

# free42 Uncertainty Propagation

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## Contents

1	Metadata	1
2	Introduction	1
3	Menu	1
3.1	Notes	1
3.1.1	[SHIFT] key magic for menus	1
3.1.2	Global Labels	1
3.1.3	UI→VU & UVU→I: Intervals	1
3.1.4	UVU→%	1
3.1.5	UxU: Multiply uncertainty	2
4	Menu Code	2
5	Functions	5
6	EOF	13

## 1 Metadata

The home for this HTML file is: <https://richmit.github.io/hp42/uprop.html>

A PDF version of this file may be found here: <https://richmit.github.io/hp42/uprop.pdf>

Files related to this document may be found on github: <https://github.com/richmit/hp42>

Directory contents:

<code>src</code>	-	The org-mode file that generated this HTML document
<code>src_42s</code>	-	Ready to convert source listings for 42s code in this document
<code>docs</code>	-	This html document
<code>bin</code>	-	Importable RAW program files

## 2 Introduction

This org-mode file contains a program, `UPROP`, that can be used to preform calculations that propagate uncertainty using the standard Gaussian model. Values are represented as complex numbers with the imaginary part being the standard deviation. i.e.  $V+iU$  means the value is  $V$  and the uncertainty is represented by  $U$  (a standard deviation).

## 3 Menu

### 3.1 Notes

#### 3.1.1 [SHIFT] key magic for menus

Menu keys that can accept a value with uncertainty in the X position of the stack behave differently when used with the [SHIFT] key. If the [SHIFT] key is pressed before such a menu key, then it is like pressing [SHIFT] [COMPLEX] and then the menu key. For example, pressing [SHIFT] [COSH] is the same as [SHIFT] [COMPLEX] [COSH]. This is a handy way to save a keystroke when entering new values.

Note that `I→VU` doesn't take a value with uncertainty, and thus pressing the [SHIFT] key before this function has no effect.

#### 3.1.2 Global Labels

The menu items correspond to global labels that you can `XEQ` from other programs. The names are the menu labels prefixed with "U" – so "SIN" becomes "USIN".

#### 3.1.3 UI→VU & UVU→I: Intervals

These functions convert between intervals and quantity with uncertainty. Intervals are specified by interval end points on levels X & Y of the stack. For `I→VU` the order is not relevant, but `VU→I` will always return the leftmost end point in Y and the rightmost end point in X.

#### 3.1.4 UVU→%

Given a quantity with uncertainty in X, it will return `T%` of the uncertainty. This value is always positive.



```

"LN"
KEY 1 XEQ 12
"E↑X"
KEY 2 XEQ 13
"Y↑X"
KEY 3 XEQ 14
"ABS"
KEY 4 XEQ 15
"GAMMA"
KEY 5 XEQ 16
KEY 7 GTO 01
KEY 8 GTO 03
KEY 9 GTO 00
MENU
STOP
GTO 02
LBL 03      @@@@ Page 3 of menu UPROP
CLMENU
"SIN"
KEY 1 XEQ 17
"COS"
KEY 2 XEQ 18
"TAN"
KEY 3 XEQ 19
"ASIN"
KEY 4 XEQ 20
"ACOS"
KEY 5 XEQ 21
"ATAN"
KEY 6 XEQ 22
KEY 7 GTO 02
KEY 8 GTO 04
KEY 9 GTO 00
MENU
STOP
GTO 03
LBL 04      @@@@ Page 4 of menu UPROP
CLMENU
"SINH"
KEY 1 XEQ 23
"COSH"
KEY 2 XEQ 24
"TANH"
KEY 3 XEQ 25
"ASINH"
KEY 4 XEQ 26
"ACOSH"
KEY 5 XEQ 27
"ATANH"
KEY 6 XEQ 28
KEY 7 GTO 03
KEY 8 GTO 05
KEY 9 GTO 00
MENU
STOP
GTO 04
LBL 05      @@@@ Page 5 of menu UPROP
CLMENU
"I→VU"
KEY 1 XEQ "UI→VU"
"VU→I"
KEY 2 XEQ 29
"VU→%"
KEY 4 XEQ 30
"×U"
KEY 6 XEQ 31
KEY 7 GTO 04
KEY 8 GTO 01
KEY 9 GTO 00
MENU
STOP
GTO 05
LBL 00 @@@@ Application Exit
EXITALL
RTN
LBL 06      @@@@ Action for menu key +

```

```

FS? 64
COMPLEX
XEQ "U+"
RTN
LBL 07      @@@@ Action for menu key -
FS? 64
COMPLEX
XEQ "U-"
RTN
LBL 08      @@@@ Action for menu key ×
FS? 64
COMPLEX
XEQ "U×"
RTN
LBL 09      @@@@ Action for menu key ÷
FS? 64
COMPLEX
XEQ "U÷"
RTN
LBL 10      @@@@ Action for menu key +/-
FS? 64
COMPLEX
XEQ "U+/-"
RTN
LBL 11      @@@@ Action for menu key 1/X
FS? 64
COMPLEX
XEQ "U1/X"
RTN
LBL 12      @@@@ Action for menu key LN
FS? 64
COMPLEX
XEQ "ULN"
RTN
LBL 13      @@@@ Action for menu key E↑X
FS? 64
COMPLEX
XEQ "UE↑X"
RTN
LBL 14      @@@@ Action for menu key Y↑X
FS? 64
COMPLEX
XEQ "UY↑X"
RTN
LBL 15      @@@@ Action for menu key ABS
FS? 64
COMPLEX
XEQ "UABS"
RTN
LBL 16      @@@@ Action for menu key GAMMA
FS? 64
COMPLEX
XEQ "UGAMMA"
RTN
LBL 17      @@@@ Action for menu key SIN
FS? 64
COMPLEX
XEQ "USIN"
RTN
LBL 18      @@@@ Action for menu key COS
FS? 64
COMPLEX
XEQ "UCOS"
RTN
LBL 19      @@@@ Action for menu key TAN
FS? 64
COMPLEX
XEQ "UTAN"
RTN
LBL 20      @@@@ Action for menu key ASIN
FS? 64
COMPLEX
XEQ "UASIN"
RTN
LBL 21      @@@@ Action for menu key ACOS
FS? 64

```

```

COMPLEX
XEQ "UACOS"
RTN
LBL 22      @@@@ Action for menu key ATAN
FS? 64
COMPLEX
XEQ "UATAN"
RTN
LBL 23      @@@@ Action for menu key SINH
FS? 64
COMPLEX
XEQ "USINH"
RTN
LBL 24      @@@@ Action for menu key COSH
FS? 64
COMPLEX
XEQ "UCOSH"
RTN
LBL 25      @@@@ Action for menu key TANH
FS? 64
COMPLEX
XEQ "UTANH"
RTN
LBL 26      @@@@ Action for menu key ASINH
FS? 64
COMPLEX
XEQ "UASINH"
RTN
LBL 27      @@@@ Action for menu key ACOSH
FS? 64
COMPLEX
XEQ "UACOSH"
RTN
LBL 28      @@@@ Action for menu key ATANH
FS? 64
COMPLEX
XEQ "UATANH"
RTN
LBL 29      @@@@ Action for menu key VU→I
FS? 64
COMPLEX
XEQ "UVU→I"
RTN
LBL 30      @@@@ Action for menu key VU→%
FS? 64
COMPLEX
XEQ "UVU→%"
RTN
LBL 31      @@@@ Action for menu key ×U
FS? 64
COMPLEX
XEQ "U×U"
RTN
@@@@ Free labels start at: 32

```

## 5 Functions

```

@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@ (UPLUS)
@@@@ IN:  Y: Y  Quantity & Uncertainty _or_ Exact Quantity
@@@@     X: X  Quantity & Uncertainty _or_ Exact Quantity
@@@@ OUT: X: Y+X Quantity & Uncertainty (Uncertainty is 0 when X & Y are exact)
LBL "U+"
FUNC 21      @@@@ X Y
L4STK
XEQ 99 @NM@ R→C      @@@@ X Y
X<>Y          @@@@ Y X
XEQ 99 @NM@ R→C      @@@@ Y X
COMPLEX      @@@@ Y.u Y.v X
X<>Y          @@@@ Y.v Y.u X
RCL ST Z      @@@@ X Y.v Y.u X
COMPLEX      @@@@ X.u X.v Y.v Y.u
Rv            @@@@ X.v Y.v Y.u X.u
+             @@@@ (Y+X).v Y.u X.u
Rv            @@@@ Y.u X.u ? (X+Y).v
COMPLEX      @@@@ TMP ? (X+Y).v (X+Y).v

```

~~~~~ (UMINUS)

LBL "U\_"

(UMULT)

LBL "Ux"

~~~~~~(UDIV)

LBL "U÷"

6

```

@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@    (UPOW)
#### IN:   Y: Y      Quantity & Uncertainty _or_ Exact Quantity
#####     X: X      Quantity & Uncertainty _or_ Exact Quantity
#### OUT:  X: Y†X    Quantity & Uncertainty (Uncertainty is 0 when X & Y are exact)
LBL "UY†X"
FUNC 21          ##### X Y
L4STK
XEQ 99 @NM@ R->C    ##### X Y
X<>Y              ##### Y X
XEQ 99 @NM@ R->C    ##### Y X
COMPLEX           ##### Y.u Y.v X
LSTO "_Yu"         ##### Y.u Y.v X
Rv                ##### Y.v X
LSTO "_Yv"         ##### Y.v X
X<>Y              ##### X Y.v
COMPLEX           ##### X.u X.v Y.v
LSTO "_Xu"         ##### X.u X.v Y.v
Rv                ##### X.v Y.v
LSTO "_Xv"         ##### X.v Y.v
Y†X               ##### (Y†X).v
RCL "_Yu"          ##### Y.u (Y†X).v
RCL× "_Xv"         ##### Y.u*X.v (Y†X).v
RCL÷ "_Yv"         ##### Y.u*X.v/Y.v (Y†X).v
RCL "_Yv"          ##### Y.v Y.u*X.v/Y.v (Y†X).v
LN                 ##### LN(Y.v) Y.u*X.v/Y.v (Y†X).v
RCL× "_Xu"         ##### X.u*LN(Y.v) Y.u*X.v/Y.v (Y†X).v
COMPLEX           ##### TMP (Y†X).v
ABS                ##### TMP (Y†X).v
RCL× ST Y          ##### TMP (Y†X).v
ABS                ##### (Y†X).u (Y†X).v
COMPLEX           ##### Y†X
RTN

```

```

##### (UINV)
#### IN:  X: X      Quantity & Uncertainty _or_ Exact Quantity
#### OUT: X: 1/X    Quantity & Uncertainty (Uncertainty is 0 when X is exact)
LBL "U1/X"
FUNC 11          ##### X
L4STK
XEQ 99 @NM@ R->C ##### X
COMPLEX          ##### X.u      X.v
ABS              ##### |X.u|    X.v
X<>Y             ##### X.v      |X.u|
1/X              ##### (1/X).v  |X.u|
X<>Y             ##### |X.u|    (1/X).v
RCL× ST Y        ##### TMP      (1/X).v
RCL× ST Y        ##### (1/X).u  (1/X).v

```

[illegible]



```

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%% (UATAN)
**** IN:  X: X           Quantity & Uncertainty _or_ Exact Quantity
**** OUT: X: ATAN(X)    Quantity & Uncertainty (Uncertainty is 0 when X is exact)

```

```

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%% (USINH)
#### IN:  X: X      Quantity & Uncertainty _or_ Exact Quantity
#### OUT: X: SINH(X) Quantity & Uncertainty (Uncertainty is 0 when X is exact)

```

```

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%% (UCOSH)
#### IN:  X: X      Quantity & Uncertainty _or_ Exact Quantity
#### OUT: X: COSH(X) Quantity & Uncertainty (Uncertainty is 0 when X is exact)

```

```

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%% (UTANH)
#### IN:  X: X           Quantity & Uncertainty _or_ Exact Quantity
#### OUT: X: TANH(X)    Quantity & Uncertainty (Uncertainty is 0 when X is exact)

```

```

##### (UASINH)
#### IN: X: X      Quantity & Uncertainty _or_ Exact Quantity
#### OUT: X: ASINH(X) Quantity & Uncertainty (Uncertainty is 0 when X is exact)

```



```

##### (UI2UV)
#### DSC: Convert interval to center+uncertanty
#### IN:  Y: Interval endpoint
####      X: Interval endpoint
#### OUT: X: Quantity & Uncertainty
#### UPD: 2021-05-07
LBL "UI-VU"
FUNC 21  #### P1      P2
L4STK
RCL ST Y  #### P2      P1      P2
RCL ST Y  #### P1      P2      P1 P2
+          #### P1+P2    P1      P2 P2
2          #### 2        P1+P2  P1 P2
÷          #### C        P1      P2 P2
RCL ST Z  #### P2      C        P1 P2
RCL ST Z  #### P1      P2      C  P1
-          #### P2-P1    C        P1 P1
ABS        #### |P2-P1|  C        P1 P1
2          #### 2        R        C  P1
÷          #### R/2      P2      C  P1
COMPLEX    #### V+iU     C        P1 P1
RTN

```

```

##### (UUV2I)
#### DSC: center+uncertanty to interval
#### IN: X: X Quantity & Uncertainty _or_ Exact Quantity
#### OUT Y: Interval left point
#### X: Interval right point
#### UPD: 2021-05-07
LBL "UVU→I"
FUNC 12 ##### X
L4STK
XEQ 99 @NM@ R->C ##### X
COMPLEX ##### X.u X.v
ABS ##### X.u X.v
RCL ST Y ##### X.v X.u X.v
RCL ST Y ##### X.u X.v X.u X.v
- ##### MIN X.u X.v X.v
RCL ST Z ##### X.v MIN X.u X.v
RCL ST Z ##### X.u X.v MIN X.u
+ ##### MAX MIN X.u X.u
RTN

```

```

##### (UV2PERC)
#### DSC: center+uncertainty to Percentage Uncertainty
#### IN:  X: X Quantity & Uncertainty _or_ Exact Quantity
#### OUT X: U%
#### UPD: 2021-05-07
LBL "UVU-%"
FUNC 11          ##### X
L4STK
XEQ 99 @NM@ R->C ##### X
COMPLEX          ##### X.u      X.v
X<>Y             ##### X.v      X.u
÷                ##### X.u/X.v
ABS              ##### |X.u/X.v|
100              ##### 100      |X.u/X.v|
x                ##### %T
RTN

```

12

6 EOF