


```

Clear["Global`*"]
Needs["Notation`"]
Msun = 2 × 1033;
Mdotsol =  $\left( \frac{Msun}{3.15 \times 10^7} \right)$ 
G = 6.67 × 10-8;
c = 3 × 1010;
σ = 5.67 × 10-5;
kb = 1.38 × 10-16;
mp = 1.67 × 10-27;
me = 9 × 10-31;
kes = 0.4;

Symbolize[ $\dot{M}$ ]
Symbolize[ $\hat{\kappa}$ ]
Symbolize[ $M_7$ ]
Symbolize[ $\alpha_{0.3}$ ]
Symbolize[ $\dot{m}$ ]
Symbolize[ $\dot{M}_{\text{Edd}}$ ]
Symbolize[ $L_{\text{Edd}}$ ]
Symbolize[ $R_s$ ]
Symbolize[ $\epsilon_{0.1}$ ]

M = 107 Msun M7;
LEdd = 4 π G  $\frac{M}{0.4 \mu e \hat{\kappa}}$  c ;

 $\dot{M}_{\text{Edd}} = \frac{L_{\text{Edd}}}{c^2 \epsilon_{0.1} 0.1}$ ;
 $\dot{M} = \dot{m} \dot{M}_{\text{Edd}}$ ;
 $R_s = 2 G \frac{M}{c^2}$ ;
R = 103 Rs r3;

Q = G  $\frac{M}{R^3}$ 

Teff =  $\left( \frac{3}{8 \pi \sigma} \frac{G M \dot{M}}{R^3} \right)^{1/4}$  // Simplify[#, Assumptions → {M7 > 0, r3 > 0}] &

Tc = 8 × 104 μ01/5 μe-1/5 r3-9/10 M7-1/5 α0.3-1/5 fT1/5  $\left( \frac{\dot{m}}{\epsilon_{0.1}} \right)^{2/5} \hat{\kappa}^{1/5}$ ;

Σ =  $\frac{\dot{M}}{3 \pi \frac{kb Tc}{\mu_0 mp} 0.3 \alpha_{0.3}}$   $\left( G \frac{M_7 10^7 Msun}{R^3} \right)^{1/2}$  // Simplify[#, Assumptions → {M7 > 0, r3 > 0}] &

```

$$6.34921 \times 10^{25}$$

Symbolize::bsymbexs :

Warning: The box structure attempting to be symbolized has a similar or identical symbol already defined, possibly overriding previously symbolized box structure. >>

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$$5.12066 \times 10^{-14}$$

$$\frac{M_7^2 r 3^3}{\mu e}$$

$$6229.49 \left(\frac{\dot{m}}{M_7 r 3^3 \epsilon_{0.1} \hat{\kappa} \mu e} \right)^{1/4}$$

$$169.123 \left(\frac{\dot{m}}{\epsilon_{0.1}} \right)^{3/5} \mu 0^{4/5}$$

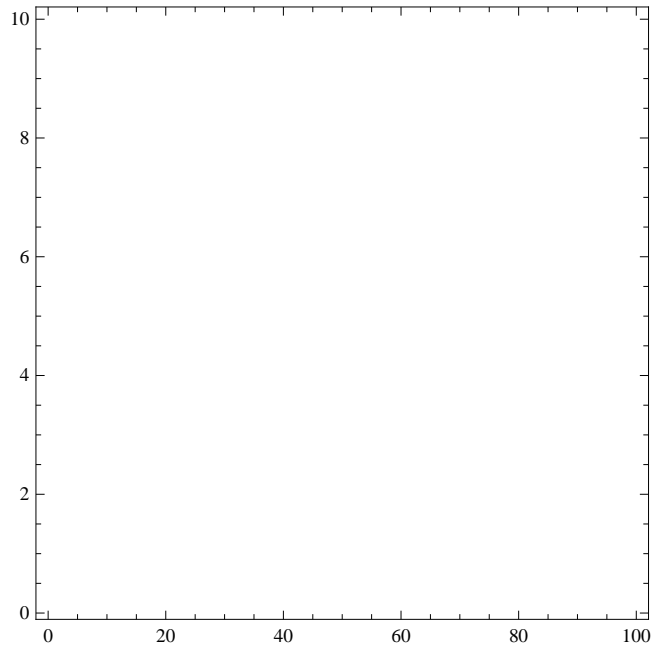
$$\alpha_{0.3}^{4/5} \hat{\kappa}^{6/5} \mu e^{4/5} \left(\frac{r 3^3 f_T}{M_7} \right)^{1/5}$$

