## BIOSTATS 710 FINAL EXAM

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(Chapter 5 through Chapter 7)

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## 1 Chapter Five

- Linkage Analysis: Use pedigrees with diseased individuals with genetic marker (polymorphism, detectable location), to access whether the DSL (Disease Susceptibility Loci) is in "linkage" with any of the markers.
- Recombinant gamete: Two types of gametes are possible when following genes on the same chromosomes. If crossing over does not occur, the products are parental gametes. If crossing over occurs, the products are recombinant gametes.

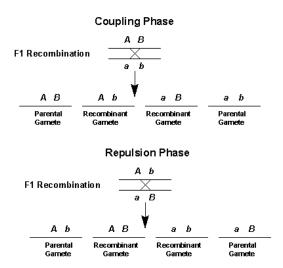


Figure 1: A sample of Recombination Gametes

• map function: Devised by Haldane, map function transform  $\theta$  (recombination fraction) into a distance measure by using the assumption that the number of crossovers follows a Poisson distribution with mean 2L.  $L = E(\sharp crossovers)/2$  and  $E(\sharp crossovers) = 2L$ 

$$P(X = k) = \frac{e^{-2L} * (2L)^k}{k!}$$

$$L = -[Ln(1-2\theta)]/2$$

Here L is measure by Morgans, 1 Morgan = distance between 2 loci.

- Morgan: Morgans or centimorgans (cM) measures the expected number of crossovers between two loci per gamete.
- physical map: A physical map gives the locations of identifiable landmarks on DNA, distance by base pairs.  $1,000,000~\mathrm{Bp} \approx 1~\mathrm{centiMorgan}$ .
- $\bullet$  association analysis: Basically look at whether marker alleles are associated with the trait.

Very different from linkage; It does not care which allele is congregating with DSL and maybe different from family to family.

- linkage disequilibrium: The genetic association will also be visible between the marker and the phenotype if a particular allele at the genetic marker tends to appear together on the same gamete with the disease allele at the disease locus. This latter concept, the association of alleles at two loci, is referred to as linkage disequilibrium (LD) refers to association between alleles at different Loci. Also, recombination breaks down LD, more recombination, faster LD decays.
- haplotype: The set of alleles lying on the same chromosome is called the haplotype. (i.e. AB and ab are two haplotypes)
  - D prime (D'): Lewontin's D' (D prime).

If 
$$D_{AB} < 0$$
,  $D'_{AB} = \frac{D_{AB}}{min(P_A P_B, P_a P_b)}$   
If  $D_{AB} > 0$ ,  $D'_{AB} = \frac{D_{AB}}{min(P_A P_b, P_a P_B)}$ 

D' ranges from -1 to +1.

more likely to take extreme values when allele frequency are small.

 $\pm 1$  implies that at least one of the possible hapletypes was not observed.

 $\bullet$  phase: D' = 1 or D' = -1, it means there's no evidence of recombination between marker and DSL.

If allele frequencies are similar, high D' implies markers are good surrogates for each other.

 $\bullet$   $\triangle :$  Also called  $r^2,$  standard squared correlation coefficient for allele freq at two markers.

range from 0 to 1.

 $r^2=1$  implies markers provide the same statistical information. population geneticists, like  $r^2$  value.

measures the loss in efficiency when marker A is replaced with marker B, in association study.

- $\star$  explain how the Haldane map function is derived
- $\star$  name the rule of thumb that relates base pairs to Morgans

## 2 Chapter Six

• linkage analysis: Mapping disease locus to positive relative to known markers. The goal is to make inference about cosegregation of 2 (or more) loci in family. these loci could be marker loci.

or at least one could be a candidate disease locus. in general, the more variable the marker, the more useful it is for linkage analysis. Because, each founder will bring a different copy to the pedigree and it will be possible to determine exactly which chromosomal segments were transmitted.

• ordered genotype: Genotype plus phase information.

$$A_1B_2/A_2B_1 \rightarrow Genotypes A_1A2 \ and \ B_1B_2$$

 $A_1B_2$  are on the same chromosome, and therefore comprise a haplotype.

 $A_2B_1$  are on the same chromosome, and therefore comprise a haplotype.

• LOD score: The LOD score is a measure of support for an arbitrary value of  $\theta$  in the range (0, 12), which is maximized when  $\theta$  is the maximum likelihood estimate.

 $LOD-score=log_{10}(LR(\theta))$  In likely hood analysis, Inference is often based on the lokely hood ration:  $LOD(\theta)=log_{10}\frac{L(\theta)}{L(1/2)}$ 

- incomplete penetrance:
- parametric linkage: Assuming a given genetic model (parametric part), we write down a likelyhood (or the observed) for the pedigree data (phenotypes, genotypes, over covariates, phase), by generally making a number of simplifying assumption that allow us to express it in turns of a few unknown parameters.
- non-parametric linkage analysis: based on idea that if a locus is associated with a disease, the relatives with similar phenotypes should share more alleles IBD at that locus than (would be) expected by their relatedness alone.

note: non-parametric linkage analysis is actually full parametric assumptions. it is nonparametric in that it does not assume a model of inheritance (autosomal dominant etc).

note: non-parametric linkage depends on marker loci that are close to disease locus also showing an increase in IBD relative to expectation.

## 3 Chapter Seven

• family-based controls: All this (previous) is predicted on being able to match individuals genetically (on P), which is hard. So we use family information as 'controls'.

these approaches are somewhat in termeeliated between linkage and association in that they require some pedigree infomation, typically from parents.

However, they retain the main feature of association. Studies in that the relationship between disease status and genotype is compared.

Note: we will consider 1. study design in which an affect individual and his/her parents are sampled and genotyped. 2. Alleles that were transmitted to the affected offsprings are compared to the alleles that were not transmitted.

- trio: The most popular family study design involves parents and their affected offspring, commonly called trios, in other words: nuclear families with one offspring and both parents.
  - manhattan plot: