

Introduction to statistics

(Day 1)

Agenda

- **Where:**
 - Mar 4: AULA GALILEO - MBC
 - Mar 5: AULA DARWIN - MBC
 - Mar 6 : Online

- **When:**
 - 14-17
 - 1 coffee break

- **Who:**
 - Paola Dalmasso
paola.dalmasso@unito.it
 - Alessia Visconti
alessia.visconti@unito.it

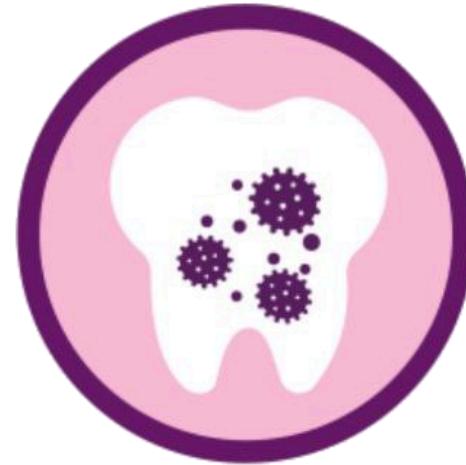
- **How (to pass):**
 - Attend at least 2 lessons

Introduction



Why are we here?

Will you buy this mouthwash?



Elimina fino al
99% dei batteri
residui dopo il
lavaggio

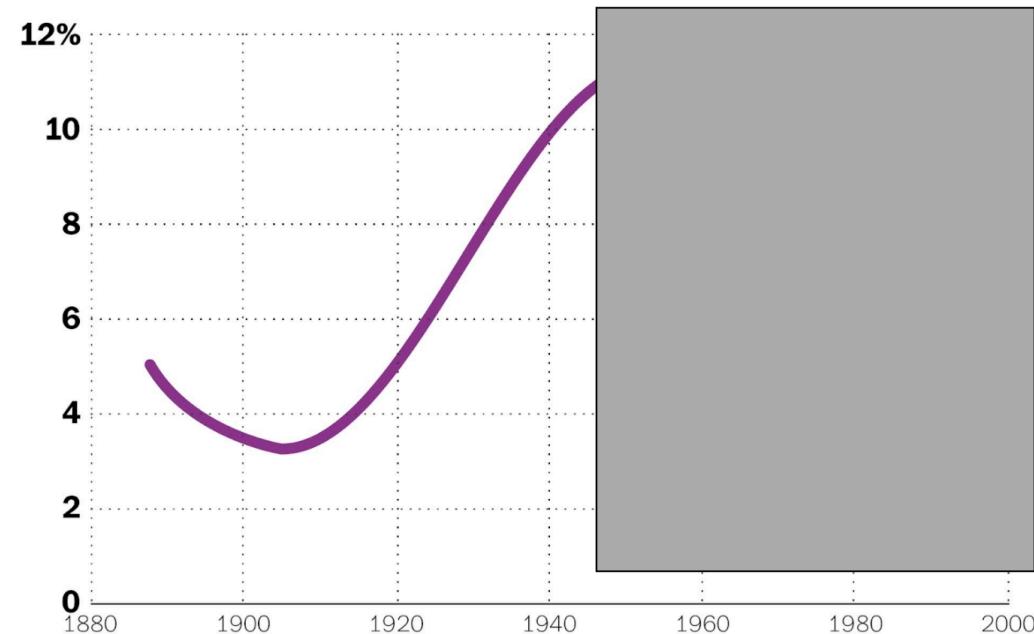


Raggiunge fino al
100% della bocca

What happens after WWII?

The history of left-handedness

Rate of left-handedness among Americans, by year of birth



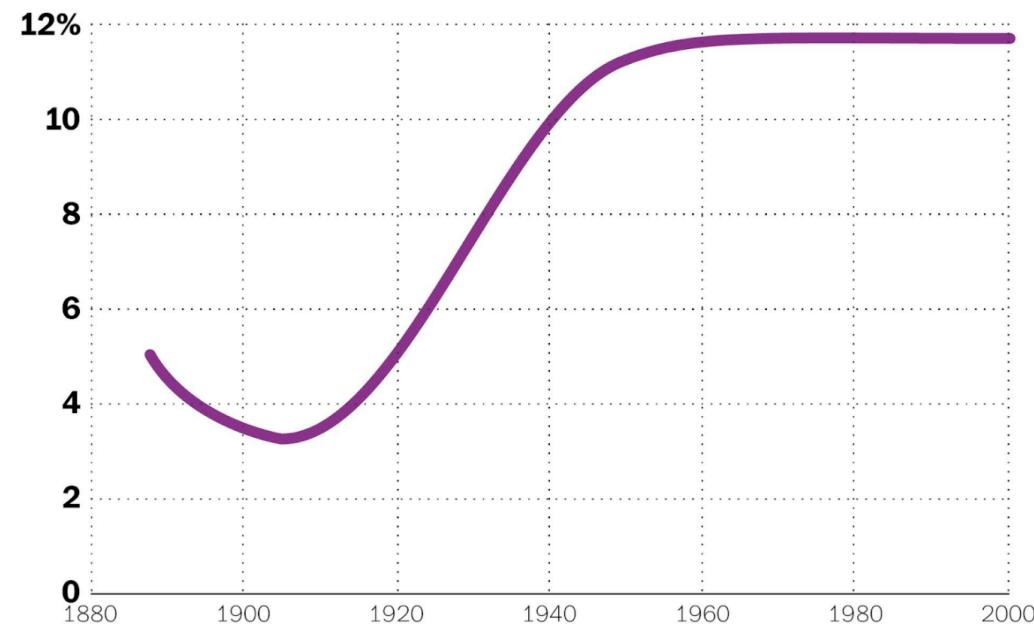
WAPO.ST/WONKBLOG

Source: Survey data reported in "The History and Geography of Human Handedness" (2009)

What happens after WWII?

The history of left-handedness

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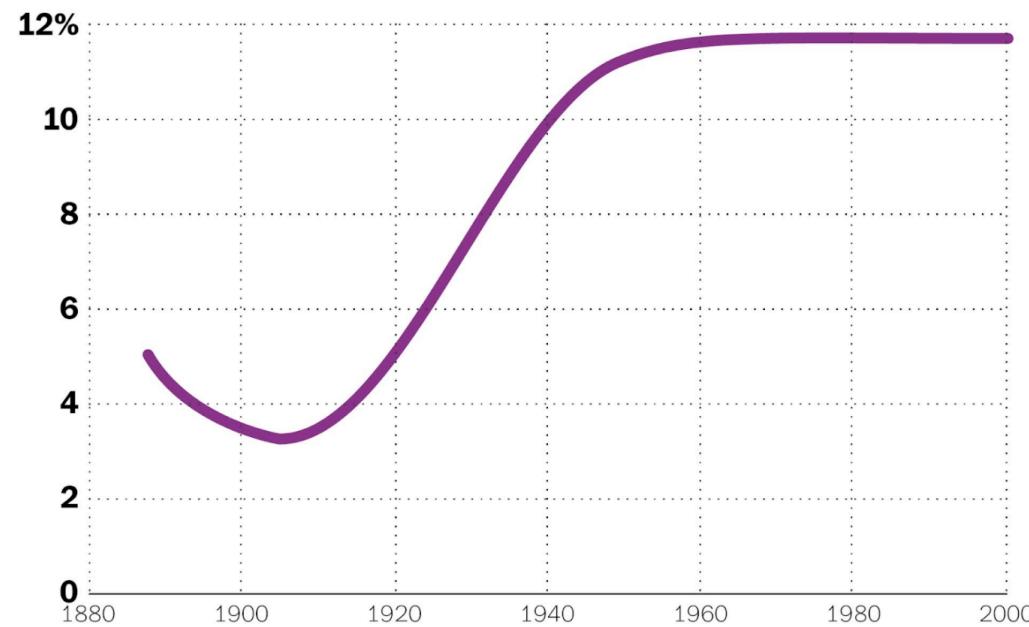
WAPO.ST/WONKBLOG

Source: Survey data reported in "The History and Geography of Human Handedness" (2009)

Civic education, about 1935

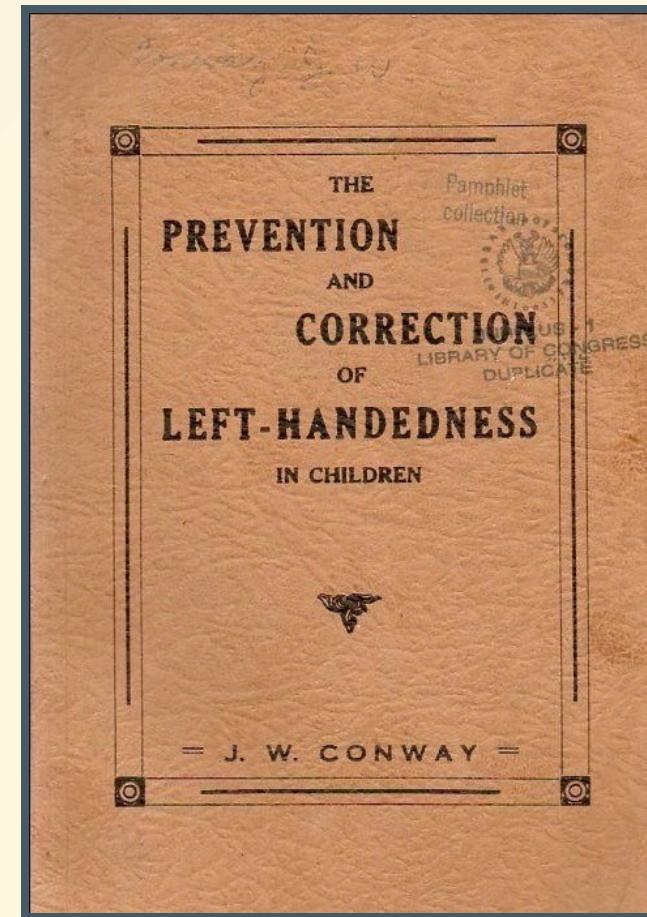
The history of left-handedness

Rate of left-handedness among Americans, by year of birth



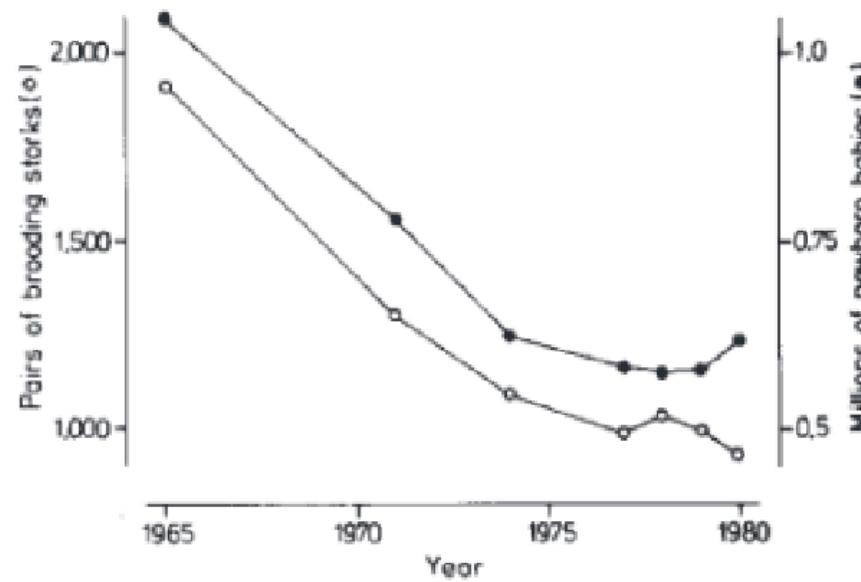
WAPO.ST/WONKBLOG

Source: Survey data reported in "The History and Geography of Human Handedness" (2009)



Storks and babies

SIR—There is concern in West Germany over the falling birth rate. The accompanying graph^{1,2} might suggest a solution that every child knows makes sense.

