GradientDescent

April 20, 2023

1 Implementing the Gradient Descent Algorithm

In this lab, we'll implement the basic functions of the Gradient Descent algorithm to find the boundary in a small dataset. First, we'll start with some functions that will help us plot and visualize the data.

```
In [1]: import matplotlib.pyplot as plt
    import numpy as np
    import pandas as pd

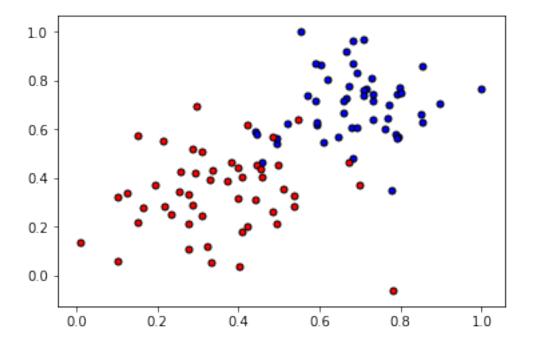
#Some helper functions for plotting and drawing lines

def plot_points(X, y):
    admitted = X[np.argwhere(y==1)]
    rejected = X[np.argwhere(y==0)]
    plt.scatter([s[0][0] for s in rejected], [s[0][1] for s in rejected], s = 25, color
    plt.scatter([s[0][0] for s in admitted], [s[0][1] for s in admitted], s = 25, color

def display(m, b, color='g--'):
    plt.xlim(-0.05,1.05)
    plt.ylim(-0.05,1.05)
    x = np.arange(-10, 10, 0.1)
    plt.plot(x, m*x+b, color)
```

1.1 Reading and plotting the data

```
In [2]: data = pd.read_csv('data.csv', header=None)
    X = np.array(data[[0,1]])
    y = np.array(data[2])
    plot_points(X,y)
    plt.show()
```



1.2 TODO: Implementing the basic functions

Here is your turn to shine. Implement the following formulas, as explained in the text. - Sigmoid activation function

$$\sigma(x) = \frac{1}{1 + e^{-x}}$$

• Output (prediction) formula

$$\hat{y} = \sigma(w_1x_1 + w_2x_2 + b)$$

• Error function

$$Error(y, \hat{y}) = -y \log(\hat{y}) - (1 - y) \log(1 - \hat{y})$$

• The function that updates the weights

$$w_i \longrightarrow w_i + \alpha(y - \hat{y})x_i$$

$$b \longrightarrow b + \alpha(y - \hat{y})$$

```
In [4]: import numpy as np
        # Activation (sigmoid) function
        def sigmoid(x):
            return 1/(1+np.exp(-x))
        # Output (prediction) formula
        def output_formula(features, weights, bias):
            return sigmoid(np.dot(features, weights) + bias)
        # Error (log-loss) formula
        def error_formula(y, output):
            return - y*np.log(output) - (1 - y) * np.log(1-output)
        # Gradient descent step
        def update_weights(x, y, weights, bias, learnrate):
            output = output_formula(x, weights, bias)
            error = y - output
            weights += learnrate*error*x
            bias += learnrate*error
            return weights, bias
```

1.3 Training function

This function will help us iterate the gradient descent algorithm through all the data, for a number of epochs. It will also plot the data, and some of the boundary lines obtained as we run the algorithm.

```
In [5]: np.random.seed(44)
        epochs = 100
        learnrate = 0.01
        def train(features, targets, epochs, learnrate, graph_lines=False):
            errors = []
            n_records, n_features = features.shape
            last_loss = None
            weights = np.random.normal(scale=1 / n_features**.5, size=n_features)
            bias = 0
            for e in range(epochs):
                del_w = np.zeros(weights.shape)
                for x, y in zip(features, targets):
                    output = output_formula(x, weights, bias)
                    error = error_formula(y, output)
                    weights, bias = update_weights(x, y, weights, bias, learnrate)
                # Printing out the log-loss error on the training set
```

```
out = output_formula(features, weights, bias)
    loss = np.mean(error_formula(targets, out))
    errors.append(loss)
    if e \% (epochs / 10) == 0:
        print("\n======= Epoch", e,"=======")
        if last_loss and last_loss < loss:</pre>
            print("Train loss: ", loss, " WARNING - Loss Increasing")
        else:
            print("Train loss: ", loss)
        last_loss = loss
        predictions = out > 0.5
        accuracy = np.mean(predictions == targets)
        print("Accuracy: ", accuracy)
    if graph_lines and e % (epochs / 100) == 0:
        display(-weights[0]/weights[1], -bias/weights[1])
# Plotting the solution boundary
plt.title("Solution boundary")
display(-weights[0]/weights[1], -bias/weights[1], 'black')
# Plotting the data
plot_points(features, targets)
plt.show()
# Plotting the error
plt.title("Error Plot")
plt.xlabel('Number of epochs')
plt.ylabel('Error')
plt.plot(errors)
plt.show()
```

1.4 Time to train the algorithm!

When we run the function, we'll obtain the following: - 10 updates with the current training loss and accuracy - A plot of the data and some of the boundary lines obtained. The final one is in black. Notice how the lines get closer and closer to the best fit, as we go through more epochs. - A plot of the error function. Notice how it decreases as we go through more epochs.

```
In [6]: train(X, y, epochs, learnrate, True)
======= Epoch 0 =======
Train loss: 0.713584519538
Accuracy: 0.4
====== Epoch 10 =======
Train loss: 0.622583521045
```

Accuracy: 0.59

======= Epoch 20 ======= Train loss: 0.554874408367

Accuracy: 0.74

======= Epoch 30 ======= Train loss: 0.501606141872

Accuracy: 0.84

======= Epoch 40 ======== Train loss: 0.459333464186

Accuracy: 0.86

Accuracy: 0.93

Accuracy: 0.93

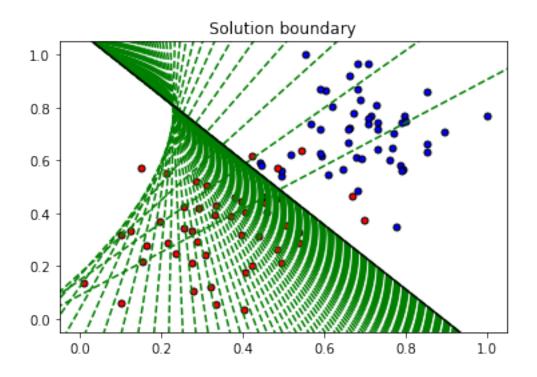
Accuracy: 0.93

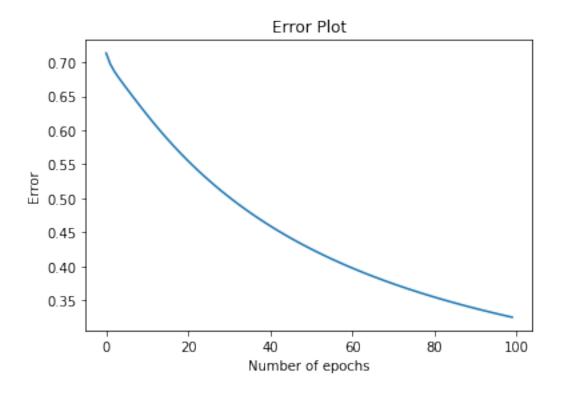
====== Epoch 80 ======= Train loss: 0.354599733682

Accuracy: 0.94

======= Epoch 90 ======= Train loss: 0.337927365888

Accuracy: 0.94





In []:

In []: