# POSL: A Parallel Oriented Solver Language

(detailed plan)

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# Contents

# Chapter 1

# Introduction

The *Introduction* of the work is presented. We describe the target problem (the formal definition will be in the next chapter), and the approaches implemented so far to solve them. The necessity of a new approach to exploit the new era of parallelism is introduced.

In this section are presented the goals of the thesis, and POSL is introduced as a new parallel approach including others and novel features. Finally, we describe the structure of the document.

# Chapter 2

# Overview of Combinatorial Optimization Problems and methods to solve them

This chapter presents an overview to the state of the art of *Combinatorial Optimization Problems* and different approaches to tackle them.

## 2.1 Combinatorial Optimization Problems

We introduce the definition of a *Combinatorial Optimization Problem* and the its link with *Constraint Satisfaction Problems* (*CSP*), where we concentrate our main efforts. We give some examples: *Resource Allocations* [1], *Task Scheduling* [8], *Master-keying* [5], *Traveling Salesman*, *Knapsack Problem*, among others.

## 2.2 Basic techniques

In this section we introduce some basic techniques used to solve the problems defined above, like tree search-based solvers, backtracking-based solvers, Monte Carlo Tree Search methods, meta-heuristics methods, etc. [1]

### 2.2.1 Constraint propagation

Constraint propagation techniques are deterministic methods to attack these kind of problems, but in some cases they are incapable to solve them [4].

### 2.2.2 Meta-heuristics and Hyper-heuristics methods

However, we cannot solve some *CSPs* only applying constraint propagation techniques. It is necessary to combine them with other methods. In this chapter is presented an overview in the field of *meta-heuristics* methods [3], nature-inspired algorithms divided in two groups:

[1] We also mention other approach that we tested at the beginning of this research (modeling *CSPs* through *relaxation*), giving a brief introduction and referencing the Section 3.1 for more information.

1. *Single Solution Based:* more exploitation-oriented, intensifying the search in some specific areas. (We will focus our attention on this first group)

2. *Population Based:* more exploration-oriented, identifying areas of the search space where there are (or where there could be) the best solutions.

#### 2.2.2.1 Single Solution Based Meta-heuristics

Methods of the first group are also called *trajectory methods*, and they are based on choosing a solution taking into account some criterion (usually random), and they move from a solution to his *neighbor*, following a trajectory into the search space.

#### 2.2.2.2 Population Based Meta-heuristics

Also there exist heuristic methods based on populations. These methods do not work with a single solution, but with a set of solutions named *population*.

### 2.2.3 Hyper-heuristic Methods

*Hyper-heuristics* are automated methodologies for selecting or generating meta-heuristics to solve hard computational problems.

## 2.3 Advances techniques

Even if many works applying basic techniques are obtained very good results solving *CSPs*, the complexity of problems grows relentlessly. For that reason applying more sophisticated techniques becomes imperative. In this section we present some of them and give an overview of its contributions.

### 2.3.1 Hybridization

The *Hybridization* approach is the one who combine different approaches into the same solution strategy, and recently, it leads to very good results in the constraint satisfaction field, some of them presented in this section.

### 2.3.2 Parallel computing

The evolution of computer architecture is leading us toward massively multi-core computers for tomorrow, composed of thousands of computing units. A parallel model to solve *CSPs* is the core of this work, and its advances are presented in this section.

Some results have been obtained on this field. The contribution in terms of hardware has been crucial, but the development of the techniques and algorithms to solve problems in parallel is also visible, focusing the main efforts in three fundamentals concepts:

1. Problem subdivision, [2]

2. Scalability and

3. Inter-process communication.

[2] In this topic, a theoretical (and still in progress) contribution is presented. We give a brief introduction and referencing the Section 3.2 for more information.

### 2.3.3 Solvers cooperation

The interaction between solvers exchanging some information is called *solver cooperation* and it is very popular in this field due to their good results, presented in this section.