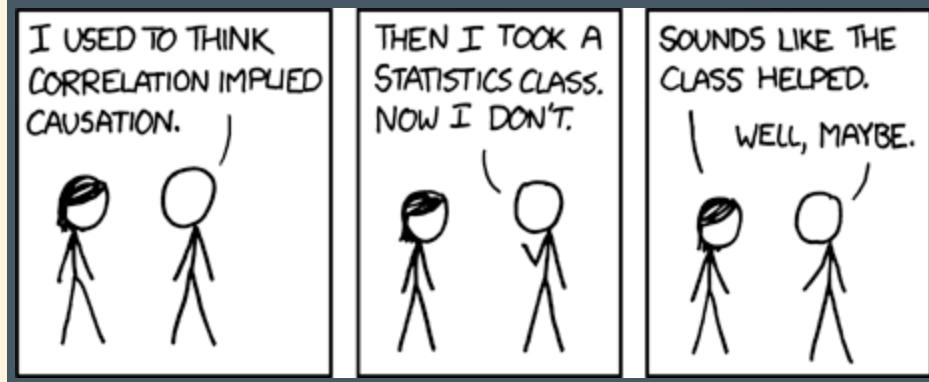


Milk and tumours

- English women, who consume large quantities of milk, develop some types of tumours 18 times more frequently than Japanese women, who rarely drink it
- Tumours usually appear late in life.
- British women live, on average, 12 years more than Japanese women

Why are we here?

- because "numbers" (or rather, the way they are presented) are sometimes deceiving



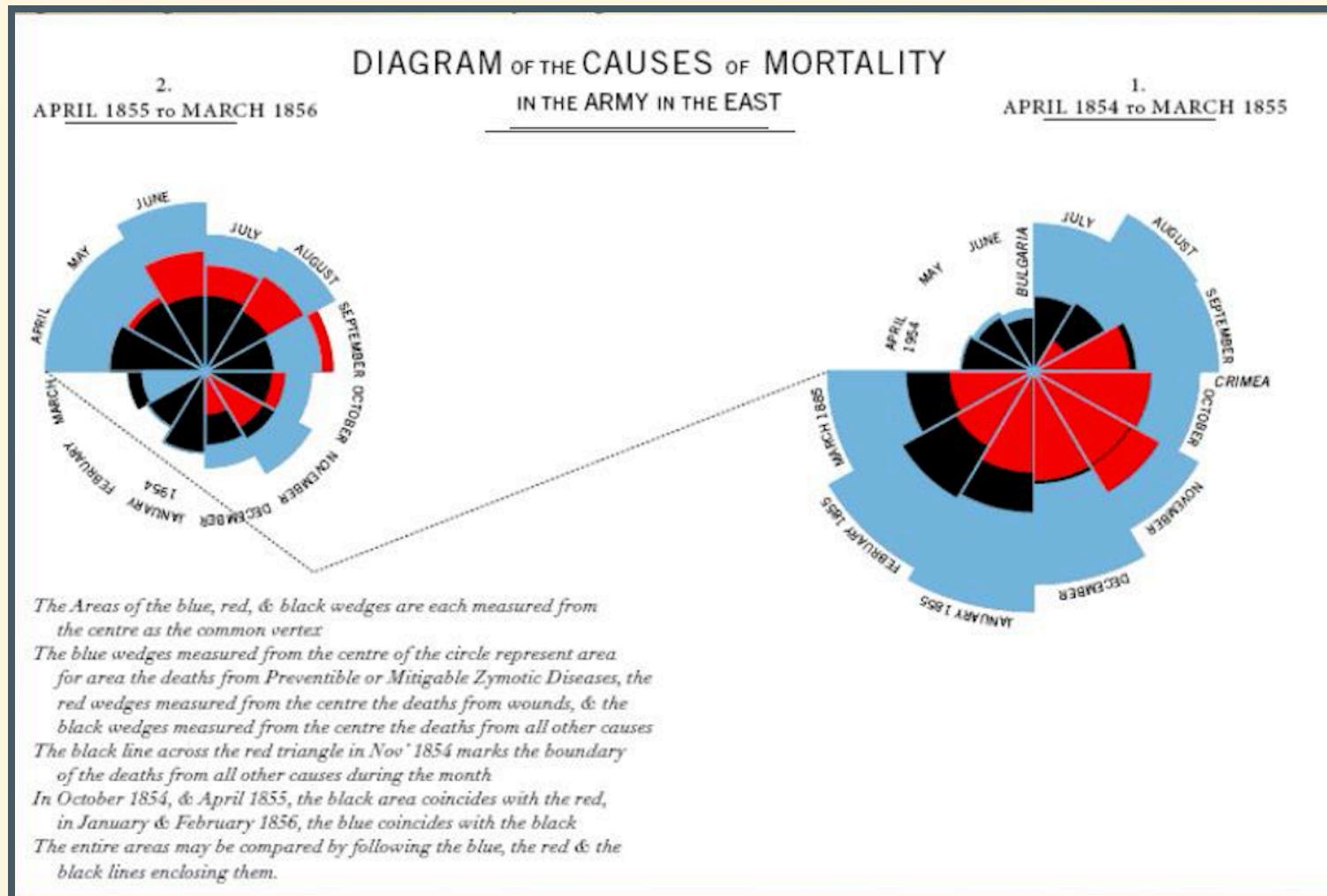
Why are we here?

“ Why do soldiers die? ”

Who is this person?



Why do soldiers die?



Why are we here?

- because "numbers" (or rather, the way they are presented) are sometimes deceiving
- Why “numbers” (and the way they are presented) help us describe, understand, and change the world

Why are we here?

- to learn how to read, understand, and critically analyse scientific papers
- to be able to carry out research involving the acquisition, processing, and analysis of data

Scientific research

Problem

“ Why do soldiers die? ”

Plan

- How do we answer?