(*Compton y parameter*)

$$y = 4 \text{ kb } \frac{\text{Tcl}}{m_e c^2} \text{Max}\left[\Sigma \frac{\kappa \epsilon s}{2}, \left(\Sigma \frac{\kappa \epsilon s}{2}\right)^2\right] /.$$

$\{\alpha_{0.3} \rightarrow 1, \mu_0 \rightarrow 0.615, \mu_e \rightarrow 0.875, \epsilon_{0.1} \rightarrow 1, \dot{m} \rightarrow 0.1, \hat{\kappa} \rightarrow 1, f_T \rightarrow 3/8\}$ // Simplify
 RegionPlot[y > 1, {M₇, 0.01, 100}, {r₃, 0.1, 10}]

$$6.81481 \times 10^{-7} \text{Tcl Max}\left[\frac{60.791}{\left(\frac{r_3^3}{M_7}\right)^{2/5}}, \frac{7.79686}{\left(\frac{r_3^3}{M_7}\right)^{1/5}}\right]$$



```

Teff1 = Teff /. { $\alpha_{0.3} \rightarrow 1$ ,  $\mu_0 \rightarrow 0.615$ ,  $\mu_e \rightarrow 0.875$ ,  $\epsilon_{0.1} \rightarrow 1$ ,  $\dot{m} \rightarrow 0.1$ ,  $\hat{\kappa} \rightarrow 1$ ,  $f_T \rightarrow 3/8$ };
 $\Sigma_1 = \Sigma /. \{\alpha_{0.3} \rightarrow 1, \mu_0 \rightarrow 0.615, \mu_e \rightarrow 0.875, \epsilon_{0.1} \rightarrow 1, \dot{m} \rightarrow 0.1, \hat{\kappa} \rightarrow 1, f_T \rightarrow 3/8\}$ ;
 $Q_1 = Q /. \{\alpha_{0.3} \rightarrow 1, \mu_0 \rightarrow 0.615, \mu_e \rightarrow 0.875, \epsilon_{0.1} \rightarrow 1, \dot{m} \rightarrow 0.1, \hat{\kappa} \rightarrow 1, f_T \rightarrow 3/8\}$ ;

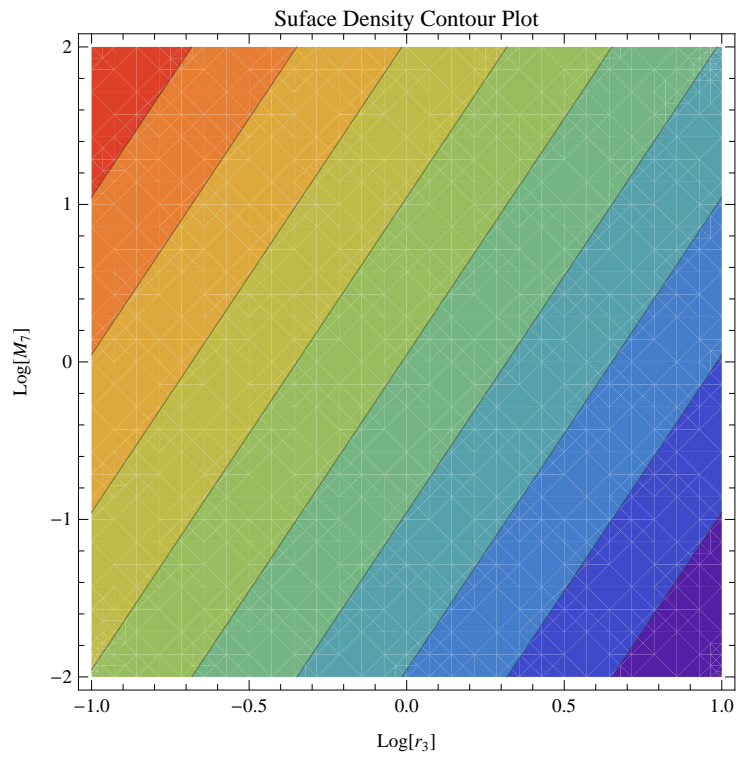
 $\Sigma_1 /. \{r_3 \rightarrow 0.1, M_7 \rightarrow 100\}$ 
 $\Sigma_1 /. \{r_3 \rightarrow 10, M_7 \rightarrow 0.01\}$ 
 $Q_1 /. \{r_3 \rightarrow 0.1, M_7 \rightarrow 0.01\}$ 
 $Q_1 /. \{r_3 \rightarrow 10, M_7 \rightarrow 100\}$ 

OurDir = SetDirectory[NotebookDirectory[]]
Needs["PlotLegends`"]
 $\Sigma_{\text{Max}} = \text{Log}[10, \Sigma_1] /. \{r_3 \rightarrow 0.1, M_7 \rightarrow 100\}$ ;
 $\Sigma_{\text{Min}} = \text{Log}[10, \Sigma_1] /. \{r_3 \rightarrow 10, M_7 \rightarrow 0.01\}$ ;
 $Q_{\text{Max}} = \text{Log}[10, Q_1] /. \{r_3 \rightarrow 0.1, M_7 \rightarrow 0.01\}$ ;
 $Q_{\text{Min}} = \text{Log}[10, Q_1] /. \{r_3 \rightarrow 10, M_7 \rightarrow 100\}$ ;
 $T_{\text{Min}} = \text{Log}[10, \text{Teff1}] /. \{r_3 \rightarrow 10, M_7 \rightarrow 100\}$ ;
 $T_{\text{Max}} = \text{Log}[10, \text{Teff1}] /. \{r_3 \rightarrow 0.1, M_7 \rightarrow 0.01\}$ ;

 $\Sigma_{\text{Legend}} = \text{Graphics}[$ 
  Legend[Function[{x}, ColorData["Rainbow"][x]], 50, NumberForm[ $\Sigma_{\text{Min}}$ , 2] // ToString,
  NumberForm[ $\Sigma_{\text{Max}}$ , 2] // ToString, LegendShadow → False, LegendBorderSpace → 2]];
 $Q_{\text{Legend}} = \text{Graphics}[$ 
  Legend[Function[{x}, ColorData["Rainbow"][x]], 50,
  NumberForm[ $Q_{\text{Min}}$ , 2] // ToString, NumberForm[ $Q_{\text{Max}}$ , 2] // ToString,
  LegendShadow → False, LegendBorderSpace → 2]];
 $\text{TeffLegend} = \text{Graphics}[$ 
  Legend[Function[{x}, ColorData["Rainbow"][x]], 50,
  NumberForm[ $T_{\text{Min}}$ , 2] // ToString, NumberForm[ $T_{\text{Max}}$ , 2] // ToString,
  LegendShadow → False, LegendBorderSpace → 2]];

SetOptions[ContourPlot, ImageSize → Medium];
GraphicsRow[
  GraphicsRow/@{
    ContourPlot[Log[10,  $\Sigma_1$ ] /. { $r_3 \rightarrow 10^x, M_7 \rightarrow 10^y$ }, {x, -1, 1}, {y, -2, 2},
      PlotLabel → "Surface Density Contour Plot", FrameLabel → {"Log[ $r_3$ ]", "Log[ $M_7$ "]},
      ColorFunction → Function[{x}, ColorData["Rainbow"][x]],  $\Sigma_{\text{Legend}}$ },
    ContourPlot[Log[10,  $Q_1$ ] /. { $r_3 \rightarrow 10^x, M_7 \rightarrow 10^y$ }, {x, -1, 1}, {y, -2, 2},
      PlotLabel → "Q Contour Plot", FrameLabel → {"Log[ $r_3$ ]", "Log[ $M_7$ "]},
      ColorFunction → Function[{x}, ColorData["Rainbow"][x]],  $Q_{\text{Legend}}$ },
    ContourPlot[{Log[10, Teff1] /. { $r_3 \rightarrow 10^x, M_7 \rightarrow 10^y$ }}, {x, -1, 1}, {y, -2, 2},
      PlotLabel → "Teff Contour Plot", FrameLabel → {"Log[ $r_3$ ]", "Log[ $M_7$ "]},
      ColorFunction → Function[{x}, ColorData["Rainbow"][x]], TeffLegend}}]
389843.
3898.43
 $5.12066 \times 10^{-7}$ 
 $5.12066 \times 10^{-21}$ 
/home/aleksey/First_Year_Project

