

# Vale + 2 x Ale ICPC Team Notebook

## Contents

1	C++	1
1.1	C++ template	1
1.2	C++ Template de Ale Castro	1
2	Graph algorithms	2
2.1	BFS	2
2.2	DFS	2
2.3	Dijkstra	2
2.4	Bellman Ford	2
2.5	Floyd Warshall	3
3	Flows	3
3.1	Hungarian Algorithm	3
4	Data Structures	3
4.1	Disjoint Set Union	3
4.2	Segment Tree	4
5	Math	4
5.1	Sieve of Eratosthenes	4
6	Dynamic Programming	4
6.1	Longest common subsequence	4
7	Geometry	4
7.1	Point	4

## 1 C++

### 1.1 C++ template

```
#include <bits/stdc++.h>

#define fi first
#define se second
#define forn(i,n) for(int i=0; i< (int)n; ++i)
#define forl(i,n) for(int i=1; i<= (int)n; ++i)
#define fore(i,l,r) for(int i=(int)l; i<= (int)r; ++i)
#define ford(i,n) for(int i=(int)(n) - 1; i>= 0; --i)
#define fored(i,l,r) for(int i=(int)r; i>= (int)l; --i)
#define pb push_back
#define el '\n'
```

```
#define d(x) cout<< #x<< " " << x<<el
#define ri(n) scanf("%d",&n)
#define sz(v) int(v.size())
#define all(v) v.begin(),v.end()

using namespace std;

typedef long long ll;
typedef double ld;
typedef pair<int,int> ii;
typedef pair<ll,ll> pll;
typedef tuple<int, int, int> iii;
typedef vector<int> vi;
typedef vector<ii> vii;
typedef vector<ll> vll;
typedef vector<ld> vd;

const int inf = 1e9;
const int nax = 1e5+200;
const ld pi = acos(-1);
const ld eps= 1e-9;

int dr[] = {1,-1,0, 0,1,-1,-1, 1};
int dc[] = {0, 0,1,-1,1, 1,-1,-1};

ostream& operator<<(ostream& os, const ii& pa) { //
    DEBUGGING
    return os << "("<< pa.fi << ", " << pa.se << ")";
}

int main(){
    ios_base::sync_with_stdio(false);
    cin.tie(NULL); cout.tie(NULL);
    cout << setprecision(20)<< fixed;
}
```

### 1.2 C++ Template de Ale Castro

```
#include <bits/stdc++.h>
using namespace std;

#define pb push_back
#define all(a) (a).begin(), (a).end()
#define endl '\n'
#define forn(i, l, n) for (int i = l; i < int(n); i++)

typedef long long ll;
typedef vector<int> vi;
typedef vector<ll> vll;
typedef pair<int, int> pii;

const int INF = 1e9 + 7;

int main() // Ale C.
{
    ios_base::sync_with_stdio(false);
```

```

cin.tie(NULL);
// freopen("output.txt", "w", stdout);
return 0;
}

```

## 2 Graph algorithms

### 2.1 BFS

```

vector<vector<int>>> gr(n);
queue<int> q;
vector<bool> vis(n, 0);
q.push(0);
vis[0] = 1;
while (q.size())
{
    int node = q.front();
    q.pop();
    for(auto v : gr[node])
    {
        if (!vis[v])
        {
            q.push(v);
            vis[v] = 1;
        }
    }
}

```

### 2.2 DFS

```

vector<bool> vis(1e5, 0);
vector<vi> gr(1e5);
void dfs(int node)
{
    if (vis[node])
        return;
    vis[node] = 1;
    cout << "Visitando: " << node << endl;
    for(i, 0, gr[node].size()) dfs(gr[node][i]);
    return;
}

```

### 2.3 Dijkstra

```

// O ((V+E)*log V)
vector<ii> g[nax];
int d[nax], p[nax];
void dijkstra(int s, int n){
    for(i, n) d[i] = inf, p[i] = -1;
}

```

```

d[s] = 0;
priority_queue<ii, vector<ii>, greater<ii>> > q;
q.push({0, s});
while(sz(q)){
    auto [dist, u] = q.top(); q.pop();
    if(dist > d[u]) continue;
    for(auto& [v, w]: g[u]){
        if (d[u] + w < d[v]){
            d[v] = d[u] + w;
            p[v] = u;
            q.push(ii(d[v], v));
        }
    }
}
}
vi find_path(int t){
    vi path;
    int cur = t;
    while(cur != -1){
        path.pb(cur);
        cur = p[cur];
    }
    reverse(all(path));
    return path;
}

```

### 2.4 Bellman Ford

```

vector<vector<pair<ll, ll>>>> gr(n + 1);
vll dis(n + 1, INF);
dis[1] = 0;
for(i, 0, n - 1)
{
    bool modif = 0;
    for(node, 1, n + 1)
    {
        if (dis[node] == INF)
            continue;
        for (auto [v, w] : gr[node])
            if (dis[node] + w < dis[v])
            {
                dis[v] = dis[node] + w;
                modif = 1;
            }
    }
    if (!modif)
        break;
}
// Cycle Check
bool cycle = 0;
for(node, 1, n + 1)
{
    if (dis[node] == INF)
        break;
}