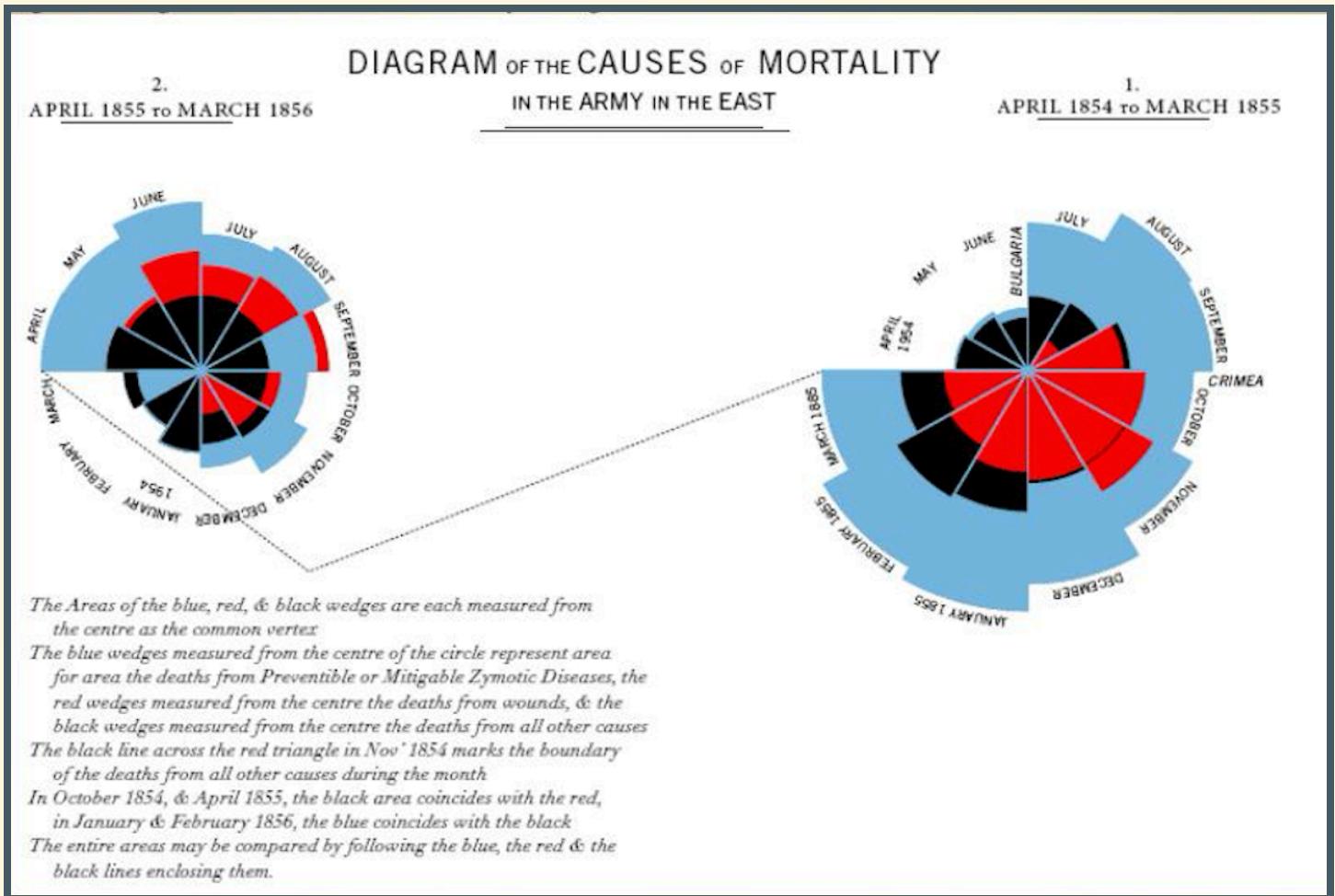


Data



Scutari Hospital. J.A. Benwell. about 1856

Analysis

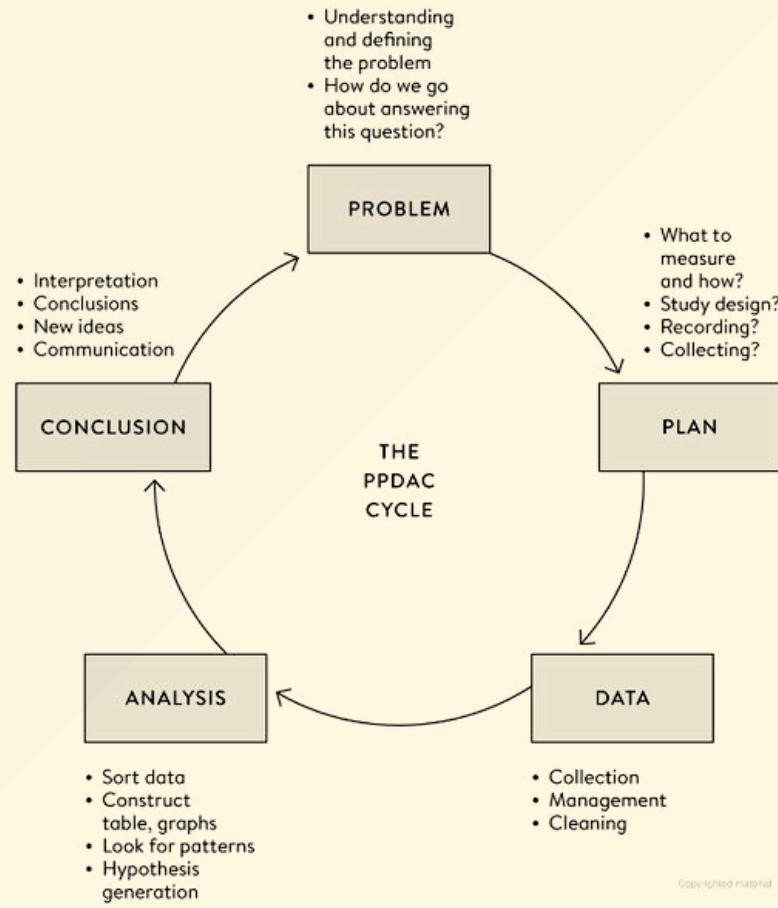


Conclusions



Florence Nightingale (1820 - 1910) at Scutari Hospital in Turkey around 1855, unknown artist

The data problem-solving cycle



Inductive reasoning

Derive a general rule from observations

What is Statistics?

- The collection, organisation, summarisation, and analysis of data
→ *Descriptive* statistics
- The drawing of inferences about a body of data when only a part of the data is observed
→ *Inferential* statistics

What will we learn?

- How to collect data
- How to summarise data
- How to make decision with data

What will we learn?

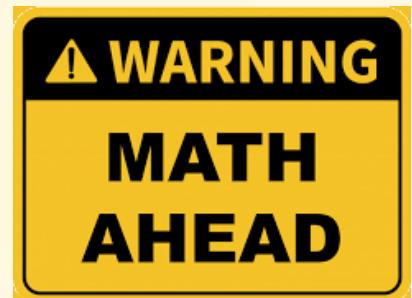
Key Points

Question In patients with coronavirus disease 2019 (COVID-19) and moderate or severe acute respiratory distress syndrome (ARDS), does intravenous dexamethasone plus standard care compared with standard care alone increase the number of days alive and free from mechanical ventilation?

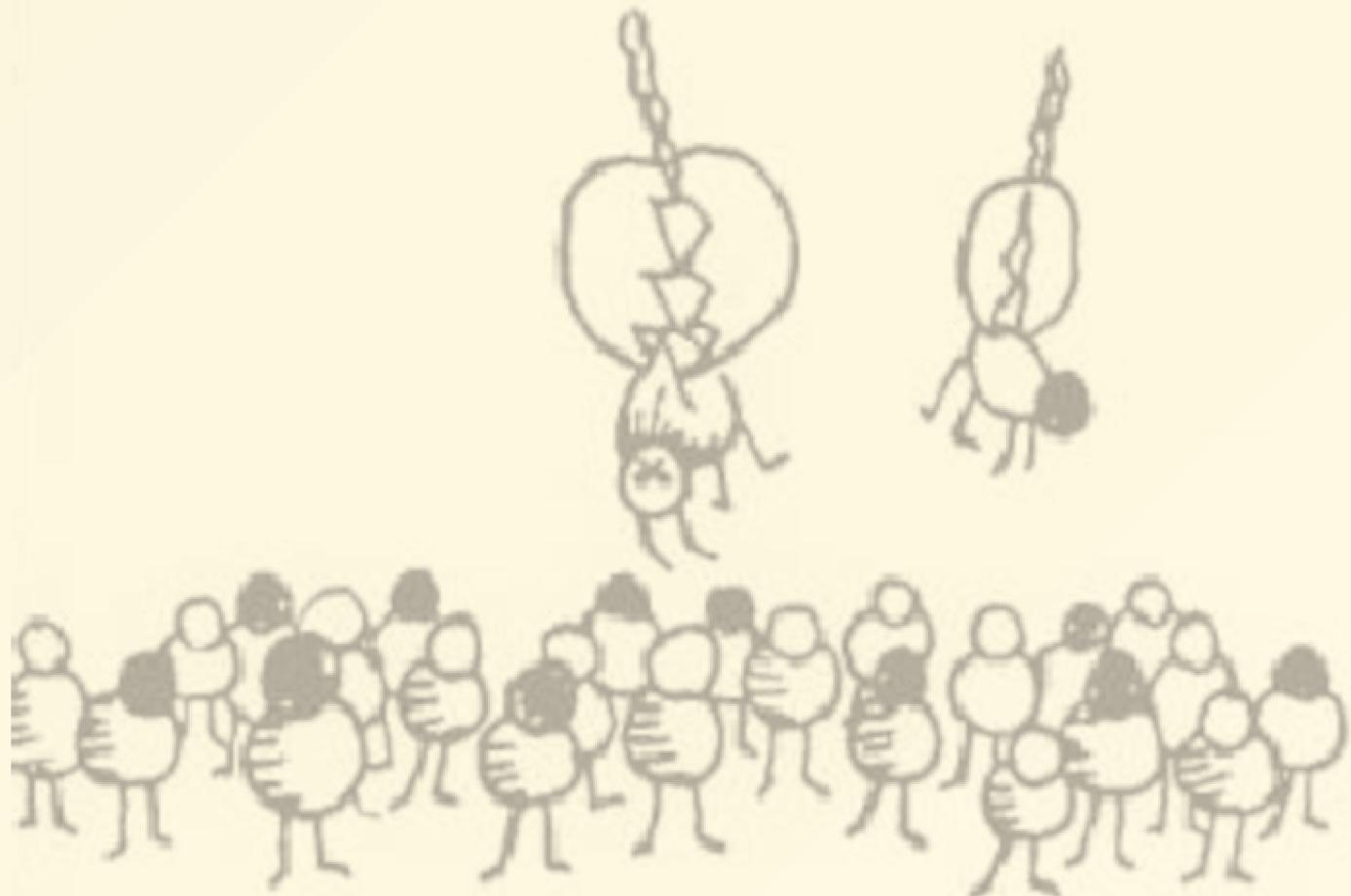
Tomazini, B.M., et al., Effect of dexamethasone on days alive and ventilator-free in patients with moderate or severe acute respiratory distress syndrome and COVID-19: the CoDEX randomized clinical trial.", JAMA, 2020, doi:10.1001/jama.2020.17021

Topics covered

- How to sample from a population
- How to use Measure of central tendency and dispersion
- How to make estimation from a sample
- How to interpret confidence intervals
- How to make and test hypotheses

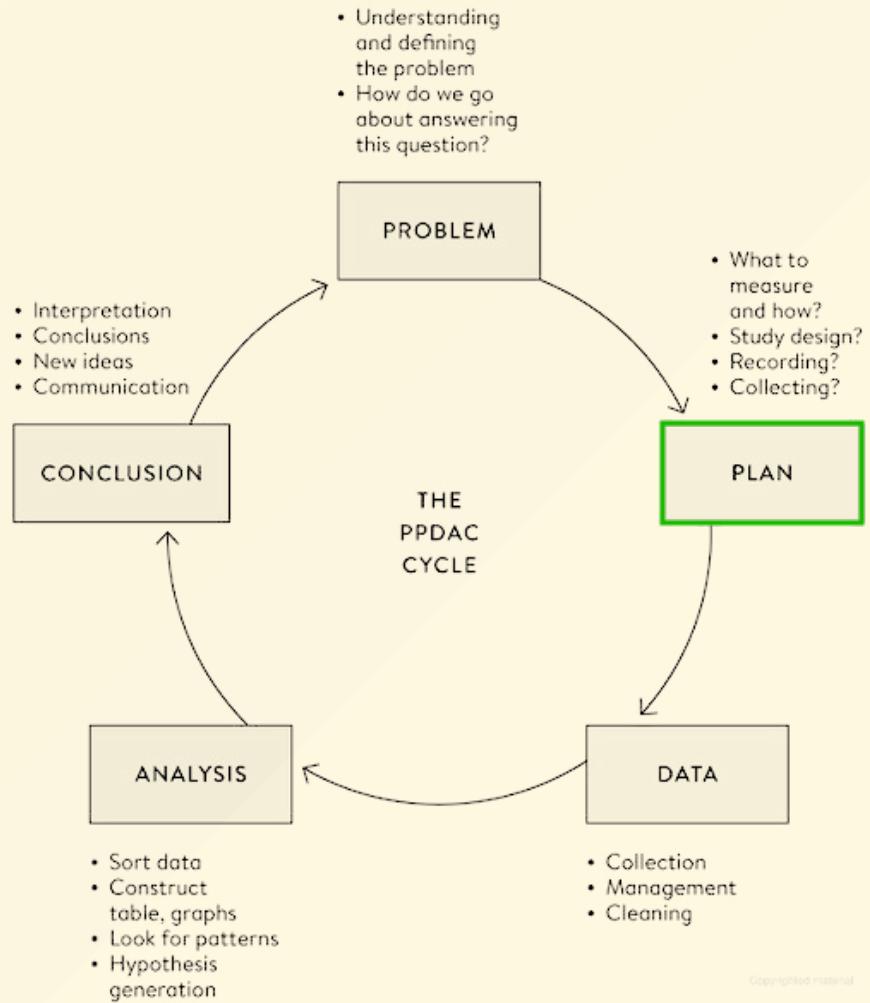


Sampling



Learning objectives

- Understand the difference between population and sample
- Understand the difference between sampling strategies
- Understand sampling error and bias



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Population vs sample



Istat | Istituto Nazionale
di Statistica

POPULATIONS AND SAMPLES

PERMANENT CENSUS OF POPULATION AND HOUSING

The permanent census of the population and housing begins in October 2018. For the first time ISTAT conducts not a ten-yearly but an annual survey of the main characteristics of the country's resident population and its social and economic conditions at national, regional and local levels.