## 2.4 Parameter setting techniques

Most of these methods to tackle combinatorial problems, involve a number of parameters that govern their behavior, and they need to be well adjusted. Most of the times they depend on the nature of the specific problem, so they require a previous analysis to study their behavior [2]. The field that studies and searches the proper parameters for an algorithm is called *parameter tuning*. It is also known as a meta-optimization problem, because the main goal is to find the best solution (parameter configuration) for a program, which will try to find the best solution for some problem as well. Finally, this chapter presents an overview of the progresses in the field of *parameter settings*.

There exist two classes to classify these methods:

1. *Off-line tunning*: Also known just as parameter tuning, were parameters are computed before running the program to tune.[3]
2. *On-line tunning*: Also known as parameter control, where parameters are adjusted while running the program.

### 2.4.1 Off-line tunning

The technique of parameter tuning or off-line tunning, is used to computed the best parameter configuration for an algorithm before solving a given instance of a problem, to obtain the best performance.

### 2.4.2 On-line tunning

Although parameter tunning shows to be an effective way to adjust parameters to sensibles algorithms, in some problems the optimal parameter settings may be different for various phases of the search process. This is the main motivation to use on-line tuning techniques to find the best parameter setting, also called *Parameter Control Techniques*.

[3] Here, we present a performed experiment applying an automatic tuner to *Adaptive Search*, giving a brief introduction, and referencing the Section 3.3 for more information.

# Chapter 3

# Prior works leading to POSL

In this chapter are presented Prior works leading to POSL.

## 3.1 Relaxation model for discrete *CSPs*

Aiming for the right direction in order to find the proper approach, our first attempt to tackle the problem of reducing the search space of a *CSP*, we model it through a continuous optimization problem, and then, applying efficient methods to solve it. This way we do not reach an optimal solution, but an approximation of it. The new variables domain would be the neighborhood of the found approximation.

## 3.2 Domain Split

A way to tackle huge combinatorial problems in parallel is to split the search space. In this section, the *problem subdivision* approach was adopted to divide the domain of a given problem, in this particular case, to solve the *k-medoids problem* in parallel. [1]

## 3.3 Tunning methods for local search algorithms

Another performed study was applying the PARAMILS tool in order to find the optimum parameter configuration to *Adaptive Search* solver. PARAMSILS (version 2.3) is a tool for parameter optimization for parametrized algorithms [7]. It is an open source program (project) in *Ruby*, and the public source include some examples and a detailed and complete User Guide with a compact explanation about how to use it with a specific solver [6].

### 3.3.1 ParamILS_2.3

PARAMILS[2] library (an open source program (project) in *Ruby*) is described. It can be downloaded from

[1] This work falls within the framework of the *Ulysses* project between France and Ireland

[2] Available on http://cs.ubc.ca/labs/beta/Projects/ParamILS

### 3.3.2 Using ParamILS

In this section we explain how to use PARAMILS, getting in details about how to write and prepare all the files that this tool needs to work.

### 3.3.3 A ParamILS wrapper

In order to use PARAMILS to tune *Adaptive Search*, and study the results, we built a wrapper in C++ to easily collect all data and process it. In this section we explain in detail that wrapper and how to use it.

### 3.3.4 Results

We present in this section all experiment designs and the obtained results, tuning *Adaptive Search* to solve *Costas Array* and *All-Interval Series* problems.

### 3.3.5 Conclusion

We close this work with a brief conclusion.

# Chapter 4

# A Parallel-Oriented Language for Modeling Constraint-Based Solvers

In this chapter we introduce POSL as our main contribution and a new way to solve *CSPs*. We resume its characteristics and advantages, and we get into details in the next sections. We describe a general outline to follow in order to build parallel solvers using POSL, and following each step is described in details.

## 4.1 First Stage: Modeling the target benchmark

In this stage we explain formally our modeling process of a benchmark to be solved (or study) through POSL. We explain how to make use of the already existing models or to create new benchmarks using the basic layer of the framework in C++ making a proper usage of the object-oriented design.

## 4.2 Second Stage: Creating POSL's modules

There exist two types of basic modules in POSL: *operation modules* and *open channels*. An *operation module* is a function receiving an input, then executes an internal algorithm, and returns an output. An *open channel* is also a function receiving and returning information, but in contrast, the *open channel* can receive information from two different ways: through parameter or from outside, i.e. by communicating with a module from another solver.