```



$0.64^{4/3}$

0.551535

$$\tau_c = 8 \times 10^4 \mu_0^{1/5} \mu_e^{-1/5} r_3^{-9/10} M_7^{-1/5} \left(\frac{\alpha}{0.3} \right)^{-1/5} f_t^{1/5} \left(\frac{\dot{m}}{(\epsilon / 0.1)} \right)^{2/5} / .$$

$$\left\{ \mu_0 \rightarrow 0.615, \mu_e \rightarrow 0.875, \alpha \rightarrow 0.3, f_t \rightarrow \frac{3}{4}, \epsilon \rightarrow 0.1, \dot{m} \rightarrow 0.1 \right\}$$

$$\frac{28\,020.5}{M_7^{1/5} r_3^{9/10}}$$

$$3.1 M_7^{-1/5} / . \{ M_7 \rightarrow 10^{-4} \}$$

$$(2.8)^{10/9}$$

19.5597

3.13937

```

ρc kb  $\frac{Tc}{\mu0 \text{ mp}}$  /. {μ0 → 0.615, Tc → 105, ρc → 1.5 × 10-8}
4 σ Tc4 / (3 c) /. {Tc → 105}
cs =  $\sqrt{\gamma (4 \sigma Tc^4 / (3 c \rho c))}$ 
H =  $\frac{Mdot}{3 \pi \Sigma cs \alpha}$  /. {μ0 → 0.615, Tc → 105, Σ → 90 000, Mdot → 1.40 × 1024, α → 0.3, γ → 4 / 3}
rul = (Solve[ $\frac{90\,000}{2 H} == \rho c, \rho c$ ])[[3]]
ρc kb  $\frac{Tc}{\mu0 \text{ mp}}$  /. {μ0 → 0.615, Tc → 105, ρc → 1.5 × 10-8}
4 σ Tc4 / (3 c) /. rul /. Tc → 105
 $\frac{H}{cs}$  /. rul /. {μ0 → 0.615, Tc → 105, Σ → 90 000, Mdot → 1.40 × 1024, α → 0.3, γ → 4 / 3}
(*  $\frac{H}{cs}$  /. rul

```

$$2 \frac{\pi}{\sqrt{G M/R^3}} /. \{M \rightarrow M_7, 10^7 M_{\text{sun}}, R \rightarrow 200 R_s, M_7 \rightarrow 1\} *)$$

