

Clear["Global`\*"]

Msun =  $2 \times 10^{33}$ ;

Mdotsol =  $\left( \frac{\text{Msun}}{3.15 \times 10^7} \right)$

G =  $6.67 \times 10^{-8}$ ;

c =  $3 \times 10^{10}$ ;

$\sigma = 5.67 \times 10^{-5}$ ;

kb =  $1.38 \times 10^{-16}$ ;

mp =  $1.67 \times 10^{-24}$ ;

Tc =  $8 \times 10^4 \mu_0^{1/5} \mu e^{-1/5} r_3^{-9/10} M_7^{-1/5} \alpha_{0.3}^{-1/5} f_T^{1/5} \left( \frac{\dot{m}}{\epsilon_{0.1}} \right)^{2/5} \hat{\kappa}^{1/5}$  ;

L\_Edd =  $4 \pi G \frac{M_7}{0.4 \mu e \hat{\kappa}} c 10^7 \text{ Msun}$ ;

$\dot{M}_{\text{Edd}} = \frac{L_{\text{Edd}}}{c^2 \epsilon_{0.1} 0.1}$ ;

$\dot{M} = \dot{m} \dot{M}_{\text{Edd}}$ ;

R\_s =  $2 G \frac{M_7}{c^2} 10^7 \text{ Msun}$ ;

$\frac{\dot{M}}{3 \pi \frac{kb T_c}{\mu_0 mp} 0.3 \alpha_{0.3}} \left( G \frac{M_7 10^7 \text{ Msun}}{r_3^3 (10^3 R_s)^3} \right)^{1/2} // \text{Simplify}[\#, \text{Assumptions} \rightarrow \{M_7 > 0, r_3 > 0\}] \ \&$

$6.34921 \times 10^{25}$

$\frac{169123. \mu_0^{4/5} \left( \frac{\dot{m}}{\epsilon_{0.1}} \right)^{3/5}}{\mu e^{4/5} \hat{\kappa}^{6/5} \left( \frac{r_3^3 f_T}{M_7} \right)^{1/5} \alpha_{0.3}^{4/5}}$

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Clear[Tc]
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$$\rho_{\text{c kb}} \frac{T_{\text{c}}}{\mu_0 \text{ mp}} /. \{\mu_0 \rightarrow 0.615, T_{\text{c}} \rightarrow 10^5, \rho_{\text{c}} \rightarrow 1.5 \times 10^{-8}\}$$

$$4 \sigma T_{\text{c}}^4 / (3 \text{ c}) /. \{T_{\text{c}} \rightarrow 10^5\}$$

$$c_{\text{s}} = \sqrt{\gamma (4 \sigma T_{\text{c}}^4 / (3 \text{ c } \rho_{\text{c}}))}$$

$$H = \frac{\text{Mdot}}{3 \pi \Sigma c_{\text{s}} \alpha} /. \{\mu_0 \rightarrow 0.615, T_{\text{c}} \rightarrow 10^5, \Sigma \rightarrow 90\,000, \text{Mdot} \rightarrow 1.40 \times 10^{24}, \alpha \rightarrow 0.3, \gamma \rightarrow 4/3\}$$

$$\text{rul} = \left( \text{solve} \left[ \frac{90\,000}{2 H} == \rho_{\text{c}}, \rho_{\text{c}} \right] \right)[[3]]$$

$$\rho_{\text{c kb}} \frac{T_{\text{c}}}{\mu_0 \text{ mp}} /. \{\mu_0 \rightarrow 0.615, T_{\text{c}} \rightarrow 10^5, \rho_{\text{c}} \rightarrow 1.5 \times 10^{-8}\}$$

$$4 \sigma T_{\text{c}}^4 / (3 \text{ c}) /. \text{rul} /. T_{\text{c}} \rightarrow 10^5$$

$$\frac{H}{c_{\text{s}}} /. \text{rul} /. \{\mu_0 \rightarrow 0.615, T_{\text{c}} \rightarrow 10^5, \Sigma \rightarrow 90\,000, \text{Mdot} \rightarrow 1.40 \times 10^{24}, \alpha \rightarrow 0.3, \gamma \rightarrow 4/3\}$$

$$(\star \frac{H}{c_{\text{s}}}) /. \text{rul}$$

$$2 \frac{\pi}{\sqrt{G M / R^3}} /. \{M \rightarrow M_7 10^7 \text{ Msun}, R \rightarrow 200 R_{\text{s}}, M_7 \rightarrow 1\} \star)$$

