits &t, int *SA, int *s,
14
                                                12
       return z;
                                                        int *bkt, int n, int K) {
15
   }
                                                        getBuckets<0>(s, bkt, n, K);
16
                                                13
                                                        forn(i, n) {
                                                14
   vector<int> getP(string s){
                                                            int j = SA[i] - 1;
18
                                                15
       vector<int> p;
                                                            if (j >= 0 && !t[j])
19
       p.resize(s.size(), 0);
                                                                 SA[bkt[s[j]]++] = j;
20
       int k = 0;
                                                        }
21
       for (int i = 1; i < s.size(); i++){ <sub>19</sub>
            while (k > 0 \&\& s[i] == s[k])
                                                   void induceSAs(bits &t, int *SA, int *s,
                k = p[k - 1];
                                                        int *bkt, int n, int K) {
            if (s[i] == s[k])
                                                        getBuckets<1>(s, bkt, n, K);
                k++;
                                                        for (int i = n - 1; i >= 0; i--) {
26
                                                22
            p[i] = k;
                                                            int j = SA[i] - 1;
                                                23
       }
                                                            if (j >= 0 && t[j])
28
                                                24
       return p;
                                                                 SA[--bkt[s[j]]] = j;
                                                25
   }
                                                        }
30
                                                26
                                                   }
31
                                                27
   vector<int> getH(string s){
32
                                                28
       vector<int> h;
                                                   void SA_IS(int *s, int *SA, int n, int
33
       h.resize(s.size() + 1, 0);
                                                    \rightarrow K) { // require last symbol is 0
34
       for (int i = 0; i < s.size(); i++)</pre>
                                                    #define isLMS(i) (i \&\&\ t[i] \&\&\ !t[i-1])
35
            h[i + 1] = ((h[i] * 111 * pow))
                                                        int i, j;
             \rightarrow s[i] - 'a' + 1) % mod;
                                                        bits t(n);
                                                32
       return h;
                                                        t[n-1] = 1;
37
                                                33
   }
                                                        for (i = n - 3; i \ge 0; i--)
38
                                                34
                                                            t[i] = (s[i] < s[i+1] | |
39
   int getHash(vector<int> &h, int 1, int
                                                             \rightarrow (s[i]==s[i+1] &&
40
       r){
                                                             \rightarrow t[i+1]==1));
       int res = (h[r + 1] - h[1] * p[r - 1]_{6}
                                                        int bkt[K + 1];
41
        \rightarrow + 1]) % mod;
                                                        getBuckets<1>(s, bkt, n, K);
                                                37
        if (res < 0)
42
                                                        fill(SA, SA + n, -1);
                                                38
            res += mod;
                                                        forn(i, n)
43
                                                39
       return res;
                                                            if (isLMS(i))
44
   }
                                                                 SA[--bkt[s[i]]] = i;
45
                                                41
                                                        induceSA1(t, SA, s, bkt, n, K);
                                                42
```