```

```

for (auto [v, w] : gr[node])
    if (dis[node] + w < dis[v])
        cycle = 1;
if (cycle)
    break;
}

```

## 2.5 Floyd Warshall

```

vector<vll> gr(n + 1, vll(n + 1, INF));
for(i, 1, n + 1) gr[i][i] = 0;
for(k, 1, n + 1)
{
    for(i, 1, n + 1)
    {
        for(j, 1, n + 1)
        {
            gr[i][j] = min(gr[i][j], gr[i][k] + gr[k][j]);
        }
    }
}

```

## 3 Flows

### 3.1 Hungarian Algorithm

```

const ld inf = 1e18; // To Maximize set "inf" to 0, and
                    // negate costs
inline bool zero(ld x){ return x == 0; } // For Integer/
LL --> change to x == 0
struct Hungarian{
    int n; vector<vd> c;
    vi l, r, p, sn; vd ds, u, v;
    Hungarian(int n): n(n), c(n, vd(n, inf)), l(n, -1), r(n, -1), p(n), sn(n), ds(n), u(n), v(n){}
    void set_cost(){ for(i, n) for(j, n) cin >> c[i][j]; }
    ld assign() {
        set_cost();
        for(i, n) u[i] = *min_element(all(c[i]));
        for(j, n){
            v[j] = c[0][j] - u[0];
            for(i, n-1) v[j] = min(v[j], c[i][j] - u[i]);
        }
        int mat = 0;
        for(i, n) for(j, n) if(r[j] == -1 && zero(c[i][j] - u[i] - v[j])){
            l[i] = j, r[j] = i, ++mat; break;
        }
        for(; mat < n; ++mat){

```

```

int s = 0, j = 0, i;
while(l[s] != -1) ++s;
for(k, n) ds[k] = c[s][k] - u[s] - v[k];
fill(all(p), -1), fill(all(sn), 0);
while(1){
    j = -1;
    for(k, n) if(!sn[k] && (j == -1 || ds[k] < ds[j])) j = k;
    sn[j] = 1, i = r[j];
    if(i == -1) break;
    for(k, n) if(!sn[k]){
        auto n_ds = ds[j] + c[i][k] - u[i] - v[k];
        if(ds[k] > n_ds) ds[k] = n_ds, p[k] = j;
    }
    for(k, n) if(k != j && sn[k]){
        auto dif = ds[k] - ds[j];
        v[k] += dif, u[r[k]] -= dif;
    }
    u[s] += ds[j];
    while(p[j] >= 0) r[j] = r[p[j]], l[r[j]] = j, j = p[j];
    r[j] = s, l[s] = j;
    ld val = 0;
    for(i, n) val += c[i][l[i]];
    return val;
}
void print_assignment(){ for(i, n) cout << i+1 << " " << l[i]+1 << el; }
};

```

## 4 Data Structures

### 4.1 Disjoint Set Union

```

struct dsu{
    vi p, r; int comp;
    dsu(int n): p(n), r(n, 1), comp(n){iota(all(p), 0);}
    int find_set(int i){return p[i] == i ? i : p[i] = find_set(p[i]);}
    bool is_same_set(int i, int j){return find_set(i) == find_set(j);}
    void union_set(int i, int j){
        if((i = find_set(i)) == (j = find_set(j))) return;
        if(r[i] > r[j]) swap(i, j);
        r[j] += r[i]; r[i] = 0;
        p[i] = j; --comp;
    }
};

```

## 4.2 Segment Tree

```

vll tr(4 * n, 0), ar(n);
void init(int node, int b, int e)
{
    if (b == e)
    {
        tr[node] = ar[b];
        return;
    }
    int mid = b + (e - b) / 2, l = node * 2 + 1, r = l + 1;
    init(l, b, mid);
    init(r, mid + 1, e);
    tr[node] = tr[l] + tr[r];
}
ll query(int node, int b, int e, int i, int j)
{
    if (b >= i && e <= j)
        return tr[node];
    int mid = b + (e - b) / 2, l = node * 2 + 1, r = l + 1;
    if (mid >= j)
        return query(l, b, mid, i, j);
    if (mid < i)
        return query(r, mid + 1, e, i, j);
    return query(l, b, mid, i, j) + query(r, mid + 1, e, i, j);
}
void update(int node, int b, int e, int pos, int val)
{
    if (b == e)
    {
        tr[node] = val;
        return;
    }
    int mid = b + (e - b) / 2, l = node * 2 + 1, r = l + 1;
    if (mid >= pos)
        update(l, b, mid, pos, val);
    else
        update(r, mid + 1, e, pos, val);
    tr[node] = tr[l] + tr[r];
}