The new permanent census of population and housing do not involve all Italian families, but a sample of them each year: about 1,400,000 families resident in 2,800 Italian municipalities.

Moreover, only a percentage of the municipalities (about 1,100 of them) will take part by census operations every year; the remainder will be called to participate once every four years. In this way, all municipalities will be surveyed at least once by 2021.

CENSIMENTI PERMANENTI



PUBLIC INSTITUTIONS

NONPROFIT INSTITUTIONS

AGRICULTURE

PERMANENT CENSUS OF POPULATION AND HOUSING

Population vs sample (in the clinic)

Delirium as a Predictor of Mortality in Mechanically Ventilated Patients in the Intensive Care Unit

E. Wesley Ely, MD, MPH

Ayumi Shintani, PhD, MPH

Brenda Truman, RN, MSN

Theodore Speroff, PhD

Sharon M. Gordon, PsyD

Frank E. Harrell, Jr, PhD

Sharon K. Inouye, MD, MPH

Gordon R. Bernard, MD

Robert S. Dittus, MD, MPH

Context In the intensive care unit (ICU), delirium is a common yet underdiagnosed form of organ dysfunction, and its contribution to patient outcomes is unclear.

Objective To determine if delirium is an independent predictor of clinical outcomes, including 6-month mortality and length of stay among ICU patients receiving mechanical ventilation.

Design, Setting, and Participants Prospective cohort study enrolling 275 consecutive mechanically ventilated patients admitted to adult medical and coronary ICUs of a US university-based medical center between February 2000 and May 2001. Patients were followed up for development of delirium over 2158 ICU days using the Confusion Assessment Method for the ICU and the Richmond Agitation-Sedation Scale.

Exercise #1

Objective To determine whether intravenous dexamethasone increases the number of ventilator-free days among patients with COVID-19-associated ARDS.

Design, Setting, and Participants Multicenter, randomized, open-label, clinical trial conducted in 41 intensive care units (ICUs) in Brazil. Patients with COVID-19 and moderate to severe ARDS, according to the Berlin definition, were enrolled from April 17 to June 23, 2020. Final follow-up was completed on July 21, 2020. The trial was stopped early following publication of a related study before reaching the planned sample size of 350 patients.

? Which is the population of this study?

- a) Patients with Acute respiratory distress syndrome (ARDS)
- b) Patients with COVID-19-associated ARDS
- c) Brazilian patients with COVID-19-associated ARDS
- d) Patients without COVID-19-associated ARDS

Exercise #1 -- Solution

Objective To determine whether intravenous dexamethasone increases the number of ventilator-free days among patients with COVID-19-associated ARDS.

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Exercise #2

Objective To determine whether intravenous dexamethasone increases the number of ventilator-free days among patients with COVID-19-associated ARDS.

Design, Setting, and Participants Multicenter, randomized, open-label, clinical trial conducted in 41 intensive care units (ICUs) in Brazil. Patients with COVID-19 and moderate to severe ARDS, according to the Berlin definition, were enrolled from April 17 to June 23, 2020. Final follow-up was completed on July 21, 2020. The trial was stopped early following publication of a related study before reaching the planned sample size of 350 patients.

? Which is the sample used in this study?

- a) Patients with Acute respiratory distress syndrome (ARDS)
- b) Patients with COVID-19-associated ARDS
- c) Brazilian patients with COVID-19-associated ARDS
- d) Patients without COVID-19-associated ARDS

Exercise #2 -- Solution

Objective To determine whether intravenous dexamethasone increases the number of ventilator-free days among patients with COVID-19-associated ARDS.

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 - c) Brazilian patients with COVID-19-associated ARDS
 - d) Patients without COVID-19-associated ARDS

Opportunity vs random sample

- 🎯 An **opportunity** sample is the sample drawn from the part of the population that is close to hand (and which may not represent the whole population)
- 📌 All the patients presenting to a given clinic in a given period of time are enrolled

Opportunity vs random sample

- 🎯 A **random** sample is the sample in which the probability of getting any particular sample may be calculated (and which should represent the whole population)
- 📌 A randomly selected set of patients with the disease is enrolled

Strategy 1: Simple random sampling

- 🎯 A sample of size n drawn from a population of size N ensuring that every possible sample of size n is equally likely

Strategy 1: Simple random sampling



$N = 90$

$n = 10$

La Tombola di PianetaBambini.it TABELLONE									
1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90

Strategy 1: Simple random sampling



$N = 90$

$n = 10$

49, 65, 25, 74, 18

90, 47, 24, 71, 37

TABELLONE									
1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
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41	42	43	44	45	46	47	48	49	50
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61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90

Strategy 2: Systematic Sampling



$$N = 90$$

$$n = 10$$

$$x = 42$$

$$\text{step} = N/n = 90/10 = 9$$

La Tombola di PianetaBambini.it TABELLONE									
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Strategy 3: Stratified Random Sampling

- 🎯 The population is divided into homogenous group (strata) and a simple random sample is drawn from each stratum

Variation #1: stratified systematic sample

Variation #2: stratified sampling proportional to size

Strategy 3: Stratified Random Sampling



$$N = 90$$

$$N_{female} = 60$$

$$N_{male} = 30$$

$$n = 9$$

$$n_{female} = 6$$

$$n_{male} = 3$$

Females : 46, 20, 26,
50, 47, 3

Males : 69, 85, 87

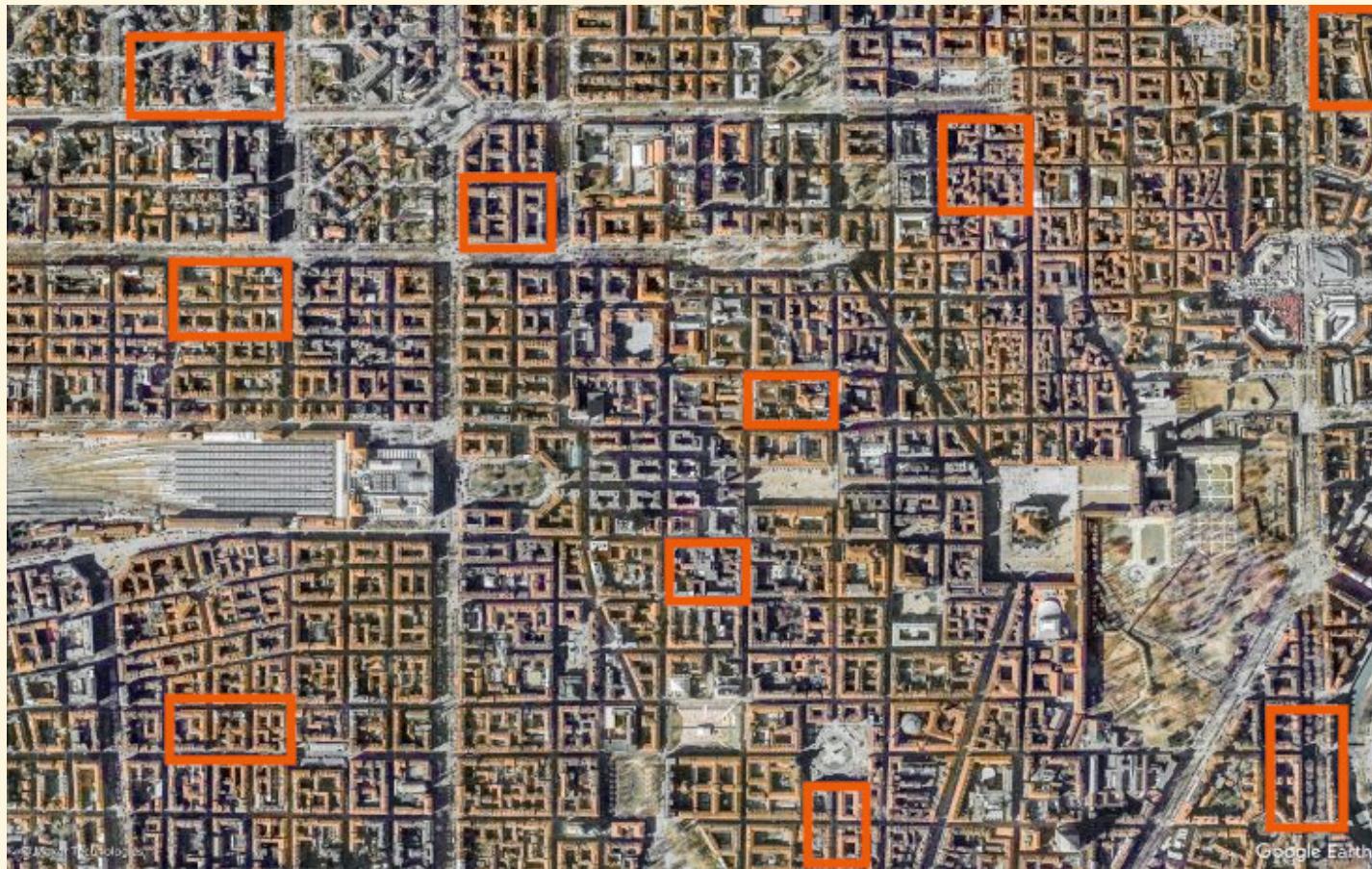
La Tombola di PianetaBambini.it										TABELLONE		
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71	72	73	74	75	76	77	78	79	80			
81	82	83	84	85	86	87	88	89	90			

