# Peer-graded Assignment: Regression Models Course Project

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## Choosing the Model

As

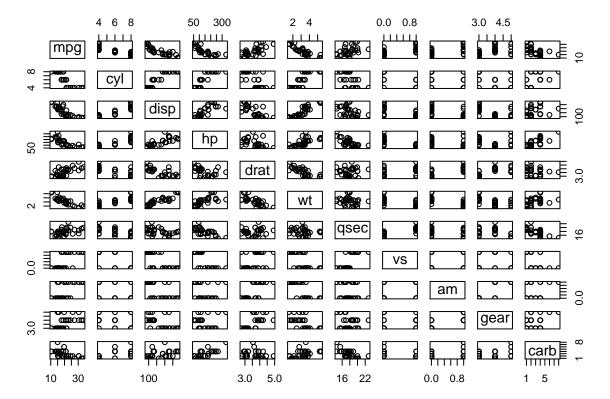
# Appendix 1: Preliminary Data Analysis

Basic properties of the 'mtcars' dataset:

```
## 'data.frame':     32 obs. of 11 variables:
## $ mpg : num     21 21 22.8 21.4 18.7 18.1 14.3 24.4 22.8 19.2 ...
## $ cyl : num     6 6 4 6 8 6 8 4 4 6 ...
## $ disp: num     160 160 108 258 360 ...
## $ hp : num     110 110 93 110 175 105 245 62 95 123 ...
## $ drat: num     3.9 3.9 3.85 3.08 3.15 2.76 3.21 3.69 3.92 3.92 ...
## $ wt : num     2.62 2.88 2.32 3.21 3.44 ...
## $ qsec: num     16.5 17 18.6 19.4 17 ...
## $ vs : num     0 0 1 1 0 1 0 1 1 1 ...
## $ am : num     1 1 1 0 0 0 0 0 0 0 ...
## $ gear: num     4 4 4 3 3 3 3 3 4 4 4 ...
## $ carb: num     4 4 1 1 2 1 4 2 2 4 ...
```

So, we're talking of a small sample of only 32 observations.

Additionally, visual correlations among pairs of potential variables can be seen as follows:



# Appendix 2: Model Selection

Given the nature of the analysis (continuous outcome, obtained from discrete and continuous regressors), the size of the dataset (only 32 observations), plus the visual correlations observed between 'mpg' (the outcome) and its potential regressors, the model to be used wil be linear (lm type), with 'am' as a not-so-dummy binary-factor variable.

#### Appendix 3: Choosing Preliminary Regressors

A preliminary analysis considered all mtcars variables as potential regressors. With variables 'cyl', 'vs', 'am', 'gear' and 'carb' as factors, the following lm function was analysed:

```
fitAll <- lm(mpg ~ ., mtcars2)
summary(fitAll)$coef</pre>
```

```
##
                  Estimate
                            Std. Error
                                           t value
                                                     Pr(>|t|)
## (Intercept) 23.87913244 20.06582026
                                        1.19004018 0.25252548
## cyl6
               -2.64869528
                            3.04089041 -0.87102622 0.39746642
## cy18
               -0.33616298
                            7.15953951 -0.04695316 0.96317000
## disp
                0.03554632
                           0.03189920
                                        1.11433290 0.28267339
               -0.07050683 0.03942556 -1.78835344 0.09393155
## hp
                            2.48348458
                                        0.47627845 0.64073922
## drat
                1.18283018
               -4.52977584
                            2.53874584 -1.78425732 0.09461859
## wt
## qsec
                0.36784482
                           0.93539569
                                        0.39325050 0.69966720
## vs1
                1.93085054
                            2.87125777
                                        0.67247551 0.51150791
```

```
## am1
               1.21211570 3.21354514 0.37718957 0.71131573
               1.11435494 3.79951726 0.29328856 0.77332027
## gear4
## gear5
               2.52839599 3.73635801 0.67670068 0.50889747
               -0.97935432 2.31797446 -0.42250436 0.67865093
## carb2
## carb3
               2.99963875 4.29354611
                                       0.69863900 0.49546781
## carb4
               1.09142288 4.44961992 0.24528452 0.80956031
## carb6
               4.47756921 6.38406242 0.70136677 0.49381268
               7.25041126 8.36056638 0.86721532 0.39948495
## carb8
```

With a P-value based criteria, no variable makes the cut (with 'hp' and 'wt' the closest, though). Therefore, the first conclusion was that some industry research was required in order to determine the best regressor candidates for 'mpg' outcome.

After some web research (such as http://www.driverside.com/auto-library/top\_10\_factors\_contributing\_to\_fuel\_economy-317 and https://www.quora.com/On-what-factors-does-mileage-of-a-vehicle-depend), the main variables suggested (and therefore candidates for main regresors), were: displacement ('disp'), power ('hp'), aerodynamics, weight ('wt') and number of forward gears ('gear').

