## Aleksandr Sherstyuk

Unofficial Transcript of Relevant Classes and Audits

#### 2023 - All Classes Audited Post Graduation

#### Reading group in Coxeter Groups via van Kampen Diagram methods

Fall

Vanderbilt University

Michael Mihalik

 Elementary proof of the deletion condition using van Kampen diagrams, walls and relation bands, parallel and strong parallel wall theorems, root systems, Stallings' theorem

### MATH 9300 - Seminar in Algebra: Groups Acting on Hyperbolic Space

Fall

Vanderbilt University

Denis Osin

• Asymptotic cones, HNN extensions, hyperbolicity, Gromov boundary, elliptic, parabolic, and hyperbolic elements

#### Review: MATH 4300 - Modern Algebra

Fall

Vanderbilt University

Larry Rolen

- In the direction of algebraic number theory
- Book: Algebra, by Hungerford

## Review: MATH 6100 - Theory of Functions of a Real Variable

Fall

Vanderbilt University

Jesse Peterson

- ullet Measure theory,  $\mathcal{L}^p$  spaces, Lebesgue integration, Fubini theorem, monotone convergence theorem Lebesgue dominated convergence theorem
- Book: Real Analysis: Modern Techniques and their Applications, by Folland

#### MATH 9201 - Seminar in Topology: Geometry and Topology of Surfaces

Spring an Runnels

Vanderbilt University

Ian Runnels

- Mapping class groups, curve complexes, hyperbolic geometry through the lens of the punctured torus
- Book: A Primer on Mapping Class Groups, by Farb, Margalit

### 2022 - Senior

### MATH 4200 - Topology (A)

Fall

 $Vanderbilt\ University$ 

Michael Mihalik

• Point-Set topology, separation axioms, function spaces, theorems of Tychonoff, Urysohn, Teitze, compactification

## MATH 4620 - Linear Optimization (A)

Fall

Vanderbilt University

Kevin Grace

- The simplex and dual simplex methods, complementary slackness, interior point method, ellipsoid method
- Book: A Gentle Introduction to Linear Optimization

#### CS 3891 - Numerical Methods for Computer Science (A)

Fall

Vanderbilt University

David Hyde

- Conditioning and stability, LU and Cholesky decomposition, Gram-Schmidt via Householder transformations and Givens rotations. Finding eigenvalues via power, inverse, QR iteration. SVD, PCA. Newton's method, secant method, the BFGS algorithm, Karush-Kuhn-Tucker conditions, conjugate gradient methods, Runge-Kutta methods
- Book: Numerical Algorithms by Solomon

## Audit: MATH 9100 - Seminar in Analysis: Approximation in C\* Algebras

Fall

Vanderbilt University

Jesse Peterson

- Completely positive maps, Arvesson's extension theorem, Voiculescu's theorem, nuclear and exact C\* algebras
- Book: C\* Algebras and Finite Dimensional Approximations by Brown, Ozawa

#### MATH 4201 - Topology (A)

Spring

 $Vanderbilt\ University$ 

Michael Mihalik

- Presented on the motivation and proof of the Seifert-van Kampen theorem in class and to an audience of prospective math grad students
- Fundamental group, covering spaces, the Galois connection, simplicial cellular and singular homology, theorems of Brouwer, Borsuk-Ulam, Euler characteristic, classifying Platonic solids and compact surfaces, fundamental theorem of algebra, Cayley complexes, ends of groups, hyperbolic geometry

## $\operatorname{CS}$ 3252 - Theory of Automata, Formal Languages, and Computation (A-)

Spring

Vanderbilt University

Douglas Fisher

- Deterministic and nondeterministic finite automata, regular expressions, context-free grammars and pushdown automata, Turing machines, undecidability and complexity theory
- Intro to Automata Theory, Languages, and Computation, by Hopcroft et al

## CE 3890 - Graduate Convex Optimization (with applications to control theory) (B)

Spring

Vanderbilt University

Ahmad Taha

- Convex sets, functions, optimization, Lagrange duality. Applications to control theory, Lyapunov stability
- Book: Convex Optimization by Boyd

### Audit: MATH 7200 - Algebraic Topology

Spring

Vanderbilt University

Anna Marie Bohmann

- Excision, Mayer-Vietoris sequences, universal coefficients theorem, the cup product and Kunneth formula, Poincare duality, Whitehead's theorem, the Hurewicz theorem
- Book: Algebraic Topology by Hatcher (chapters 2 and 3, and parts of 4)

#### CMST 1501 - Public Communication of Science (C+)

Spring

Vanderbilt University

Misti Yang

- Developed a presentation and video explaining covering spaces at a level accessible to high schoolers. Led to an ongoing personal project to add math animations to my completed script over the summer
- Professor Yang, whom I was close to, passed away on March 23 unexpectedly
- Theory and practice of speaking before an audience. Designed around the communication of science to non-specialists. Issues of adaptation, organization, evidence, delivery, and style

### 2021 - Second Gap Year During Covid-19, All Classes Audited

## MATH 8300 - Combinatorial and Geometric Group Theory

Fall

Vanderbilt University

Denis Osin

- Audited the first part of the class
- van Kampen diagrams, The Dehn function and the word problem, groups acting on trees

#### CS 3252 - Theory of Automata

Fall

Vanderbilt University

Douglas Fisher

- I later took this class. DFAs, NFAs, pumping lemma, formal grammars
- Book: Intro to Automata Theory, Languages, and Computation by Hopcroft et al

## MATH 8120 - Operator Algebras

Spring

Vanderbilt University

Jesse Peterson

- Gelfand-Mazur theorem, spectral radius formula for C\* algebras, Gelfand transform, GNS construction, von Neumann's bicommutant theorem, Kaplansky density theorem
- Book: An Introduction to Operator Algebras, by Zhu

## MATH 7210 - Riemannian Geometry

Spring

Vanderbilt University

Ioana Suvaina

• I audited the first half of the class. Tangent bundles, Riemannian manifolds, the Levi-Civita connection

### 2020 - First Gap Year During Covid-19, All Classes Audited

## MATH 9300 - Seminar in Algebra: Category Theory

Fall

Vanderbilt University

Constantine Tsinakis

- Categories, functors, natural transformations, limits, colimits, adjoint functors, Yoneda lemma, monads, topoi
- Presented on string diagrams, 2-category theory, elementary theory of topoi

#### MATH 7120 - Functional Analysis

Fall

Vanderbilt University

Vaughan Jones

- Class got canceled due to the passing of Dr. Jones. I continued self teaching using Kreyszig, then Lax
- Han-Banach, open mapping, closed graph, uniform bounded, bounded inverse theorems, spectral theory, distribution theory

## MATH 9800 - Seminar in Number Theory: Modular Forms

Fall

Fall

Vanderbilt University

Larry Rolen

• Survey of the theory of modular forms and its applications, as well as its connections to other objects of number theory and other areas of mathematics

## MATH 4300 - Modern Algebra

Mark Sapir

Vanderbilt University

• Worked independently out of his textbook, Combinatorial Algebra: Syntax and Semantics, with him

### MATH 4301 - Modern Algebra

Spring

Vanderbilt University

Mark Sapir

Specialized topics included Grobner bases, combinatorial algebraic geometry, van Kampen diagrams

#### MATH 7130 - Harmonic Analysis

Vanderbilt University

Spring

Alex Powell

- Presented on: Pontryagin duality for LCAGs, representation theory, characters, and the "Fourier transform", and Heisenberg's U.P. for finite nonabelian groups; elementary Tannaka-Krein duality
- Book: Intro to Harmonic Analysis, by Heil
- Presentation Resources: Harmonic Analysis on Finite Groups, by Terras; Tao's Lecture Notes 9-10 for 247B

#### MATH 9301 - Seminar in Algebra: Growth of Groups

Spring

Vanderbilt University

Denis Osin

• Ultrafilters and ultralimits, asymptotic cones, quasi-isometry, Svarc-Milnor lemma, Grigorchuk's group and groups of intermediate growth, Gromov's gap, amenability

#### CS 6310 - Design and Analysis of Algorithms

Spring

Vanderbilt University

Jeremy Spinrad

• Ford Fulkerson, Edmonds Blossom, Fortune's algorithms, Van Emde Boas trees, Voronoi cells

## 2019 - Junior, Spring Classes Taken Pass/Fail due to Covid-19

#### MATH 4710 - Graph Theory (B)

Fall

Vanderbilt University

Mark Ellingham

- Network flows, matchings, colorability, connectivity, graph polynomials
- Book: Graph Theory, by Bondy, Murty

# $\operatorname{CS}$ 6311 / $\operatorname{CS}$ 3860 - Graph Algorithms (A)

Fall

Vanderbilt University

Jeremy Spinrad

- Worked on open problems as an undergraduate researcher
- Graph classes admitting efficient computer representations. Recognition, enumeration, and reconstruction algorithms
- Book: Efficient Graph Representations, by Spinrad

#### MATH 3890 - Mathematical Game Theory (B-)

Fall

Vanderbilt University

Paul Edelman

- $\bullet$  Cooperative and noncooperative. Proofs of theorems of Von Neumann Morganstern, Nash
- Shapley value, Banzhaf index, connections to linear optimization
- Book: Game Theory: Alive!, by Karlin, Peres

#### ECON 4260 - Game Theory with Economic Applications (B)

Fall

Vanderbilt University

John Weymark

• Analysis of specific economic models. Decision theory, utility theory, Cournot duopoly, Bertrand competition

#### MATH 2820 - Intro to Probability and Mathematical Statistics (Pass)

Spring

Vanderbilt University

Jakayla Robbins

- Probability theory, moment generating functions, joint densities, confidence intervals, biased and unbiased estimators
- Book: Probability and Statistics, by Devore

### MATH 3100 - Intro to Analysis (Pass)

Spring

Vanderbilt University

Gieri Simonett

- Sequences and series, uniform convergence, differentiation and integration. Bolzano-Weierstrass, Heine-Borel
- Book: Intro to Analysis, by Gaughan

