

free42 Simple Math Functions

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1 Metadata

The home for this HTML file is: <https://richmit.github.io/hp42/sfun.html>

A PDF version of this file may be found here: <https://richmit.github.io/hp42/sfun.pdf>

Files related to this document may be found on github: <https://github.com/richmit/hp42>

Directory contents:

src	-	The org-mode file that generated this HTML document
src_42s	-	Ready to convert source listings for 42s code in this document
docs	-	This html document
bin	-	Importable RAW program files

2 Introduction

This org-mode file collects together a handful simple mathematical functions that I find useful.

3 SFUN Menu

Menu		Description
L&P:lnYX	lnYX	Base Y Logarithm of X
L&P:□□□□		
L&P:ln2	ln2	Base 2 logarithm
L&P:LN		Base 3 logarithm
L&P:LOG		Base 10 logarithm
L&P:□□□□		
L&P:Y↑X		Raise Y to the power of X
L&P:□□□□		
L&P:2↑X	LBL 58	Raise 2 to the power of X
L&P:EXP		Raise e to the power of X
L&P:10↑X		Raise 10 to the power of X
L&P:□□□□		
L&P:Y√X	YROOT	Yth roots preferring real & pure imaginary answers
L&P:□□□□		
L&P:2√X	LBL 57	Square root preferring real & pure imaginary answers
L&P:3√X	LBL 56	Cube root preferring real & pure imaginary answers
L&P:5√X	LBL 55	Fifth root preferring real & pure imaginary answers
L&P:7√X	LBL 54	Seventh root preferring real & pure imaginary answers
CPLX:RPART		Real Part of a number or matrix
CPLX:IPART		Imaginary Part of a number or matrix
CPLX:CONJ		Complex conjugate of a number or matrix
CPLX:CABS		Magnitude of a number or matrix (built in ABS fails on a complex matrix)
CPLX:CARG		Complex argument of a number or matrix
TRIG:SIN		
TRIG:COS		
TRIG:TAN		
TRIG:ASIN		
TRIG:ACOS		
TRIG:ATAN		
TRIG:CSC		1/SIN(X)
TRIG:SEC		1/COS(X)
TRIG:COT		1/TAN(X)
TRIG:ACSC		SIN(1/X)
TRIG:ASEC		COS(1/X)
TRIG:ACOT		TAN(1/X)
TRIG:TAN2		
TRIG:HYPOT		
TRIG:HAV		Haversine = 1/2-cos(X)/2
TRIG:AHAV		Inverse Haversine = 2*asin(sqrt(X))
TRIG:□□□□		
TRIG:□□□□		
HYP:SINH		
HYP:COSH		
HYP:TANH		
HYP:ASINH		
HYP:ACOSH		
HYP:ATANH		
HYP:CSCH		1/SINH(X)
HYP:SECH		1/COSH(X)
HYP:COTH		1/TANH(X)
HYP:ACSCH		SINH(1/X)

Continued on next page

Menu		Description		
HYP:ASECH		COSH(1/X)		
HYP:ACOTH		TANH(1/X)		
PERC:%T		Percentage of total	Y: TOTAL X: PART	X: % of Total
PERC:%CH		percentage of change from Y to X	Y: OLD X: New	X: % Change
PERC:%		Percentage	Y: Y X: X	Y: Y X: X% of Y
INT:FLOR	FLOOR	Truncate toward negative infinity		
INT:CEIL		Truncate toward positive infinity		
INT:ROUND	ROUND	Truncate toward nearest integer (even rule)		
INT:TRUNC	IP	Truncate toward zero		
INT:□□□□				
INT:FP				
INT:GCD		Greatest Common Denominator		
INT:LCM		Least Common Multiple		
INT:□□□□				
INT:□□□□				
INT:DIV	BASE÷			
INT:REM	MOD			
BINO:COMB				
BINO:PERM				
BINO:!	N!			
BINO:PSI	DIGAMM			
BINO:GAM	GAMMA			
BINO:BETA		Beta function		
ERR:ERF		Error Function		
ERR:ERFC		Complementary Error Function		
ERR:□□□□				
ERR:NPDF		Standard Normal Probability Density Function		
ERR:NCDF		Standard Normal Cumulative Distribution Function		
ERR:□□□□				
MISC: /		Parallel Operator	Y X	X: 1/(1/X+1/Y)

```
(MJR-generate-42-menu-code "SFUN" 0 tbl 0 1 'stay 'up 'auto #'MJR-custom-gen-lab #'MJR-custom-gen-sub)
```

**** DSC: Auto-generated menu program

LBL 01 @@@@ Page 1 of menu SFUN

```

KEY 9 GTO 00
MENU
STOP
GTO 01
LBL 02          @@@@ Page 2 of menu SFUN
CLMENU
"BINO"
KEY 1 GTO 09
"ERR"
KEY 2 GTO 10
"MISC"
KEY 3 GTO 11
KEY 7 GTO 01
KEY 8 GTO 01
KEY 9 GTO 00
MENU
STOP
GTO 02
LBL 03          @@@@ Page 1 of menu L&P
CLMENU
"lnYX"
KEY 1 XEQ "lnYX"
"ln2"
KEY 3 XEQ "ln2"
"LN"
KEY 4 XEQ 14
"LOG"
KEY 5 XEQ 15
KEY 7 GTO 13
KEY 8 GTO 12
KEY 9 GTO 01
MENU
STOP
GTO 03
LBL 12          @@@@ Page 2 of menu L&P
CLMENU
"Y↑X"
KEY 1 XEQ 16
"2↑X"
KEY 3 XEQ 58
"EXP"
KEY 4 XEQ "EXP"
"10↑X"
KEY 5 XEQ 17
KEY 7 GTO 03
KEY 8 GTO 13
KEY 9 GTO 01
MENU
STOP
GTO 12
LBL 13          @@@@ Page 3 of menu L&P
CLMENU
"Y√X"
KEY 1 XEQ "YROOT"
"2√X"
KEY 3 XEQ 57
"3√X"

```

```

KEY 4 XEQ 56
"5√X"
KEY 5 XEQ 55
"7√X"
KEY 6 XEQ 54
KEY 7 GTO 12
KEY 8 GTO 03
KEY 9 GTO 01
MENU
STOP
GTO 13
LBL 04          @@@@ Page 1 of menu CPLX
CLMENU
"RPART"
KEY 1 XEQ "RPART"
"IPART"
KEY 2 XEQ "IPART"
"CONJ"
KEY 3 XEQ "CONJ"
"CABS"
KEY 4 XEQ "CABS"
"CARG"
KEY 5 XEQ "CARG"
KEY 9 GTO 01
MENU
STOP
GTO 04
LBL 05          @@@@ Page 1 of menu TRIG
CLMENU
"SIN"
KEY 1 XEQ 20
"COS"
KEY 2 XEQ 21
"TAN"
KEY 3 XEQ 22
"ASIN"
KEY 4 XEQ 23
"ACOS"
KEY 5 XEQ 24
"ATAN"
KEY 6 XEQ 25
KEY 7 GTO 19
KEY 8 GTO 18
KEY 9 GTO 01
MENU
STOP
GTO 05
LBL 18          @@@@ Page 2 of menu TRIG
CLMENU
"CSC"
KEY 1 XEQ "CSC"
"SEC"
KEY 2 XEQ "SEC"
"COT"
KEY 3 XEQ "COT"
"ACSC"
KEY 4 XEQ "ACSC"

```

```

"ASEC"
KEY 5 XEQ "ASEC"
"ACOT"
KEY 6 XEQ "ACOT"
KEY 7 GTO 05
KEY 8 GTO 19
KEY 9 GTO 01
MENU
STOP
GTO 18
LBL 19          @@@@ Page 3 of menu TRIG
CLMENU
"TAN2"
KEY 1 XEQ "TAN2"
"HYPOT"
KEY 2 XEQ "HYPOT"
"HAV"
KEY 3 XEQ "HAV"
"AHAV"
KEY 4 XEQ "AHAV"
KEY 7 GTO 18
KEY 8 GTO 05
KEY 9 GTO 01
MENU
STOP
GTO 19
LBL 06          @@@@ Page 1 of menu HYP
CLMENU
"SINH"
KEY 1 XEQ 27
"COSH"
KEY 2 XEQ 28
"TANH"
KEY 3 XEQ 29
"ASINH"
KEY 4 XEQ 30
"ACOSH"
KEY 5 XEQ 31
"ATANH"
KEY 6 XEQ 32
KEY 7 GTO 26
KEY 8 GTO 26
KEY 9 GTO 01
MENU
STOP
GTO 06
LBL 26          @@@@ Page 2 of menu HYP
CLMENU
"CSCH"
KEY 1 XEQ "CSCH"
"SECH"
KEY 2 XEQ "SECH"
"COTH"
KEY 3 XEQ "COTH"
"ACSCH"
KEY 4 XEQ "ACSCH"
"ASECH"

```

```

KEY 5 XEQ "ASECH"
"ACOTH"
KEY 6 XEQ "ACOTH"
KEY 7 GTO 06
KEY 8 GTO 06
KEY 9 GTO 01
MENU
STOP
GTO 26
LBL 07          @@@@ Page 1 of menu PERC
CLMENU
"%T"
KEY 1 XEQ "%T"
"%CH"
KEY 2 XEQ 33
"%"
KEY 3 XEQ 34
KEY 9 GTO 01
MENU
STOP
GTO 07
LBL 08          @@@@ Page 1 of menu INT
CLMENU
"FLOR"
KEY 1 XEQ "FLOOR"
"CEIL"
KEY 2 XEQ "CEIL"
"ROND"
KEY 3 XEQ "ROUND"
"TRUN"
KEY 4 XEQ 36
"FP"
KEY 6 XEQ 37
KEY 7 GTO 35
KEY 8 GTO 35
KEY 9 GTO 01
MENU
STOP
GTO 08
LBL 35          @@@@ Page 2 of menu INT
CLMENU
"GCD"
KEY 1 XEQ "GCD"
"LCM"
KEY 2 XEQ "LCM"
"DIV"
KEY 5 XEQ 38
"REM"
KEY 6 XEQ 39
KEY 7 GTO 08
KEY 8 GTO 08
KEY 9 GTO 01
MENU
STOP
GTO 35
LBL 09          @@@@ Page 1 of menu BINO
CLMENU

```

```

"COMB"
KEY 1 XEQ 40
"PERM"
KEY 2 XEQ 41
"! "
KEY 3 XEQ 42
"PSI"
KEY 4 XEQ "DIGAMM"
"GAM"
KEY 5 XEQ 43
"BETA"
KEY 6 XEQ "BETA"
KEY 9 GTO 02
MENU
STOP
GTO 09
LBL 10          @@@@ Page 1 of menu ERR
CLMENU
"ERF"
KEY 1 XEQ "ERF"
"ERFC"
KEY 2 XEQ "ERFC"
"NPDF"
KEY 4 XEQ "NPDF"
"NCDF"
KEY 5 XEQ "NCDF"
KEY 9 GTO 02
MENU
STOP
GTO 10
LBL 11          @@@@ Page 1 of menu MISC
CLMENU
"||"
KEY 1 XEQ "||"
KEY 9 GTO 02
MENU
STOP
GTO 11
LBL 00 @@@@ Application Exit
EXITALL
RTN
LBL 14          @@@@ Action for menu key LN
LN
RTN
LBL 15          @@@@ Action for menu key LOG
LOG
RTN
LBL 16          @@@@ Action for menu key Y↑X
Y↑X
RTN
LBL 17          @@@@ Action for menu key 10↑X
10↑X
RTN
LBL 20          @@@@ Action for menu key SIN
SIN
RTN
LBL 21          @@@@ Action for menu key COS

```


COS
 RTN
 LBL 22 @@@@ Action for menu key TAN
 TAN
 RTN
 LBL 23 @@@@ Action for menu key ASIN
 ASIN
 RTN
 LBL 24 @@@@ Action for menu key ACOS
 ACOS
 RTN
 LBL 25 @@@@ Action for menu key ATAN
 ATAN
 RTN
 LBL 27 @@@@ Action for menu key SINH
 SINH
 RTN
 LBL 28 @@@@ Action for menu key COSH
 COSH
 RTN
 LBL 29 @@@@ Action for menu key TANH
 TANH
 RTN
 LBL 30 @@@@ Action for menu key ASINH
 ASINH
 RTN
 LBL 31 @@@@ Action for menu key ACOSH
 ACOSH
 RTN
 LBL 32 @@@@ Action for menu key ATANH
 ATANH
 RTN
 LBL 33 @@@@ Action for menu key %CH
 %CH
 RTN
 LBL 34 @@@@ Action for menu key %
 %
 RTN
 LBL 36 @@@@ Action for menu key TRUN
 IP
 RTN
 LBL 37 @@@@ Action for menu key FP
 FP
 RTN
 LBL 38 @@@@ Action for menu key DIV
 BASE÷
 RTN
 LBL 39 @@@@ Action for menu key REM
 MOD
 RTN
 LBL 40 @@@@ Action for menu key COMB
 COMB
 RTN
 LBL 41 @@@@ Action for menu key PERM
 PERM
 RTN
 LBL 42 @@@@ Action for menu key !

[illegible]

```

#### DSC: Complex Conjugate
#### IN:  X: Number or numeric matrix (element-wise)
#### OUT: X: conj(x)
#### TST: free42_3.0.2
#### LBL: 77-80
#### BUG: Fails on alpha string matrix
#### UPD: 2021-04-22
LBL "CONJ"

```

[illegible]

11

```

@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@
@@@@ DSC: Complex Argument
@@@@ IN:  X: Number or numeric matrix (element-wise)
@@@@ OUT: X: arg(x)
@@@@ TST: CPXRES free42_3.0
@@@@ LBL: 85-88
@@@@ BUG: Returns 0 for real 0 input
@@@@ UPD: 2021-04-22
LBL "CARG"
FUNC 11          @@@# REQ:free42>=2.5.24
L4STK           @@@# REQ:free42>=3.0
ENTER
XEQ 89          @@@@ ATYP
X=0?
RTNERR 4        @@@# REQ:free42>=2.5.24
1/X             @@@# REQ:free42<2.5.24
84
+
GTO IND ST X
LBL 85          @@@@ Real Number
0
RTN
LBL 86          @@@@ Real Matrix
R↓
DIM?
NEWMAT
RTN
LBL 87          @@@@ Complex Number
LBL 88          @@@@ Complex Matrix
R↓
XEQ 98          @@@@ C-M&A
RTN

```

```

#####
#### DSC: Complex Number -> Real Part & Imaginary Part
#### NAM: C+R&I 98
#### IN:  X: Complex Number or Complex Matrix

```


5.3 Integers

15

```

##### (FLOOR)
#### DSC: Floor -- Round toward negative infinity
#### IN:  X: real number
#### OUT: X: floor(X)
#### UPD: 2021-02-23
#### TST: free42_3.0.2

LBL "FLOOR"
FUNC 11      @### REQ:free42>=2.5.24
L4STK      @### REQ:free42>=3.0
FP
LASTX
IP
0<=? ST Y   @### TODO: Memory leak in free42 < 3.0.3
RTN
1
-
RTN

```

[illegible]

```

##### (GCD)
#### DSC: GCD
#### IN:  Y: real number
####      X: real number
#### OUT: X: GCD(|IP(X)|, |IP(X)|)
#### LBL: 66
#### UPD: 2021-04-22
#### TST: free42_3.0.2
LBL "GCD"
FUNC 21      @### REQ:free42>=2.5.24
L4STK      @### REQ:free42>=3.0
ABS
IP
X<>Y
ABS
IP

```



```

##### (LCM)
#### DSC: LCM
#### IN: Y: real number
#### X: real number
#### OUT: X: LCM(|IP(X)|, |IP(X)|)
#### USE: GCD
#### UPD: 2021-04-22
#### TST: free42_3.0.2
LBL "LCM"
FUNC 21      @### REQ:free42>=2.5.24
L4STK      @### REQ:free42>=3.0
ABS        @### |X|          Y
IP         @### IP(|X|)      Y
X=0?
RTN
X<>Y      @### Y          IP(|X|)
ABS       @### |Y|          IP(|X|)
IP        @### IP(|Y|)      IP(|X|)
X=0?
RTN
RCL ST Y   @### IP(|X|)      IP(|Y|)      IP(|X|)
RCL ST Y   @### IP(|Y|)      IP(|X|)      IP(|Y|)      IP(|X|)
*          @### IP(|Y|)*IP(|X|) IP(|Y|)      IP(|X|)
RCL ST Z   @### IP(|X|)      IP(|Y|)*IP(|X|) IP(|Y|)      IP(|X|)
RCL ST Z   @### IP(|Y|)      IP(|X|)      IP(|Y|)*IP(|X|) IP(|Y|)
XEQ "GCD"  @### GCD          IP(|Y|)*IP(|X|) IP(|Y|)      IP(|Y|)
÷          @### LCM          IP(|Y|)      IP(|Y|)      IP(|Y|)
RTN

