

# Kruskal (MST): Really Special Subtree

Given an undirected weighted connected graph, find the Really Special SubTree in it. The Really Special SubTree is defined as a subgraph consisting of all the nodes in the graph and:

- There is only one exclusive path from a node to every other node.
- The subgraph is of minimum overall weight (sum of all edges) among all such subgraphs.
- No cycles are formed

To create the Really Special SubTree, always pick the edge with smallest weight. Determine if including it will create a cycle. If so, ignore the edge. If there are edges of equal weight available:

- Choose the edge that minimizes the sum  $u + v + wt$  where  $u$  and  $v$  are vertices and  $wt$  is the edge weight.
- If there is still a collision, choose any of them.

Print the overall weight of the tree formed using the rules.

For example, given the following edges:

```
u v wt
1 2 2
2 3 3
3 1 5
```

First choose  $1 \rightarrow 2$  at weight  $2$ . Next choose  $2 \rightarrow 3$  at weight  $3$ . All nodes are connected without cycles for a total weight of  $3 + 2 = 5$ .

## Function Description

Complete the **kruskals** function in the editor below. It should return an integer that represents the total weight of the subtree formed.

kruskals has the following parameters:

- **g\_nodes**: an integer that represents the number of nodes in the tree
- **g\_from**: an array of integers that represent beginning edge node numbers
- **g\_to**: an array of integers that represent ending edge node numbers
- **g\_weight**: an array of integers that represent the weights of each edge

## Input Format

The first line has two space-separated integers **g\_nodes** and **g\_edges**, the number of nodes and edges in the graph.

The next **g\_edges** lines each consist of three space-separated integers **g\_from**, **g\_to** and **g\_weight**, where **g\_from** and **g\_to** denote the two nodes between which the **undirected** edge exists and **g\_weight** denotes the weight of that edge.

## Constraints

- $2 \leq g\_nodes \leq 3000$
- $1 \leq g\_edges \leq \frac{N*(N-1)}{2}$
- $1 \leq g\_from, g\_to \leq N$

- $0 \leq g\_weight \leq 10^5$

**\*\*Note: \*\*** If there are edges between the same pair of nodes with different weights, they are to be considered as is, like multiple edges.

### Output Format

Print a single integer denoting the total weight of the Really Special SubTree.

### Sample Input 0

```
4 6
1 2 5
1 3 3
4 1 6
2 4 7
3 2 4
3 4 5
```

### Sample Output 0

```
12
```

### Explanation 0

The graph given in the test case is shown above.

Applying [Kruskal's algorithm](#), all of the edges are sorted in ascending order of weight.

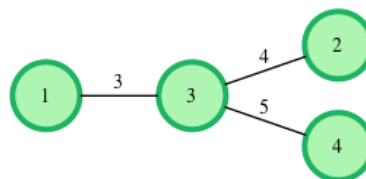
After sorting, the edge choices are available as :

$1 \rightarrow 3(w = 3)$ ,  $2 \rightarrow 3(w = 4)$ ,  $1 \rightarrow 2(w = 4)$ ,  $3 \rightarrow 4(w = 5)$ ,  $1 \rightarrow 4(w = 6)$  and  $2 \rightarrow 4(w = 7)$

Select  $1 \rightarrow 3(w = 3)$  because it has the lowest weight without creating a cycle. Select  $2 \rightarrow 3(w = 4)$  because it has the lowest weight without creating a cycle.

The edge  $1 \rightarrow 2(w = 4)$  would form a cycle, so it is ignored.

Select  $3 \rightarrow 4(w = 5)$  to finish the MST yielding a total weight of  $3 + 4 + 5 = 12$ .



### Sample Input 1

```
5 7
1 2 20
1 3 50
1 4 70
1 5 90
2 3 30
3 4 40
4 5 60
```

### Sample Output 1

```
150
```

### Explanation 1

Given the graph above, select edges  $1 \rightarrow 2, 2 \rightarrow 3, 3 \rightarrow 4, 4 \rightarrow 5$  with weights  $20 + 30 + 40 + 60 = 150$ .