

# Social Networks & Recommendation Systems

## III. Real networks properties and their visualization.

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MSc program in Data Science has been developed  
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„NERW PW. Science - Education - Development - Cooperation”  
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# Project

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### Exercise 1.

Draw a histogram with marked sigma intervals for random variables from the normal distribution

$$f(x) = \frac{1}{\sqrt{2\pi}} \exp\left(\frac{-x^2}{2}\right).$$

### Exercise 2.

Check the Pareto rule for variables from the geometric distribution

$$p_k = (1 - p)^{k-1}p.$$

## Exercise 3.

Draw a histogram with marked sigma intervals for variables drawn from a continuous power distribution

$$f(x) = \frac{\alpha - 1}{x_{\min}} \left( \frac{x}{x_{\min}} \right)^{-\alpha}.$$

## Exercise 4.

Check the Pareto rule for variables from the zeta distribution

$$p_k = \frac{1}{\zeta(s)} k^{-s}.$$

# Why power law networks are scale free?

## Exercise 5. Empirical justification

- generate BA network and ER graphs using built-in functions.
- observe the presence of hubs.
- draw a vertex degree histogram.
- compute estimators of expectation and variance for vertex degrees.
- how are the two cases different?

## Warning!

Exercises 1-5 in total are worth 2 points for the project.

- P3.1 Read documentation of the pre-defined graph layout functions in your chosen environment. For the selected real graph, test several visualization methods. [1.5P]
- P3.2 Rewrite your code into functional form (applies to Wolfram language only). [1.5P]
- P3.3 Implement the graph visualization based on the spring method according to the specification below [3P]

## *Physical* **approach**

- In every vertex we put the same electric charge,



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- In every vertex we put the same electric charge,
- every edge we replace with a spring,

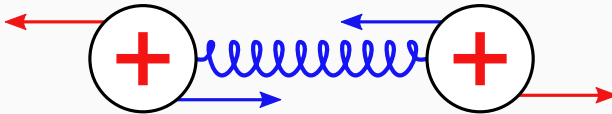
## *Physical* **approach**

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# Graph visualization methods

## *Physical* approach

- In every vertex we put the same electric charge,
- every edge we replace with a spring,
- we start with the random configuration,
- forces by minimizing electrostatic energy and potential elasticity do the work for us.



## Work plan (Mathematica/Python/R)

- Write the energy of the spring system.

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- Apply simulated annealing for finding optimal configuration.

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- Write the energy of the spring system.
- Draw the graph in *some* configuration.
- Apply simulated annealing for finding optimal configuration.
- Prepare animation.



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