```

5.4 Binomials, Factorials, Beta, etc...

```

#####
@@@ DSC: beta function
@@@ IN:  Y: Number
@@@ IN:  X: Number
@@@ OUT: X: beta(x, y) = beta(y, x)
@@@ TST: free42_3.0.2
@@@ UPD: 2021-02-23
LBL "BETA"
FUNC 21      @@@ REQ:free42>=2.5.24
L4STK      @@@ REQ:free42>=3.0
RCL ST Y
GAMMA
RCL ST Y
GAMMA
x
RCL ST Z

```

[illegible]

(DIGAMM)

```

@0000 DSC: digamma function
@0000 IN:  X: Number
@0000 OUT: X: psi(X)
@0000 FAQ: Good to about 1e-5 for real X>0.1
@0000 TST: free42_3.0.2
@0000 UPD: 2021-05-02

LBL "DIGAMM"
FUNC 11          @0## REQ:free42>=2.5.24
L4STK           @0## REQ:free42>=3.0
LSTO "_X"       @0000 X
2              @0000 2 X
+              @0000 2+X
LSTO "_S"       @0000 S
LN             @0000 SUM          ln(s)
2             @0000 2 S SUM
RCL× "_S"      @0000 2*S SUM
1/X           @0000 TRM SUM
-             @0000 SUM          ln(s) -1/(2*s)
RCL "_S"      @0000 S SUM
X↑2           @0000 S^2 SUM
LSTO "_SS"     @0000 SS SUM
12            @0000 12 S^2 SUM
×             @0000 12*S^2 SUM
1/X           @0000 TRM SUM
-             @0000 SUM          ln(s) -1/(2*s) -1/(12*s^2)
RCL "_SS"     @0000 S^2 SUM
RCL× "_SS"    @0000 S^4 SUM
STO ST Z      @0000 S^4 SUM S^4
120
×
1/X
+             @0000 SUM S^4          ln(s) -1/(2*s) -1/(12*s^2) +1/(120*s^4)
X<>Y
RCL× "_SS"    @0000 S^6 SUM
STO ST Z      @0000 S^6 SUM S^6
252
×
1/X
-             @0000 SUM S^6          ln(s) -1/(2*s) -1/(12*s^2) +1/(120*s^4) -1/(252*s^6)
X<>Y
RCL× "_SS"    @0000 S^8 SUM
STO ST Z      @0000 S^8 SUM S^8
240
×
1/X
+             @0000 SUM S^8          ln(s) -1/(2*s) -1/(12*s^2) +1/(120*s^4) -1/(252*s^6) +1/(240*s^8)
X<>Y
RCL× "_SS"    @0000 S^10 SUM
STO ST Z      @0000 S^10 SUM S^10
660

```



```

#####
#### DSC: Standard Normal CDF
#### IN: X: real number
#### OUT: X: Standard Normal CDF value at X
#### BUG: Only good to 7 decimal places
#### FAQ: No dependancies, variables, loops, or branches
#### REF: Zelen & Severo (1964)
#### UPD: 2021-04-22
#### TST: free42_3.0.2
#### TC: -2 0.02275013194817920720028
#### TC: -1 0.1586552539314570514148
#### TC: 0 0.5
#### TC: 1 0.8413447460685429485852
#### TC: 2 0.9772498680518207927997
LBL "NCDF"
FUNC 11      @## REQ:free42>=2.5.24
L4STK      @## REQ:free42>=3.0
0.2316419   @## b0                X          ?          ?
RCL* ST Y   @## b0*X              X          ?          ?
1           @## 1                  b0*X       X          ?
+           @## 1+b0*X            X          ?          ?
1/X         @## 1/(1+b0*X)        X          ?          ?
           @## T                  X          ?          ?
X<>Y        @## X                 T          ?          ?
X+2         @## X^2               T          ?          ?
-2          @## -2               X^2         ?          ?
÷           @## -X^2/2            T          ?          ?
E+X         @## EXP(-X^2/2)       T          ?          ?
2           @## 2                 EXP(-X^2/2) T          ?
PI          @## PI                2          EXP(-X^2/2) T
*           @## PI*2              EXP(-X^2/2) T          T
SQRT        @## SQRT(PI*2)        EXP(-X^2/2) T          T
÷           @## EXP(-X^2/2)/SQRT(PI*2) T        T          T
           @## N                 T          T          T
RCL ST Y    @## T                 N          T          T
*           @## NT                T          T          T
0.319381530 @## b1               NT         T          T
RCL* ST Y    @## PR               NT         T          T
RCL ST Z     @## T                PR         NT         T
STO* ST Z    @## T                PR         NT^2       T
R↓          @## PR               NT^2       T          T
-0.356563782 @## b2              PR         NT^2       T
RCL* ST Z    @## NT              PR         NT^2       T
+           @## PR               NT^2       T          T
RCL ST Z     @## T                PR         NT^2       T
STO* ST Z    @## T                PR         NT^3       T
R↓          @## PR               NT^3       T          T
1.781477937 @## b3              PR         NT^3       T
RCL* ST Z    @## NT              PR         NT^3       T
+           @## PR               NT^3       T          T
RCL ST Z     @## T                PR         NT^3       T
STO* ST Z    @## T                PR         NT^4       T
R↓          @## PR               NT^4       T          T
-1.821255978 @## b4              PR         NT^4       T
RCL* ST Z    @## NT              PR         NT^4       T
+           @## PR               NT^4       T          T

