Assignment 4

Exercise 1:

Construct both regular expression and deterministic automatons that accept the following languages over {0, 1}.

a) Strings that do not contain 00.

b) Strings that contain at least three symbols.

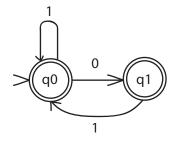
RegEx:

$$r = (0?)(10?)*$$

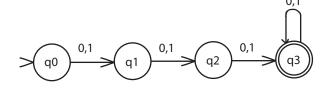
RegEx:

$$r = (0|1)(0|1)(0|1)(0|1)*$$

DFA:



DFA:



- c) Strings where each 0 is directly followed by 1.
- d) Strings that both start and end with 00.

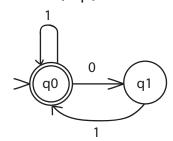
RegEx:

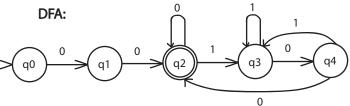
$$r = (01|1)*$$

RegEx:

$$r = (00)((0|1)*(00))*(0)*$$

DFA:



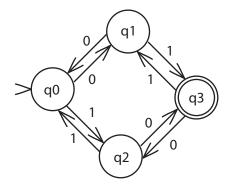


e) Strings having an odd number of 0:s and an odd number of 1:s.

RegEx:

$$r = ((00|11)*(01|10)(11|00)*(10|01)(00|11)*[(11|00))*(01|10)(00|11)*$$

DFA:



Exercise 2:

Present a deterministic finite automata and a regular expression for the lan-guage over {0, 1, 2, 3, 4, 5} where each string satisfies all the following criteria:

- The string may either be empty or start with 0.
- Either 1 or 3 must follow after 0.
- -2 must follow after 1.
- 0 may follow after 2, otherwise the string must end.
- 5 must follow after 3, but there may be zero or more 4 between 3 and 5.
- 0 may follow after 5, otherwise the string must end.

RegEx:

$$r = (0?(12|34*5))*$$

DFA:

