free42 Simple Math Functions

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| 6 | END | 29 |
| 7 | EOF | 29 |

1 Metadata

The home for this HTML file is: https://richmit.github.io/hp42/sfun.html
A PDF version of this file may be found here: https://richmit.github.io/hp42/sfun.pdf
Files related to this document may be found on github: https://github.com/richmit/hp42
Directory contents:

rc - The org-mode file that generated this HTML document rc_42s - Ready to convert source listings for 42s code in this document

docs - This html document and associated PDF

bin - Importable RAW program files

2 Introduction

This org-mode file collects together a handful simple mathematical functions that I find useful.

| Menu | | Description |
|-------------------------|--------|--|
| L&P:lnYX | lnYX | Base Y Logarithm of X |
| $L\&P:\Box\Box\Box\Box$ | | |
| L&P:ln2 | ln2 | Base 2 logarithm |
| L&P:LN | | Base 3 logarithm |
| L&P:LOG | | Base 10 logarithm |
| $L\&P:\Box\Box\Box\Box$ | | |
| L&P:Y↑X | | Raise Y to the power of X |
| L&P:□□□□ | | · |
| L&P:2↑X | LBL 58 | Raise 2 to the power of X |
| L&P:EXP | | Raise e to the power of X |
| L&P:10↑X | | Raise 10 to the power of X |
| L&P:□□□□ | | |
| L&P:Y,X | YROOT | Yth roots prefering real & pure imaginary answers |
| L&P: | 110001 | Ten took proteing ten or pure imaginary and ten |
| L&P:2\X | LBL 57 | Square root prefering real & pure imaginary answers |
| I (-D.2 N | | |
| L&P:3X | LBL 56 | Cube root prefering real & pure imaginary answers |
| L&P:5\X | LBL 55 | Fifth root prefering real & pure imaginary answers |
| L&P:7\(X | LBL 54 | Seventh root prefering real & pure imaginary answers |
| CPLX:RPART | | Real Part of anumber or matrix |
| CPLX:IPART | | Imaginary Part of a number or matrix |
| CPLX:CONJ | | Complex conjugate of a number or matrix |
| CPLX:CABS | | Magnitude of a number or matrix (built in ABS fails on a complex matrix) |
| CPLX:CARG | | Complex argument of a number or matrix |
| TRIG:SIN | | |
| TRIG:COS | | |
| TRIG:TAN | | |
| TRIG:ASIN | | |
| TRIG:ACOS | | |
| TRIG:ATAN | | |
| TRIG:CSC | | 1/SIN(X) |
| TRIG:SEC | | 1/COS(X) |
| TRIG:COT | | 1/TAN(X) |
| TRIG:ACSC | | SIN(1/X) |
| TRIG:ASEC | | $\hat{\cos}(1/\hat{X})$ |
| TRIG:ACOT | | TAN(1/X) |
| TRIG:TAN2 | | |
| TRIG:HYPOT | | |
| TRIG:HAV | | Haversine = 1/2 - cos(X)/2 |
| TRIG:AHAV | | Inverse Haversine = $2*asin(sqrt(X))$ |
| TRIG: | | |
| TRIG: | | |
| HYP:SINH | | |
| HYP:COSH | | |
| HYP:TANH | | |
| HYP:ASINH | | |
| HYP:ACOSH | | |
| HYP:ATANH | | |
| HYP:CSCH | | 1/SINH(X) |
| HYP:SECH | | |
| | | 1/COSH(X) |
| HYP:COTH HYP:ACSCH | | 1/TANH(X) |
| 11 LE AL 3U D | | SINH(1/X) |

| Menu | | Description | | |
|------------------------------------|-------------|--|------------------|-----------------|
| HYP:ASECH | | COSH(1/X) | | |
| HYP:ACOTH | | TANH(1/X) | | |
| PERC:%T | | Percentage of total | Y: TOTAL X: PART | X: % of Total |
| PERC:%CH | | percentage of change from Y to X | Y: OLD X: New | X: % Change |
| PERC:% | | Percentage | Y: Y X: X | Y: Y X: X% of Y |
| INT:FLOR | FLOOR | Truncate toward negative infinity | | |
| INT:CEIL | | Truncate toward positive infinity | | |
| INT:ROND | ROUND | Truncate toward nearest integer (even rule) | | |
| INT:TRUN | IP | Truncate toward zero | | |
| $INT:\Box\Box\Box\Box$ | | | | |
| INT:FP | | | | |
| INT:GCD | | Greatest Common Denominator | | |
| INT:LCM | | Least Common Multiple | | |
| $INT:\square\square\square\square$ | | | | |
| $INT:\square\square\square\square$ | | | | |
| INT:DIV | $BASE \div$ | | | |
| INT:REM | MOD | | | |
| BINO:COMB | | | | |
| BINO:PERM | | | | |
| BINO:! | N! | | | |
| BINO:PSI | DIGAMM | | | |
| BINO:GAM | GAMMA | | | |
| BINO:BETA | | Beta function | | |
| ERR:ERF | | Error Function | | |
| ERR:ERFC | | Complementary Error Function | | |
| ERR: | | | | |
| ERR:NPDF | | Standard Normal Probablity Density FUnction | | |
| ERR:NCDF | | Standard Normal Cumulative Distribution FUnction | | |
| ERR: | | | | |
| MISC: | | Parallel Operator | ΥX | X: 1/(1/X+1/Y) |
| | | | | |

4 Menu Code

(MJR-generate-42-menu-code "SFUN" 0 tbl 0 1 'stay 'up 'auto #'MJR-custom-gen-lab #'MJR-custom-gen-sub)

@@@@ DSC: Auto-generated menu program

LBL "SFUN"

0000 Page 1 of menu SFUN

LBL 01 CLMENU

"L&P"

KEY 1 GTO 03

"CPLX"

KEY 2 GTO 04

"TRIG"

KEY 3 GTO 05

"HYP"

KEY 4 GTO 06

"PERC"

KEY 5 GTO 07

"INT"

