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**Q1** - Let  $P$  be an EC point. What is the **minimum** number of EC operations necessary to compute  $[63]P$ ? And more specifically which are these operations?

10, specifically:

5 doubles  $\rightarrow P \times P, 2P \times 2P, 4P \times 4P, 8P \times 8P, 16P \times 16P,$

5 sums  $\rightarrow 2P+P, 4P+3P, 8P+7P, 16P+15P, 32P+31P.$

**Q2** - Consider both commitments introduced in our classes (Feldman and Pedersen), and assume they “commit” a value  $x$ . Under which (eventually different) assumptions they can be considered secure?

Feldman

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Pedersen

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a) no specific assumptions

b) must use a large prime  $p$  in the modular exponentiations

c) require that the committed value  $x$  is drawn from a large space

d) both large prime  $p$  and  $x$  drawn from large space

**Q3** - A strong prime  $p$  is defined as:

- ☐ a) a prime number  $p$  much larger than usual
- ☐ b) a prime  $p$  such as  $2p+1 = q$  is also prime
- ☒ c) a prime  $p$  such as  $p = 2q+1$  and  $q$  is also prime
- ☐ d) a prime  $p$  such as the Euler  $\phi(p)$  is also prime

**Q4** - Describe the Boneh-Franklin Identity Based Encryption scheme, specifying in particular, i) how a message is encrypted, ii) how a message is decrypted, and iii) what is the private key used by the receiver.

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**Q5** - Consider an RSA digital signature based on a (2,2) secret sharing, and assume all following operations are based on modulo  $n$ , with  $n$  being the RSA parameter. The tag  $H(m)^d$  is reconstructed by:

- ☐ a) Summing the tags constructed using the two shares
- ☒ b) Multiplying the tags constructed using the two shares
- ☐ c) Interpolating the tags constructed using the two shares using Lagrange coefficients
- ☐ d) Using a special approach proposed by Shoup.

**Q6** - Assume arithmetic modulus 100. A Linear secret sharing scheme involving 3 parties is described by the following access control matrix:

A:	1	1	0
B:	0	1	1
C:	0	0	-1

Assume that the following shares are revealed:

A  $\rightarrow$  51  
B  $\rightarrow$  63  
D  $\rightarrow$  11

What is the secret?

- a) 1    b) 3    c) 23    d) 25    e) 75    f) 77    g) 97    h) 99    i) another result = \_\_\_\_\_

**Q7** - A same message  $M$  is RSA-encrypted using two different public keys  $e_1 = 5$  and  $e_2 = 7$ , but same RSA modulus  $n=143$ . The two resulting ciphertexts are:  $c_1=23$  and  $c_2=4$ . Decrypt the message applying the Common Modulus Attack (show the detailed computations required).

*Just in case you need to rapidly compute inverses modulus 143, here a few ones:*

$x = \{4, 5, 7, 17, 20, 23, 29, 92\} \rightarrow x^{-1} \text{ mod } 143 = \{36, 86, 41, 101, 93, 56, 74, 14\}$

Answer: by the extended GCD(7,5)  $\rightarrow \{r,s\}=\{-2,3\}$

Hence

$$M = 23^3 \times 4^{-2} \text{ mod } 143 = 23^3 \times 36^2 \text{ mod } 143 = 108$$

**Network Security – prof. Giuseppe Bianchi – 3rd term exam, 14 February 2020**

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**Q8** - A Shamir Secret Sharing scheme uses a non-prime modulus  $p=55$  (if you need modular inverses see table on the right). Of the 5 participating parties  $P_1, \dots, P_5$ , with respective  $x$  coordinates  $x_i = \{1, 2, 3, 4, 5\}$ , parties  $P_1$ ,  $P_3$  and  $P_5$  aim at reconstructing the secret.

a) compute the Lagrange Interpolation coefficients for parties 1, 3, 5;

b) Reconstruct the secret, assuming that the shares are:

$$P_1 \rightarrow 46$$

$$P_3 \rightarrow 51$$

$$P_5 \rightarrow 2$$

c) Prove that the system is NOT unconditionally secure, by showing that the knowledge of the two shares  $P_3$  and  $P_5$  leak information about the secret – specifically, after knowing shares  $P_3$  and  $P_5$  which would be the only possible remaining secret values?

[Answer:

$\lambda_1=50$ ,  $\lambda_3=40$ ,  $\lambda_5=21$

Secret = 37;

set of possible secrets: the 11 possible values which satisfy  $47+50x \bmod 55 \rightarrow$

$\rightarrow \{42, 37, 32, 27, 22, 17, 12, 7, 2, 52, 47\}$

x	1/x mod 55
1	1
2	28
3	37
4	14
6	46
7	8
8	7
9	49
12	23
13	17
14	4
16	31
17	13
18	52
19	29
21	21
23	12
24	39
26	36
27	53
28	2
29	19
31	16
32	43
34	34
36	26
37	3
38	42
39	24
41	51
42	38
43	32
46	6
47	48
48	47
49	9
51	41
52	18
53	27
54	54

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**Q9** - Prove that any linear secret sharing scheme is homomorphic with respect to the sum operation.

**Q10** – 1) Determine the access control matrix that implements the policy:  $\pi = (A \cap B) \cup (C \cap D \cap E)$ , and then 2) turn it into a linear secret sharing scheme, by computing the shares to assigned to the 5 parties (use modulus 100, share secret  $S=10$ , invent your own random values if/when necessary)