# **Bike rental prediction**

The aim of this work is to predict the total amount of rented bike. The predictors are:

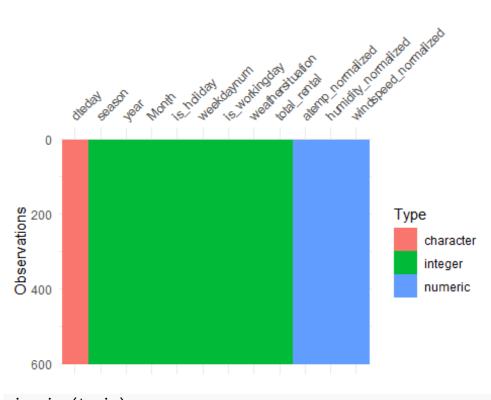
- instant: record index
- dteday : date
- season: season (1:winter, 2:spring, 3:summer, 4:fall)
- year: (0: 2011, 1:2012)
- month: month (1 to 12)
- holiday: weather day is holiday or not (extracted from [Web Link])
- weekdaynum: day of the week
- is\_workingday: if day is neither weekend nor holiday is 1, otherwise is 0.
- weathersituation:
  - o 1: Clear, Few clouds, Partly cloudy, Partly cloudy
  - o 2: Mist + Cloudy, Mist + Broken clouds, Mist + Few clouds, Mist
  - 3: Light Snow, Light Rain + Thunderstorm + Scattered clouds, Light Rain + Scattered clouds
  - o 4: Heavy Rain + Ice Pallets + Thunderstorm + Mist, Snow + Fog
- atemp\_normalized: Normalized feeling temperature in Celsius. The values are derived via (t-tmin)/(tmax-tmin), tmin=-16, t\_max=+50 (only in hourly scale)
- humidity normalized: Normalized humidity. The values are divided to 100 (max)
- windspeed\_normalized: Normalized wind speed. The values are divided to 67 (max)

```
train <- read.csv(file.choose())
rownames(train) <- train$ID
train <- train[,2:13]
train2 <- train[,2:12]</pre>
```

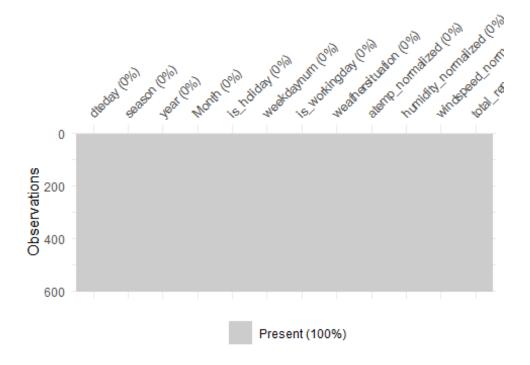
ID variables has been sected as row names and the date has been used with the only purpose to represent the outcome graphically. So, the final amount of variables used was 11.

```
str(train)
## 'data.frame': 599 obs. of 12 variables:
## $ dteday : chr "01-01-2011" "02-01-2011" "03-01-2011" "04-01-
2011" ...
## $ season : int 1 1 1 1 1 1 1 1 1 ...
```

```
$ year
##
                               00000000000...
##
   $ Month
                        : int
                               1 1 1 1 1 1 1 1 1 1 ...
   $ is_holiday
                               0000000000...
                        : int
## $ weekdaynum
                        : int
                               6012345601...
## $ is workingday
                               0011111001...
                        : int
## $ weathersituation
                        : int
                               2 2 1 1 1 1 2 2 1 1 ...
## $ atemp normalized
                               0.364 0.354 0.189 0.212 0.229 ...
                        : num
## $ humidity_normalized : num
                              0.806 0.696 0.437 0.59 0.437 ...
## $ windspeed_normalized: num
                              0.16 0.249 0.248 0.16 0.187 ...
## $ total_rental
                        : int
                              985 801 1349 1562 1600 1606 1510 959 822 1321 ...
library(visdat)
vis_dat(train)
```



vis\_miss(train)



library(skimr)

skim(train)

Data summary

Name train
Number of rows 599
Number of columns 12

Column type frequency:

character 1 numeric 11

Group variables None

## Variable type: character

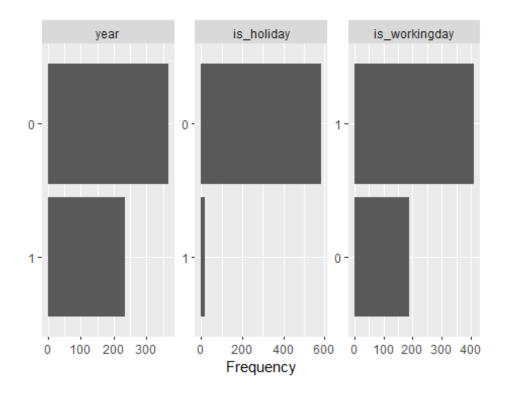
skim_variable	n_missing	complete_rate	min	max	empty	n_unique	whitespace
dteday	0	1	10	10	0	599	0