Strategy 4: Cluster sampling

- 🎯 The population is divided into clusters, and a simple random sample is drawn

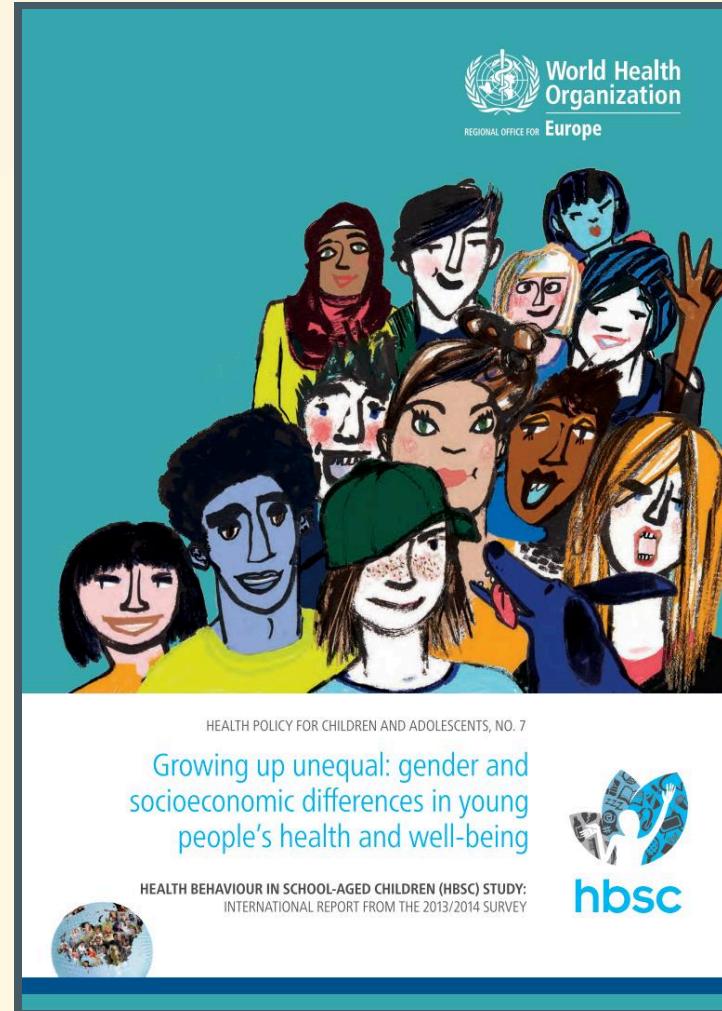
Variation: one stage (observing everything) *vs*
two stage (sampling within clusters)

Strategy 4: Cluster sampling



Sampling in the wild

<https://hbsc.org>



Exercise #3

- ? A representative of a cheese factory is asking questions on cheese consumption to every 5th customer entering the supermarket

Which kind of sampling strategy are they using?

- a) simple random sampling
- b) systematic sampling
- c) stratified sampling
- d) none of the above

Exercise #3 -- Solution

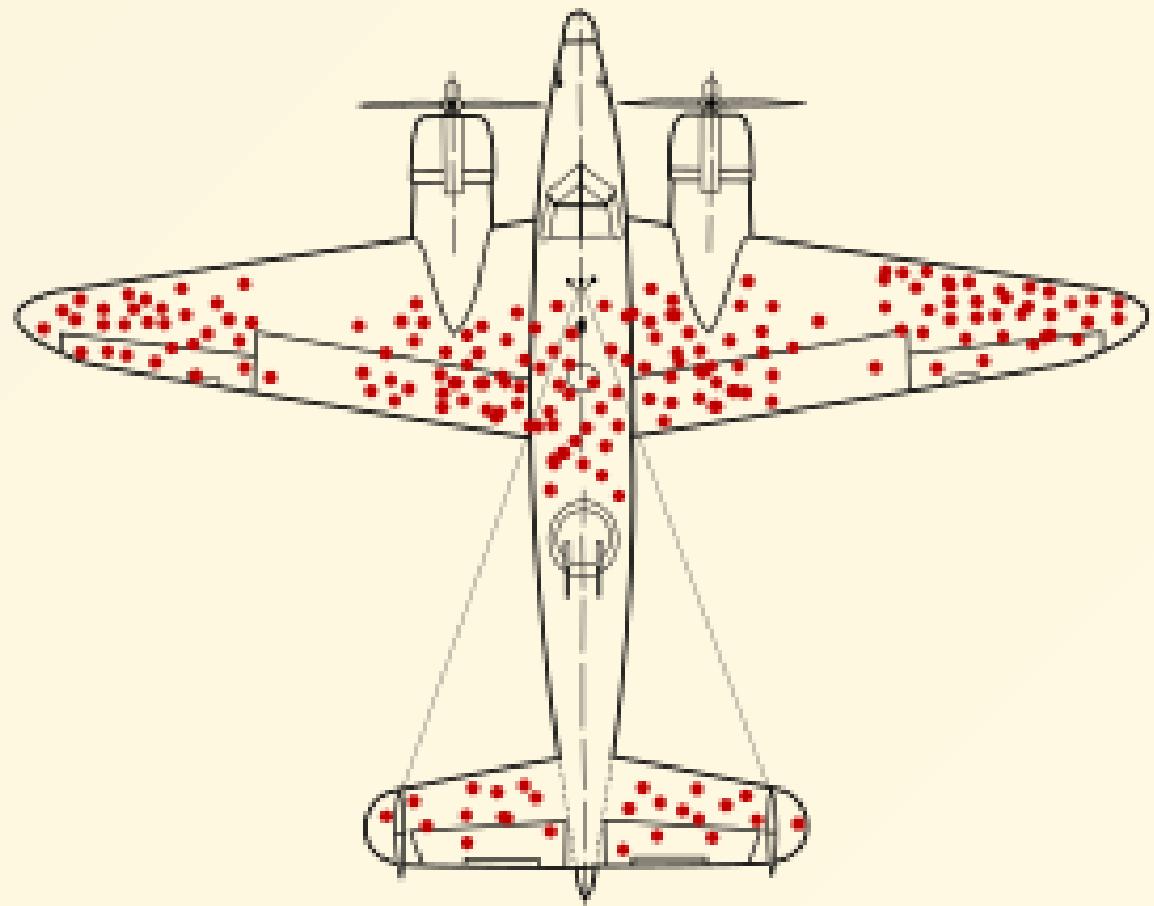
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Selection bias

- Survivor bias



Selection bias

- Survivor bias

"Buildings used to be more beautiful/longer lasting"

Selection bias

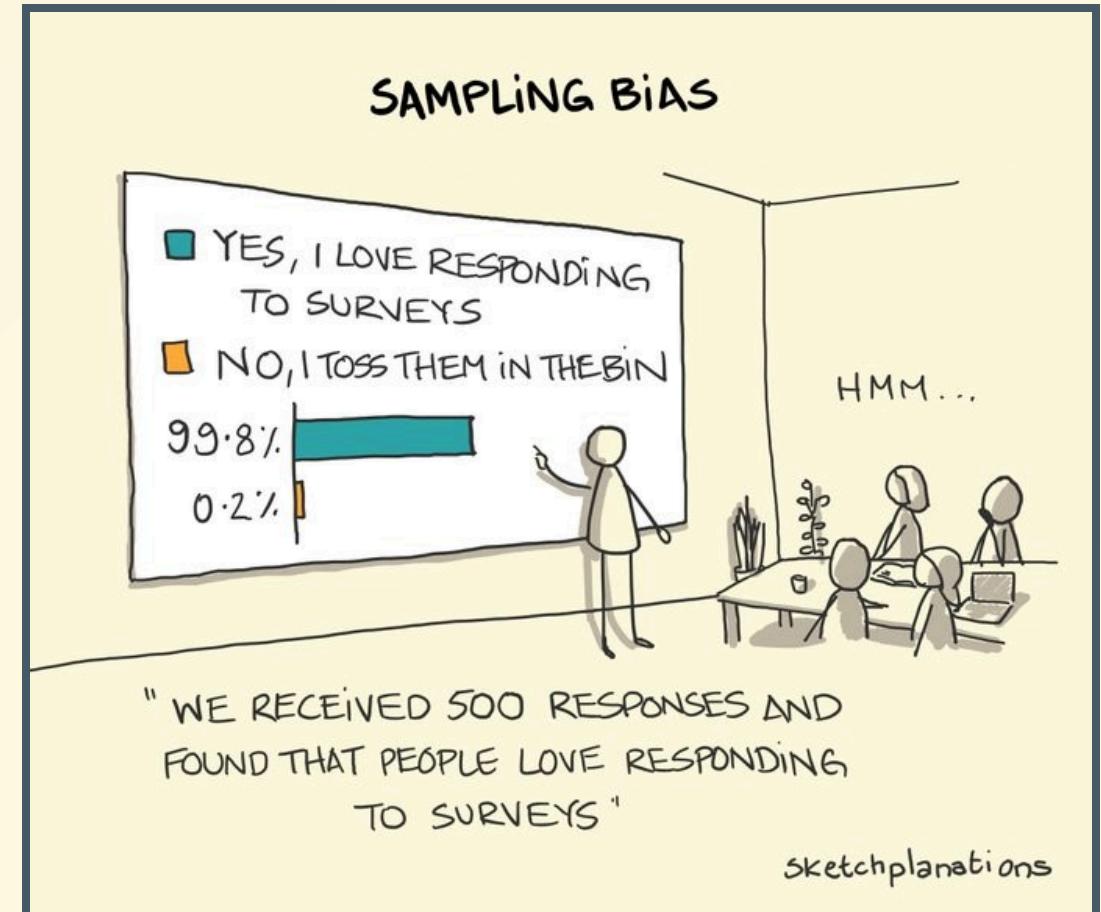
- Survivor bias

"Buildings used to be more beautiful/longer lasting"

*"I don't understand why, nowadays, one should do X,
I never did it, and I'm still here to tell it"*

Selection bias

- Survivor bias
- Volunteer bias



Selection bias

- Survivor bias
- Volunteer bias

A teacher wonders if extra lessons improve exam performance.
She prepares them, inviting interested students to sign up.

Selection bias

- Survivor bias
- Volunteer bias
- Lost to follow up bias

Selection bias

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- Volunteer bias
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A pharma company is testing a new drug on a court of 100 cancer patients recruited in a center of excellence, 30 of whom did not show up at the follow up. What do we conclude about this new drug knowing that these 30 people...

Selection bias

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A pharma company is testing a new drug on a court of 100 cancer patients recruited in a center of excellence, 30 of whom did not show up at the follow up. What do we conclude about this new drug knowing that these 30 people....
- died?

Selection bias

- Survivor bias
- Volunteer bias
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A pharma company is testing a new drug on a court of 100 cancer patients recruited in a center of excellence, 30 of whom did not show up at the follow up. What do we conclude about this new drug knowing that these 30 people....

- died?
- stopped the drug?