Besides aerodynamics (not available in the dataset), the visual correlations between them and 'mpg' are pretty clear, as seen in Appendix 1 (such as the inverse relation between 'mpg' and both 'hp' or 'wt'-both of which had the lowest P-values when including all variables in the model, as seen before-). Therefore, including 'am' (required in order to answer the main question), they were selected as candidates for regression modeling in the next appendix.

Finally, given the lowest P-value results obtained by 'wt' and 'hp' regressors (in comparison with the rest), plus the well known Weight/Power KPI (Key Performance Indicator) from the automotive industry, in further analysis both 'wt' and 'hp' will be considered primary potential regressors while 'disp' and 'gear' will be considered secondary potential regressors (just to prioritize further analysis. Cuantitative analysis will finally determine which regressors to keep).

## Appendix 4: Regression Modeling

For the regression analysis, two types of models were used.

The first one with different intersection points but the same slope for all regression lines (no interaction between 'am' -the binary factor regressor- and the rest of the regressors), such as:

```
## lm(formula = mpg ~ hp + wt + factor(am), data = mtcars)
```

The second one, with different intersects AND slopes for regression lines (factor(am):regressor type interactions), such as:

```
## lm(formula = mpg ~ hp + wt + factor(am) + factor(am):hp + factor(am):wt,
## data = mtcars)
```

Additionally, ANOVA comparisons (incrementally adding regressors from the preliminary set, defined in Appendix 3) were used in order to determine the best regressor mix for each model. The order in which regressor candidates were added, followed the primary and secondary criteria specified in Appendix 3. Therefore, the regressor sequences to be considered, were the following (all with 'am' included):

```
1. 'wt' - 'hp' - 'disp'
```

#### Model 1: Different intersection points, with same slopes

```
## Analysis of Variance Table
##
## Model 1: mpg ~ factor(am)
## Model 2: mpg ~ wt + factor(am)
## Model 3: mpg ~ hp + wt + factor(am)
## Model 4: mpg ~ wt + hp + disp + factor(am)
     Res.Df
              RSS Df Sum of Sq
##
                                           Pr(>F)
## 1
         30 720.90
## 2
         29 278.32
                         442.58 66.4206 9.394e-09 ***
                   1
         28 180.29
                          98.03 14.7118 0.0006826 ***
## 3
                   1
## 4
         27 179.91
                           0.38 0.0576 0.8122229
                   1
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

ANOVA test with 2nd sequence (replacing 'disp' by 'gear') resulted in almost same outcome.

Just in case, ANOVA analysis of the first sequence was carried on, reordering the sequence as follows: 'wt' - 'disp' - 'hp'

```
## Analysis of Variance Table
##
## Model 1: mpg ~ factor(am)
## Model 2: mpg ~ wt + factor(am)
## Model 3: mpg ~ wt + disp + factor(am)
## Model 4: mpg ~ wt + hp + disp + factor(am)
     Res.Df
##
              RSS Df Sum of Sq
                                         Pr(>F)
## 1
         30 720.90
         29 278.32 1
## 2
                        442.58 66.421 9.394e-09 ***
         28 246.56 1
                         31.76 4.767 0.037878 *
## 4
         27 179.91
                          66.65 10.002 0.003842 **
                   1
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

Interestingly enough, the result sugests that all 4 regressors are relevant for the outcome. Same test was carried on with the sequence number 2, with less promising results.

Sequences 3 and 4 were not relevant as soon as regressors 'disp' or 'gear' were included (including sequence reordering).

Therefore, for this type of model (different intersections, with same slopes), the following model was selected, with regressors: 'wt', 'hp', 'disp' and 'am' (just in case, an extra ANOVA sequence was carried on, including 'gear' as a fifth regressor, with no relevant result obtained).

```
##
## Call:
## lm(formula = mpg ~ wt + hp + disp + factor(am), data = mtcars)
##
## Coefficients:
## (Intercept) wt hp disp factor(am)1
## 34.209443 -3.046747 -0.039323 0.002489 2.159271
```

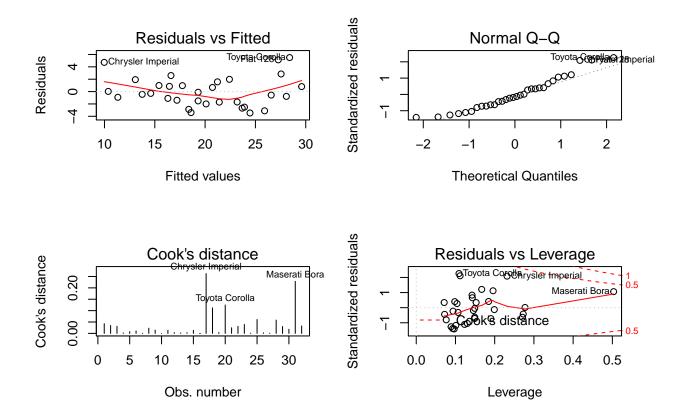
## Model 2: Different intersection points and slopes

ANOVA analysis to sequences 1 and 2 suggests 'wt', 'hp' and 'am' are the only relevant regressors (including 'disp' or 'gear' in any order, didn't make a difference) when including variable slopes.