7.78685

$$\frac{56\,474.8}{M^{1/5} r^{9/10}}$$

$$\frac{1553.47}{M^{4/5} r^{18/5}}$$

$$39.4141 \sqrt{\frac{\gamma}{M^{4/5} r^{18/5} \rho c}}$$

$$\frac{1.20885 \times 10^{17}}{\sqrt{\frac{1}{M^{4/5} r^{18/5} \rho c}}}$$

$$\left\{ \rho c \rightarrow \frac{5.1748 \times 10^{-9}}{M^{4/15} r^{6/5}} \right\}$$

$$\frac{56\,474.8}{M^{1/5} r^{9/10}}$$

$$\frac{1553.47}{M^{4/5} r^{18/5}}$$

$$1.3745 \times 10^7 M^{8/15} r^{12/5}$$

```

(*Example of a particular profile*)
M = 107 Msun;
μe = 1;
μ0 = 0.615;
κes = 0.4 μe;
(*Import profile and extract physical parameters*)
MyFile = "profile-43395-0.1-700";
MyFileP = StringSplit[MyFile, "-"] // #[[2 ;;]] &;
MyFileP = ToExpression /@ MyFileP;
Σ = MyFileP[[1]];

Ṁ = MyFileP[[2]] 10 × 4 π G  $\frac{M}{c \kappa es}$ ;

R = MyFileP[[3]] 2 G  $\frac{M}{c^2}$ ;

(*Kinematic viscosity*)
ν =  $\frac{\dot{M}}{3 \pi \Sigma}$ ;

(*Keplerian angular velocity*)
Ω =  $\sqrt{G \frac{M}{R^3}}$ ;

(*Central sound speed*)
cs0 =  $\sqrt{k_b \frac{T_c}{\mu_0 m_p}}$ ;

Teff =  $\left( \left( \frac{9}{8} \nu \Sigma \right) \frac{\Omega^2}{\sigma} \right)^{0.25}$ ;

Tss[Tc_, u_, Σ_] := Tc  $\left( 1 - 4 \left( \frac{u}{\Sigma} \right)^2 \right)^{1/4}$ ;

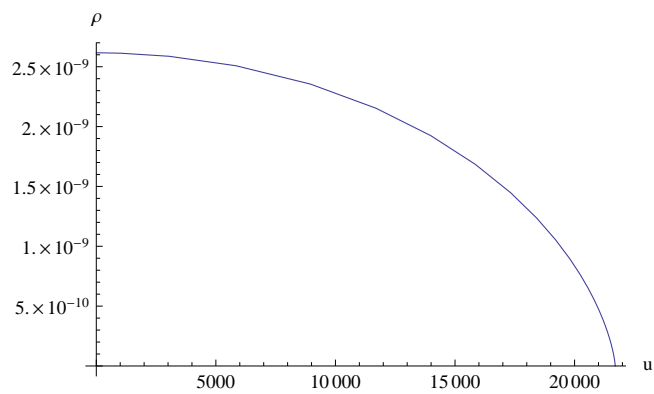
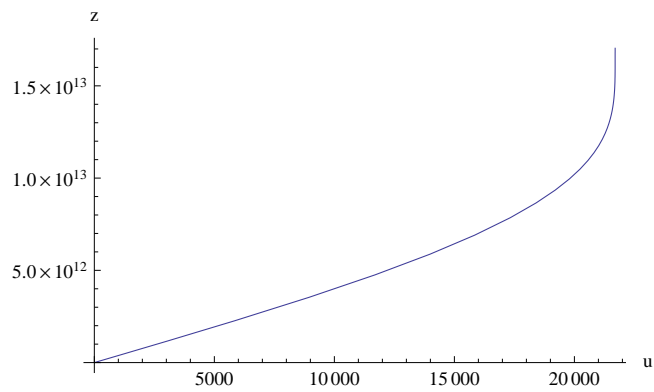
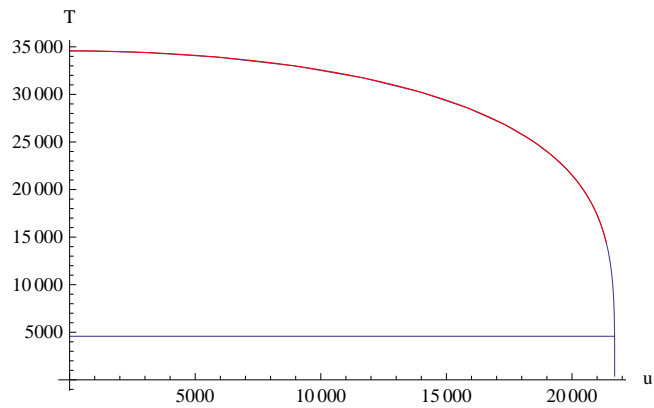
