# **Tree Flow**

Recall that a tree is an undirected, connected acyclic graph. We have a weighted tree, T, with n vertices; let  $dist_{u,v}$  be the total sum of edge weights on the path between nodes u and v.

Let's consider all the matrices,  $A_{u,v}$ , such that:

- $\bullet \ \ A_{u,v} = -A_{v,u}$
- $0 \leq |A_{u,v}| \leq dist_{u,v}$
- ullet  $\sum_{i=1}^n A_{u,i} = 0$  for each u 
  eq 1 and u 
  eq n

We consider the *total value* of matrix A to be:

$$\sum_{i=1}^n A_{1,i}$$

Calculate and print the maximum total value of A for a given tree, T.

#### **Input Format**

The first line contains a single positive integer, n, denoting the number of vertices in tree T. Each line i of the n-1 subsequent lines contains three space-separated positive integers denoting the respective  $a_i$ ,  $b_i$ , and  $c_i$  values defining an edge connecting nodes  $a_i$  and  $b_i$  (where  $1 \le a_i, b_i \le n$ ) with edge weight  $c_i$ .

#### **Constraints**

- $2 \le n \le 500000$
- $1 \le c_i \le 10^4$
- ullet Test cases with  $n \leq 10$  have 30% of total score
- ullet Test cases with  $n \leq 500$  have 60% of total score

#### **Output Format**

Print a single integer denoting the maximum total value of matrix A satisfying the properties specified in the *Problem Statement* above.

### **Sample Input**

3 122 131

#### **Sample Output**

3

## **Explanation**

In the sample case, matrix  $oldsymbol{A}$  is:

$$A = egin{pmatrix} 0 & 2 & 1 \ -2 & 0 & 2 \ -1 & -2 & 0 \end{pmatrix}$$

The sum of the elements of the first row is equal to  ${\bf 3}.$