## MATH 3230 - Intro to Differential Geometry (Pass)

Spring

Vanderbilt University

Rares Rasdeaconu

- Smooth structures, tangent space, Sard's theorem, transversality, intersection theory modulo 2, basic Morse theory
- Book: Differential Topology by Pollack, Guillemin

## MATH 4310 - Set Theory (Pass)

Spring

Vanderbilt University

Constantine Tsinakis

• Equivalence of the axiom of choice, Zorn's lemma, and the well-ordering principle. Cardinal and ordinal arithmetic

• Book: Set Theory and Metric Spaces, by Kaplansky

### Audit: MATH 3310 - Intro to Mathematical Logic

Spring

Vanderbilt University

Jose Gil-Ferez

• First order logic, Godel's theorems, introduction to model theory, compactness

#### Math 4300 - Graduate Modern Algebra (B-)

Fall

Vanderbilt University

Aleksandr Olshanskiy

- Sylow theorems, Jordan-Holder theorem, Nielsen-Schreier theorem, Tietze transformations, basic ring and field theory
- Book: Advanced Modern Algebra, by Rotman

### Math 4710 - Graph Theory (C)

Fall

Vanderbilt University

Mark Ellingham

- Network flows, matchings, colorability, connectivity, graph polynomials
- Book: Graph Theory, by Bondy, Murty

### CS 3650 - Algorithms (B)

Fall

Vanderbilt University

Jeremy Spinrad

- Dynamic programming, BFS, DFS, Bellman-Ford, Huffman coding, NP completeness, reductions
- Book: Algorithms, by Cormen et al

## Math 3200 - Intro to Topology (B)

Spring

Vanderbilt University

Anna Marie Bohmann

- Continuity, Hausdorff property, connectedness, compactness, metric spaces
- Book: Topology: Pure and Applied, by Adams, Franzosa

## Math 3890 - Advanced Linear Algebra (A-)

Spring

 $Vanderbilt\ University$ 

Akram Aldroubi

• Banach and Hilbert spaces, Riesz representation, singular value decomposition, Courant-Fischer theorem

#### Audit Math 4700 - Combinatorics

Spring

Vanderbilt University

Mark Ellingham

- Combinations, permutations, Stanley's 12-fold way, inclusion-exlusion, recurrence relations, generating functions, Burnside's lemma, Polya enumeration
- Book: Enumerative Combinatorics, by Stanley

#### ECON 3893 - Market Design and Resource Allocation (B+)

Spring

 $Vanderbilt\ University$ 

Eun Jeong Heo

- Top trading cycle, stable marriage problem, cake cutting algorithms, Gallai-Edmonds decomposition
- Presented on the paper Fair Matching Under Constraints, by Fuhito Kojima, Yuichiro Kamada.
- Book: Market Design: Auctions and Matching, by Haeringer

## ECON 4220 - Social Choice Theory (B+)

Spring

Vanderbilt University

John Weymark

- $\bullet\,$  Arrow's impossibility theorem, Gibbard-Satterthwaite theorem, Sen's liberal paradox
- Report on the paper Efficient and Incentive-Compatible Liver Exchange by Utku Unver, Tayfun Sonmez
- Book: A Primer in Social Choice Theory, by Gaertner

## Audit: CS 6310 - Graduate Design and Analysis of Algorithms

Spring

Vanderbilt University

Jeremy Spinrad

• Ford Fulkerson, Edmonds Blossom, Fortune's algorithms, Van Emde Boas trees, Voronoi cells

#### 2017 - Freshman

### Math 2500 - Honors Multivariate Calculus and Linear Algebra (B+)

Fall

Vanderbilt University

Bruce Hughes

- Jacobian, implicit and inverse function theorems, Lagrange multipliers
- Book: Multivariable Mathematics, by Shifrin

## $\operatorname{CS}$ 2201 - Program Design and Data Structures (B-)

Fall

Vanderbilt University

Gerald Roth

• C++, basic data structures and algorithms, recursion

## Math 2501 - Honors Multivariate Calculus and Linear Algebra (A-)

Spring Bruce Hughes

Vanderbilt University

Differential forms on manifolds, generalized stokes theorem, spectral theorem
Book: Multivariable Mathematics, by Shifrin

# Math 2420 - Methods of Ordinary Differential Equations (A)

Spring

Vanderbilt University

Gennadi Kasparov

- Higher-order linear differential equations, Laplace transform, series solutions
- Book: Fundamentals of Differential Equations, by Nagle, Saff, Snider

## CS 2212 - Discrete Structures (A)

Vanderbilt University

• Sets, relations, basic combinatorics, recurrence relations, boolean algebra, propositional calculus

Abstract Algebra (B)

Summer Keith Oulette

Dominique Piot

Spring

• Basic number theory, polynomial rings, ring theory, Euclidian division algorithm

Complex Analysis (B)

UCLA

Summer

UCLA Robert Greene

• Cauchy-Riemann equations, Cauchy's integral theorem and formula, Taylor and Laurent series, residue theorem