### 4.2.1 Operation Module

In this sub-section we expose the definition and the characteristics and the details of the *operation module*, and give some examples. We explain how to create new *operation modules* using the basic layer of the framework.

### 4.2.2 Open channel

In this sub-section we expose the definition and the characteristics and the details of the *open channel*, and give some examples. We explain how to create new *open channels* using the basic layer of the framework.

## 4.3 Third Stage: Assembling POSL's modules

In this stage a generic strategy is coded through a operator based language: POSL. We call this the *computation strategy*. The operators are parametrized functions receiving information and allow interactions between modules (*operation modules* and *open channels*). In this section are defined the operators and some examples are presented. We explain how to create new *operators* using the basic layer of the framework.

## 4.4 Forth Stage: Creating POSL solvers

With operation modules and open channels already assembled through the *computation strategy*, we can create solvers by instantiating modules. POSL provides an environment to this end and we present the procedure to use it.

## 4.5 Fifth Stage: Connecting the solvers

Once we have defined our solver strategy, the last step is to declare the *communication channels*, i.e. connecting the solvers each others. In this last stage, POSL provides to the user a platform to easily define cooperative meta–strategies that solvers must follow (POSL meta–solvers). The steps to create *communication channels* through *communication operators* are explained and some examples are presented. We explain how to create new *communication operators* using the basic layer of the framework.

## 4.6 Step-by-step POSL code example

In this section we summarize all the steps to build a POSL meta–solver through an real example, providing schemes to make more comprehensive the process.

# Chapter 5

# Study and evaluation process

In this chapter we expose all details about the process of evaluation of POSL, i.e. all the experiments we perform. For each benchmark, we explain also the strategy (or strategies) used in the solving (evaluation) process.

## 5.1 Social Golfers Problem

We present in this sub-section the definition, characteristics and some implementation details of the *Social Golfers Problem*, explaining also our interest in it. Studied strategies used to evaluate POSL through this benchmark are presented and explained in details.

## 5.2 Costas Array Problem

We present in this sub-section the definition, characteristics and some implementation details of the *Costas Array Problem*, explaining also our interest in it. Studied strategies used to evaluate POSL through this benchmark are presented and explained in details.

## 5.3 N-Queen Problem

We present in this sub-section the definition, characteristics and some implementation details of the *N-Queen Problem*, explaining also our interest in it. Studied strategies used to evaluate POSL through this benchmark are presented and explained in details.

## 5.4 Golomb Ruler Problem

We present in this sub-section the definition, characteristics and some implementation details of the *Golomb Ruler Problem*, explaining also our interest in it. Studied strategies used to evaluate POSL through this benchmark are presented and explained in details.

## 5.5 All-Interval Series Problem

We present in this sub-section the definition, characteristics and some implementation details of the *All Interval Problem*, explaining also our interest in it. Studied strategies used to evaluate POSL through this benchmark are presented and explained in details.

## 5.6 ...

Maybe others...

# Chapter 6

# Analysis of results

In this chapter we explain the used environments were we run the experiments (description of my desktop machine, *Curiosiphi* server, and eventually *Grid5000*). We describe all the experiments and we expose a complete analysis of the obtained result.

# Chapter 7

# Conclusions and future works

We resume our work, emphasizing on our contribution and obtained results, and we expose the conclusions of the work. We also discus future branches to follow that can be derived from our work. Finally we give our conclusions.

# Appendix A

# POSL strategies

In this appendix we present some secondaries *computation strategies* (written in symbolic POSL code) used during our work, not directly related with our main results.

# Appendix B

# POSL code

In this appendix we present the POSL code used during our work in all the main performed experiments.

# Appendix C

# Complete results

In most of the cases, the complete result tables show interesting behaviors of POSL, like for example, the percentage of times when the communication was effective (a solver was able tu find a solution thanks to the received information). For that reason we present in this Appendix this results.

# Appendix D

# POSL Documentation

A complete and detailed documentation of the code is presented in this Appendix.

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