Computational Statistics II
Assignment 2: Bootstrap confidence intervals

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Aim of this assignment is to evaluate and compare the performances of the Bootsterap confidence intervals for estimating the variance on simulated data sets. You will be asked to simulate 1D samples of size $n = 10$ and $n = 100$, and to compare the obtained performances.

1. Simulate data from: Normal distribution; Uniform distribution; Cauchy distribution. Choose the parameters of Normal and Uniform distributions so that the mean is zero and the variance 1. For the Cauchy distribution, choose location $= 0$ and scale $= 1$. Explore the cases $n = 10$ and $n = 100$.

2. Compute the classical t-distribution confidence intervals and the Bootstrap intervals: asymptotic normal, Bootstrap-t, percentile, and BCa for estimating the variance. Use the unbiased variance estimator.

3. Evaluate the coverage probabilities of all confidence intervals in the cases $n = 10$ and $n = 100$, and for the three distributions. Compare the performances of the intervals. Is it what is expected from theory?

4. **Bonus.** Compute the BCA confidence intervals of previous point 4, and its coverage probability.