## Variable type: numeric

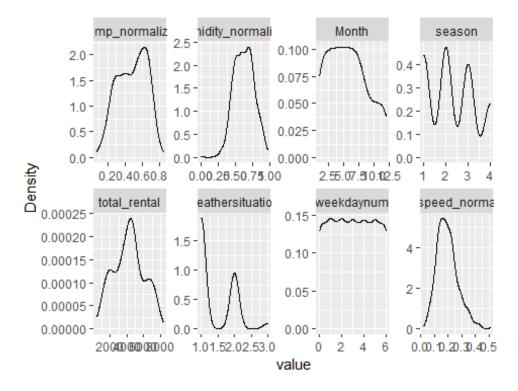
	n_missi	complet							p1	
skim_variable	ng	e_rate	mean	sd	p0	p25	p50	p75	00	hist

skim_variable	n_missi ng	complet e_rate	mean	sd	р0	p25	p50	p75	p1 00	hist
season	0	1	2.27	1.03	1.00	1.00	2.00	3.00	4.0	<b>II</b> _ <b>L</b>
year	0	1	0.39	0.49	0.00	0.00	0.00	1.00	1.0 0	<b>I</b> ■
Month	0	1	5.68	3.21	1.00	3.00	5.00	8.00	12. 00	
is_holiday	0	1	0.03	0.16	0.00	0.00	0.00	0.00	1.0 0	■
weekdaynum	0	1	2.99	2.00	0.00	1.00	3.00	5.00	6.0 0	
is_workingday	0	1	0.69	0.46	0.00	0.00	1.00	1.00	1.0 0	■
weathersituati on	0	1	1.39	0.55	1.00	1.00	1.00	2.00	3.0	<b>■</b> -■
atemp_normali zed	0	1	0.48	0.17	0.08	0.34	0.50	0.62	0.8 4	_===
humidity_nor malized	0	1	0.62	0.15	0.00	0.51	0.62	0.73	0.9 7	<b>II</b> _
windspeed_no rmalized	0	1	0.19	0.08	0.02	0.14	0.18	0.23	0.5 1	_=
total_rental	0	1	4220.6 0	1819. 67	431. 00	2904. 00	4294. 00	5353. 50	83 62. 00	<b></b> _
library(DataExplorer)										

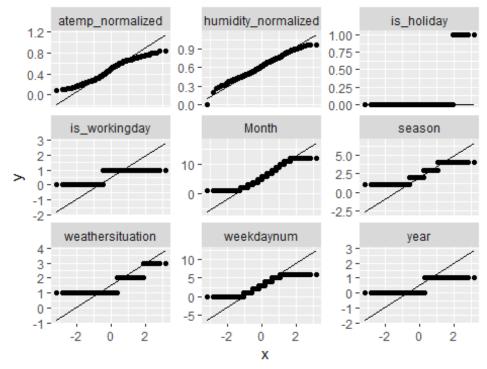
library(DataExplorer)
plot\_bar(train)



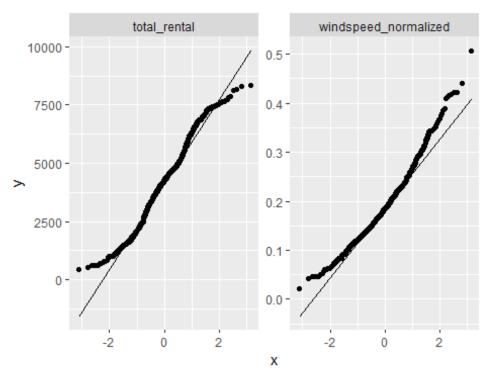
## plot\_density(train)



#### plot\_qq(train)

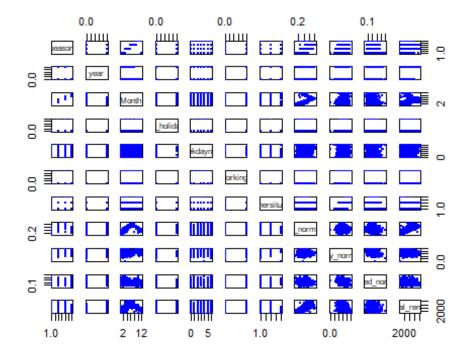


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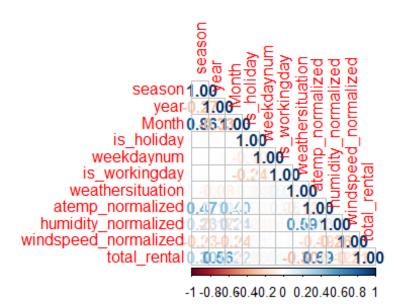


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pairs(train2, pch=20, cex=0.4, col="blue")



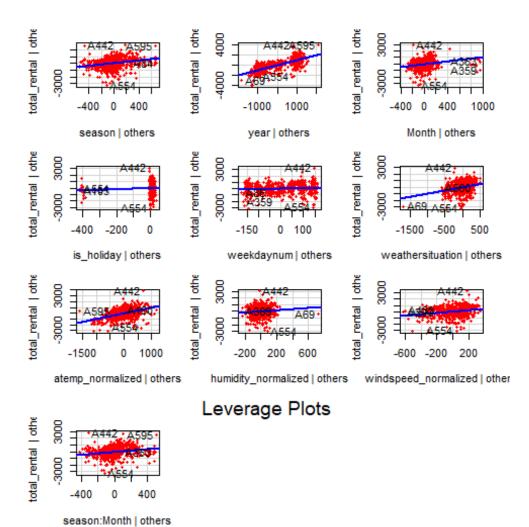
```
corrmat <- cor(train2)
library(corrplot)
corrplot(corrmat, method='number', type='lower')</pre>
```

