Formal Grammar

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formula family \rightarrow
                            name
                            type
                            parameters
                            variables
                            blocks
                            quantifiers
                            quantifier prefix
                            operators
                            output
                 name \rightarrow name: [a-zA-Z0-9](_?\s?[a-zA-Z0-9])*
                 type →
                           type: CNF
                         | type: circuit
           parameters →
                          parameters: parameter declaration
parameter declaration → param name : param type
                            param constraints
                           parameter_declaration
                          | ε
           param type → natural
     param contraints →
                           , param name <= expression
                           param constraints
                          , param_name >= expression
                            param constraints
                          | ε
            variables → variables: variable declaration
 variable declaration \rightarrow
                           var name subindices
                            variable_declaration
           subindices → (subindices list) subindices constraints
      subindices list \rightarrow index more subindices
      more\_subindices \rightarrow  , subindices\_list
             in range → subindices list in range
                range → [expression, expression]
               blocks \rightarrow blocks: block definition
     block definition → define block
```

```
single block
                                  subindices constraints
                                  block definition
                                | define blocks
                                       multiple blocks
                                  subindices_constraints
                                 grouped in
                                  block definition
           single block → block name := block body
        \begin{array}{ccc} \texttt{multiple\_blocks} & \to & & \texttt{single\_block} \\ & & & \texttt{multiple\_blocks} \end{array}
              block body \rightarrow block name more names
                               -block name more names
                               | variable name more names
                               | -variable name more names
              subindices constraints → where constraints
                              | ε
             constraints \rightarrow constraint more_contraints
                                constraint and constraint more constraints
                                 constraint or constraint more constraints
              \begin{array}{ccc} \text{constraint} & \rightarrow & & \text{in\_range} \\ & & & \text{assignment} \end{array}
                                 expression
       more\_constraints \rightarrow , constraints
                              ع |
              grouped in → grouped in block_name
             quantifiers → quantifiers: quantifier declaration
                                 block block name quantified with quantifier
quantifier declaration
                                 quantifier declaration
                                  blocks in block name quantified with
                                 quantifier
                                 quantifier declaration
              quantifier \rightarrow E
     quantifier prefix → quantifier prefix: block_name
               operators → operators: operator_declaration
```

```
| ε
operator_declaration \rightarrow
                             block block_name has operator op
                             operator_declaration
                           | blocks in block_name have operator op
                             operator_declaration
                   op \rightarrow AND
                           OR
                           XOR
               output → output: block_name
          param name →
                            [a-zA-Z] ( ?[a-zA-Z0-9]) *
             var_name \rightarrow [a-z](?[a-z0-9])*
                index \rightarrow [a-z](_?[a-z0-9])*
           block name →
                             [A-Z](_?[a-zA-Z0-9])* subindices_list
                             expression == expression
           expression →
```

expression → expression == expression
expression != expression
expression <= expression
expression >= expression
expression >= expression
expression + expression
expression - expression
expression + expression
expression / expression
expression / expression
expression / expression
expression mod expression
param_name
index

assignment \rightarrow index = expression