```
induceSAs(t, SA, s, bkt, n, K);
                                                  int N, m, SA [MAX_N], LCP [MAX_N];
43
                                                  int x [MAX_N], y [MAX_N], w [MAX_N], c
       int n1 = 0;
44
       forn(i, n)
                                                       [MAX_N];
45
            if (isLMS(SA[i]))
                                               91
                SA[n1++] = SA[i];
                                                  inline bool cmp (const int a, const int
                                                      b, const int 1) { return (y [a] == y
       fill(SA + n1, SA + n, -1);
       int name = 0, prev = -1;
                                                       [b] && y [a + 1] == y [b + 1]); }
49
       forn(i, n1) {
                                               93
            int pos = SA[i];
                                                  void Sort () {
                                               94
51
            bool diff = false;
                                                       for (int i = 0; i < m; ++i) w[i] =
                                               95
            for (int d = 0; d < n; d++)
                                                       → 0;
                                                      for (int i = 0; i < N; ++i)</pre>
                if (prev == -1 \mid \mid s[pos+d]
                   != s[prev+d] || t[pos+d]
                                                       \rightarrow ++w[x[y[i]]];
                     != t[prev+d])
                                                      for (int i = 0; i < m - 1; ++i) w[i
                    diff = true, d = n;
                                                       \rightarrow + 1] += w[i];
                else if (d > 0 &&
                                                      for (int i = N - 1; i >= 0; --i)
56
                                                       \Rightarrow SA[--w[x[y[i]]]] = y[i];
                 isLMS(prev+d)))
                                                  }
                    d = n;
                                              100
            if (diff)
                                                  void DA () {
                                              101
                                                       for (int i = 0; i < N; ++i) x[i] =
                name++, prev = pos;
                                              102
59
            SA[n1 + (pos >> 1)] = name - 1;
                                                       \rightarrow str[i], y[i] = i;
       }
                                                       Sort ();
61
       for (i = n - 1, j = n - 1; i >= n1;_{104}
                                                       for (int i, j = 1, p = 1; p < N; j
                                                       \rightarrow <<= 1, m = p) {
        if (SA[i] >= 0)
                                                           for (p = 0, i = N - j; i < N;
                SA[j--] = SA[i];
                                                           \rightarrow i++) y[p++] = i;
       int *s1 = SA + n - n1;
                                                           for (int k = 0; k < N; ++k) if
65
                                              106
       if (name < n1)
                                                               (SA[k] >= j) y[p++] = SA[k]
            SA_{IS}(s1, SA, n1, name - 1);
                                                            → - j;
67
                                                           Sort();
       else
                                              107
            forn(i, n1)
                                                           for (swap (x, y), p = 1,
                SA[s1[i]] = i;
                                                            \rightarrow x[SA[0]] = 0, i = 1; i < N;
       getBuckets<1>(s, bkt, n, K);
                                                            \rightarrow ++i) x[SA [i]] = cmp (SA[i -
       for (i = 1, j = 0; i < n; i++)
                                                               1], SA[i], j) ? p - 1 : p++;
72
            if (isLMS(i))
                                                      }
                                              109
                s1[j++] = i;
                                                  }
                                              110
74
       forn(i, n1)
                                              111
            SA[i] = s1[SA[i]];
                                                  void kasaiLCP () {
                                              112
       fill(SA + n1, SA + n, -1);
                                                       for (int i = 0; i < N; i++) c[SA[i]]</pre>
                                              113
       for (i = n1 - 1; i \ge 0; i - -) {
                                                       \rightarrow = i;
            j = SA[i], SA[i] = -1;
                                                       for (int i = 0, j, k = 0; i < N; LCP
                                              114
79
            SA[--bkt[s[j]]] = j;
                                                           [c[i++]] = k)
       }
                                                           if (c [i] > 0) for (k ? k-- : 0,
                                              115
       induceSAl(t, SA, s, bkt, n, K);
                                                               j = SA[c[i] - 1]; str[i + k]
                                                           \rightarrow == str[j + k]; k++);
       induceSAs(t, SA, s, bkt, n, K);
   }
                                                           else k = 0;
                                              116
84
   // O(n) ended
                                                  }
85
                                              117
86
                                              118
   // O(n logn)
                                                  void suffixArray () { // require last
                                              119
   string str;
                                                       symbol is char(0)
```

```
int num = 0;
   long long phi = n, nn = n;
   for (long long x:primes){
       if (x*x>nn)
            break;
       if (nn \% x == 0){
            while (nn \% x == 0)
                nn /= x;
            phi -= phi/x;
            num++;
10
       }
11
12
   if (nn != 1){
13
       phi -= phi/nn;
14
       num++;
15
   }
16
   if (!((num == 1 && n % 2 != 0) || n == 4
17
       || n == 2 || (num == 2 && n % 2 == 0
       && n % 4 != 0))){
       cout << "'-1\n";
18
       continue;
19
20
   vector<long long> v;
   long long pp = phi;
   for (long long x:primes){
       if (x*x>pp)
            break;
25
       if (pp \% x == 0){
26
            while (pp \% x == 0)
27
                pp /= x;
28
            v.push_back(x);
       }
   }
31
   if (pp != 1){
       v.push_back(pp);
33
34
   while (true){
       long long a = primes[rand()%5000]%n;
36
       if (\gcd(a, n) != 1)
            continue;
38
       bool bb = false;
39
       for (long long x:v)
40
            if (pow(a, phi/x) == 1){
41
                bb = true;
42
                break;
43
            }
       if (!bb){
45
            cout << a << "\n";
46
            break;
47
       }
48
   }
49
```

```
const int LOG = 19;
                                                        std::reverse(a.begin() + 1,
                                                43
   const int N = (1 \ll LOG);
                                                        \rightarrow a.end());
   typedef std::complex<double> cd;
                                                        for (cd& elem: a)
                                                            elem /= N;
   int rev[N];
                                                   }
                                                47
   cd W[N];
   void precalc() {
9
        const double pi = std::acos(-1);
10
                                                 void fast_fourier(vector<int>& a) { //
        for (int i = 0; i != N; ++i)
                                                       AND-FFT.
            W[i] = cd(std::cos(2 * pi * i))
12
                                                        for (int k = 1; k < SZ(a); k *= 2)
             \rightarrow N), std::sin(2 * pi * i /
                                                            for (int start = 0; start < (1</pre>
               N));
                                                                << K); start += 2 * k) {
13
                                                                 for (int off = 0; off < k;</pre>
                                                 4
        int last = 0;
14

→ ++off) {

        for (int i = 1; i != N; ++i) {
                                                                     int a_val = a[start +
            if (i == (2 << last))</pre>
                                                                      \rightarrow off];
                ++last;
                                                                     int b_val = a[start + k
                                                 6
                                                                      → + off];
            rev[i] = rev[i ^ (1 << last)] |
19
             \rightarrow (1 << (LOG - 1 - last));
                                                                     a[start + off] = b_val;
       }
20
                                                                     a[start + k + off] =
                                                9
   }
21
                                                                          add(a_val, b_val);
22
                                                                 }
                                                10
   void fft(vector<cd>& a) {
23
                                                            }
                                                11
        for (int i = 0; i != N; ++i)
24
                                                   }
                                                12
            if (i < rev[i])</pre>
25
                std::swap(a[i], a[rev[i]]);
                                                   void inverse_fast_fourier(vector<int>&
27
                                                        a) {
        for (int lvl = 0; lvl != LOG; ++lvl)<sub>15</sub>
                                                        for (int k = 1; k < SZ(a); k *= 2)
            for (int start = 0; start != N; \frac{1}{16}
                                                            for (int start = 0; start < (1</pre>
               start += (2 << lvl))
                                                             \rightarrow << K); start += 2 * k) {
                for (int pos = 0; pos != (1
30
                                                                 for (int off = 0; off < k;</pre>
                 ++off) {
                     cd x = a[start + pos];
                                                                     int a_val = a[start +
                     cd y = a[start + pos +
32
                                                                      → off];
                      \rightarrow (1 << lv1)];
                                                                     int b_val = a[start + k
                                                                      → + off];
                     y *= W[pos << (LOG - 1
34
                      \rightarrow lvl)];
                                                                     a[start + off] =
                                                21
35

    sub(b_val, a_val);

                     a[start + pos] = x + y;
                                                                     a[start + k + off] =
                     a[start + pos + (1 <<
                                                                      → a_val;
                      \rightarrow lvl)] = x - y;
                                                                 }
                }
                                                            }
   }
39
                                                   }
                                                25
40
   void inv_fft(vector<cd>& a) {
41
        fft(a);
42
```

```
struct Edge {
                                                      return result;
                                               42
                                                  }
       int a;
                                               43
       int b;
                                               44
                                                  vector<int> min_avg_cycle(int n,
       int cost;
   };
                                                      vector<Edge> &edges) {
                                                       const int inf = 1e3;
                                               46
   vector<int> negative_cycle(int n,
                                               47
       vector<Edge> &edges) {
                                                       for (auto &e : edges)
                                               48
       // O(nm), return ids of edges in
                                                           e.cost *= n * n;
                                               49
        → negative cycle
                                               50
                                                       int l = -inf;
                                                       int r = inf;
       vector<int> d(n);
10
                                                      while (l + 1 < r) {
       vector<int> p(n, -1); // last edge
11
                                                           int m = (1 + r) / 2;
        \rightarrow ids
                                               54
                                                           for (auto &e : edges)
                                               55
12
       const int inf = 1e9;
                                                               e.cost -= m;
13
                                               56
                                               57
       int x = -1;
                                                           if (negative_cycle(n,
       for (int i = 0; i < n; i++) {
                                                               edges).empty())
            x = -1;
                                                               1 = m;
17
                                               59
            for (int j = 0; j <
                                                           else
18
                                               60
               edges.size(); j++) {
                                                               r = m;
                                               61
                Edge &e = edges[j];
19
                                               62
                                                           for (auto &e : edges)
                                               63
                if (d[e.b] > d[e.a] +
                                                               e.cost += m;
                                                       }
                 → e.cost) {
                    d[e.b] = max(-inf,
                                               66
22
                     \rightarrow d[e.a] + e.cost);
                                                       if (r >= 0) // if only negative
                                               67
                    p[e.b] = j;
                                                           needed
23
                    x = e.b;
                                                           return vector<int>();
24
                                               68
                }
                                               69
            }
                                                       for (auto &e : edges)
       }
                                                           e.cost -= r;
                                               71
                                               72
       if (x == -1)
                                                       vector<int> result =
29
                                               73
            return vector<int>(); // no
                                                       → negative_cycle(n, edges);
               negative cycle
                                               74
       for (int i = 0; i < n; i++)
                                                       for (auto &e : edges)
            x = edges[p[x]].a;
                                                           e.cost += r;
                                               77
34
                                               78
       vector<int> result;
                                                       for (auto &e : edges)
35
                                               79
       for (int cur = x; ; cur =
                                                           e.cost \neq n * n;
                                               80
           edges[p[cur]].a) {
            if (cur == x && result.size() > 82
                                                      return result;

→ 0) break;

                                                  }
            result.push_back(p[cur]);
                                               84
       }
                                                  struct edge {
                                               85
39
       reverse(result.begin(),
                                                       int from, to;
                                               86
40
        → result.end());
                                                       int c, f, cost;
                                               87
                                                  };
                                               88
41
```

```
Добавим к нашему графу вершину ѕ и
89
   const int max_n = 200;
90
                                                       рёбра из неё во все остальные
91
                                                       вершины. Запустим алгоритм
   vector<int> gr[max_n];
92
                                                       Форда-Беллмана и попросим его
   vector<edge> edges;
93
                                                       построить нам квадратную матрицу со
94
                                                       следующим условием: d[i][u] - длина
   void add(int fr, int to, int c, int
95
                                                       минимального пути от s до и ровно
       cost) {
                                                       из і ребер. Тогда длина
        gr[fr].push_back(edges.size());
96
                                                       оптимального цикла µ* минимального
        edges.push_back({fr, to, c, 0,
97

    cost});

                                                       среднего веса вычисляется как
        gr[to].push_back(edges.size());
                                                       minumaxkd[n][u]-d[k][u]n-k.
        edges.push_back({to, fr, 0, 0,
99
                                               2
        \rightarrow -cost}); // single
                                                 Достаточно будет доказать это правило
100
                                                      для \mu * = 0, так как для других \mu *
101
                                                      можно просто отнять эту величину от
   void calc_min_circulation(int n) {
102
                                                      всех ребер и получить снова случай с
        while (true) {
103
                                                      μ*=0.
            vector<Edge> eds;
104
            vector<int> origin;
                                               4
105
                                                  Чтобы найти цикл после построения
                                               5
106
            for (int i = 0; i <
                                                      матрицы d[k][u], запомним, при каких
107
                edges.size(); i++) {
                                                      и и к достигается оптимальное
                edge &e = edges[i];
108
                                                      значение \mu *, и, используя d[n][u],
                if (e.c - e.f > 0) {
                                                      поднимемся по указателям предков.
                     eds.push_back({e.from,
110
                                                      Как только мы попадем в уже
                     → e.to, e.cost});
                                                      посещенную вершину
                                                                             мы нашли цикл
                     origin.push_back(i);
111
                                                      минимального среднего веса.
                }
112
            }
                                               6
113
                                                  Этот алгоритм работает за O(VE)
                                               7
            vector<int> cycle =
                                                   func findMinCycle(Graph G)
                                               9
                negative_cycle(n, eds);
                                                       // вводим мнимую вершину s, от
                                              10
116
                                                            которой проведём рёбра нулевого
            if (cycle.empty())
117
                                                            веса в каждую вершину графа
                break;
118
                                                       Node s
                                              11
119
                                                       Edge[] e
            for (auto id : cycle) {
                                              12
                                                       insert(s)
                                              13
                int x = origin[id];
121
                                                       i = 0
                edges[x].f += 1;
                                              14
122
                                                       for u in G
                edges[x ^1].f -= 1;
                                              15
123
                                                           e[i].begin = s
            }
                                              16
124
                                                           e[i].end = u
        }
                                              17
125
                                                           e[i].weight = 0
                                              18
126
                                                           i++
                                              19
                                                       // строим матрицу кратчайших
                                                           расстояний, запустив алгоритм
                                                           Форда-Беллмана из вершины ѕ
                                                       fordBellman(s)
                                              21
                                                       // т - длина оптимального цикла
                                              22
```

Кол-во корневых деревьев:

$$t(G) = \frac{1}{n}\lambda_2 \dots \lambda_n \ (\lambda_1 = 0)$$

Кол-во эйлеровых циклов:

$$e(D) = t^{-}(D, x) \cdot \prod_{y \in D} (outdeg(y) - 1)!$$

Наличие совершенного паросочетания: T — матрица с нулями на диагонали. Если есть ребро (i,j), то $a_{i,j} := x_{i,j}, \, a_{j,i} = -x_{i,j}$ $\det(T) = 0 \Leftrightarrow$ нет совершенного паросочетания.

Whitespace code FFT