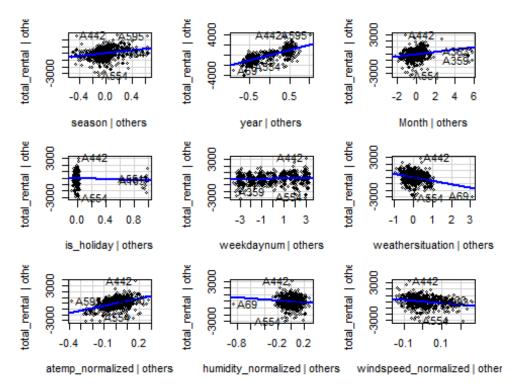


The dataset contains 5 categorical variables, 2 binary variables and four continuous variables with no missing observations. The majority of the observations is related to 2011, it wasn't a holiday but it was a working day. In addition, the majority of the observations was from january to july, with cloudy weather on spring and the most positive correlated variables was weather and humidity and month and season.

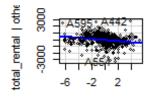
```
regression <- step(lm(total_rental~.+Month*season, data=train2), direction='both')</pre>
## Start: AIC=8006.87
## total_rental ~ season + year + Month + is_holiday + weekdaynum +
       is workingday + weathersituation + atemp normalized + humidity normalized +
##
       windspeed normalized + Month * season
##
##
##
                          Df Sum of Sq
                                             RSS
                                                    AIC
## - is workingday
                               1185120 368693883 8006.8
## <none>
                                       367508764 8006.9
## - is holiday
                               1784748 369293511 8007.8
## - humidity_normalized
                               4674773 372183537 8012.4
## - weekdaynum
                           1 5528283 373037047 8013.8
                           1 16590088 384098851 8031.3
## - windspeed normalized
## - season:Month
                           1 17226659 384735422 8032.3
## - weathersituation
                           1 31665457 399174221 8054.4
## - atemp normalized
                           1 94956923 462465686 8142.5
## - year
                           1 493402107 860910870 8514.8
##
## Step: AIC=8006.8
## total_rental ~ season + year + Month + is_holiday + weekdaynum +
       weathersituation + atemp normalized + humidity normalized +
##
##
       windspeed_normalized + season:Month
##
##
                          Df Sum of Sq
                                             RSS
                                                    AIC
## <none>
                                       368693883 8006.8
## + is workingday
                               1185120 367508764 8006.9
## - is_holiday
                           1
                               2709972 371403855 8009.2
## - humidity normalized
                           1 4813416 373507299 8012.6
## - weekdaynum
                               5557591 374251474 8013.8
## - windspeed normalized 1 16565569 385259452 8031.1
                           1 16945383 385639266 8031.7
## - season:Month
## - weathersituation
                           1 30998548 399692431 8053.2
## - atemp normalized
                           1 96737206 465431089 8144.4
## - year
                           1 492946978 861640861 8513.3
summary(regression)
##
## Call:
## lm(formula = total rental ~ season + year + Month + is holiday +
       weekdaynum + weathersituation + atemp_normalized + humidity_normalized +
##
       windspeed normalized + season:Month, data = train2)
##
##
## Residuals:
                                    3Q
        Min
                  10
                       Median
##
                                            Max
```

```
## -3123.36 -443.86
                       55.08 487.27 3106.38
##
## Coefficients:
##
                       Estimate Std. Error t value Pr(>|t|)
                                           3.689 0.000246 ***
## (Intercept)
                                    252.40
                         931.10
## season
                         1052.74
                                    158.27
                                            6.652 6.64e-11 ***
                                    73.54 28.039 < 2e-16 ***
## year
                        2061.89
## Month
                         164.80
                                     33.17
                                            4.969 8.83e-07 ***
## is holiday
                        -420.34
                                    202.19 -2.079 0.038058 *
## weekdaynum
                                     16.33
                                            2.977 0.003029 **
                          48.61
## weathersituation
                         -548.04
                                     77.94 -7.031 5.71e-12 ***
                                    340.33 12.421 < 2e-16 ***
## atemp normalized
                        4227.25
## humidity normalized
                        -843.69
                                    304.51
                                           -2.771 0.005771 **
                                    461.77 -5.140 3.75e-07 ***
## windspeed normalized -2373.48
## season:Month
                                     15.43 -5.199 2.78e-07 ***
                          -80.21
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '* 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 791.9 on 588 degrees of freedom
## Multiple R-squared: 0.8138, Adjusted R-squared: 0.8106
## F-statistic:
                 257 on 10 and 588 DF, p-value: < 2.2e-16
library(car)
leveragePlots(regression, pch=20, col='red')
```



