UNIVERSITY OF EDINBURGH COLLEGE OF SCIENCE AND ENGINEERING SCHOOL OF INFORMATICS

INFR08013 INFORMATICS 1 - FUNCTIONAL PROGRAMMING

Friday $20\frac{\text{th}}{}$ December 2013

14:30 to 16:30

INSTRUCTIONS TO CANDIDATES

- 1. Note that ALL QUESTIONS ARE COMPULSORY.
- 2. DIFFERENT QUESTIONS MAY HAVE DIFFERENT NUMBERS OF TOTAL MARKS. Take note of this in allocating time to questions.
- 3. This is an OPEN BOOK examination: notes and printed material are allowed, but no electronic devices or electronic media.

Convener: J. Bradfield External Examiner: C. Johnson

THIS EXAMINATION WILL BE MARKED ANONYMOUSLY

1. (a) Write a function f:: String -> Int that converts a list of base-4 digits to the corresponding numerical value. For example:

```
f "203" = (2 * 4^2) + (0 * 4^1) + (3 * 4^0) = 35
f "13" = 7
f "1302" = 114
f "130321" = 1849
```

Use basic functions, list comprehension, and library functions, but not recursion. You may assume that the input is a string of base-4 digits. Credit may be given for indicating how you have tested your function.

[Hint: Start by reversing the order of the digits in the list.]

[12 marks]

(b) Write a second function g:: String -> Int that behaves like f, this time using basic functions, library functions and recursion, but not list comprehension. Credit may be given for indicating how you have tested your function.

[Hint: Start by reversing the order of the digits in the list.]

[12 marks]

2. (a) Write a function p:: [Int] -> Bool that, given a non-empty list of numbers, returns True if each positive number in the list is greater than or equal to twice the first number in the list. For example:

```
p [2,6,-3,18,-7,10] = True
p [13] = True
p [-3,6,1,-6,9,18] = True
p [5,-2,-6,7] = False
```

The function should give an error if applied to an empty list.

Use basic functions, list comprehension, and library functions, but not recursion. Credit may be given for indicating how you have tested your function.

[16 marks]

(b) Write a second function q:: [Int] -> Bool that behaves like p, this time using basic functions and recursion, but not list comprehension or library functions. Credit may be given for indicating how you have tested your function.

[16 marks]

(c) Write a third function r :: [Int] -> Bool that also behaves like p, this time using the following higher-order library functions:

```
map :: (a -> b) -> [a] -> [b]
filter :: (a -> Bool) -> [a] -> [a]
foldr :: (a -> b -> b) -> b -> [a] -> b
```

Do not use recursion or list comprehension. Credit may be given for indicating how you have tested your function.

[12 marks]

3. The following data type represents arithmetic expressions over a single variable:

The template file includes code that enables QuickCheck to generate arbitary values of type Expr, to aid testing.

Note: In this question, you will need to convert integers to and from strings: show 234 = "234" and read "234" :: Int = 234.

(a) Polish Prefix Notation (PPN) is a parenthesis-free way of writing arithmetic expressions. Operators precede all of their operands, like so:

```
X*3 in PPN is *X3

-(X*3) in PPN is -*X3

(5+-X)*17 in PPN is *+5-X17

(15+-(7*(X+1)))*3 in PPN is *+15-*7+X13
```

Write a function ppn :: Expr -> [String] which converts an expression to its equivalent in PPN. We will represent PPN expressions as lists of strings. For instance, for the third example above:

```
ppn ((Const 5 :+: Neg X) :*: Const 17)
     should produce
["*", "+", "5", "-", "X", "17"]
```

Credit may be given for indicating how you have tested your function.

[16 marks]

- (b) The algorithm for evaluating an PPN expression uses a list for storing intermediate results. Starting with an empty list, and given a value for the variable X, we scan the expression from right to left until it is exhausted:
 - If the next item is the variable X, add its value to the front of the list.
 - If the next item is a constant, add it to the front of the list.
 - If the next item is an operator with n arguments, then remove the first n items from the front of the list, apply the corresponding operation to them, and add the result to the front of the list. If there were fewer than n items on the list, then the original expression was ill-formed.
 - If the next item is something else, then the original expression was ill-formed.

At this point, there should be one item on the list, and that is the result; otherwise the original expression was ill-formed.

Implement this as a function evalppn :: [String] -> Int -> Int, where the first argument is the PPN expression and the second argument is the value of X. For example:

```
evalppn ["*", "X", "3"] 10 = 30
evalppn ["-", "*", "X", "3"] 20 = -60
evalppn ["*", "+", "5", "-", "X", "17"] 10 = -85
evalppn ["*", "+", "15", "-", "*", "7", "+", "X", "1", "3"] 2
= -18
```

evalppn ["+", "-", "*", "X", "3"] 20 should produce an error, because there are not enough items on the list of intermediate values to perform the final addition.

Credit may be given for indicating how you have tested your function. The template file includes a function $evalExpr :: Expr \rightarrow Int \rightarrow Int$ to evaluate expressions, where evalExpr e n produces the value of e when the variable X has value evaluation of an expression using <math>evalExpr should produce the same result as evaluation of its PPN version using evalppn.

[16 marks]