# **Lena Sort**



Lena developed a sorting algorithm described by the following pseudocode:

```
lena_sort(array nums) {
  if (nums.size \leq 1) {
    return nums;
  pivot = nums[0];
  array less;
  array more;
  for (i = 1; i < nums.size; ++i) {
   // Comparison
    if (nums[i] < pivot) {
      less.append(nums[i]);
       more.append(nums[i]);
  sorted less = lena sort(less):
  sorted_more = lena_sort(more);
  ans = sorted_less + pivot + sorted_more;
  return ans;
}
```

We consider a *comparison* to be any time some nums[i] is compared with pivot.

You must solve q queries where each query i consists of some  $len_i$  and  $c_i$ . For each query, construct an array of  $len_i$  distinct elements in the inclusive range between 1 and  $10^9$  that will be sorted by  $lena\_sort$  in exactly  $c_i$  comparisons, then print each respective element of the unsorted array as a single line of  $len_i$  space-separated integers; if no such array exists, print -1 instead.

#### **Input Format**

The first line contains a single integer denoting q (the number of queries).

Each line i of the q subsequent lines contains two space-separated integers describing the respective values of  $len_i$  (the length of the array) and  $c_i$  (the number of comparisons) for query i.

### **Constraints**

- $1 \le q \le 10^5$
- $1 \leq len_i \leq 10^5$
- $0 \le c_i \le 10^9$
- ullet 1  $\leq$  the sum of  $\mathit{len}_i$  over all queries  $\leq 10^6$

#### **Output Format**

Print the answer to each query on a new line. For each query i, print  $len_i$  space-separated integers describing each respective element in an unsorted array that Lena's algorithm will sort in exactly  $c_i$  comparisons; if no such array exists, print -1 instead.

# Sample Input 0

```
2
5 6
5 100
```

# Sample Output 0

```
4 2 1 3 5
-1
```

### **Explanation 0**

We perform the following q=2 queries:

- 1. One array with len = 5 elements is [4, 2, 1, 3, 5]. The sequence of sorting operations looks like this:
  - Run lena\_sort on [4, 2, 1, 3, 5]. Compare pivot = 4 with 2, 1, 3, and 5 for a total of 4 comparisons. We're then left with less = [2, 1, 3] and more = [5]; we only need to continue sorting less, as more is sorted with respect to itself because it only contains one element.
  - Run lena\_sort on less = [2, 1, 3]. Compare pivot = 2 with 1 and 3 for a total of 2 comparisons. We're then left with less = [1] and more = [3], so we stop sorting.

We sorted [4, 2, 1, 3, 5] in 4 + 2 = 6 comparisons and c = 6, so we print  $4 \ 2 \ 1 \ 3 \ 5$  on a new line.

2. It's not possible to construct an array with len = 5 elements that  $lena\_sort$  will sort in exactly c = 100 comparisons, so we print -1 on a new line.

# Sample Input 1

```
3
10
46
32
```

# Sample Output 1

```
1
4321
213
```

## **Explanation 1**

We perform the following q = 3 queries:

- 1. We want an array with len = 1 element that  $lena\_sort$  sorts in c = 0 comparisons; any array with 1 element is already sorted (i.e.,  $lena\_sort$  performs 0 comparisons), so we choose [1] as our array and print 1 on a new line.
- 2. One array with len = 4 elements is [4, 3, 2, 1]; sorting it with  $lena\_sort$  looks like this:
  - $lena\_sort$  on [4,3,2,1]. Compare pivot=4 with 3, 2, and 1 for a total of 3 comparisons. We're then left with less=[3,2,1] and more=[]; we only need to continue sorting less, as more is empty.
  - Run lena\_sort on less = [3, 2, 1]. Compare pivot = 3 with 2 and 1 for a total of 2 comparisons. We're then left with less = [1, 2] and more = [], so we only continue sorting less.
  - Run  $lena\_sort$  on less = [2, 1]. Compare pivot = 2 with 1 for a total of 1 comparison. We then stop sorting, as less = [1] and more = [].

We sorted [4,3,2,1] in 3+2+1=6 comparisons and c=6, so we print  $4\ 3\ 2\ 1$  on a new line.

3. One array with len=3 elements is [2,1,3]. When we run  $lena\_sort$  on it, we compare pivot=2 with 1 and 3 for a total of 2 comparisons. We're then left with less=[1] and more=[3], so we stop sorting.

We sorted [2,1,3] in 2 comparisons and c=2, so we print  $2\ 1\ 3$  on a new line.