profile = Import[NotebookDirectory[] <> MyFile, "Table"];
(*Finding the points which bracket the effective temperature*)
tlow = (Position[profile[[All, 4]], x_ /; x < Teff])[[1]];
thigh = (Position[profile[[All, 4]], x_ /; x > Teff])[[1]];
Extract[profile[[All, 1]], {thigh, tlow}]

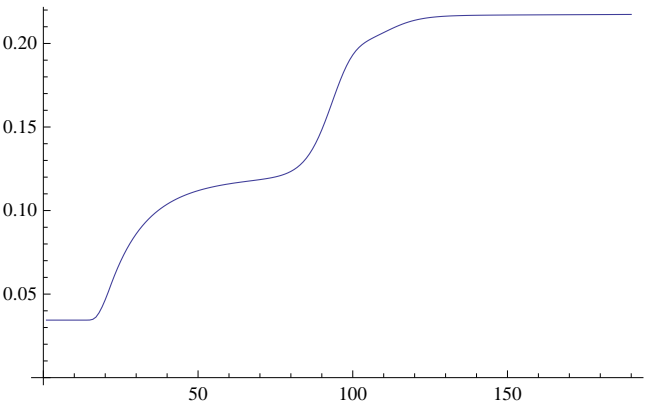
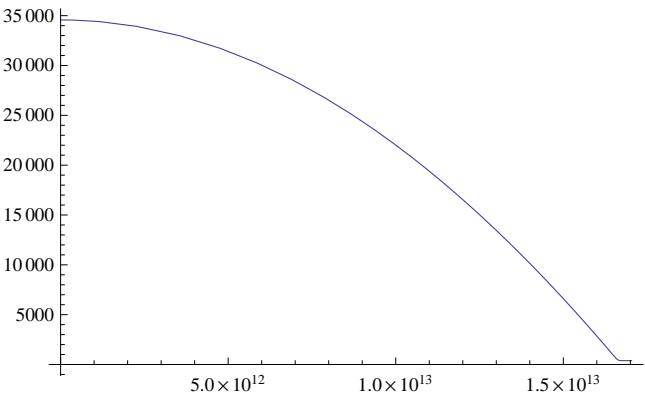
Print["u*=",  $\frac{\Sigma}{2} \sqrt{1 - \frac{8}{(3/2) \kappa es \Sigma}}$ ]

u0 = profile[[All, 1]] // Min;
umax = profile[[All, 1]] // Max;
Tc = profile[[1, 4]];
t1 = Show[{profile[[All, {1, 4}]]} // ListLinePlot[#, PlotRange → All] &,
  Plot[Teff, {u, u0, umax}], PlotRange → All, AxesLabel → {"u", "T"}, AxesOrigin → {0, 0}];
t2 = Plot[Tss[Tc, u, Σ], {u, 0, umax}, PlotStyle → Directive[Red]];
Show[t1, t2]
{profile[[All, {1, 2}]]} // ListLinePlot[#, AxesLabel → {"u", "z"}, PlotRange → All] &
{profile[[All, {1, 3}]]} // ListLinePlot[#, AxesLabel → {"u", "ρ"}, PlotRange → All] &
profile[[All, {2, 4}]] //
  ListLinePlot[#, PlotRange → All, AxesOrigin → {0, 0}, PlotRange → All] &
(profile[[All, 6]] - profile[[All, 7]]) // ListLinePlot[#, AxesOrigin → {0, 0}] &

2.15535 × 106

```


$\{21\,694., 21\,694.\}$
 $u^* = 21\,694.2$




$$\frac{1.38 \times 10^{-23} \cdot 10^9}{1.6 \times 10^{-19}}$$

86 250 .