

# Unique Divide And Conquer



Divide-and-Conquer on a tree is a powerful approach to solving tree problems.

Imagine a tree,  $t$ , with  $n$  vertices. Let's remove some vertex  $v$  from tree  $t$ , splitting  $t$  into zero or more connected components,  $t_1, t_2, \dots, t_k$ , with vertices  $n_1, n_2, \dots, n_k$ . We can prove that there is a vertex,  $v$ , such that the size of each formed components is *at most*  $\lfloor \frac{n}{2} \rfloor$ .

The Divide-and-Conquer approach can be described as follows:

- Initially, there is a tree,  $t$ , with  $n$  vertices.
- Find vertex  $v$  such that, if  $v$  is removed from the tree, the size of each formed component after removing  $v$  is *at most*  $\lfloor \frac{n}{2} \rfloor$ .
- Remove  $v$  from tree  $t$ .
- Perform this approach recursively for each of the connected components.

We can prove that if we find such a vertex  $v$  in linear time (e.g., using *DFS*), the entire approach works in  $O(n \cdot \log n)$ . Of course, sometimes there are several such vertices  $v$  that we can choose on some step, we can take and remove any of them. However, right now we are interested in trees such that *at each step* there is a unique vertex  $v$  that we can choose.

Given  $n$ , count the number of tree  $t$ 's such that the Divide-and-Conquer approach works determinately on them. As this number can be quite large, your answer must be modulo  $m$ .

## Input Format

A single line of two space-separated positive integers describing the respective values of  $n$  (the number of vertices in tree  $t$ ) and  $m$  (the modulo value).

## Constraints

- $1 \leq n \leq 3000$
- $n < m \leq 10^9$
- $m$  is a prime number.

## Subtasks

- $n \leq 9$  for 40% of the maximum score.
- $n \leq 500$  for 70% of the maximum score.

## Output Format

Print a single integer denoting the number of tree  $t$ 's such that vertex  $v$  is unique at each step when applying the Divide-and-Conquer approach, modulo  $m$ .

## Sample Input 0

```
1 103
```

## Sample Output 0

```
1
```

### Explanation 0

For  $n = 1$ , there is only one way to build a tree so we print the value of  $1 \bmod 103 = 1$  as our answer.

### Sample Input 1

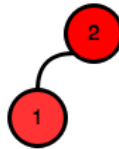
2 103

### Sample Output 1

0

### Explanation 1

For  $n = 2$ , there is only one way to build a tree:



This tree is *not valid* because we can choose to remove either node 1 or node 2 in the first step. Thus, we print 0 as no valid tree exists.

### Sample Input 2

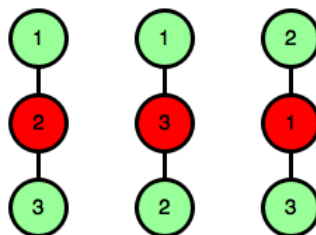
3 103

### Sample Output 2

3

### Explanation 2

For  $n = 3$ , there are 3 valid trees depicted in the diagram below (the unique vertex removed in the first step is shown in red):



Thus, we print the value of  $3 \bmod 103 = 3$  as our answer.

### Sample Input 3

4 103

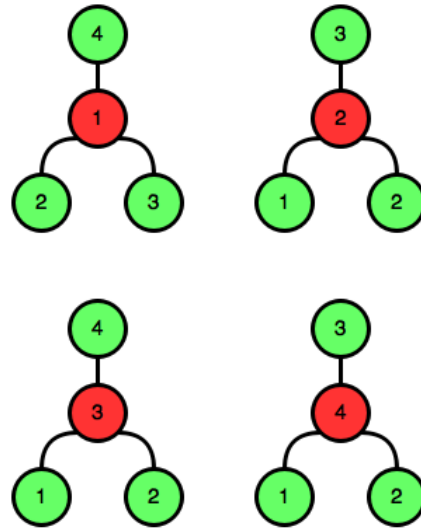
### Sample Output 3

4

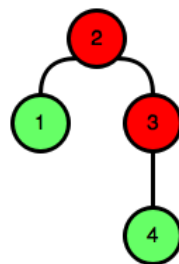
### Explanation 3

For  $n = 4$ , there are 4 valid trees depicted in the diagram below (the unique vertex removed in the first

step is shown in red):



The figure below shows an invalid tree with  $n = 4$ :



This tree is *not valid* because we can choose to remove node **2** or node **3** in the first step. Because we had four valid trees, we print the value of  $4 \bmod 103 = 4$  as our answer.