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$$5.01996 \times 10^{-8} \sqrt{\frac{T_{\text{c}}^4 \gamma}{\rho_{\text{c}}}}$$

$$\frac{9.49125 \times 10^{15}}{\sqrt{\frac{1}{\rho_{\text{c}}}}}$$

$$\{\rho_{\text{c}} \rightarrow 2.82223 \times 10^{-8}\}$$

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(*Example of a particular profile*)
M = 107 Msun;
μe = 1;
μ0 = 0.615;
κes = 0.4 μe;
(*Import profile and extract physical parameters*)
MyFile = "profile-35035-0.1-1000";
MyFileP = StringSplit[MyFile, "-"] // #[[2 ;;]] &;
MyFileP = ToExpression /@ MyFileP;
Σ = MyFileP[[1]];

Ṁ = MyFileP[[2]] 10 × 4 π G  $\frac{M}{c \kappa es}$ ;

R = MyFileP[[3]] 2 G  $\frac{M}{c^2}$ ;

(*Kinematic viscosity*)
ν =  $\frac{\dot{M}}{3 \pi \Sigma}$ ;

(*Keplerian angular velocity*)
Ω =  $\sqrt{G \frac{M}{R^3}}$ ;

(*Central sound speed*)
cs0 =  $\sqrt{k_b \frac{Tc}{\mu_0 mp}}$ 

Teff =  $\left( \left( \frac{9}{8} \nu \Sigma \right) \frac{\Omega^2}{\sigma} \right)^{0.25}$ ;

Tss[Tc_, u_, Σ_] := Tc  $\left( 1 - 4 \left( \frac{u}{\Sigma} \right)^2 \right)^{1/4}$ ;

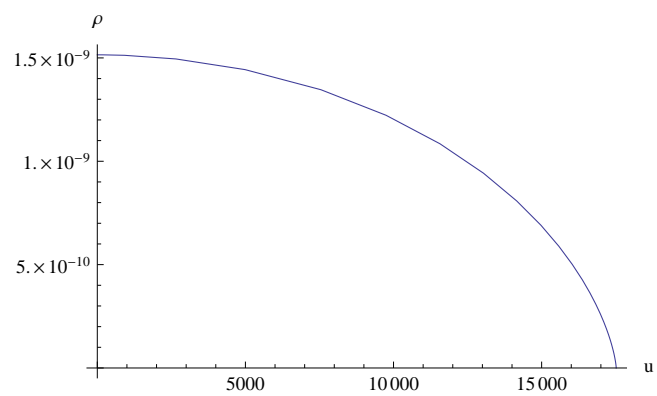
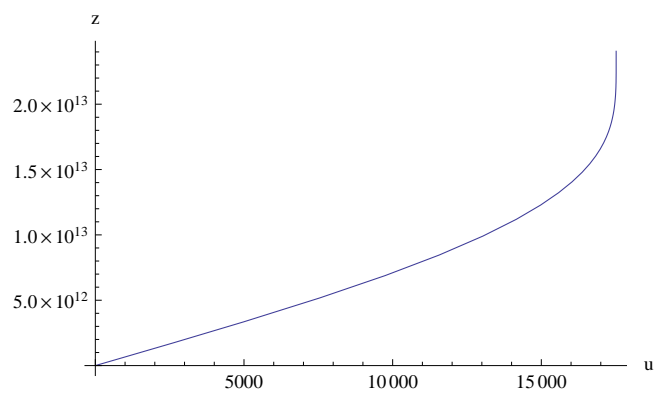
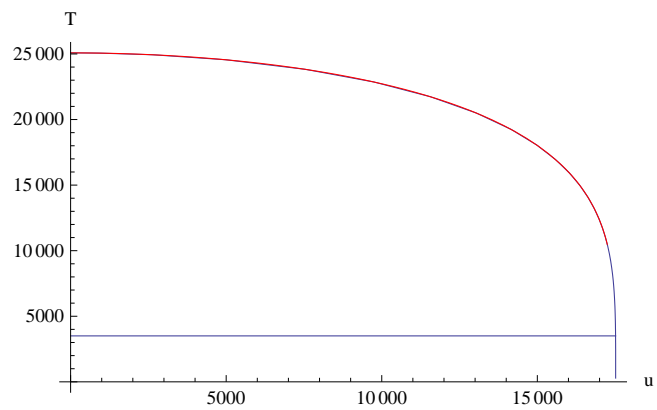
(*Finding the points which bracket the effective temperature*)
tlow = (Position[profile[[All, 4]], x_ /; x < Teff])[[1]];
thigh = (Position[profile[[All, 4]], x_ /; x > Teff])[[1]];
Extract[profile[[All, 1]], {thigh, tlow}]

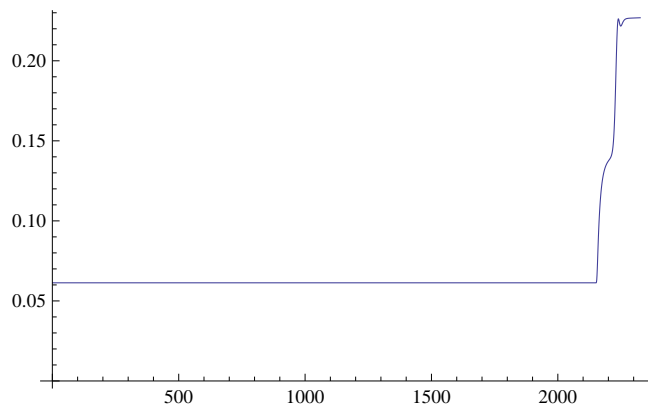
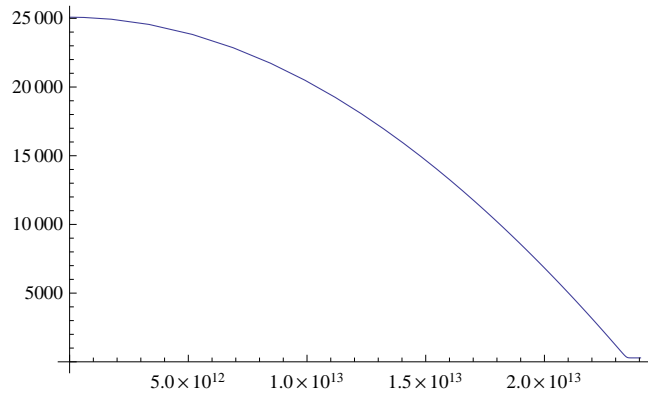
Print["u*=",  $\frac{\Sigma}{2} \sqrt{1 - \frac{8}{(3/2) \kappa es \Sigma}}$ ]

profile = Import[NotebookDirectory[] <> MyFile, "Table"];
u0 = profile[[All, 1]] // Min;
umax = profile[[All, 1]] // Max;
Tc = profile[[1, 4]];
t1 = Show[{profile[[All, {1, 4}]]} // ListLinePlot[#, PlotRange → All] &,
  Plot[Teff, {u, u0, umax}], PlotRange → All, AxesLabel → {"u", "T"}, AxesOrigin → {0, 0}];
t2 = Plot[Tss[Tc, u, Σ], {u, 0, umax}, PlotStyle → Directive[Red]];
Show[t1, t2]
{profile[[All, {1, 2}]]} // ListLinePlot[#, AxesLabel → {"u", "z"}, PlotRange → All] &
{profile[[All, {1, 3}]]} // ListLinePlot[#, AxesLabel → {"u", "ρ"}, PlotRange → All] &
profile[[All, {2, 4}]] //
  ListLinePlot[#, PlotRange → All, AxesOrigin → {0, 0}, PlotRange → All] &
(profile[[All, 6]] - profile[[All, 7]]) // ListLinePlot[#, AxesOrigin → {0, 0}] &

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1.83576 × 10<sup>6</sup>

$\{17\,514., 17\,514.\}$  $u^*=17\,514.2$ 



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profile[[All, 3]] profile[[All, 4]]-7/2 // ListLogPlot
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