KEY 6 GTO 08

KEY 7 GTO 02

KEY 8 GTO 02

```
KEY 9 GTO 00
MENU
STOP
GTO 01
LBL 02
                  0000 Page 2 of menu SFUN
CLMENU
"BINO"
KEY 1 GTO 09
"ERR"
KEY 2 GTO 10
"MISC"
KEY 3 GTO 11
KEY 7 GTO 01
KEY 8 GTO 01
KEY 9 GTO 00
MENU
STOP
GTO 02
LBL 03
                  @@@@ Page 1 of menu L&P
CLMENU
"lnYX"
KEY 1 XEQ "lnYX"
"ln2"
KEY 3 XEQ "ln2"
"LN"
KEY 4 XEQ 14
"LOG"
KEY 5 XEQ 15
KEY 7 GTO 13
KEY 8 GTO 12
KEY 9 GTO 01
MENU
STOP
GTO 03
LBL 12
                  @@@@ Page 2 of menu L&P
CLMENU
"Y†X"
KEY 1 XEQ 16
"2†X"
KEY 3 XEQ 58
"EXP"
KEY 4 XEQ "EXP"
"10†X"
KEY 5 XEQ 17
KEY 7 GTO 03
KEY 8 GTO 13
KEY 9 GTO 01
MENU
STOP
GTO 12
LBL 13
                  0000 Page 3 of menu L&P
CLMENU
"Y,/X"
KEY 1 XEQ "YROOT"
"2\X"
KEY 3 XEQ 57
"3<sub>√</sub>X"
```

```
KEY 4 XEQ 56
"5\X"
KEY 5 XEQ 55
"7\X"
KEY 6 XEQ 54
KEY 7 GTO 12
KEY 8 GTO 03
KEY 9 GTO 01
MENU
STOP
GTO 13
LBL 04
                  @@@@ Page 1 of menu CPLX
CLMENU
"RPART"
KEY 1 XEQ "RPART"
"IPART"
KEY 2 XEQ "IPART"
"CONJ"
KEY 3 XEQ "CONJ"
"CABS"
KEY 4 XEQ "CABS"
"CARG"
KEY 5 XEQ "CARG"
KEY 9 GTO 01
MENU
STOP
GTO 04
LBL 05
                  0000 Page 1 of menu TRIG
CLMENU
"SIN"
KEY 1 XEQ 20
"COS"
KEY 2 XEQ 21
"TAN"
KEY 3 XEQ 22
"ASIN"
KEY 4 XEQ 23
"ACOS"
KEY 5 XEQ 24
"ATAN"
KEY 6 XEQ 25
KEY 7 GTO 19
KEY 8 GTO 18
KEY 9 GTO 01
MENU
STOP
GTO 05
LBL 18
                  0000 Page 2 of menu TRIG
CLMENU
"CSC"
KEY 1 XEQ "CSC"
"SEC"
KEY 2 XEQ "SEC"
"COT"
KEY 3 XEQ "COT"
"ACSC"
KEY 4 XEQ "ACSC"
```

```
"ASEC"
KEY 5 XEQ "ASEC"
"ACOT"
KEY 6 XEQ "ACOT"
KEY 7 GTO 05
KEY 8 GTO 19
KEY 9 GTO 01
MENU
STOP
GTO 18
LBL 19
                  @@@@ Page 3 of menu TRIG
CLMENU
"TAN2"
KEY 1 XEQ "TAN2"
"HYPOT"
KEY 2 XEQ "HYPOT"
"HAV"
KEY 3 XEQ "HAV"
"AHAV"
KEY 4 XEQ "AHAV"
KEY 7 GTO 18
KEY 8 GTO 05
KEY 9 GTO 01
MENU
STOP
GTO 19
LBL 06
                  @@@@ Page 1 of menu HYP
CLMENU
"SINH"
KEY 1 XEQ 27
"COSH"
KEY 2 XEQ 28
"TANH"
KEY 3 XEQ 29
"ASINH"
KEY 4 XEQ 30
"ACOSH"
KEY 5 XEQ 31
"ATANH"
KEY 6 XEQ 32
KEY 7 GTO 26
KEY 8 GTO 26
KEY 9 GTO 01
MENU
STOP
GTO 06
LBL 26
                  @@@@ Page 2 of menu HYP
CLMENU
"CSCH"
KEY 1 XEQ "CSCH"
"SECH"
KEY 2 XEQ "SECH"
"COTH"
KEY 3 XEQ "COTH"
"ACSCH"
KEY 4 XEQ "ACSCH"
"ASECH"
```

```
KEY 5 XEQ "ASECH"
"ACOTH"
KEY 6 XEQ "ACOTH"
KEY 7 GTO 06
KEY 8 GTO 06
KEY 9 GTO 01
MENU
STOP
GTO 26
LBL 07
                  @@@@ Page 1 of menu PERC
CLMENU
"%T"
KEY 1 XEQ "%T"
"%CH"
KEY 2 XEQ 33
"%"
KEY 3 XEQ 34
KEY 9 GTO 01
MENU
STOP
GTO 07
LBL 08
                  @@@@ Page 1 of menu INT
CLMENU
"FLOR"
KEY 1 XEQ "FLOOR"
"CEIL"
KEY 2 XEQ "CEIL"
"ROND"
KEY 3 XEQ "ROUND"
"TRUN"
KEY 4 XEQ 36
"FP"
KEY 6 XEQ 37
KEY 7 GTO 35
KEY 8 GTO 35
KEY 9 GTO 01
MENU
STOP
GTO 08
LBL 35
                  0000 Page 2 of menu INT
CLMENU
"GCD"
KEY 1 XEQ "GCD"
"LCM"
KEY 2 XEQ "LCM"
"DIV"
KEY 5 XEQ 38
"REM"
KEY 6 XEQ 39
KEY 7 GTO 08
KEY 8 GTO 08
KEY 9 GTO 01
MENU
STOP
GTO 35
LBL 09
                  @@@@ Page 1 of menu BINO
CLMENU
```

```
"COMB"
KEY 1 XEQ 40
"PERM"
KEY 2 XEQ 41
n i n
KEY 3 XEQ 42
"PSI"
KEY 4 XEQ "DIGAMM"
"GAM"
KEY 5 XEQ 43
"BETA"
KEY 6 XEQ "BETA"
KEY 9 GTO 02
MENU
STOP
GTO 09
LBL 10
                  @@@@ Page 1 of menu ERR
CLMENU
"ERF"
KEY 1 XEQ "ERF"
"ERFC"
KEY 2 XEQ "ERFC"
"NPDF"
KEY 4 XEQ "NPDF"
"NCDF"
KEY 5 XEQ "NCDF"
KEY 9 GTO 02
MENU
STOP
GTO 10
LBL 11
                  0000 Page 1 of menu MISC
CLMENU
"||"
KEY 1 XEQ "||"
KEY 9 GTO 02
MENU
STOP
GTO 11
LBL 00 @@@@ Application Exit
EXITALL
RTN
LBL 14
          0000 Action for menu key LN
LN
RTN
LBL 15
          @@@@ Action for menu key LOG
LOG
RTN
LBL 16
          @@@@ Action for menu key YTX
Υ↑X
RTN
LBL 17
          @@@@ Action for menu key 10<sup>†</sup>X
10↑X
RTN
LBL 20
          0000 Action for menu key SIN
SIN
RTN
          @@@@ Action for menu key COS
LBL 21
```

| COS | | | | | | |
|----------------|------|-----------|-----|----------|--------|-------|
| RTN | | | | | | |
| LBL 22 | 0000 | Action | for | menu | key | TAN |
| TAN | | | | | | |
| RTN | | | | | | |
| | 0000 | Action | for | menu | key | ASIN |
| ASIN | | | | | | |
| RTN | | | _ | | _ | |
| LBL 24 | 0000 | Action | for | menu | key | ACOS |
| ACOS | | | | | | |
| RTN | | | | | | |
| | @@@@ | Action | ior | menu | key | ATAN |
| ATAN | | | | | | |
| RTN | 0000 | A -4 | ٠ | | 1 | CTNII |
| | 0000 | Action | ior | menu | кеу | SINH |
| SINH | | | | | | |
| RTN | 0000 | A -4 | ٠ | | 1 | COCII |
| LBL 28 | 0000 | Action | ior | menu | кеу | CUSH |
| COSH RTN | | | | | | |
| LBL 29 | 0000 | Action | for | m 0 m 11 | 1-0 | TANU |
| TANH | 0000 | Action | 101 | menu | кеу | IANH |
| RTN | | | | | | |
| | രരരര | Action | for | manıı | kov | АСТИН |
| ASINH | 6666 | ACCION | 101 | menu | ксу | ADIMI |
| RTN | | | | | | |
| LBL 31 | രരരര | Action | for | menii | kev | ACOSH |
| ACOSH | | | | | J | |
| RTN | | | | | | |
| LBL 32 | 0000 | Action | for | menu | kev | ATANH |
| ATANH | | | | | , | |
| RTN | | | | | | |
| LBL 33 | 0000 | Action | for | menu | key | %СН |
| %СН | | | | | - | |
| RTN | | | | | | |
| LBL 34 | 0000 | Action | for | menu | key | % |
| % | | | | | | |
| RTN | | | | | | |
| LBL 36 | 0000 | Action | for | menu | key | TRUN |
| IP | | | | | | |
| RTN | | | | | | |
| LBL 37 | 0000 | Action | for | menu | key | FP |
| FP | | | | | | |
| RTN | | | _ | | _ | |
| | 0000 | Action | for | menu | key | DIV |
| BASE÷ | | | | | | |
| RTN | 2222 | | | | | DEM |
| | 0000 | Action | ior | menu | кеу | REM |
| MOD | | | | | | |
| RTN | 2222 | A | c | | 1 | COMP |
| | 0000 | Action | ior | menu | кеу | COMB |
| COMB | | | | | | |
| RTN | 0000 | 1 at i a- | for | mo=== | le co- | DEDM |
| LBL 41 PERM | @@@@ | Action | TOL | menu | кеу | renii |
| RTN | | | | | | |
| LBL 42 | രരരര | Action | for | menii | kev | |
| -DU 42 | | | 101 | omu | 11-0 у | • |
| | | | | | | |

```
N!
RTN
LBL 43
        0000 Action for menu key GAM
GAMMA
0000 Free labels start at: 44
5 Functions
5.1 Complex Numbers
(RPART)
0000 DSC: Real part
@@@@ IN: X: Number or numeric matrix (element-wise)
0000 OUT: X: rpart(x)
@@@@ LBL: 69-72
0000 TST: free42_3.0.2
@@@@ UPD: 2021-04-22
LBL "RPART"
FUNC 11
             @@## REQ:free42>=2.5.24
L4STK
             @@## REQ:free42>=3.0
ENTER
XEQ 89
             0000 ATYP
X=0?
RTNERR 4
             @@## REQ:free42>=2.5.24
1/X
             @@## REQ:free42<2.5.24
68
GTO IND ST X
LBL 69
             0000 Real Number
LBL 70
             0000 Real Matrix
R↓
RTN
LBL 71
             @@@@ Complex Number
LBL 72
             @@@@ Complex Matrix
R↓
XEQ 98
             @@@@ C-R&I
X<>Y
RTN
(IPART)
0000 DSC: Imaginary Part
@@@@ IN: X: Number or numeric matrix (element-wise)
0000 OUT: X: ipart(x)
@@@@ LBL: 73-76
@@@@ TST: free42_3.0.2
@@@@ UPD: 2021-04-22
LBL "IPART"
FUNC 11
             @@## REQ:free42>=2.5.24
L4STK
             @@## REQ:free42>=3.0
ENTER
XEQ 89
             0000 ATYP
X=0?
             @@## REQ:free42>=2.5.24
RTNERR 4
1/X
             @@## REQ:free42<2.5.24
72
```

+

10

```
GTO IND ST X
LBL 73
             0000 Real Number
0
RTN
LBL 74
             0000 Real Matrix
R↓
DIM?
NEWMAT
RTN
LBL 75
             0000 Complex Number
LBL 76
             0000 Complex Matrix
XEQ 98
              @@@@ C→R&I
RTN
(CONJ)
@@@@ DSC: Complex Conjugate
@@@@ IN: X: Number or numeric matrix (element-wise)
0000 OUT: X: conj(x)
0000 TST: free42_3.0.2
0000 LBL: 77-80
0000 BUG: Fails on alpha string matrix
0000 UPD: 2021-04-22
LBL "CONJ"
FUNC 11
             @@## REO:free42>=2.5.24
             @@## REQ:free42>=3.0
L4STK
ENTER
XEQ 89
             0000 ATYP
X=0?
RTNERR 4
             @@## REQ:free42>=2.5.24
             @@## REQ:free42<2.5.24
1/X
76
GTO IND ST X
LBL 77
             0000 Real Number
LBL 78
             0000 Real Matrix
R.↓
RTN
LBL 79
             0000 Complex Number
LBL 80
             @@@@ Complex Matrix
COMPLEX
+/-
COMPLEX
RTN
(CABS)
0000 DSC: Magnitude/absolute value
@@@@ IN: X: Number or numeric matrix (element-wise) -- built in ABS won't work with a complex matrix
@@@@ OUT: X: |x|
@@@@ TST: CPXRES free42_3.0
0000 LBL: 81-84
0000 BUG: Returns 0 for real 0 input
@@@@ UPD: 2021-04-22
LBL "CABS"
FUNC 11
             @@## REO:free42>=2.5.24
L4STK
             @@## REQ:free42>=3.0
```

```
ENTER
XEQ 89
             @@@@ ATYP
X=0?
RTNERR 4
             @@## REQ:free42>=2.5.24
1/X
             @@## REQ:free42<2.5.24
80
GTO IND ST X
LBL 81
             0000 Real Number
LBL 82
             0000 Real Matrix
R↓
ABS
RTN
LBL 83
             @@@@ Complex Number
LBL 84
             @@@@ Complex Matrix
R↓
XEQ 98
             @@@@ C→M&A
X<>Y
RTN
(CARG)
@@@@ DSC: Complex Argument
0000 IN: X: Number or numeric matrix (element-wise)
0000 OUT: X: arg(x)
@@@@ TST: CPXRES free42_3.0
@@@@ LBL: 85-88
@@@@ BUG: Returns 0 for real 0 input
0000 UPD: 2021-04-22
LBL "CARG"
FUNC 11
             @@## REQ:free42>=2.5.24
             @@## REQ:free42>=3.0
L4STK
ENTER
XEQ 89
             @@@@ ATYP
X=0?
RTNERR 4
             @@## REQ:free42>=2.5.24
             @@## REQ:free42<2.5.24
1/X
84
GTO IND ST X
LBL 85
             0000 Real Number
RTN
LBL 86
             0000 Real Matrix
DIM?
NEWMAT
RTN
LBL 87
             @@@@ Complex Number
LBL 88
             @@@@ Complex Matrix
R↓
XEQ 98
             @@@@ C→M&A
RTN
0000 DSC: Complex Number -> Real Part & Imaginary Part
@@@@ NAM: C→R&I 98
```

@@@@ IN: X: Complex Number or Complex Matrix

12

```
@@@@ OUT: Y: Real Part of X
0000
        X: Imaginary Part of X
@@@@ LBL: 97
@@@@ TST: free42_3.0.2
@@@@ UPD: 2021-04-22
LBL 98
FUNC 12
             @@## REQ:free42>=2.5.24
L4STK
             @@## REQ:free42>=3.0
ENTER
FS? 73
GTO 97
@@@@ RECT MODE
COMPLEX
RTN
LBL 97
@@@@ POLAR MODE
RECT
COMPLEX
POT.AR.
RTN
0000 DSC: Complex Number -> Magnitude & Argument (angle)
@@@@ NAM: C→M&A 98
@@@@ IN: X: Complex Number or Complex Matrix
@@@@ OUT: Y: Magnitude of X
0000
        X: Complex Argument (angle) of X
0000 LBL: 99
0000 TST: free42_3.0.2
@@@@ UPD: 2021-04-22
LBL 98
FUNC 12
             @@## REO:free42>=2.5.24
I.4STK
             @@## REQ:free42>=3.0
ENTER
FS? 73
GTO 99
@@@@ RECT MODE
POLAR
COMPLEX
RECT
R.TN
LBL 99
@@@@ POLAR MODE
COMPLEX
RTN
@@@@ DSC: Arithmetic Type
0000 NAM: ATYP 89
0000 IN: X: an object
0000 OUT: X: 1 if input X was a real number
0000
           2 if input X was a real matrix
0000
           3 if input X was a complex number
0000
           4 if input X was a complex matrix
0000
           O if none of the above are true
@@@@ TST: free42 3.0.2
@@@@ FAQ: Even on free42<2.5.24 or a real 42s, X, Y, & Z are preserved. T & Last X not so much.
```

```
0000 BUG: A 2 will be returned for a real matrix containing strings
@@@@ BUG: In infinite stack mode with an empty stack 2 will be returned as X=O when we do L4STK
@@@@ LBL: 90-97
@@@@ UPD: 2021-02-23
LBL 89
FUNC 11
              @@## REQ:free42>=2.5.24
L4STK
              @@## REQ:free42>=3.0
MAT?
GTO 90
GTO 91
LBL 90
              0000 Matrix
CLA
ARCL ST X
67
POSA
X>0?
GTO 96
GTO 97
I.BI. 96
              @@@@ Complex Matrix
4
RTN
LBL 97
              0000 Real/String Matrix
2
RTN
LBL 91
              @@@@ Not matrix
REAL?
GTO 92
GTO 93
LBL 92
              0000 Real number
1
RTN
              @@@@ Not matrix or real
LBL 93
CPX?
GTO 94
GTO 95
LBL 94
              0000 Complex number
3
RTN
LBL 95
              0000 Not matrix, real, or complex
0
RTN
5.2 Percentages
(PTOT)
@@@@ DSC: Percentage of total (just like hp-12c button)
@@@@ IN: Y: Real Number -- Total
         X: Real Number -- Part
0000 OUT: Y: Y
0000
         X: 100*X/Y
0000 UPD: 2021-03-12
LBL "%T"
FUNC 22
              @@## REQ:free42>=2.5.24
L4STK
              @@## REQ:free42>=3.0
RCL÷ ST Y
100
```

5.3 Integers

```
(ROUND)
@@@@ DSC: Properly round to integer. N.5 rounded to nearest even number.
0000 IN: X: real number
0000 OUT: X: floor(X)
0000 UPD: 2021-02-23
@@@@ TST: free42 3.0.2
@@@@ TC: -2.0 -2 →Int
0000 TC: -1.6 -2 →Nearest
@@@@ TC: -1.5 -2 →Even
0000 TC: -1.4 -1 →Nearest
0000 TC: -1.0 -1 →Int
0000 TC: -1.6 -1 →Nearest
0000 TC: -0.5 0 Even Rule
0000 TC: -0.4 0 →Nearest
@@@@ TC: 0.0 0 →Int
@@@@ TC: 0.4 0 →Nearest
@@@@ TC: 0.5 0 Even Rule
@@@@ TC: 1.6 1 →Nearest
@@@@ TC: 1.0 1 →Int
0000 TC: 1.4 1 →Nearest
@@@@ TC: 1.5 2 →Even
@@@@ TC: 1.6 2 →Nearest
0000 TC: 2.0 2 →Int
LBL "ROUND"
FUNC 11
             @@## REQ:free42>=2.5.24
L4STK
             @@## REQ:free42>=3.0
ENTER
             @@@@ X
                         Х
FP
             0000 FP
                         Х
ABS
             @@@@ |FP|
                         Х
0.5
             0000 1/2
                         |FP|
                                Х
             0000 |FP|-1/2 X
X<>Y
             @@@@ X
                         |FP|-1/2 X
SIGN
             0000 SGN
                         |FP|-1/2 X
             0000 X
                         SGN
                                |FP|-1/2 X
LASTX
ΙP
             @@@@ IP(X)
                         SGN
                                |FP|-1/2 X
O=? ST Z @@## TODO: Memory leak in free42 < 3.0.3
GTO 67
0<? ST Z @@## TODO: Memory leak in free42 < 3.0.3</pre>
+
RTN
LBL 67
0000 FP=1/2
XEQ 68
             @@@@ ODD?
+
RTN
@@@@ DSC: RETYES if X is odd, RTNNO otherwise
LBL 68
             @@@@ ODD?
FUNC 00
L4STK
2
÷
```

```
FP
X=0?
RTNNO
RTNYES
(FLOOR)
0000 DSC: Floor -- Round toward negative infinity
0000 IN: X: real number
@@@@ OUT: X: floor(X)
0000 UPD: 2021-02-23
@@@@ TST: free42_3.0.2
LBL "FLOOR"
FUNC 11
            @@## REQ:free42>=2.5.24
L4STK
            @@## REQ:free42>=3.0
FP
I.ASTX
ΙP
0 \le? ST Y @@## TODO: Memory leak in free42 < 3.0.3
RTN
1
RTN
(CEIL)
@@@@ DSC: Ceiling -- Round toward positive infinity
0000 IN: X: real number
@@@@ OUT: X: ceil(X)
0000 UPD: 2021-02-23
0000 TST: free42_3.0.2
LBL "CEIL"
            @@## REQ:free42>=2.5.24
FUNC 11
L4STK
            @@## REQ:free42>=3.0
FP
LASTX
ΤP
0 \ge? ST Y @@## TODO: Memory leak in free42 < 3.0.3
RTN
1
RTN
(GCD)
@@@@ DSC: GCD
0000 IN: Y: real number
0000
       X: real number
@@@@ OUT: X: GCD(|IP(X)|, |IP(X)|)
0000 LBL: 66
@@@@ UPD: 2021-04-22
@@@@ TST: free42_3.0.2
LBL "GCD"
FUNC 21
            @@## REQ:free42>=2.5.24
L4STK
            @@## REQ:free42>=3.0
ABS
ΙP
X<>Y
ABS
ΙP
```

```
X>Y?
X<>Y
LBL 66
STO ST Z
MOD
X>0?
GTO 66
R↓
RTN
                                                                           (LCM)
@@@@ DSC: LCM
0000 IN: Y: real number
0000
        X: real number
@@@@ OUT: X: LCM(|IP(X)|, |IP(X)|)
@@@@ USE: GCD
@@@@ UPD: 2021-04-22
@@@@ TST: free42_3.0.2
LBL "LCM"
FUNC 21
              @@## REQ:free42>=2.5.24
L4STK
              @@## REQ:free42>=3.0
ABS
              0000 IXI
ΙP
              0000 IP(|X|)
                                Y
X=0?
RTN
X<>Y
              0000 Y
                                IP(|X|)
ABS
              @@@@ |Y|
                                IP(|X|)
ΙP
              0000 IP(|Y|)
                                IP(|X|)
X=0?
RTN
RCL ST Y
              0000 IP(|X|)
                                IP(|Y|)
                                              IP(|X|)
RCL ST Y
              0000 IP(|Y|)
                                IP(|X|)
                                              IP(|Y|)
                                                            IP(|X|)
              @@@@ IP(|Y|)*IP(|X|) IP(|Y|)
                                              IP(|X|)
RCL ST Z
              0000 IP(|X|)
                                IP(|Y|)*IP(|X|) IP(|Y|)
                                                            IP(|X|)
RCL ST Z
              0000 IP(|Y|)
                                IP(|X|)
                                              IP(|Y|)*IP(|X|) IP(|Y|)
XEQ "GCD"
              @@@@ GCD
                                IP(|Y|)*IP(|X|) IP(|Y|)
                                                            IP(|Y|)
              @@@@ LCM
                                IP(|Y|)
                                              IP(|Y|)
                                                            IP(|Y|)
RTN
    Binomials, Factorals, Beta, etc...
(BETA)
QQQQ DSC: beta function
@@@@ IN: Y: Number
0000 IN: X: Number
0000 OUT: X: beta(x, y) = beta(y, x)
@@@@ TST: free42_3.0.2
0000 UPD: 2021-02-23
LBL "BETA"
FUNC 21
              @@## REQ:free42>=2.5.24
L4STK
              @@## REQ:free42>=3.0
RCL ST Y
GAMMA
RCL ST Y
GAMMA
RCL ST Z
```

```
GAMMA
÷
RTN
0000 DSC: digamma function
@@@@ IN: X: Number
@@@@ OUT: X: psi(X)
@@@@ FAQ: Good to about 1e-5 for real X>0.1
0000 TST: free42 3.0.2
0000 UPD: 2021-05-02
LBL "DIGAMM"
FUNC 11
              @@## REQ:free42>=2.5.24
L4STK
              @@## REQ:free42>=3.0
LSTO "_X"
              @@@@ X
              0000 2 X
              @@@@ 2+X
LSTO "_S"
              0000 S
LN
              0000 SUM
                                 ln(s)
2
              0000 2 S SUM
RCL× "_S"
              0000 2*S SUM
              0000 TRM SUM
1/X
              @@@@ SUM
                                 ln(s) -1/(2*s)
RCL "_S"
              0000 S SUM
              0000 S^2 SUM
X↑2
LSTO "_SS"
              0000 SS SUM
12
              0000 12 S^2 SUM
              0000 12*S^2 SUM
1/X
              0000 TRM SUM
              @@@@ SUM
                                  ln(s) -1/(2*s) -1/(12*s^2)
RCL "_SS"
              0000 S^2 SUM
RCL× "_SS"
              0000 S^4 SUM
STO ST Z
              0000 S^4 SUM S^4
120
1/X
                                  ln(s) -1/(2*s) -1/(12*s^2) +1/(120*s^4)
              0000 SUM S^4
X<>Y
RCL× "_SS"
              0000 S^6 SUM
STO ST Z
              0000 S^6 SUM S^6
252
1/X
              0000 SUM S^6
                                  ln(s) -1/(2*s) -1/(12*s^2) +1/(120*s^4) -1/(252*s^6)
X<>Y
RCL× "_SS"
              0000 S^8 SUM
STO ST Z
              0000 S^8 SUM S^8
240
1/X
              0000 SUM S^8
                                  \ln(s) - 1/(2*s) - 1/(12*s^2) + 1/(120*s^4) - 1/(252*s^6) + 1/(240*s^8)
X<>Y
RCL× "_SS"
              0000 S^10 SUM
STO ST Z
              @@@@ S^10 SUM S^10
660
```

(DIGAMM)

RCL ST Z

```
×
1/X
                0000 SUM S^10
                                      ln(s) -1/(2*s) -1/(12*s^2) +1/(120*s^4) -1/(252*s^6) +1/(240*s^8) -5/(660*s^10)
X<>Y
RCL× "_SS"
                @@@@ S^12 SUM
STO ST Z
                0000 S^12 SUM S^12
32760
1/X
691
                 0000 SUM S^12
                                      ln(s) -1/(2*s) -1/(12*s^2) +1/(120*s^4) -1/(252*s^6) +1/(240*s^8) -5/(660*s^10) +691/(32760*s^12)
X<>Y
RCL× "_SS"
                0000 S^14 SUM
12
×
1/X
                                      \ln(s) - 1/(2*s) - 1/(12*s^2) + 1/(120*s^4) - 1/(252*s^6) + 1/(240*s^8) - 5/(660*s^10) + 691/(32760*s^12) - 1/(12*s^14)
                 0000 SUM
RCL "_X"
1/X
                 0000 SUM
                                      \ln(s) - 1/(2*s) - 1/(12*s^2) + 1/(120*s^4) - 1/(252*s^6) + 1/(240*s^8) - 5/(660*s^{10}) + 691/(32760*s^{12}) - 1/(12*s^{14}) - 1/x
RCL "_X"
1
1/X
                 0000 SUM
                                      \ln(s) - 1/(2*s) - 1/(12*s^2) + 1/(120*s^4) - 1/(252*s^6) + 1/(240*s^8) - 5/(660*s^10) + 691/(32760*s^12) - 1/(12*s^14) - 1/x - 1/(x+1)
RTN
5.5 Error & Standard Normal Functions
                                                                                            (NPDF)
```

```
0000 DSC: Standard Normal PDF
0000 IN: X: real number
@@@@ OUT: X: Standard Normal PDF value at X
0000 UPD: 2021-04-22
@@@@ TST: free42_3.0.2
@@@ TC: -2 0.05399096651318805195056
@@@@ TC: -1 0.2419707245191433497978
@@@@ TC: 0 0.3989422804014326779399
@@@@ TC: 1 0.2419707245191433497978
@@@@ TC:
         2 0.05399096651318805195056
LBL "NPDF"
FUNC 11
              @@## REQ:free42>=2.5.24
              @@## REQ:free42>=3.0
L4STK
X↑2
              0000 X^2
-2
              @@@@ -2
                                       X^2
              @@@@ -X^2/2
E↑X
              0000 \text{ EXP}(-X^2/2)
2
              @@@@ 2
                                       EXP(-X^2/2)
ΡI
              0000 PI
                                                   EXP(-X^2/2)
              0000 PI*2
                                       EXP(-X^2/2)
SQRT
              @@@@ SQRT(PI*2)
                                       EXP(-X^2/2)
              @@@@ EXP(-X^2/2)/SQRT(PI*2)
RTN
```

| 000000000000000000000000000000000000000 | | | | | |
|---|---|-----------------|------------|--|--|
| 0000 DSC: Stand | ard Normal CDF | | | | |
| 0000 IN: X: re | 0000 IN: X: real number | | | | |
| 0000 OUT: X: St | 2000 OUT: X: Standard Normal CDF value at X | | | | |
| | @@@@ BUG: Only good to 7 decimal places | | | | |
| 0000 FAQ: No de | pendancies, variables, loop | s, or branches | | | |
| 0000 REF: Zelen | & Severo (1964) | | | | |
| 0000 UPD: 2021- | 04-22 | | | | |
| 0000 TST: free4 | 2_3.0.2 | | | | |
| 0000 TC: -2 0. | 02275013194817920720028 | | | | |
| 0000 TC: -1 0. | 1586552539314570514148 | | | | |
| 0000 TC: 0 0. | 5 | | | | |
| | 8413447460685429485852 | | | | |
| | 9772498680518207927997 | | | | |
| LBL "NCDF" | | | | | |
| FUNC 11 | @@## REQ:free42>=2.5.24 | | | | |
| L4STK | @@## REQ:free42>=3.0 | | | | |
| 0.2316419 | @@@@ b0 | Χ ? | ? | | |
| RCL× ST Y | @@@@ b0*X | Χ ? | ? | | |
| 1 | 0000 1 | b0*X X | ? | | |
| + | @@@@ 1+b0*X | Χ ? | ? | | |
| 1/X | @@@@ 1/(1+b0*X) | Χ ? | ? | | |
| | 0000 T | Χ ? | ? | | |
| Х<>Х | 0000 X | T ? | ? | | |
| X12 | 0000 X^2 | T ? | ? | | |
| -2 | 0000 -2 | X^2 ? | ? | | |
| ÷ | @@@@ -X^2/2 | T ? | ? | | |
| E↑X | 0000 EXP(-X^2/2) | T ? | ? | | |
| 2 | 0000 2 | $EXP(-X^2/2)$ T | ? | | |
| PI | 0000 PI | 2 EXP | (-X^2/2) T | | |
| × | @@@@ PI*2 | $EXP(-X^2/2)$ T | T | | |
| SQRT | @@@@ SQRT(PI*2) | $EXP(-X^2/2)$ T | T | | |
| ÷ | @@@@ EXP(-X^2/2)/SQRT(PI*2 | | T | | |
| | 0000 N | T T | T | | |
| RCL ST Y | 0000 T | N T | T | | |
| × | 0000 NT | T T | T | | |
| 0.319381530 | 0000 b1 | NT T | T | | |
| RCL× ST Y | 0000 PR | NT T | T | | |
| RCL ST Z | 0000 T | PR NT | T | | |
| STO× ST Z | 0000 T | PR NT^ | | | |
| R↓ | 0000 PR | NT^2 T | T | | |
| -0.356563782 | | PR NT^ | | | |
| RCL× ST Z | 0000 NT | PR NT^ | | | |
| + | 0000 PR | NT^2 T | T | | |
| RCL ST Z | 0000 T | PR NT^ | | | |
| STO× ST Z | 0000 T | PR NT^ | | | |
| R↓ | 0000 PR | NT^3 T | T | | |
| 1.781477937 | 0000 b3 | PR NT^ | | | |
| RCL× ST Z | 0000 NT | PR NT^ | | | |
| + | 0000 PR | NT^3 T | T | | |
| RCL ST Z | 0000 T | PR NT^ | | | |
| STO× ST Z | 0000 T | PR NT^ | | | |
| R↓ | 0000 PR | NT^4 T | T T | | |
| -1.821255978 | 0000 b4 | PR NT^ | | | |
| RCL× ST Z | 0000 NT | PR NT^ | | | |
| + | 0000 PR | NT^4 T | T | | |

(NCDF)

```
RCL ST Z
              0000 T
                                      PR
                                                  NT^4
                                                             Т
STO× ST Z
              0000 T
                                      PR
                                                  NT<sup>5</sup>
                                                             Т
R↓
              0000 PR
                                      NT^5
                                                  Т
                                                             Т
1.330274429
              @@@@ ъ5
                                      PR
                                                  NT^5
                                                             Т
RCL× ST Z
              0000 NT
                                      PR
                                                  NT<sup>5</sup>
                                                             Т
              0000 PR
                                      NT^5
                                                  Т
                                                             Т
1
              0000 1
                                      PR
                                                  NT<sup>5</sup>
                                                             Т
X<>Y
              @@@@ PR.
                                      1
                                                  NT<sup>5</sup>
                                                             Т
                                      NT<sup>5</sup>
                                                  Т
                                                             Т
              0000 1-PR
RTN
(ERF)
0000 DSC: erf (error) function
0000 IN: X: real number
@@@@ OUT: X: erf(X)
@@@@ USE: NCDF
@@@@ LBL: Use: 64-65
@@@@ UPD: 2021-03-30
@@@@ TST: free42_3.0.2
@@@@ TC: -1 -0.8427007929497148693412
0000 TC: 0 0.0
@@@@ TC: 1 0.8427007929497148693412
@@@@ TC: 2 0.9953222650189527341621
LBL "ERF"
FUNC 11
              @@## REO:free42>=2.5.24
L4STK
              @@## REQ:free42>=3.0
ENTER
ENTER
2
SQRT
ABS
XEQ "NCDF"
2
1
X<>Y
X<0?
GTO 64
GTO 65
LBL 64
R↓
+/-
RTN
LBL 65
R↓
RTN
(ERFC)
@@@@ DSC: erfc (complementary error) function
0000 IN: X: real number
@@@@ OUT: X: erfc(X)
0000 USE: ERF
0000 UPD: 2021-03-30
0000 TST: free42 3.0.2
@@@@ TC: -1 1.842700792949714869341
```

```
@@@@ TC: 0 1.0
@@@@ TC: 1 0.1572992070502851306588
@@@@ TC: 2 0.004677734981047265837931
LBL "ERFC"
FUNC 11
          @@## REQ:free42>=2.5.24
L4STK
          @@## REQ:free42>=3.0
XEQ "ERF"
1
X<>Y
RTN
  Hyperbolic Trigonometric Functions
(CSCH)
0000 DSC: 1/SINH(X)
LBL "CSCH"
          @@## REQ:free42>=2.5.24
FUNC 11
L4STK
          @@## REQ:free42>=3.0
SINH
1/X
RTN
(SECH)
@@@@ DSC: 1/COSH(X)
LBL "SECH"
FUNC 11
          @@## REO:free42>=2.5.24
L4STK
          @@## REQ:free42>=3.0
COSH
1/X
RTN
(COTH)
0000 DSC: 1/TANH(X)
LBL "COTH"
FUNC 11
          @@## REQ:free42>=2.5.24
L4STK
          @@## REQ:free42>=3.0
TANH
1/X
RTN
(ACSCH)
@@@@ DSC: SINH(1/X)
LBL "ACSCH"
          @@## REO:free42>=2.5.24
FUNC 11
L4STK
          @@## REQ:free42>=3.0
1/X
ASINH
RTN
(ASECH)
0000 DSC: COSH(1/X)
LBL "ASECH"
FUNC 11
          @@## REQ:free42>=2.5.24
L4STK
          @@## REQ:free42>=3.0
1/X
```

```
ACOSH
RTN
(ACOTH)
0000 DSC: TANH(1/X)
LBL "ACOTH"
FUNC 11
           @@## REQ:free42>=2.5.24
L4STK
           @@## REQ:free42>=3.0
1/X
ATANH
RTN
5.7 Trigonometric Functions
(AHAV)
0000 DSC: Inverse Haversine
0000 IN: X: number
@@@@ OUT: X: ahav(X)=2*asin(sqrt(X))
0000 UPD: 2021-04-18
@@@@ TST: free42_3.0.2
LBL "AHAV"
FUNC 11
           @@## REQ:free42>=2.5.24
L4STK
           @@## REQ:free42>=3.0
SQRT
ASIN
2
RTN
(HAV)
@@@@ DSC: Haversine
0000 IN: X: number
0000 OUT: X: hav(X)=1/2-cos(X)/2
@@@@ UPD: 2021-04-18
0000 TST: free42_3.0.2
LBL "HAV"
FUNC 11
           @@## REQ:free42>=2.5.24
L4STK
           @@## REQ:free42>=3.0
COS
-2
0.5
+
RTN
(HYPOT)
@@@@ DSC: Hypot
0000 IN: Y: number
0000 IN: X: number
@@@@ OUT: X: sqrt(abs(x)^2+abs(y)^2)
0000 UPD: 2021-02-23
@@@@ TST: free42_3.0.2
LBL "HYPOT"
FUNC 21
           @@## REO:free42>=2.5.24
L4STK
           @@## REQ:free42>=3.0
ABS
X<>Y
```

ABS COMPLEX ABS RTN (CSC) @@@@ DSC: 1/SIN(X) LBL "CSC" FUNC 11 @@## REO:free42>=2.5.24 @@## REQ:free42>=3.0 L4STK SIN 1/X RTN (SEC) @@@@ DSC: 1/COS(X) LBL "SEC" FUNC 11 @@## REQ:free42>=2.5.24 I.4STK @@## REQ:free42>=3.0 COS 1/X RTN (COT) @@@@ DSC: 1/TAN(X) LBL "COT" FUNC 11 @@## REO:free42>=2.5.24 @@## REQ:free42>=3.0 L4STK TAN 1/X RTN (ACSC) 0000 DSC: SIN(1/X) LBL "ACSC" @@## REQ:free42>=2.5.24 FUNC 11 @@## REQ:free42>=3.0 L4STK 1/X ASIN RTN (ASEC) @@@@ DSC: COS(1/X) LBL "ASEC" @@## REQ:free42>=2.5.24 FUNC 11 L4STK @@## REQ:free42>=3.0 1/X ACOS RTN (ACOT) @@@@ DSC: TAN(1/X) LBL "ACOT" FUNC 11 @@## REQ:free42>=2.5.24 L4STK @@## REQ:free42>=3.0 1/X

ATAN

```
@@@@ DSC: ATAN2
0000 IN: Y: number
0000 IN: X: number
@@@@ OUT: X: atan2(y, x)
@@@@ BUG: Only works in RAD mode
@@@@ UPD: 2021-02-23
@@@@ TST: free42_3.0.2
                                 = 45°
0000 TC: atan(1, 1) => pi/4
0000 TC: atan(-1, 1) = -pi/4
                                 = -45°
0000 TC: atan(1,-1) \Rightarrow 3*pi/4 = 135°
0000 TC: atan(-1,-1) = -3*pi/4 = -135°
@@@@ TC: atan( 0, 1) => 0
                                 = 0°
@@@@ TC: atan( 1, 0) => pi
                                 = 90°
0000 TC: atan(-1, 0) => -pi
                                 = -90°
@@@@ TC: atan( 0, 0) => ERROR
0000 LBL: Used 59-63
LBL "TAN2"
FUNC 21
               @@## REQ:free42>=2.5.24
L4STK
               @@## REQ:free42>=3.0
X>0?
GTO 59
X=0?
GTO 60
0000 X<0
X<>Y
X<0?
GTO 61
@@@@ X<O & Y>=O
X<>Y
ATAN
PΤ
+
RTN
LBL 61
0000 X<0 & Y<0
X<>Y
ATAN
РΤ
RTN
LBL 60
X<>Y
X=0?
GTO 62
X>0?
GTO 63
@@@@ X=O & Y<O
ΡI
-2
RTN
LBL 63
```

(ATAN2)

```
@@@@ X=O & Y>O
ΡI
2
RTN
LBL 62
@@@@ X=O & Y=O ERROR O/O
RTN
LBL 59
@@@@ X>O
ATAN
RTN
   Logs, Powers & Roots
(lnYX)
@@@@ DSC: Base Y Logarithm of X
0000 IN: Y: logarithm base
0000
       X: number or matrix (element-wise)
@@@@ OUT: X: log_y(x)
@@@@ UPD: 2021-04-14
0000 TST: free42_3.0.2
LBL "lnYX"
FUNC 21
            @@## REO:free42>=2.5.24
            @@## REQ:free42>=3.0
L4STK
LN
X<>Y
LN
RTN
(ln2)
0000 DSC: Base 2 Logarithm
0000 IN: X: number or matrix (element-wise)
0000 OUT: X: log_2(x)
@@@@ UPD: 2021-02-23
@@@@ TST: free42_3.0.2
LBL "ln2"
FUNC 11
            @@## REQ:free42>=2.5.24
L4STK
            @@## REQ:free42>=3.0
LN
2
LN
RTN
0000 DSC: Raise 2 to the power of X
0000 NAM: 21X 58
@@@@ IN: X: number or matrix (element-wise)
0000 OUT: X: 2^X
@@@@ UPD: 2021-02-23
@@@@ TST: free42_3.0.2
LBL 58
FUNC 11
            @@## REQ:free42>=2.5.24
```

```
L4STK
            @@## REQ:free42>=3.0
X<>Y
Y^X
R.TN
0000 DSC: Square root prefering real & pure imaginary answers
@@@@ NAM: ROOT2 57
0000 IN: X: Number or numeric matrix (element-wise)
@@@@ OUT: X: root of X
@@@@ FAQ: See XYROOT for details
0000 TST: free42_3.0.2
@@@@ UPD: 2021-04-14
LBL 57
FUNC 11
            @@## REO:free42>=2.5.24
2
X<>Y
XEQ "YROOT"
RTN
0000 DSC: Cube root prefering real & pure imaginary answers
0000 NAM: ROOT3 56
@@@@ IN: X: Number or numeric matrix (element-wise)
@@@@ OUT: X: root of X
@@@@ FAQ: See XYROOT for details
@@@@ TST: free42_3.0.2
0000 UPD: 2021-04-14
I.BI. 56
FUNC 11
            @@## REQ:free42>=2.5.24
X<>Y
XEQ "YROOT"
RTN
0000 DSC: Fifth root prefering real & pure imaginary answers
@@@@ NAM: ROOT5 55
@@@@ IN: X: Number or numeric matrix (element-wise)
@@@@ OUT: X: root of X
@@@@ FAQ: See XYROOT for details
@@@@ TST: free42 3.0.2
0000 UPD: 2021-04-14
LBL 55
FUNC 11
            @@## REQ:free42>=2.5.24
5
X<>Y
XEQ "YROOT"
RTN
0000 DSC: Seventh root prefering real & pure imaginary answers
@@@@ NAM: ROOT7 54
0000 IN: X: Number or numeric matrix (element-wise)
@@@@ OUT: X: root of X
@@@@ FAQ: See XYROOT for details
```

```
@@@@ TST: free42_3.0.2
0000 UPD: 2021-04-14
LBL 54
FUNC 11
              @@## REQ:free42>=2.5.24
X<>Y
XEQ "YROOT"
RTN
(YROOT)
0000 DSC: Nth roots prefering real & pure imaginary answers
@@@@ IN: Y: Number
@@@@ IN: X: Number or numeric matrix (element-wise)
@@@@ OUT: X: Yth root of X
0000 BUG: The principal value is not always returned (by design)
0000 BUG: Real integers are not recognized in complex form. i.e. 0+2i \neq 2
0000 FAQ: Return is pure imaginary when Y is an odd integer and X<0
0000 FAQ: Return is real when Y is an even integer and X<0
@@@@ TST: free42 3.0.2
0000 UPD: 2021-02-23
LBL "YROOT"
FUNC 21
              @@## REQ:free42>=2.5.24
L4STK
              @@## REQ:free42>=3.0
REAL?
GTO 48
GTO 51
LBL 48
0000 X is real
X≥0?
GTO 51
0000 X is negative, real
RCL ST Y
REAL?
GTO 49
GTO 50
0000 X is negative, real; Y is real
FP
X≠0?
GTO 50
0000 X is negative, real; Y is real integer
ABS
RCL ST Y
X<>Y
XEQ 51
+/-
X<>Y
2
FP
X=0?
GTO 53
GTO 52
0000 X is negative, real; Y is real integer even
R↓
```

```
-1
SQRT
RTN
LBL 52
0000 X is negative, real; Y is real integer odd
R↓
RTN
LBL 50
@@@@ Not special case. Stack: Y X Y
LBL 51
0000 Not special case. Stack: X Y
X<>Y
1/X
Y↑X
RTN
5.9 Everything Else
\tt coordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordoocoordooco
@@@@ DSC: Parallel Operator
0000 IN: Y: A Number
0000 IN: X: A Number
@@@@ OUT: X: 1/(1/X+1/Y)
@@@@ UPD: 2021-04-28
LBL "||"
                                                                  @@## REQ:free42>=2.5.24
FUNC 21
                                                                 @@## REQ:free42>=3.0
L4STK
1/X
X<>Y
1/X
1/X
RTN
6 END
END
```

7 EOF