

# Company Retreat

The *LRT Company* has  $n$  employees. Each employee has a unique ID number from  $1$  to  $n$ , where the director's ID is number  $1$ . Every employee in the company has *exactly one* immediate supervisor — except the director, who has no supervisor. The company's employee hierarchy forms a tree of employee IDs that's rooted at employee number  $1$  (the director).

The director decides to have a retreat lasting  $m$  days. Each day, the employees will be assigned to different groups for team building exercises. Groups are constructed in the following way:

- An employee can invite their immediate supervisor (the director has no supervisor and, thus, doesn't invite anyone). If employee  $a$  is invited by employee  $b$ , then  $a$  and  $b$  are considered to be in the same group.
- Once an employee is invited to be in a group, they are in that group. This means that if two employees have the same immediate supervisor, only one of them can invite that supervisor to be in their group.
- Every employee must be in a group, even if they are the only employee in it.

The venue where *LRT* is hosting the retreat has different pricing for each of the  $m$  days of the retreat. For each day  $j$ , there is a cost of  $d_j$  dollars per group and a per-group size limit of  $p_j$  (i.e., the maximum number of people that can be in any group on that day).

Help the director find optimal groupings for each day so the cost of the  $m$ -day retreat is minimal, then print the total cost of the retreat. As this answer can be quite large, your answer must be modulo  $10^9 + 7$ .

## Input Format

The first line contains two space-separated integers denoting the respective values of  $n$  (the number of employees) and  $m$  (the retreat's duration in days).

The next line contains  $n - 1$  space-separated integers where each integer  $i$  denotes  $s_i$  ( $1 < i \leq n$ ), which is the ID number of employee  $i$ 's direct supervisor.

Each line  $j$  of the  $m$  subsequent lines contain two space-separated integers describing the respective values of  $d_j$  (the cost per group in dollars) and  $p_j$  (the maximum number of people per group) for the  $j^{\text{th}}$  day of the retreat.

## Constraints

- $1 \leq n, m \leq 10^5$
- $1 \leq s_i \leq n$
- $1 \leq d_j, p_j \leq 10^9$

## Subtask

- $1 \leq n, m \leq 2000$  for 40% of the maximum possible score.

## Output Format

Print a single integer denoting the minimum total cost for the  $m$ -day retreat. As this number can be quite large, print your answer modulo  $10^9 + 7$ .

## Sample Input

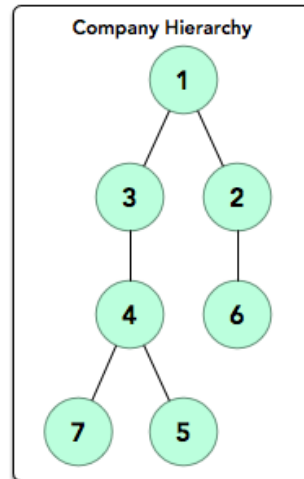
7 3  
1 1 3 4 2 4  
5 3  
6 2  
1 1

## Sample Output

46

## Explanation

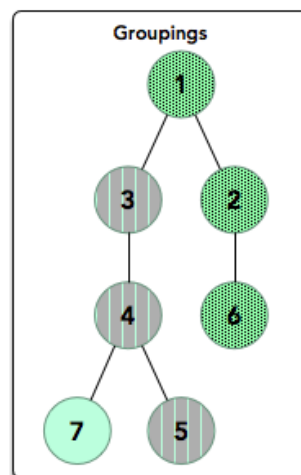
In the *Sample Case* above, the company has **7** employees and the retreat goes on for **3** days. The hierarchy looks like this:



On the first day, the cost per group is **5** dollars and each group has a maximum size of **3**. The employees split into the following three groups:

1. Employee **6** invites their manager, employee **2**. Employee **2** then invites their manager, employee **1** (the director).
2. Employee **5** invites their manager, employee **4**. Employee **4** then invites their manager, employee **3**.
3. Employee **7**'s manager is already in another group, so they are in a group by themselves.

These groupings are demonstrated in the following image where each group has a different pattern:



In other words, the final groups are **{1, 2, 6}**, **{3, 4, 5}**, and **{7}**. This means the total cost for the first day is **groups**  $\times$  **cost** = **3**  $\times$  **5** = **15** dollars.

On the second day, they split into **4** groups with a maximum size of **2** at a total cost of **24** dollars. On the third day, they split into **7** groups of size **1** at a total cost of **7** dollars. When we sum the costs for all three

days, we get  $15 + 24 + 7 = 46 \%$   $(10^9 + 7) = 46$  as our answer.