Selection bias

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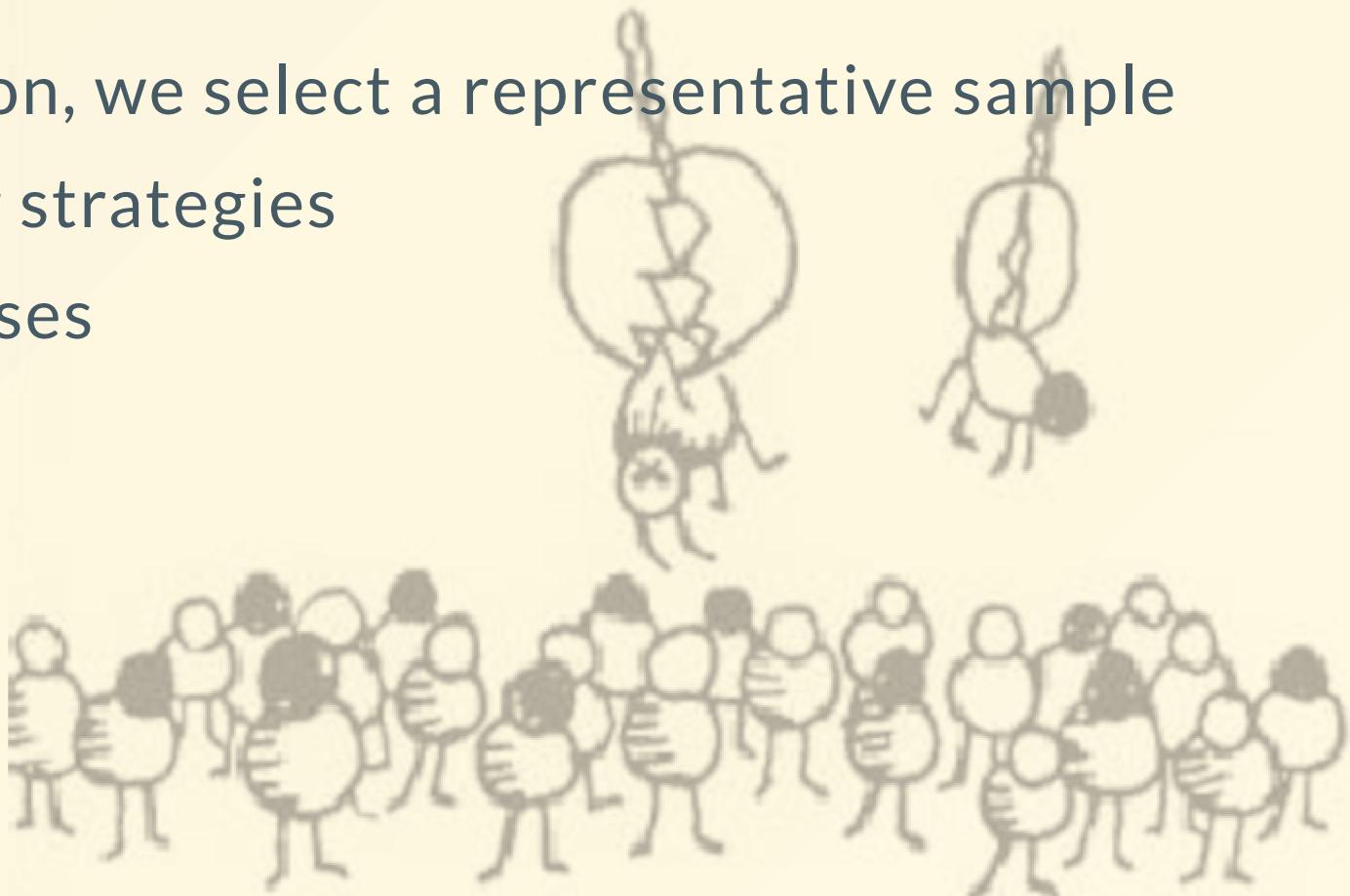
- died?
- stopped the drug?
- went back home?

Selection bias

- Survivor bias
- Volunteer bias
- Lost to follow up bias
- ...

Summary

- When can't study a population, we select a representative sample
- There are different sampling strategies
- Samples may suffer from biases

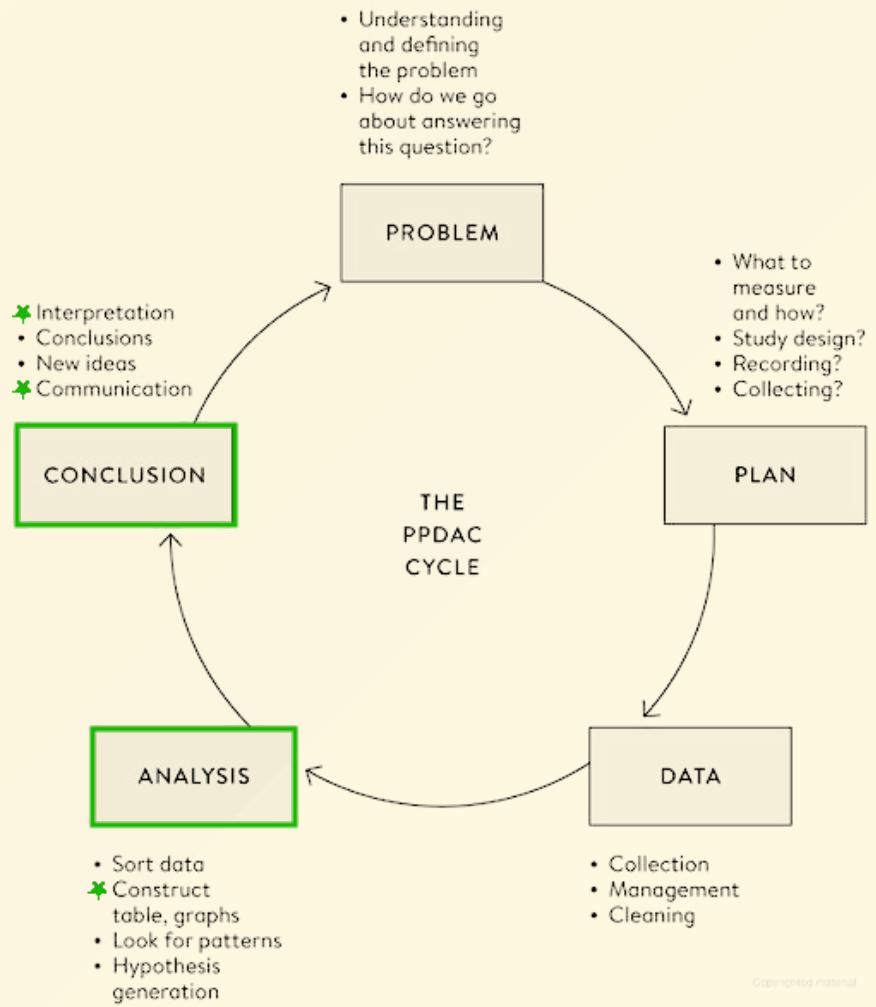


Summarise data



Learning objectives

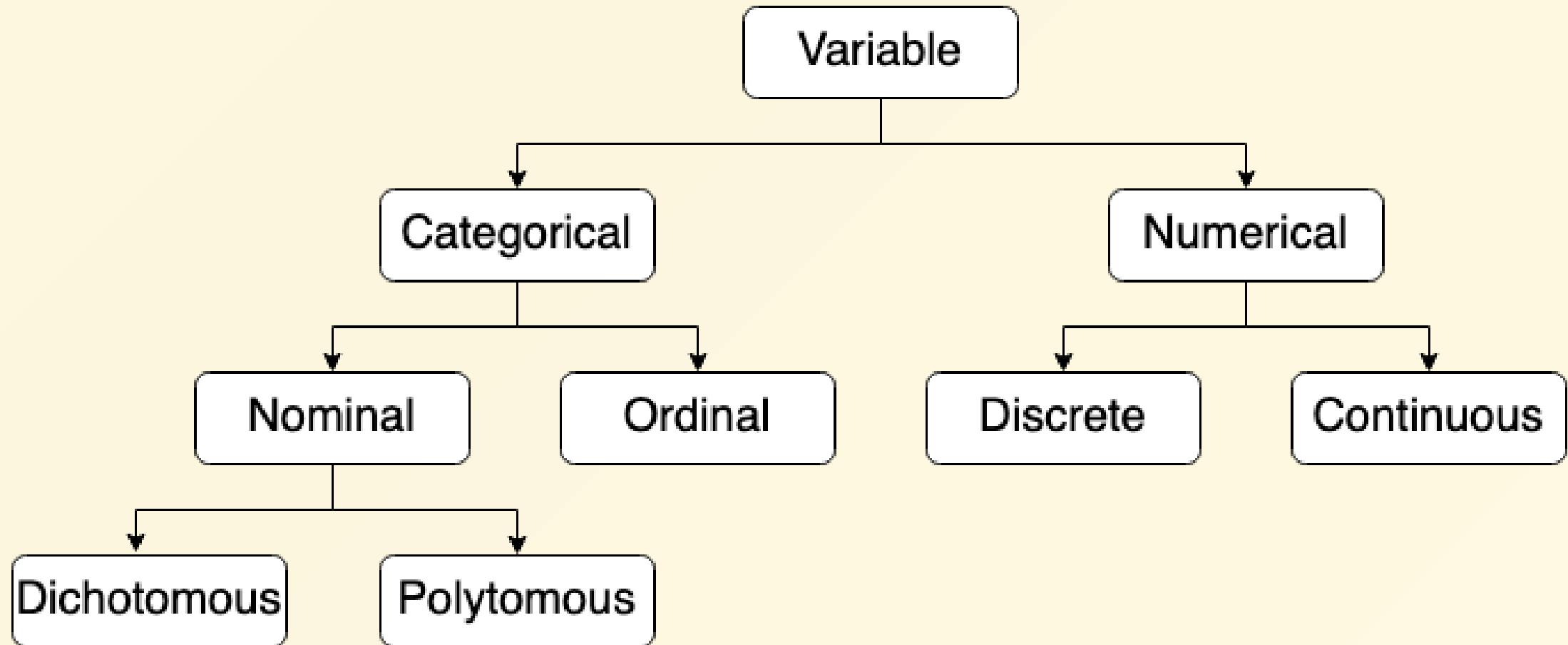
- Understand the differences between data types
- Be able to summarise each data type using Measure of central tendency and dispersion
- Understand the difference between parameters and statistics
- Understand why visualise your data is important