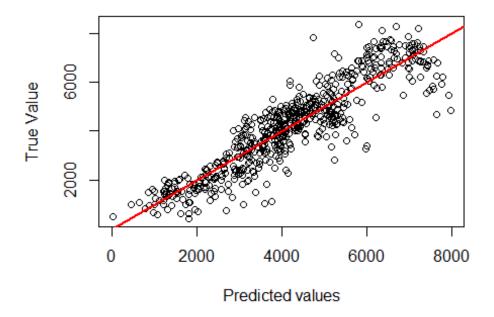


#### Added-Variable Plots

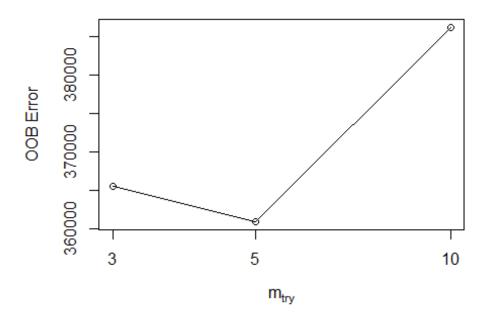


season:Month | others

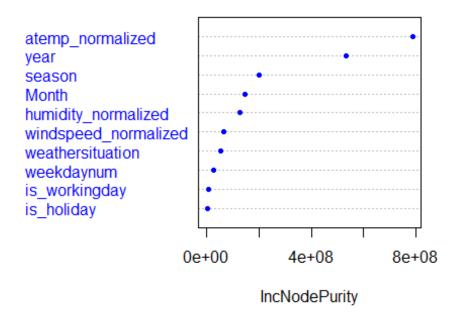
```
predictregression <- predict(regression, data=train2 ,interval = "confidence")
plot(predictregression[,1], train2$total_rental, xlab='Predicted values',
ylab='True Value')
abline(a = 0, b = 1, col = "red",lwd = 2)</pre>
```



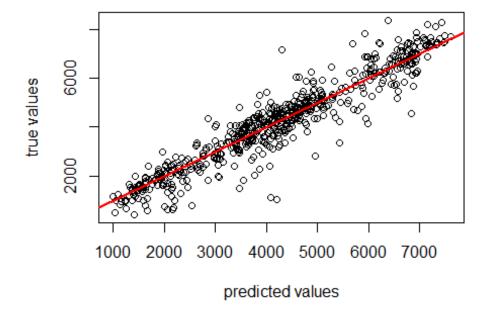
Thanks to a mixed variables selection approach I detected a multiple regression model with 10 variables and an adjusted R-squared index of 0.81. By analyzing the residual plots, I can see that A442 is a high leverage point and the predicted values are not so strictly linearly correlated with the true values, so I tryed out the random forest model.







```
predicttree <- predict(rf, data=train2)
plot(predicttree, train2$total_rental, xlab="predicted values", ylab="true
values")
abline(0, 1, col='red', lwd=2)</pre>
```