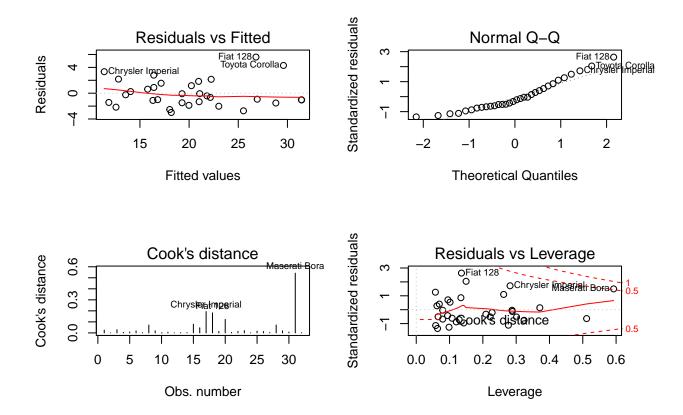
```
## Analysis of Variance Table
##
## Model 1: mpg ~ factor(am)
## Model 2: mpg ~ wt + factor(am) + factor(am):wt
## Model 3: mpg ~ hp + wt + factor(am) + factor(am):hp + factor(am):wt
## Model 4: mpg ~ wt + hp + factor(gear) + factor(am) + factor(am):wt + factor(am):hp +
       factor(am):factor(gear)
               RSS Df Sum of Sq
##
    Res.Df
                                           Pr(>F)
## 1
         30 720.90
## 2
         28 188.01 2
                         532.89 49.5549 3.013e-09 ***
         26 135.90 2
                         52.11 4.8456
                                          0.01707 *
## 4
         24 129.04 2
                           6.86 0.6378
                                          0.53720
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
Therefore, for this type of model, only 'wt', 'hp' and 'am' regressors were considered, in the following model:
##
## Call:
## lm(formula = mpg ~ hp + wt + factor(am) + factor(am):hp + factor(am):wt,
       data = mtcars)
##
## Coefficients:
                                                       factor(am)1
##
      (Intercept)
                                               wt
                               hp
##
         30.70393
                         -0.04094
                                         -1.85591
                                                          13.74000
## hp:factor(am)1 wt:factor(am)1
##
         0.02779
                         -5.76895
```

# Appendix 5: Regression Diagnostics

## Model 1: Different intersection points, with same slopes



Model 2: Different intersection points and slopes



## Appendix 6: Confidence Intervals

#### Model 1: Different intersection points, with same slopes

```
## Estimate Std. Error t value Pr(>|t|)
## (Intercept) 34.209443370 2.82282610 12.1188632 1.979953e-12
## wt -3.046747000 1.15711931 -2.6330448 1.382936e-02
## hp -0.039323213 0.01243358 -3.1626624 3.842032e-03
## disp 0.002489354 0.01037681 0.2398959 8.122229e-01
## factor(am)1 2.159270737 1.43517565 1.5045341 1.440531e-01
```

Considering that the 5th row represents the impact on the intercept once we include the factor that the transmission is manual (without changing the slopes), the confidence interval for that impact is:

```
sumCoef1[5,1] + c(-1,1) * qt(.975, df = model1$df) * sumCoef1[5,2]
```

```
## [1] -0.7854664 5.1040079
```

Which means that, with a 95% confidence, we estimate that cars with a manual transmission result in a -0.79 to 5.1 general impact in MPG, compared to those with automatic transmission, at the average value of any of this model's regressors ('wt' or 'hp').

#### Model 2: Different intersection points and slopes

#### ## [1] 5.058741 22.421266

In this case, with a 95% confidence, we estimate that cars with a manual transmission result in a 5.06 to 22.4 general impact in MPG, compared to those with automatic transmission, at the average value of any of this model's regressors ('wt' or 'hp'). Additionally, considering the wt:factor(am)1 interaction for now (its P-value for hp, plus its slopes, makes the other interaction irrelevant for now):

```
sumCoef2[3,1] + sumCoef2[6,1] + c(-1,1) * qt(.975, df = model2$df) * (sumCoef2[3,2] + sumCoef2[6,2])
## [1] -13.826629 -1.423088
```

With a 95% confidence, we also estimate that cars with a manual transmission result in a -13.8 to -1.42 added impact in MPG for each 1000 lbs increase in weight.