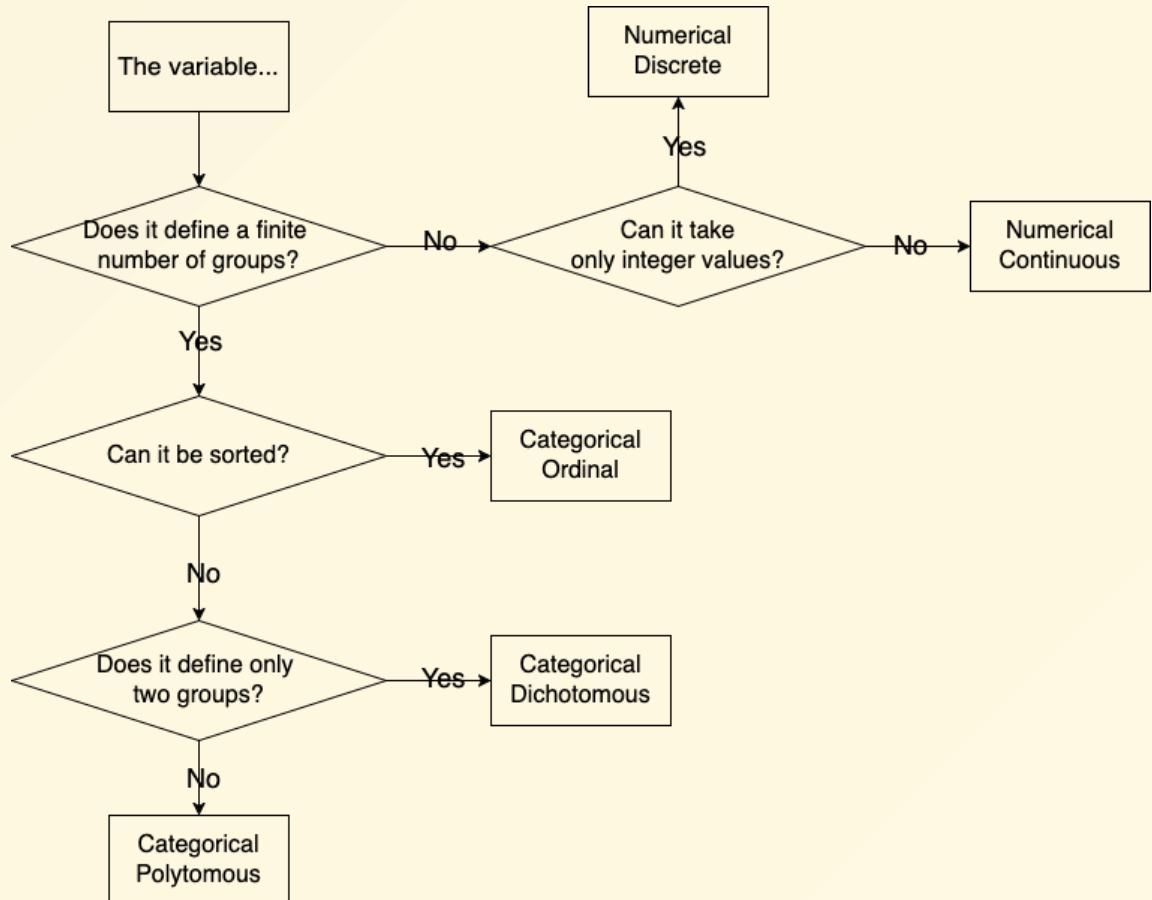
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Spiegelhalter, D., *The Art of Statistics: Learning From Data*, Pelican, 2019

Type of data

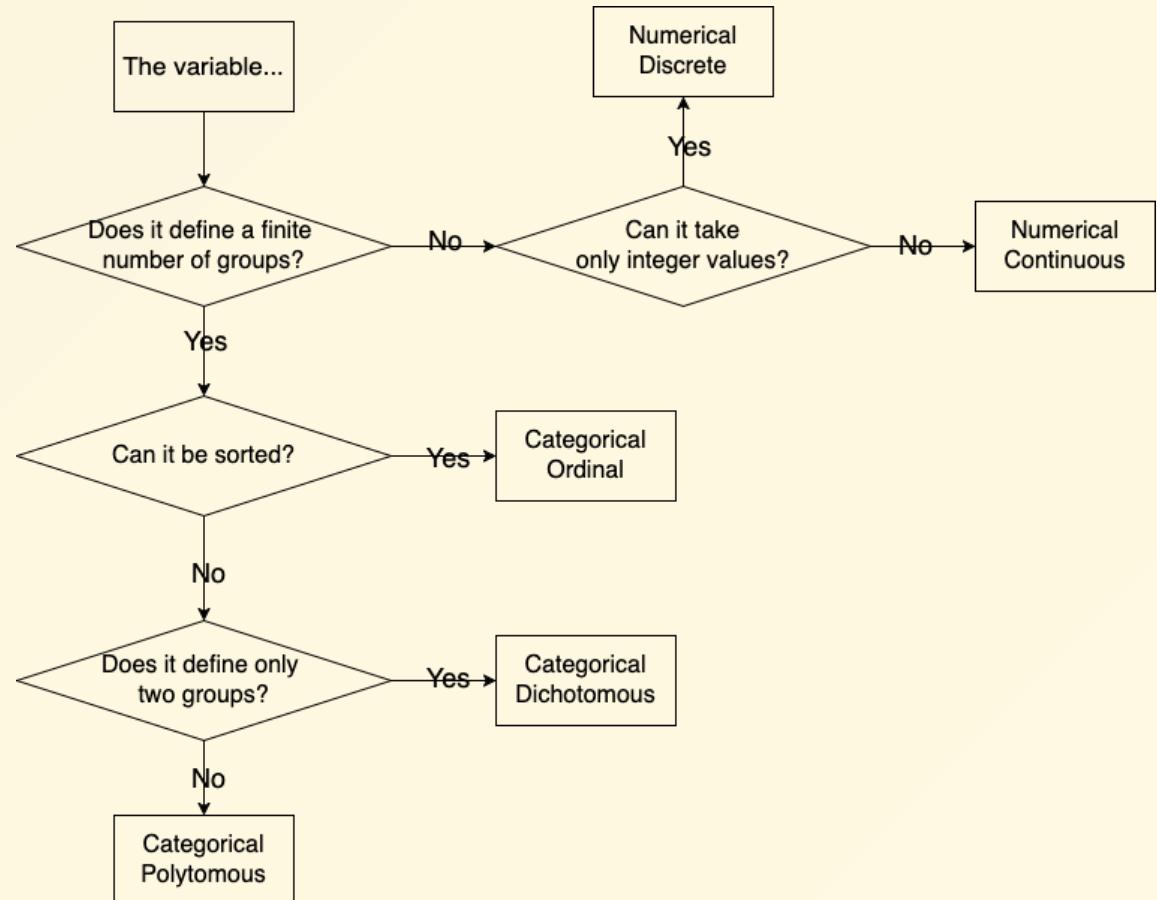


What type of data is this?



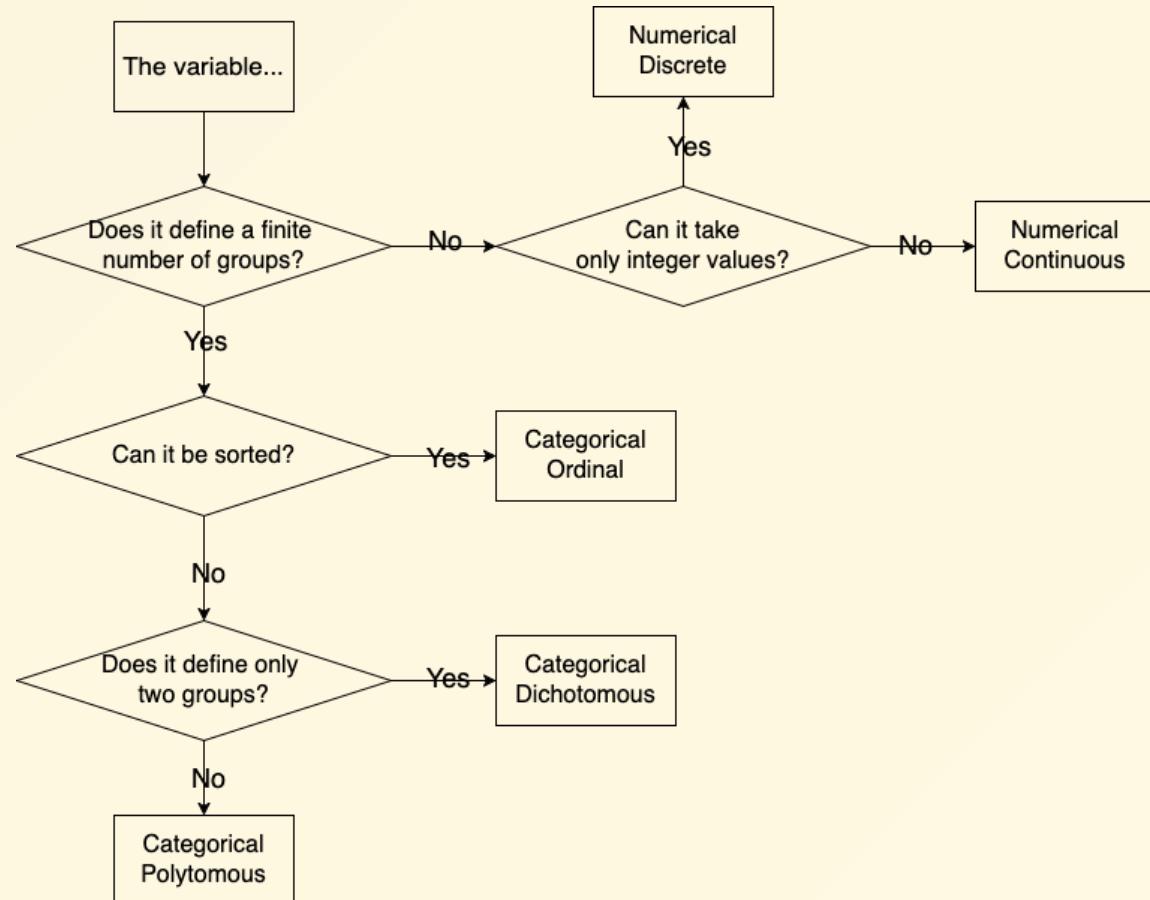
What type of data is this?