On performing the Random forest model with 500 decision tree and 10 variables, the lowest outof-bound error was with 5 variables that are temperature, year, season, month and humidity. The predicted values appears to be better correlated to the true values. However, I tried out a xboosting approach.

```
library(xgboost)
library(caret)
set.seed(1)
parts = createDataPartition(train$total_rental, p = .8, list = F)
dtrain = train[parts, ]
dval = train[-parts, ]
trainx <- data.matrix(dtrain[,2:11])</pre>
trainy <- dtrain[,12]</pre>
valx <- data.matrix(dval[,2:11])</pre>
valy <- dval[,12]</pre>
xgb train <- xgb.DMatrix(data = trainx, label = trainy)</pre>
xgb_val = xgb.DMatrix(data = valx, label = valy)
watchlist = list(train=xgb_train, test=xgb_val)
model = xgb.train(data = xgb_train, max.depth = 3, watchlist=watchlist, nrounds =
1000)
## [1]
       train-rmse:3277.441411 test-rmse:3329.171422
## [2]
       train-rmse:2369.285545
                                test-rmse:2407.019713
## [3] train-rmse:1748.973800 test-rmse:1783.337871
## [4] train-rmse:1330.722948 test-rmse:1369.903655
## [5]
       train-rmse:1050.826862 test-rmse:1093.075921
       train-rmse:860.810336
## [6]
                                test-rmse:902.889883
## [7] train-rmse:739.781082
                                test-rmse:783.383027
## [8]
       train-rmse:666.037170
                                test-rmse:713.964892
## [9] train-rmse:611.083939
                                test-rmse:668.093585
## [10] train-rmse:576.350617
                                test-rmse:644.766440
## [11] train-rmse:553.378189
                                test-rmse:627.588410
## [12] train-rmse:532.452962
                                test-rmse:615.343333
## [13] train-rmse:519.870470
                                test-rmse:602.004164
## [14] train-rmse:506.400856
                                test-rmse:603.462537
## [15] train-rmse:496.600521
                                test-rmse:610.956891
## [16] train-rmse:486.338402
                                test-rmse:607.356179
## [17] train-rmse:477.259697
                                test-rmse:601.315362
## [18] train-rmse:468.534068
                                test-rmse:603.736155
## [19] train-rmse:462.306788
                                test-rmse:602.064996
## [20] train-rmse:453.036487
                                test-rmse:608.112655
## [21] train-rmse:448.744357
                                test-rmse:607.080090
## [22] train-rmse:446.253321
                                test-rmse:609.972597
## [23] train-rmse:441.375431
                                test-rmse:611.256720
## [24] train-rmse:435.209042
                                test-rmse:604.496118
```

```
## [25] train-rmse:433.166126
                                test-rmse:603.430653
## [26] train-rmse:430.003636
                                test-rmse:606.187653
## [27] train-rmse:426.360104
                                test-rmse:606.696160
## [28] train-rmse:422.223835
                                test-rmse:603.349047
## [29] train-rmse:420.501511
                                test-rmse:602.768278
## [30] train-rmse:419.580312
                                test-rmse:603.857396
## [31] train-rmse:411.665150
                                test-rmse:603.262044
## [32] train-rmse:400.681074
                                test-rmse:596.005863
## [33] train-rmse:392.714331
                                test-rmse:600.051284
## [34] train-rmse:385.992769
                                test-rmse:598.368226
## [35] train-rmse:382.585996
                                test-rmse:598.003450
                                test-rmse:599.914533
## [36] train-rmse:380.837483
## [37] train-rmse:379.912872
                                test-rmse:599.147234
## [38] train-rmse:375.580778
                                test-rmse:596.077874
## [39] train-rmse:372.475307
                                test-rmse:595.814966
                                test-rmse:595.311334
## [40] train-rmse:370.853049
## [41] train-rmse:366.336626
                                test-rmse:594.580783
                                test-rmse:597.145588
## [42] train-rmse:359.864605
## [43] train-rmse:357.205530
                                test-rmse:602.432910
## [44] train-rmse:352.631053
                                test-rmse:603.224914
## [45] train-rmse:349.209175
                                test-rmse:602.394038
## [46] train-rmse:346.646125
                                test-rmse:602.217108
## [47] train-rmse:344.663097
                                test-rmse:608.215642
## [48] train-rmse:337.610449
                                test-rmse:613.384211
## [49] train-rmse:333.269389
                                test-rmse:613.088160
## [50] train-rmse:330.045873
                                test-rmse:612.634779
## [51] train-rmse:328.493371
                                test-rmse:613.958725
## [52] train-rmse:326.644141
                                test-rmse:612.870341
## [53] train-rmse:322.044929
                                test-rmse:617.400230
## [54] train-rmse:320.207719
                                test-rmse:613.348647
## [55] train-rmse:319.804592
                                test-rmse:612.928276
## [56] train-rmse:316.057822
                                test-rmse:610.453972
## [57] train-rmse:314.068998
                                test-rmse:610.583511
## [58] train-rmse:312.767757
                                test-rmse:611.574831
## [59] train-rmse:309.471670
                                test-rmse:609.160567
## [60] train-rmse:305.666830
                                test-rmse:613.580512
## [61] train-rmse:303.507675
                                test-rmse:615.620142
## [62] train-rmse:299.941514
                                test-rmse:615.126427
## [63] train-rmse:297.141902
                                test-rmse:615.598784
## [64] train-rmse:295.423624
                                test-rmse:616.356244
## [65] train-rmse:292.353481
                                test-rmse:619.804110
## [66] train-rmse:292.064461
                                test-rmse:620.669052
## [67] train-rmse:290.801069
                                test-rmse:621.204508
## [68] train-rmse:289.574608
                                test-rmse:620.152032
## [69] train-rmse:287.812788
                                test-rmse:619.791246
## [70] train-rmse:285.375026
                                test-rmse:618.297869
## [71] train-rmse:284.851850
                                test-rmse:618.158073
## [72] train-rmse:283.411139
                                test-rmse:616.655765
                                test-rmse:616.844095
## [73] train-rmse:283.104640
## [74] train-rmse:280.626281
                                test-rmse:620.044579
## [75] train-rmse:278.250184
                                test-rmse:620.661515
```

```
## [76] train-rmse:275.845591
                                 test-rmse:622.184865
## [77] train-rmse:273.365020
                                 test-rmse:621.695789
## [78] train-rmse:272.063584
                                 test-rmse:621.992403
## [79] train-rmse:269.092221
                                 test-rmse:622.441445
## [80] train-rmse:266.317701
                                 test-rmse:624.156772
## [81] train-rmse:264.138347
                                 test-rmse:625.415300
## [82] train-rmse:262.356470
                                 test-rmse:628.667722
## [83] train-rmse:259.965988
                                 test-rmse:629.326279
## [84] train-rmse:257.354537
                                 test-rmse:633.396880
## [85] train-rmse:254.993042
                                 test-rmse:632.047542
## [86] train-rmse:254.076600
                                 test-rmse:631.250265
## [87] train-rmse:251.398202
                                 test-rmse:630.827862
   [88] train-rmse:247.965686
                                 test-rmse:631.739351
## [89] train-rmse:245.801643
                                 test-rmse:631.932526
## [90] train-rmse:244.749305
                                 test-rmse:631.071203
## [91] train-rmse:242.716086
                                 test-rmse:631.734038
## [92] train-rmse:241.968479
                                 test-rmse:633.395039
## [93] train-rmse:240.950445
                                 test-rmse:632.954881
## [94] train-rmse:239.222632
                                 test-rmse:634.810381
## [95] train-rmse:238.616848
                                 test-rmse:635.924840
## [96] train-rmse:236.828863
                                 test-rmse:636.198689
## [97] train-rmse:235.976937
                                 test-rmse:633.612597
## [98] train-rmse:234.408008
                                 test-rmse:635.044525
## [99] train-rmse:233.605377
                                 test-rmse:634.926206
            train-rmse:232.657022
## [100]
                                     test-rmse:634.921731
            train-rmse:231.439259
## [101]
                                     test-rmse:633.823510
## [102]
            train-rmse:231.278492
                                     test-rmse:633.724209
            train-rmse:228.626026
## [103]
                                     test-rmse:632.670360
## [104]
            train-rmse:226.578848
                                     test-rmse:633.948948
## [105]
            train-rmse:224.596544
                                     test-rmse:634.099186
## [106]
            train-rmse:222.664676
                                     test-rmse:635.515277
            train-rmse:221.358992
                                     test-rmse:635.695031
## [107]
## [108]
            train-rmse:219.480178
                                     test-rmse:635.813208
## [109]
            train-rmse:217.686429
                                     test-rmse:636.455777
## [110]
            train-rmse:217.155540
                                     test-rmse:635.975725
## [111]
            train-rmse:215.697360
                                     test-rmse:637.418479
                                     test-rmse:637.540479
## [112]
            train-rmse:213.870466
## [113]
            train-rmse:212.086803
