BIOST 536: Homework 4

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Characteristic	Overall, $N = 975$	Cancer, $N = 200$	No cancer, $N = 775$
Cider consumption,	11 (2, 31)	22 (4, 50)	10 (2, 26)
g/day			
Cider consumption,			
g/day			
10 or less	477 (49%)	72 (36%)	405~(52%)
More than 10	498 (51%)	128 (64%)	370 (48%)
Age, yr	52 (41, 63)	61 (53, 67)	49 (39, 62)
Age, yr			
25-34	$116 \ (12\%)$	1 (0.5%)	115 (15%)
35-44	199 (20%)	9(4.5%)	190 (25%)
45-54	213 (22%)	46 (23%)	$167\ (22\%)$
55-64	242 (25%)	76 (38%)	166 (21%)
65-74	161 (17%)	55 (28%)	106 (14%)
75+	44 (4.5%)	13~(6.5%)	31 (4.0%)

1. Fit a logistic model relating binary cider exposure (> 10 g/day) to the risk of esophageal cancer, using grouped-linear adjustment for age and the six age groups in the variable agegp. Report the odds ratio and 95% confidence interval for binary cider exposure. Optional: Write a sentence appropriate for the results section of a scientific paper reporting the results of this analysis. Note, here and below: your sentence should include both a point estimate and CI for the parameter(s) of interest.

Based on a logistic regression model with grouped-linear adjustment of age (see Table 1), the odds of esophageal cancer for patients consuming over 10 grams of cider per day is 2.19 times (95% robust Wald CI: 1.55-3.08; Wald test p-value<0.001) the odds for patients of the same age level consuming 10 or less grams of cider per day. This provides evidence that daily cider consumption beneath 10 g offers health benefit over consumption above 10 g with grouped-linear adjustment of age.

2. Fit a logistic model relating binary cider exposure (> 10 g/day) to the risk of esophageal cancer using indicator variables to adjust for age and the six age groups in the variable agegp. Report the odds ratio and 95% confidence interval for binary cider exposure. Optional: Write a sentence appropriate for the results section of a scientific paper reporting the results of this analysis.

Based on a logistic regression model adjusting for age groups (see Table 1), the odds of esophageal cancer for patients consuming over 10 grams of cider per day is 2.03 times (95% robust Wald CI: 1.44-2.85; Wald test p-value<0.001) the odds for patients of the same age group consuming 10 or less grams of cider per day. This provides evidence that daily cider consumption beneath 10 grams offers health benefit over consumption of 10 or more grams with adjustment of age group.

(a) Compare the results for the exposure variable in the Q1 and Q2 analyses. Are results similar or very different?

Our estimate of the age-adjusted OR associated with exposure are similar when age is treated as an ordinal numeric variable versus a nominal categorical variable. The more flexible model from Q2 yields a slightly attenuated effect size. Considering estimate uncertainty, the Q2 model provides a slightly narrower confidence interval. At a significance level $\alpha = 0.5$, both models indicate that patients consuming over 10 grams of cider per day have statistically significant higher odds of developing esophageal cancer.

(b) (Optional) Which result would you prefer to report in a scientific article, and why?

Encoding age as a nominal variable, rather than an ordinal one, is preferred as it allows the estimated chances of esophageal cancer to differ across age groups.

4. Fit a logistic model relating binary cider exposure (> 10 g/day) to the risk of esophageal cancer using linear adjustment for age (as a continuous variable). Report the odds ratio and 95% confidence interval for binary cider exposure. Optional: Write a sentence appropriate for the results section of a scientific paper reporting the results of this analysis.

Based on a logistic regression model adjusting for age, the odds of esophageal cancer for patients consuming over 10 grams of cider per day is 2.17 times (95% robust Wald CI: 1.54-3.06; Wald test p-value<0.001) the odds for patients of the same age consuming 10 or less grams of cider per day. This provides evidence that daily cider consumption beneath 10 grams offers health benefit over consumption of 10 or more grams with adjustment of age.

5. Fit a logistic model relating binary cider exposure ($> 10~\rm g/day$) to the risk of esophageal cancer using quadratic adjustment for age (as a continuous variable). Report the odds ratio and 95% confidence interval for binary cider exposure.

Based on a logistic regression model with quadratic adjustment for age, the quadratic-age-adjusted odds of esophageal cancer for patients consuming over 10 grams of cider per day is 1.97 times (95% robust Wald CI: 1.4-2.77; Wald test p-value=0.0011) the odds for patients consuming 10 or less grams of cider per day. This provides evidence that daily cider consumption beneath 10 grams offers health benefit over consumption of 10 or more grams with quadratic adjustment of age.

6.

(a) Fit a logistic model relating binary cider exposure (> 10 g/day) to the risk of esophageal cancer using linear spline adjustment for age. Use the same age groups as for the ageg variable for your splines. Report the odds ratio and 95% confidence interval for binary cider exposure.

Based on a logistic regression model with linear spline adjustment for age, the linear-spline-adjusted odds of esophageal cancer for patients consuming over 10 grams of cider per day is 1.98 times (95% robust Wald CI: 1.41-2.79; Wald test p-value<0.001) the odds for patients consuming 10 or less grams of cider per day. This provides evidence that daily cider consumption beneath 10 grams offers health benefit over consumption of 10 or more grams with linear spline adjustment of age.

7.

(a) Compare the OR estimates from Q4, Q5, and Q6. Are your results similar or very different?

The estimated age-adjusted OR associated with exposure is very similar across linear adjustment for age (2.17), quadratic adjustment for age (1.97), or linear spline adjustment for age (1.98). The latter two are most similar and both produce narrower confidence intervals than the first.

At a significance level $\alpha = 0.5$, all three models agree that patients consuming over 10 grams of cider per day have statistically significant higher odds of developing esophageal cancer.

(b) (Optional) Which approach would you prefer if you were studying this exposure and wanted to adjust for age as a potential confounder, and why?

For the strongest precision and most flexibility in modeling age, I prefer the linear spline model.

8. For each model in Q1 through Q6, how many degrees of freedom are used to include age in the model? That is, how many model parameters are used for age? Include the model intercept in your count.

Q1: $logit(p) = \beta_0 + \beta^* BiCider + \beta_1 AgeG$ requires 2 df to include age.

Q2: $logit(p) = \beta_0 + \beta^* BiCider + \beta_1 AgeG_2 + \beta_2 AgeG_3 + \beta_3 AgeG_4 + \beta_4 AgeG_5 + \beta_5 AgeG_6$ requires 6 df to include age.

Q4: $logit(p) = \beta_0 + \beta^* BiCider + \beta_1 Age$ requires 2 df to include age.

Q5: $logit(p) = \beta_0 + \beta^* BiCider + \beta_1 Age + \beta_2 Age^2$ requires 3 df to include age.

Q6:
$$logit(p) = \beta_0 + \beta^* BiCider + \beta_1 Age + \beta_2 (Age - 35)^+ + \beta_3 (Age - 45)^+ + \beta_3 (Age - 55)^+ + \beta_4 (Age - 65)^+ + \beta_5 (Age - 75)^+$$
 requires 6 df to include age.

- 9. For each question (a)-(e), if you say that models are nested, write out the full and "reduced" models, and give the restrictions on the full model that yield the reduced model.
- (a) Are the models in Q1 and Q2 nested?

Yes, the full and reduced models are

Full:
$$logit(p) = \beta_0 + \beta^* BiCider + \beta_1 AgeG$$

Reduced:
$$logit(p) = \beta_0 + \beta^* BiCider + \beta AgeG_2 + 2 \times \beta AgeG_3 + 3 \times \beta AgeG_4 + 4 \times \beta AgeG_5 + 5 \times \beta AgeG_6$$

(b) Are the models in Q1 and Q4 nested?

No, the two models are not nested.

(c) Are the models in Q4 and Q5 nested?

Yes, the full and reduced models are

Full:
$$logit(p) = \beta_0 + \beta^* BiCider + \beta_1 Age + \beta_2 Age^2$$

Reduced:
$$logit(p) = \beta_0 + \beta^* BiCider + \beta_1 Age$$

(d) Are the models in Q4 and Q6 nested?