```

## 5 Math

### 5.1 Sieve of Eratosthenes

```

// O(n)
// pr contains prime numbers
// lp[i] == i if i is prime
// else lp[i] is minimum prime factor of i
const int nax = 1e7;
int lp[nax+1];

```

```

vector<int> pr; // It can be sped up if change for an array
void sieve() {
    fore(i, 2, nax-1) {
        if (lp[i] == 0) {
            lp[i] = i; pr.pb(i);
        }
        for (int j=0, mult= i*pr[j]; j<sz(pr) && pr[j]<=lp[i]
            && mult<nax; ++j, mult= i*pr[j])
            lp[mult] = pr[j];
    }
}

```

## 6 Dynamic Programming

### 6.1 Longest common subsequence

```

const int nax = 1005;
int dp[nax][nax];
int lcs(const string &s, const string &t) {
    int n = sz(s), m = sz(t);
    forn(j, m+1) dp[0][j] = 0;
    forn(i, n+1) dp[i][0] = 0;
    forl(i, n) {
        forl(j, m) {
            dp[i][j] = max(dp[i-1][j], dp[i][j-1]);
            if (s[i-1] == t[j-1]) {
                dp[i][j] = max(dp[i][j], dp[i-1][j-1] + 1);
            }
        }
    }
    return dp[n][m];
}

```

## 7 Geometry

### 7.1 Point

```

struct pt {
    ld x, y;
    pt() {}
    pt(ld x, ld y): x(x), y(y) {}
    pt(ld ang): x(cos(ang)), y(sin(ang)) {} // Polar
    unit point: ang(radians)
    // ----- BASIC OPERATORS ----- //
    pt operator+(pt p) { return pt(x+p.x, y+p.y); }
    pt operator-(pt p) { return pt(x-p.x, y-p.y); }
    pt operator*(ld t) { return pt(x*t, y*t); }
    pt operator/(ld t) { return pt(x/t, y/t); }
}

```

```

ld operator*(pt p){ return x*p.x + y*p.y; }
ld operator%(pt p){ return x*p.y - y*p.x; }
// ----- COMPARISON OPERATORS ----- //
bool operator==(pt p){ return abs(x - p.x) <= eps &&
abs(y - p.y) <= eps; }
bool operator<(pt p) const{ // for sort, convex
hull/set/map
return x < p.x - eps || (abs(x - p.x) <=
eps && y < p.y - eps); }
bool operator!=(pt p){ return !operator==(p); }
// ----- NORMS ----- //
ld norm2(){ return *this**this; }
ld norm(){ return sqrt(norm2()); }
pt unit(){ return *this/norm(); }
// ----- SIDE, LEFT ----- //
ld side(pt p, pt q){ return (q-p) % (*this-p); } // C is
: >0 L, ==0 on AB, <0 R
bool left(pt p, pt q){ // Left of directed line
PQ? (eps == 0 if integer)
return side(p, q) > eps; } // (change to
>= -eps to accept collinear)
// ----- ANGLES ----- //
ld angle(){ return atan2(y, x); } // Angle from origin,
in [-pi, pi]
ld min_angle(pt p){ return acos(*this*p / (norm()*p.
norm())); } // In [0, pi]
ld angle(pt a, pt b, bool CW){ // Angle< AB(*this) > in
direction CW
ld ma = (a - b).min_angle(*this - b);
return side(a, b) * (CW ? -1 : 1) <= 0 ? ma : 2*pi -
ma; }
bool in_angle(pt a, pt b, pt c, bool CW=1){ // Is pt

```

```

inside infinite angle ABC
return angle(a, b, CW) <= c.angle(a, b, CW); } //
From AB to AC in CW direction
// ----- ROTATIONS ----- //
pt rot(pt p){ return pt(*this % p, *this * p); } //
use ccw90(1,0), cw90(-1,0)
pt rot(ld ang){ return rot(pt(sin(ang), cos(ang))
); } // CCW, ang (radians)
pt rot_around(ld ang, pt p){ return p + (*this -
p).rot(ang); }
pt perp(){ return rot(pt(1, 0)); }
// ----- SEGMENTS ----- //
bool in_disk(pt p, pt q){ return (p - *this) * (q - *
this) <= 0; }
bool on_segment(pt p, pt q){ return side(p, q) == 0 &&
in_disk(p, q); }
};
int sgn(ld x){
if(x < 0) return -1;
return x == 0 ? 0 : 1;
}
void segment_intersection(pt a, pt b, pt c, pt d, vector<
pt>& out){ // AB y CD
ld sa = a.side(c, d), sb = b.side(c, d);
ld sc = c.side(a, b), sd = d.side(a, b); //
proper cut
if(sgn(sa)*sgn(sb) < 0 && sgn(sc)*sgn(sd) < 0) out.pb((
a*sb - b*sa) / (sb-sa));
for(pt p : {c, d}) if(p.on_segment(a, b)) out.pb(p);
for(pt p : {a, b}) if(p.on_segment(c, d)) out.pb(p);
}

```