                                     test-rmse:635.032821
## [114]
            train-rmse:211.340698
                                     test-rmse:634.331322
## [115]
            train-rmse:209.484430
                                     test-rmse:634.522993
## [116]
            train-rmse:208.521738
                                     test-rmse:634.337899
## [117]
            train-rmse:207.763861
                                     test-rmse:634.955768
            train-rmse:206.157710
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## [126]
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            train-rmse:193.778854
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            train-rmse:179.536565
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            train-rmse:114.853925
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## [227]
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            train-rmse:99.726920
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## [239]
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## [381]
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##
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##
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                                     test-rmse:672.197536
##
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##
   [607]
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                                     test-rmse:672.179487
            train-rmse:13.925737
                                     test-rmse:672.182243
##
  [608]
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##
  [609]
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##
  [610]
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            train-rmse:13.757152
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                                     test-rmse:672.385443
## [613]
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##
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##
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##
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            train-rmse:13.442473
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##
  [617]
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##
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##
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##
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##
  [626]
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## [627]
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## [628]
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## [629]
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                                     test-rmse:672.345846
##
   [630]
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## [631]
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## [632]
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                                     test-rmse:672.300258
            train-rmse:12.449863
## [633]
## [634]
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## [635]
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                                     test-rmse:672.274878
## [636]
            train-rmse:12.246738
                                     test-rmse:672.248252
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##
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##
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  [643]
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##
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##
   [645]
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##
  [646]
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##
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##
##
   [649]
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##
  [650]
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##
  [651]
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## [654]
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## [655]
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            train-rmse:11.165284
##
   [656]
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            train-rmse:11.096900
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##
  [657]
##
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## [659]
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##
            train-rmse:10.933764
##
   [663]
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##
  [664]
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  [666]
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##
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  [668]
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##
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##
  [673]
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##
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   [675]
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   [676]
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            train-rmse:10.203380
##
  [677]
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  [678]
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## [679]
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##
  [680]
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##
   [681]
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## [683]
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            train-rmse:9.785238 test-rmse:672.584942
##
  [685]
## [686]
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## [687]
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## [690]
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            train-rmse:9.462350 test-rmse:672.591255
## [692]
## [693]
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            train-rmse:9.414754 test-rmse:672.680687
## [694]
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## [695]
## [696]
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            train-rmse:9.300704 test-rmse:672.705344
## [697]
## [698]
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## [699]
            train-rmse:9.275716 test-rmse:672.739874
## [700]
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            train-rmse:9.227287 test-rmse:672.710286
## [701]
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## [702]
            train-rmse:9.153424 test-rmse:672.729607
## [703]
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## [704]
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            train-rmse:8.925517 test-rmse:672.768227
## [706]
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## [722]
## [723]
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## [724]
            train-rmse:8.230235 test-rmse:672.957477
## [725]
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            train-rmse:8.113691 test-rmse:672.986649
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## [727]
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## [731]
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## [732]
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## [733]
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## [734]
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            train-rmse:7.811718 test-rmse:673.001303
## [735]
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## [736]
## [737]
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## [738]
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```

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## [739]
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## [740]
## [741]
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            train-rmse:7.492391 test-rmse:673.049394
## [743]
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## [748]
## [749]
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## [750]
            train-rmse:7.248224 test-rmse:673.111431
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## [753]
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## [756]
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## [757]
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## [759]
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## [760]
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## [762]
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## [766]
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## [780]
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            train-rmse:6.172430 test-rmse:673.361567
## [782]
## [783]
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## [785]
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            train-rmse:6.037229 test-rmse:673.329079
## [786]
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## [787]
## [788]
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## [789]
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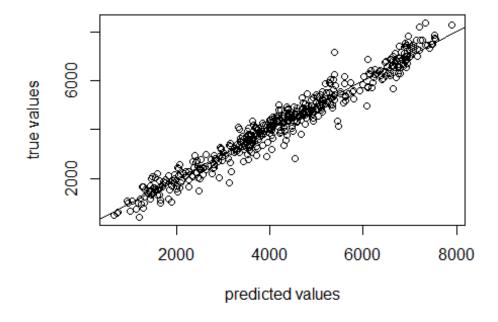
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## [872]
            train-rmse:4.212573 test-rmse:673.502766
            train-rmse:4.205596 test-rmse:673.500472
## [873]
## [874]
            train-rmse:4.175368 test-rmse:673.514043
            train-rmse:4.165328 test-rmse:673.511739
## [875]
##
   [876]
            train-rmse:4.153903 test-rmse:673.510447
## [877]
            train-rmse:4.125617 test-rmse:673.518617
## [878]
            train-rmse:4.088582 test-rmse:673.540591
            train-rmse:4.063151 test-rmse:673.547616
## [879]
            train-rmse:4.047231 test-rmse:673.550139
## [880]
## [881]
            train-rmse:4.029090 test-rmse:673.541855
            train-rmse:4.006012 test-rmse:673.528869
## [882]
## [883]
            train-rmse:3.982091 test-rmse:673.531203
            train-rmse:3.976464 test-rmse:673.525710
## [884]
##
   [885]
            train-rmse:3.953822 test-rmse:673.525033
## [886]
            train-rmse:3.932309 test-rmse:673.526847
## [887]
            train-rmse:3.923949 test-rmse:673.539865
            train-rmse:3.904368 test-rmse:673.566171
## [888]
            train-rmse:3.872079 test-rmse:673.584463
## [889]
## [890]
            train-rmse:3.856161 test-rmse:673.596205
## [891]
            train-rmse:3.850818 test-rmse:673.596121
```

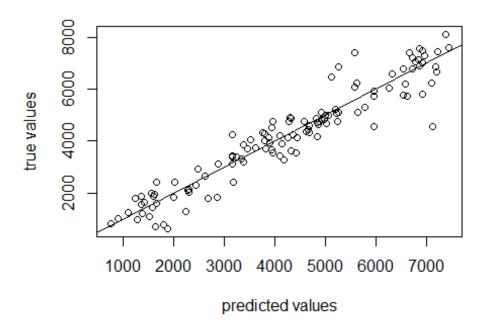
```
train-rmse:3.829542 test-rmse:673.599377
## [892]
            train-rmse:3.810080 test-rmse:673.594033
## [893]
## [894]
            train-rmse:3.784026 test-rmse:673.606097
   [895]
            train-rmse:3.771924 test-rmse:673.628931
##
            train-rmse:3.746627 test-rmse:673.621494
## [896]
## [897]
            train-rmse:3.732937 test-rmse:673.615549
            train-rmse:3.709978 test-rmse:673.615305
## [898]
            train-rmse:3.689879 test-rmse:673.616993
## [899]
## [900]
            train-rmse:3.679645 test-rmse:673.615553
            train-rmse:3.677916 test-rmse:673.613724
## [901]
## [902]
            train-rmse:3.653544 test-rmse:673.615627
## [903]
            train-rmse:3.632363 test-rmse:673.616022
## [904]
            train-rmse:3.614908 test-rmse:673.630389
            train-rmse:3.605096 test-rmse:673.641403
## [905]
            train-rmse:3.586652 test-rmse:673.636383
## [906]
## [907]
            train-rmse:3.556934 test-rmse:673.619227
            train-rmse:3.535249 test-rmse:673.629800
## [908]
## [909]
            train-rmse:3.529607 test-rmse:673.641896
            train-rmse:3.525721 test-rmse:673.634779
## [910]
## [911]
            train-rmse:3.500690 test-rmse:673.626033
## [912]
            train-rmse:3.470426 test-rmse:673.618377
## [913]
            train-rmse:3.465600 test-rmse:673.623692
## [914]
            train-rmse:3.454401 test-rmse:673.626470
            train-rmse:3.438968 test-rmse:673.615464
## [915]
            train-rmse:3.420844 test-rmse:673.609810
## [916]
## [917]
            train-rmse:3.396350 test-rmse:673.636507
## [918]
            train-rmse:3.374398 test-rmse:673.645021
## [919]
            train-rmse:3.355075 test-rmse:673.646690
## [920]
            train-rmse:3.344875 test-rmse:673.646489
            train-rmse:3.336728 test-rmse:673.657234
## [921]
            train-rmse:3.317130 test-rmse:673.651271
## [922]
## [923]
            train-rmse:3.287614 test-rmse:673.650353
## [924]
            train-rmse:3.272855 test-rmse:673.620155
## [925]
            train-rmse:3.270836 test-rmse:673.622121
            train-rmse:3.253255 test-rmse:673.640492
## [926]
## [927]
            train-rmse:3.251272 test-rmse:673.636794
## [928]
            train-rmse:3.249804 test-rmse:673.638233
## [929]
            train-rmse:3.242239 test-rmse:673.632571
            train-rmse:3.224187 test-rmse:673.637018
## [930]
            train-rmse:3.209885 test-rmse:673.638887
## [931]
## [932]
            train-rmse:3.173524 test-rmse:673.674633
## [933]
            train-rmse:3.157430 test-rmse:673.701304
## [934]
            train-rmse:3.119644 test-rmse:673.702118
            train-rmse:3.101102 test-rmse:673.721174
## [935]
## [936]
            train-rmse:3.089493 test-rmse:673.737808
## [937]
            train-rmse:3.061996 test-rmse:673.746312
## [938]
            train-rmse:3.054586 test-rmse:673.749230
            train-rmse:3.036004 test-rmse:673.738880
## [939]
            train-rmse:3.017714 test-rmse:673.753111
## [940]
## [941]
            train-rmse:3.003461 test-rmse:673.757747
## [942]
            train-rmse:2.992651 test-rmse:673.774215
```

```
train-rmse:2.982112 test-rmse:673.768770
## [943]
            train-rmse:2.968516 test-rmse:673.774495
## [944]
            train-rmse:2.961010 test-rmse:673.784546
## [945]
## [946]
            train-rmse:2.946615 test-rmse:673.795135
            train-rmse:2.931095 test-rmse:673.793938
## [947]
## [948]
            train-rmse:2.921222 test-rmse:673.822788
            train-rmse:2.915758 test-rmse:673.818642
## [949]
## [950]
            train-rmse:2.897244 test-rmse:673.823774
## [951]
            train-rmse:2.887563 test-rmse:673.815421
            train-rmse:2.872548 test-rmse:673.809098
## [952]
## [953]
            train-rmse:2.855244 test-rmse:673.812587
## [954]
            train-rmse:2.825535 test-rmse:673.812593
