

# Box Operations



Alice purchased an array of  $n$  wooden boxes that she indexed from  $0$  to  $n - 1$ . On each box  $i$ , she writes an integer that we'll refer to as  $box_i$ .

Alice wants you to perform  $q$  operations on the array of boxes. Each operation is in one of the following forms:

(Note: For each type of operations,  $l \leq i \leq r$ )

- **1 l r c**: Add  $c$  to each  $box_i$ . Note that  $c$  can be negative.
- **2 l r d**: Replace each  $box_i$  with  $\left\lfloor \frac{box_i}{d} \right\rfloor$ .
- **3 l r**: Print the minimum value of any  $box_i$ .
- **4 l r**: Print the sum of all  $box_i$ .

Recall that  $\lfloor x \rfloor$  is the maximum integer  $y$  such that  $y \leq x$  (e.g.,  $\lfloor -2.5 \rfloor = -3$  and  $\lfloor -7 \rfloor = -7$ ).

Given  $n$ , the value of each  $box_i$ , and  $q$  operations, can you perform all the operations efficiently?

## Input Format

The first line contains two space-separated integers denoting the respective values of  $n$  (the number of boxes) and  $q$  (the number of operations).

The second line contains  $n$  space-separated integers describing the respective values of  $box_0, box_1, \dots, box_{n-1}$  (i.e., the integers written on each box).

Each of the  $q$  subsequent lines describes an operation in one of the four formats defined above.

## Constraints

- $1 \leq n, q \leq 10^5$
- $-10^9 \leq box_i \leq 10^9$
- $0 \leq l \leq r \leq n - 1$
- $-10^4 \leq c \leq 10^4$
- $2 \leq d \leq 10^9$

## Output Format

For each operation of type **3** or type **4**, print the answer on a new line.

## Sample Input 0

```
10 10
-5 -4 -3 -2 -1 0 1 2 3 4
1 0 4 1
1 5 9 1
2 0 9 3
3 0 9
4 0 9
3 0 1
4 2 3
3 4 5
4 6 7
3 8 9
```

## Sample Output 0

-2  
-2  
-2  
-2  
0  
1  
1

### Explanation 0

Initially, the array of boxes looks like this:



We perform the following sequence of operations on the array of boxes:

1. The first operation is **1 0 4 1**, so we add 1 to each  $box_i$  where  $0 \leq i \leq 4$ :



2. The second operation is **1 5 9 1**, so we add  $c = 1$  to each  $box_i$  where  $5 \leq i \leq 9$ :



3. The third operation is **2 0 9 3**, so we divide each  $box_i$  where  $0 \leq i \leq 9$  by  $d = 3$  and take the floor:



4. The fourth operation is **3 0 9**, so we print the minimum value of  $box_i$  for  $0 \leq i \leq 9$ , which is the result of  $\min(-2, -1, -1, -1, 0, 0, 0, 1, 1, 1) = -2$ .

5. The fifth operation is **4 0 9**, so we print the sum of  $box_i$  for  $0 \leq i \leq 9$ , which is the result of  $-2 + -1 + -1 + -1 + 0 + 0 + 0 + 1 + 1 + 1 = -2$ .

... and so on.