```

(NCDF)

RCL ST Z	0000 T	PR	NT~4	T
STO× ST Z	0000 T	PR	NT~5	T
R↓	0000 PR	NT~5	T	T
1.330274429	0000 b5	PR	NT~5	T
RCL× ST Z	0000 NT	PR	NT~5	T
+	0000 PR	NT~5	T	T
1	0000 1	PR	NT~5	T
X<>Y	0000 PR	1	NT~5	T
-	0000 1-PR	NT~5	T	T
RTN				

[illegible]

```

@@@@@ DSC: erf (error) function
@@@@@ IN:  X: real number
@@@@@ OUT: X: erf(X)
@@@@@ USE:  NCDF
@@@@@ LBL: Use: 64-65
@@@@@ UPD: 2021-03-30
@@@@@ TST: free42_3.0.2
@@@@@ TC:  -1  -0.8427007929497148693412
@@@@@ TC:   0   0.0
@@@@@ TC:   1  0.8427007929497148693412
@@@@@ TC:   2  0.9953222650189527341621
LBL "ERF"
FUNC 11                @@@# REQ:free42>=2.5.24
L4STK                  @@@# REQ:free42>=3.0
ENTER
ENTER
2
SQRT
*
ABS
XEQ "NCDF"
2
*
1
-
X<>Y
X<0?
GTO 64
GTO 65
LBL 64
R↓
+/-
RTN
LBL 65
R↓
RTN

```

(ERFC)

```

#### DSC:  erfc (complementary error) function
#### IN:   X:  real number
#### OUT:  X:  erfc(X)
#### USE:  ERF
#### UPD:  2021-03-30
#### TST:  free42_3.0.2
#### TC:   -1 1.842700792949714869341

```

```

@@@ TC:  0 1.0
@@@ TC:  1 0.1572992070502851306588
@@@ TC:  2 0.004677734981047265837931
LBL "ERFC"
FUNC 11          @### REQ:free42>=2.5.24
L4STK           @### REQ:free42>=3.0
XEQ "ERF"
1
X<>Y
-
RTN

```

5.6 Hyperbolic Trigonometric Functions

```

##### (CSCH)
@@@ DSC: 1/SINH(X)
LBL "CSCH"
FUNC 11          @### REQ:free42>=2.5.24
L4STK           @### REQ:free42>=3.0
SINH
1/X
RTN

```

```

@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@    (SECH)
@@@ DSC: 1/COSH(X)
LBL "SECH"
FUNC 11          @### REQ:free42>=2.5.24
L4STK            @### REQ:free42>=3.0
COSH
1/X
RTN
```

```

@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@      (COTH)
@@@ DSC: 1/TANH(X)
LBL "COTH"
FUNC 11          @### REQ:free42>=2.5.24
L4STK           @### REQ:free42>=3.0
TANH
1/X
RTN
```

```

@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@    (ACSCH)
@@@ DSC: SINH(1/X)
LBL "ACSCH"
FUNC 11          @### REQ:free42>=2.5.24
L4STK           @### REQ:free42>=3.0
1/X
ASINH
RTN
```

```

##### (ASECH)
@@@ DSC: COSH(1/X)
LBL "ASECH"
FUNC 11      @### REQ:free42>=2.5.24
L4STK        @### REQ:free42>=3.0
1/X
```

```

#####(ACOTH)
@@@ DSC: TANH(1/X)
LBL "ACOTH"
FUNC 11      @### REQ:free42>=2.5.24
L4STK        @### REQ:free42>=3.0
1/X
ATANH
RTN
```

```

@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@    (AHAV)
#### DSC: Inverse Haversine
#### IN: X: number
#### OUT: X: ahav(X)=2*asin(sqrt(X))
#### UPD: 2021-04-18
#### TST: free42_3.0.2
LBL "AHAV"
FUNC 11      @### REQ:free42>=2.5.24
L4STK       @### REQ:free42>=3.0
SQRT
ASIN
2
x
RTN
```

```

##### (HYPOT)
#### DSC: Hypot
#### IN:  Y: number
#### IN:  X: number
#### OUT: X: sqrt(abs(x)^2+abs(y)^2)
#### UPD: 2021-02-23
#### TST: free42_3.0.2
LBL "HYPOT"
FUNC 21      @### REQ:free42>=2.5.24
L4STK      @### REQ:free42>=3.0
ABS
X<>Y

