

# Subset Component



You are given an array with  $n$  64-bit integers:  $d[0], d[1], \dots, d[n-1]$ .

$\text{BIT}(x, i) = (x \gg i) \& 1$ . (where  $B(x, i)$  is the  $i^{\text{th}}$  lower bit of  $x$  in binary form.)

If we regard every bit as a vertex of a graph  $G$ , there exists one undirected edge between vertex  $i$  and vertex  $j$  if there exists at least one  $k$  such that  $\text{BIT}(d[k], i) == 1 \ \&\& \ \text{BIT}(d[k], j) == 1$ .

For every subset of the input array, how many **connected-components** are there in that graph?

The number of connected-components in a graph are the sets of nodes, which are accessible to each other, but not to/from the nodes in any other set.

For example if a graph has six nodes, labelled  $\{1, 2, 3, 4, 5, 6\}$ . And contains the edges  $(1, 2), (2, 4)$  and  $(3, 5)$ . There are three connected-components:  $\{1, 2, 4\}$ ,  $\{3, 5\}$  and  $\{6\}$ . Because  $\{1, 2, 4\}$  can be accessed from each other through one or more edges,  $\{3, 5\}$  can access each other and  $\{6\}$  is isolated from everyone else.

You only need to output the sum of the number of connected-component( $S$ ) in every graph.

## Input Format

```
n
d[0] d[1] ... d[n - 1]
```

## Constraints

$$1 \leq n \leq 20$$
$$0 \leq d[i] \leq 2^{63} - 1$$

## Output Format

Print the value of  $S$ .

## Sample Input 0

```
3
2 5 9
```

## Sample Output 0

```
504
```

## Explanation 0

There are 8 subset of  $\{2, 5, 9\}$ .

$\{\}$   
 $\Rightarrow$  We don't have any number in this subset  $\Rightarrow$  no edge in the graph  $\Rightarrow$  Every node is a component by itself  $\Rightarrow$  Number of connected-components = 64.

$\{2\}$   
 $\Rightarrow$  The Binary Representation of 2 is **00000010**. There is a bit at only one position.  $\Rightarrow$  So there is no edge in the graph, every node is a connected-component by itself  $\Rightarrow$  Number of connected-components = 64.

$\{5\}$

=> The Binary Representation of 5 is **00000101**. There is a bit at the 0<sup>th</sup> and 2<sup>nd</sup> position. => So there is an edge: (0, 2) in the graph => There is one component with a pair of nodes (0,2) in the graph. Apart from that, all remaining 62 vertices are independent components of one node each (1,3,4,5,6...63) => Number of connected-components = 63.

{9}

=> The Binary Representation of 9 is **00001001**. => There is a 1-bit at the 0<sup>th</sup> and 3<sup>rd</sup> position in this binary representation. => edge: (0, 3) in the graph => Number of components = 63

{2, 5}

=> This will contain the edge (0, 2) in the graph which will form one component

=> Other nodes are all independent components

=> Number of connected-component = 63

{2, 9}

=> This has edge (0,3) in the graph

=> Similar to examples above, this has 63 connected components

{5, 9}

=> This has edges (0, 2) and (0, 3) in the graph

=> Similar to examples above, this has 62 connected components

{2, 5, 9}

=> This has edges(0, 2) (0, 3) in the graph. All three vertices (0,2,3) make one component => Other 61 vertices are all independent components

=> Number of connected-components = 62

$$S = 64 + 64 + 63 + 63 + 63 + 63 + 62 + 62 = 504$$