## [955]
            train-rmse:2.805207 test-rmse:673.811016
            train-rmse:2.789086 test-rmse:673.845056
## [956]
            train-rmse:2.775518 test-rmse:673.847146
## [957]
            train-rmse:2.762399 test-rmse:673.848803
## [958]
            train-rmse:2.744209 test-rmse:673.843728
## [959]
## [960]
            train-rmse:2.733713 test-rmse:673.846038
            train-rmse:2.711741 test-rmse:673.844228
## [961]
## [962]
            train-rmse:2.701286 test-rmse:673.844108
## [963]
            train-rmse:2.692216 test-rmse:673.844357
## [964]
            train-rmse:2.682219 test-rmse:673.845211
            train-rmse:2.673336 test-rmse:673.859889
## [965]
            train-rmse:2.655346 test-rmse:673.856586
## [966]
            train-rmse:2.642512 test-rmse:673.854996
## [967]
## [968]
            train-rmse:2.620716 test-rmse:673.869005
## [969]
            train-rmse:2.617786 test-rmse:673.871376
## [970]
            train-rmse: 2.616171 test-rmse: 673.866794
## [971]
            train-rmse:2.596478 test-rmse:673.875766
            train-rmse:2.584962 test-rmse:673.880339
## [972]
            train-rmse:2.574630 test-rmse:673.888960
## [973]
## [974]
            train-rmse:2.567684 test-rmse:673.889667
## [975]
            train-rmse:2.566325 test-rmse:673.890107
## [976]
            train-rmse:2.556200 test-rmse:673.892981
            train-rmse:2.535480 test-rmse:673.916273
## [977]
## [978]
            train-rmse:2.525640 test-rmse:673.917590
## [979]
            train-rmse:2.518694 test-rmse:673.929335
## [980]
            train-rmse:2.506003 test-rmse:673.936370
            train-rmse:2.496922 test-rmse:673.939695
## [981]
            train-rmse:2.479899 test-rmse:673.949020
## [982]
## [983]
            train-rmse:2.472667 test-rmse:673.938812
## [984]
            train-rmse:2.465353 test-rmse:673.934797
## [985]
            train-rmse:2.453830 test-rmse:673.946359
## [986]
            train-rmse:2.445554 test-rmse:673.947327
## [987]
            train-rmse:2.441706 test-rmse:673.944572
            train-rmse:2.438891 test-rmse:673.950740
## [988]
## [989]
            train-rmse:2.428770 test-rmse:673.951231
            train-rmse:2.410818 test-rmse:673.950054
## [990]
            train-rmse:2.394088 test-rmse:673.953171
## [991]
## [992]
            train-rmse:2.379902 test-rmse:673.960288
## [993]
            train-rmse:2.364100 test-rmse:673.961768
```

```
## [994]
            train-rmse:2.353947 test-rmse:673.964916
## [995]
            train-rmse:2.338375 test-rmse:673.971266
## [996]
            train-rmse:2.332695 test-rmse:673.966899
## [997]
            train-rmse:2.323624 test-rmse:673.969360
            train-rmse:2.316842 test-rmse:673.971371
## [998]
## [999]
            train-rmse:2.303906 test-rmse:673.962400
            train-rmse:2.287694 test-rmse:673.963848
## [1000]
final = xgboost(data = xgb_train, max.depth = 3, nrounds = 41, verbose = 0)
predictboosttrain <- predict(final, newdata=trainx)</pre>
predictboostval <- predict(final, newdata=valx)</pre>
plot(predictboosttrain, trainy, xlab="predicted values", ylab="true values")
abline(0,1)
```



plot(predictboostval, valy, xlab="predicted values", ylab="true values")
abline(0,1)



The iteration that leads to the lowest values of rmse was 41 and the predicted values appears well correlated to the true values in both train and validation set.

```
test <- read.csv(file.choose())
rownames(test) <- test$ID

test <- test[,2:12]
test2 <- test[2:11]
testx <- data.matrix(test2[,1:10])
test$total_rental <- predict(final, newdata=testx)

library(ggplot2)
train$dteday <- as.Date(train$dteday, format = "%d-%m-%y")
trainrental <- ggplot(train, aes(x=dteday, y=total_rental)) +geom_line()
test$dteday <- as.Date(test$dteday, format = "%d-%m-%y")
testrental <- ggplot(test, aes(x=dteday, y=total_rental)) +geom_line()
library(gridExtra)
grid.arrange(trainrental, testrental)</pre>
```