Yes, the full and reduced models are

Full:
$$logit(p) = \beta_0 + \beta^* BiCider + \beta_1 Age + \beta_2 (Age - 35)^+ + \beta_3 (Age - 45)^+ + \beta_3 (Age - 55)^+ + \beta_4 (Age - 65)^+ + \beta_5 (Age - 75)^+$$

Reduced:
$$logit(p) = \beta_0 + \beta^* BiCider + \beta_1 Age$$

(e) Are the modest in Q5 and Q6 nested?

No, the two models are not nested.

End of report. Code appendix begins on the next page.

Code Appendix

```
# clear environment
rm(list=ls())
# setup options
knitr::opts_chunk$set(echo = FALSE, warning=FALSE, message=FALSE)
options(knitr.kable.NA = '-', digits = 2)
labs = knitr::all_labels()
labs = labs[!labs %in% c("setup", "allcode")]
# load relevant packages
library(dplyr)
                  # data frame manipulation
library(ggplot2)
library(gtsummary) # table summaries
# library(dagR)
                    # DAG simulation
library(broom)
                    # model coefficient table
# library(knitr)
                    # pretty tables
library(rigr)
                    # regression
# load data
load("../data/esophcts.Rdata")
esph <- esophcts
# names(esph)
# dim(esph)
# define a binary exposure variable and age group covariate
esph$bicider <- ifelse(esph$cider > 10, 1, 0) # cider consumption >10 g/day
esph$agegp <- as.factor(esph$agegp)</pre>
levels(esph$agegp) <- c("25-34", "35-44", "45-54", "55-64", "65-74", "75+")</pre>
## table summary of outcome, exposure, and covariates
esph %>%
    # relabel disease and exposure labels
   dplyr::mutate(
     D = ifelse(case==1, "Cancer", "No cancer"),
     E = cider,
     BiE = ifelse(bicider==1, "More than 10", "10 or less"),
     C = age,
     FaC = agegp,
      # only keep newly defined columns
     .keep="none") %>%
    # create table summary
    gtsummary::tbl_summary(
      by = D, label = list(c(BiE, E)~"Cider consumption, g/day",
                           c(C, FaC)~"Age, yr")) %>%
    add_overall() %>%
   bold_labels()
## ========
## Question 1
## fit logistic regression model of risk of esophageal cancer
```

```
mod <- rigr::regress("odds", case ~ bicider + as.numeric(agegp), esph)</pre>
# the selected coefficients are already exponentiated
coef \leftarrow coef(mod)[,c(4:6,8)]
# or, using qlm()
# mod <- glm(case ~ bicider + as.numeric(agegp), family=binomial(), esph)</pre>
# coef <- cbind('e(Est)'=coef(mod), confint(mod)) %>% exp()
## =======
## Question 2
## =======
## fit logistic regression model of risk of esophageal cancer
mod2 <- regress("odds", case ~ bicider + agegp, esph)</pre>
coef2 \leftarrow coef(mod2)[,c(4:6,8)]
## =======
## Question 4
## =======
## fit logistic regression model of risk of esophageal cancer
mod3 <- regress("odds", case ~ bicider + age, esph)</pre>
coef3 \leftarrow coef(mod3)[,c(4:6,8)]
## =======
## Question 5
## =======
## fit logistic regression model of risk of esophageal cancer
mod4 <- regress("odds", case ~ bicider + poly(age,2), esph)</pre>
coef4 \leftarrow coef(mod4)[,c(4:6,8)]
# or, using qlm()
\# mod <- glm(case ~ bicider + I(age^4), family=binomial(), esph)
# coef <- cbind('e(Est)'=coef(mod), confint(mod)) %>% exp()
## =======
## Question 6 INCOMPLETE
## ========
## fit logistic regression model of risk of esophageal cancer
mod5 <- regress("odds", case ~ bicider + age + s1+s2+s3+s4+s5, esph)</pre>
coef5 \leftarrow coef(mod5)[,c(4:6,8)]
```

End of document.