```

```

##### (CSC)
#### DSC: 1/SIN(X)
LBL "CSC"
FUNC 11      #### REQ:free42>=2.5.24
L4STK        #### REQ:free42>=3.0
SIN
1/X
RTN

```

```

##### (SEC)
@@@ DSC: 1/CDS(X)
LBL "SEC"
FUNC 11          @### REQ:free42>=2.5.24
L4STK            @### REQ:free42>=3.0
COS
1/X
RTN

```

```

#####(COT)
@@@ DSC: 1/TAN(X)
LBL "COT"
FUNC 11      @### REQ:free42>=2.5.24
L4STK        @### REQ:free42>=3.0
TAN
1/X
RTN
```

```

@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@      (ACSC)
@@@ DSC: SIN(1/X)
LBL "ACSC"
FUNC 11          @### REQ:free42>=2.5.24
L4STK           @### REQ:free42>=3.0
1/X
ASIN
RTN
```

```

@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@      (ASEC)
@@@ DSC: COS(1/X)
LBL "ASEC"
FUNC 11           @### REQ:free42>=2.5.24
L4STK            @### REQ:free42>=3.0
1/X
ACOS
RTN
```

```

##### (ACOT)
@@@ DSC: TAN(1/X)
LBL "ACOT"
FUNC 11      @### REQ:free42>=2.5.24
L4STK        @### REQ:free42>=3.0
1/X
ATAN

```



```

##### (ATAN2)
#### DSC: ATAN2
#### IN: Y: number
#### IN: X: number
#### OUT: X: atan2(y, x)
#### BUG: Only works in RAD mode
#### UPD: 2021-02-23
#### TST: free42_3.0.2
#### TC: atan( 1, 1) => pi/4 = 45°
#### TC: atan(-1, 1) => -pi/4 = -45°
#### TC: atan( 1,-1) => 3*pi/4 = 135°
#### TC: atan(-1,-1) => -3*pi/4 = -135°
#### TC: atan( 0, 1) => 0 = 0°
#### TC: atan( 1, 0) => pi = 90°
#### TC: atan(-1, 0) => -pi = -90°
#### TC: atan( 0, 0) => ERROR
#### LBL: Used 59-63
LBL "TAN2"
FUNC 21 @### REQ:free42>=2.5.24
L4STK @### REQ:free42>=3.0
X>0?
GTO 59
X=0?
GTO 60
#### X<0
X<>Y
X<0?
GTO 61
#### X<0 & Y>=0
X<>Y
÷
ATAN
PI
+
RTN
LBL 61
#### X<0 & Y<0
X<>Y
÷
ATAN
PI
-
RTN
LBL 60
X<>Y
X=0?
GTO 62
X>0?
GTO 63
#### X=0 & Y<0
PI
-2
÷
RTN
LBL 63

```

5.8 Logs, Powers & Roots

```

@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@          (ln2)
#### DSC: Base 2 Logarithm
#### IN: X: number or matrix (element-wise)
#### OUT: X: log_2(x)
#### UPD: 2021-02-23
#### TST: free42_3.0.2
LBL "ln2"
FUNC 11      @### REQ:free42>=2.5.24
L4STK        @### REQ:free42>=3.0
LN
2
LN
÷
RTN
```

26

[illegible]

5.9 Everything Else

@@@ DSC: Parallel Operator

0000 IN: X: A Number

@@@ UPD: 2021-04-28

LBL " | | "

```
L4STK      @@## REQ:free42>=3.0
```

$$X \leftrightarrow Y$$
$$+ \quad$$

RTN

[illegible]

7 EOF