# **Minimum MST Graph**



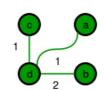
Allison loves graph theory and just started learning about Minimum Spanning Trees(MST). She has three integers, n, m, and s, and uses them to construct a graph with the following properties:

- The graph has n nodes and m undirected edges where each edge has a positive integer length.
- No edge may directly connect a node to itself, and each pair of nodes can only be directly connected by *at most* one edge.
- The graph is *connected*, meaning each node is reachable from any other node.
- The *value* of the minimum spanning tree is *s*. Value of the MST is the sum of all the lengths of all edges of which are part of the tree.
- The sum of the lengths of all edges is as small as possible.

For example, let's say n=4, m=5 and s=4. We need to construct a graph with 4 nodes and 5 edges. The value of minimum spanning tree must be 4. The diagram belows shows a way to construct such a graph while keeping the lengths of all edges is as small as possible:



Original Graph



Minimum Spanning Tree

Here the sum of lengths of all edges is 7.

Given n, m, and s for g graphs satisfying the conditions above, find and print the minimum sum of the lengths of all the edges in each graph on a new line.

**Note:** It is guaranteed that, for all given combinations of n, m, and s, we can construct a valid graph.

#### **Input Format**

The first line contains an integer, g, denoting the number of graphs.

Each of the g subsequent lines contains three space-separated integers describing the respective values of n (the number of nodes in the graph), m (the number of edges in the graph), and s (the value of the MST graph).

#### **Constraints**

For 20% of the maximum score:

• 
$$1 \le g \le 100$$

• 
$$2 \le n \le 10$$

• 
$$1 \le m \le 50$$

• 
$$1 \le s \le 20$$

For 50% of the maximum score:

• 
$$1 \le g \le 100$$

• 
$$2 \le n \le 50$$

• 
$$1 \le m \le 2000$$

• 
$$1 \le s \le 200$$

For 70% of the maximum score:

- $1 \le g \le 100$
- $2 \le n \le 10^5$
- $1 \le m \le 10^{10}$
- $1 \le s \le 10^6$

For 100% of the maximum score:

- $1 \le g \le 1000$
- $2 \le n \le 10^8$
- $1 \le m \le 10^{16}$
- $1 \le s \le 10^{10}$

# **Output Format**

For each graph, print an integer on a new line denoting the minimum sum of the lengths of all edges in a graph satisfying the given conditions.

#### **Sample Input**

2 4 5 4 4 3 6

### **Sample Output**

7 6

## **Explanation**

• Graph **1**:

The answer for this sample is already explained the problem statement.

• Graph 2:

We must construct a graph with n=4 nodes, m=3 edges, and an MST value of s=6. Recall that a connected graph with n nodes and n-1 edges is already a tree, so the MST will contain all m=3 edges and the total length of all the edges of the graph will be equal to the value of the minimum spanning tree. So the answer is 6.