

Flipping the Matrix



Sean invented a game involving a $2n \times 2n$ matrix where each cell of the matrix contains an integer. He can reverse any of its rows or columns any number of times. The goal of the game is to maximize the sum of the elements in the $n \times n$ submatrix located in the upper-left quadrant of the matrix.

Given the initial configurations for q matrices, help Sean reverse the rows and columns of each matrix in the best possible way so that the sum of the elements in the matrix's upper-left quadrant is maximal.

For example, given the matrix:

```
1 2
3 4
```

It is 2×2 so we want to maximize the top left 1×1 matrix. Reverse row 1:

```
1 2
4 3
```

And now reverse column 0:

```
4 2
1 3
```

The maximal sum is 4.

Function Description

Complete the `flippingMatrix` function in the editor below. It should return an integer that represents the maximum sum possible for the top $n \times n$ matrix.

`flippingMatrix` has the following parameters:

- *matrix*: a $2n \times 2n$ array of integers

Input Format

The first line contains an integer q , the number of queries.

The next q sets of lines are in the following format:

- The first line of each query contains an integer, n .
- Each of the next $2n$ lines contains $2n$ space-separated integers $matrix[i][j]$ in row i of the matrix.

Constraints

- $1 \leq q \leq 16$
- $1 \leq n \leq 128$
- $0 \leq matrix[i][j] \leq 4096$, where $0 \leq i, j < 2n$.

Output Format

You must print q lines of output. For each query, print the maximum possible sum of the elements in the matrix's upper-left quadrant.

Sample Input

```
1
```

```
2
112 42 83 119
56 125 56 49
15 78 101 43
62 98 114 108
```

Sample Output

```
414
```

Explanation

We start out with the following $2n \times 2n$ matrix:

$$\mathbf{matrix} = \begin{bmatrix} 112 & 42 & 83 & 119 \\ 56 & 125 & 56 & 49 \\ 15 & 78 & 101 & 43 \\ 62 & 98 & 114 & 108 \end{bmatrix}$$

We can perform the following operations to maximize the sum of the $n \times n$ submatrix in the upper-left corner:

- Reverse column 2 ($[83, 56, 101, 114] \rightarrow [114, 101, 56, 83]$), resulting in the matrix:

$$\mathbf{matrix} = \begin{bmatrix} 112 & 42 & 114 & 119 \\ 56 & 125 & 101 & 49 \\ 15 & 78 & 56 & 43 \\ 62 & 98 & 83 & 108 \end{bmatrix}$$

- Reverse row 0 ($[112, 42, 114, 119] \rightarrow [119, 114, 42, 112]$), resulting in the matrix:

$$\mathbf{matrix} = \begin{bmatrix} 119 & 114 & 42 & 112 \\ 56 & 125 & 101 & 49 \\ 15 & 78 & 56 & 43 \\ 62 & 98 & 83 & 108 \end{bmatrix}$$

When we sum the values in the $n \times n$ submatrix in the upper-left quadrant, we get $119 + 114 + 56 + 125 = 414$.