? The number of death in a hospital



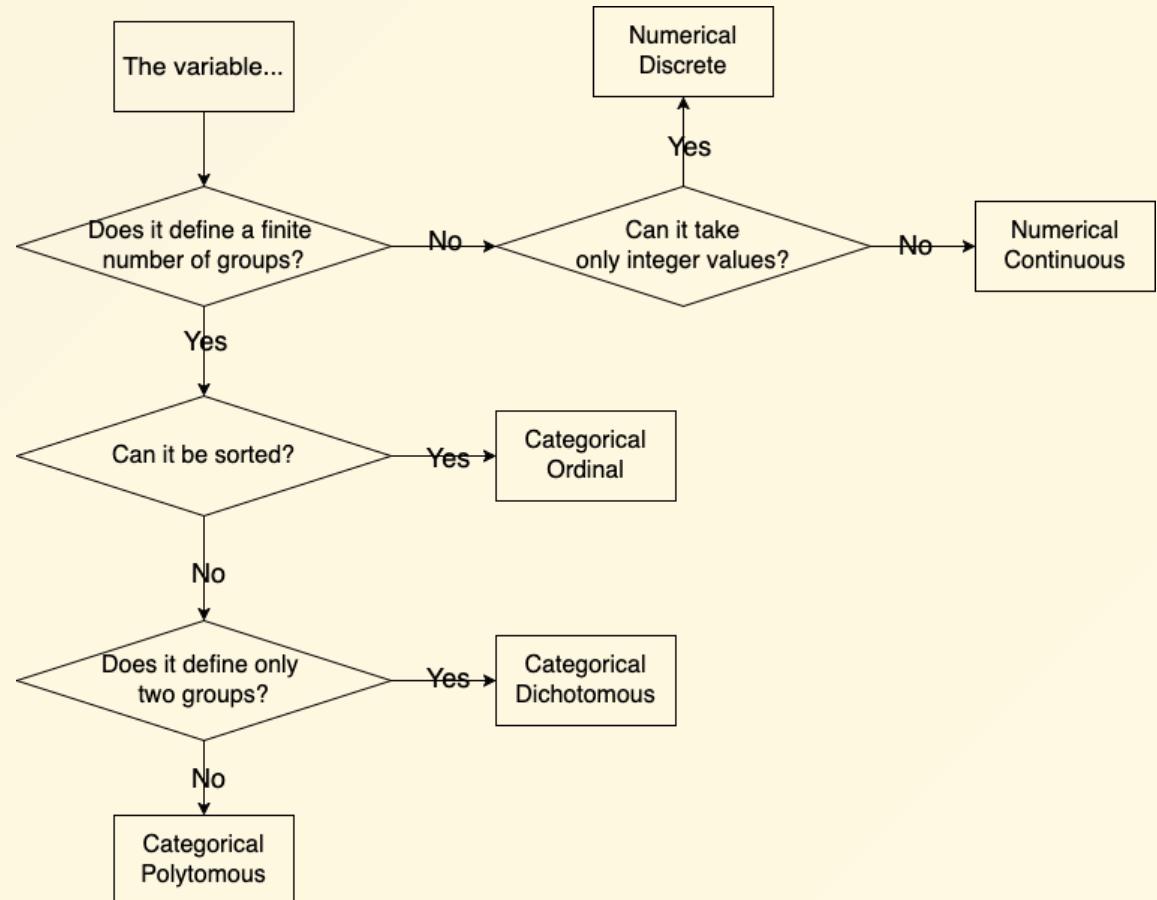
What type of data is this?

? The size of a T-shirt



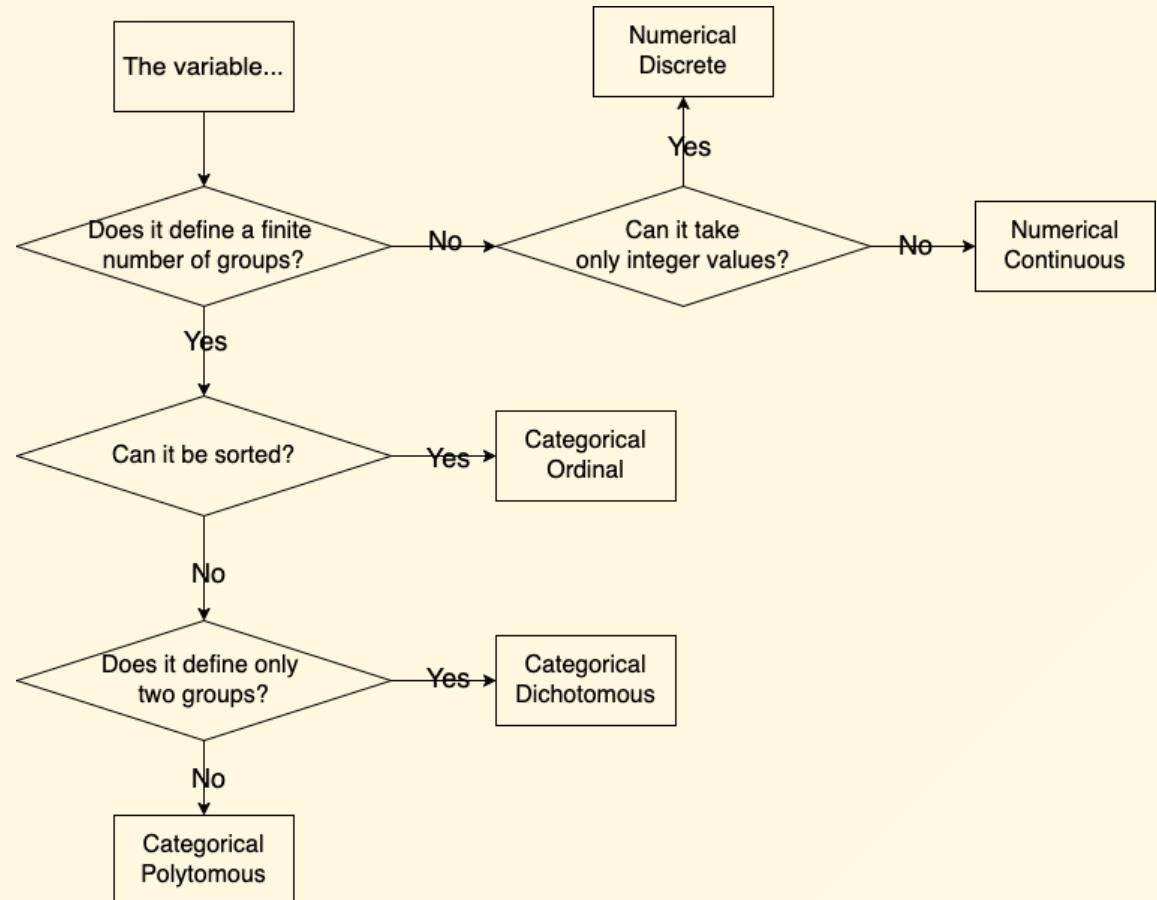
What type of data is this?

? One's nationality



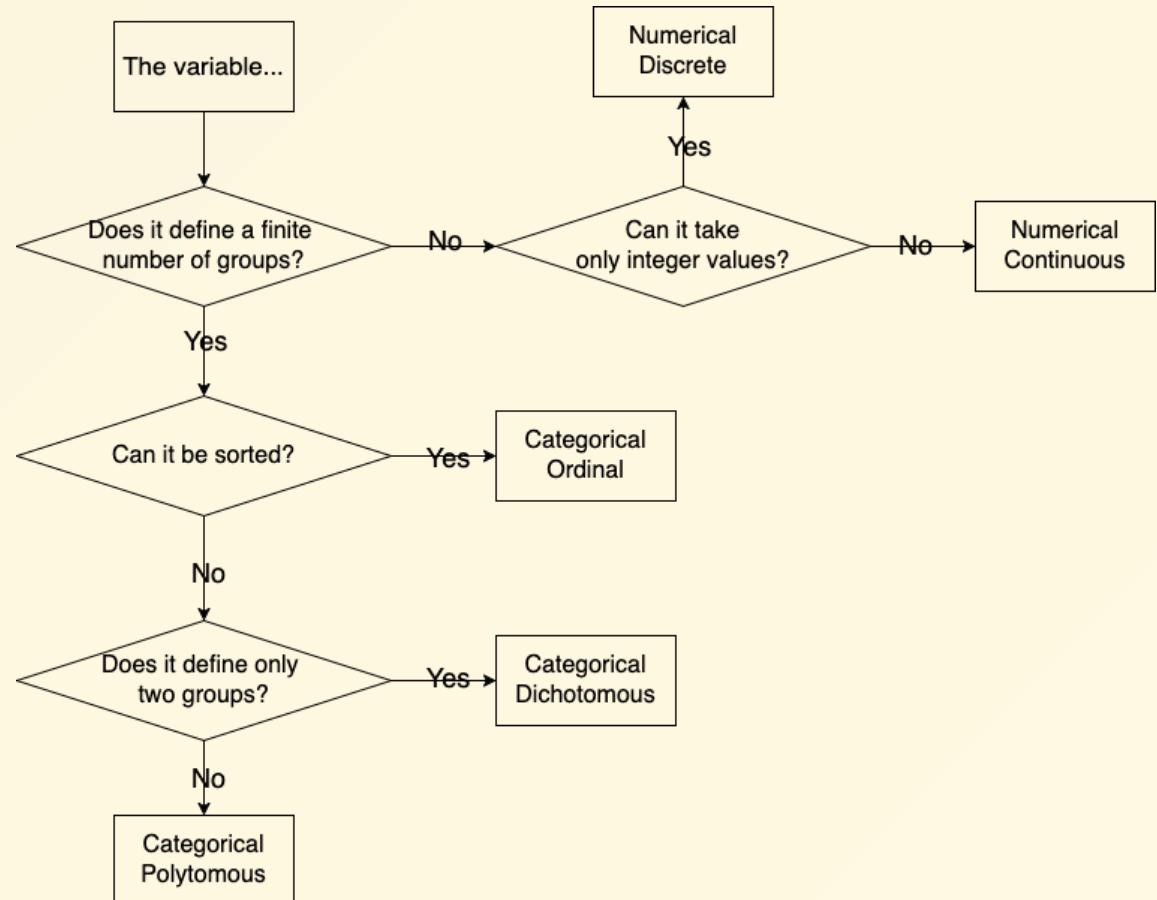
What type of data is this?

? Fasting blood sugar levels



What type of data is this?

? Passing the driving licence test



Exercise #4

? Which types of data are included in this table?

02:00

Visconti A., et al., Total serum *N*-glycans associate with response to immune checkpoint inhibition therapy and survival in patients with advanced melanoma, BMC Cancer, 2023 doi:10.1186/s12885-023-10511-3

Table 1 Patient characteristics.

	All cohorts
N (pre-treatment)	88
N (follow-up)	66
Sex	
<i>Male</i>	57 (64.8%)
<i>Female</i>	31 (35.2%)
Age (years)	60.5 ± 15.0
BMI (kg/m²)	28.0 ± 5.4
BRAF mutant	40 (45.5%)
LDH (\leqULN)	58 (65.9%)
Metastatic stage	
<i>Stage III unresectable</i>	2 (2.3%)
<i>M1a</i>	14 (15.9%)
<i>M1b</i>	17 (19.3%)
<i>M1c</i>	32 (36.4%)
<i>M1d</i>	23 (26.1%)
ECOG performance status	
0	47 (53.4%)
1	31 (35.2%)
2	8 (9.1%)
3	2 (2.3%)
ICI therapy	
<i>Ipilimumab</i>	1 (1.1%)
<i>Pembrolizumab</i>	20 (22.7%)
<i>Nivolumab</i>	30 (34.1%)
<i>Ipilimumab + Nivolumab</i>	37 (42.0%)

Why do we care?

Table 1 Patient characteristics. Categorical variables are presented as number (percentage). Continuous variables are presented as mean \pm standard deviation.

Visconti A., et al., Total serum *N*-glycans associate with response to immune checkpoint inhibition therapy and survival in patients with advanced melanoma, BMC Cancer, 2023 doi:10.1186/s12885-023-10511-3

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Ipilimumab + Nivolumab	37 (42.0%)

Categorical variables

Frequency table

- absolute frequency (the number)
- relative frequency (the percentage)

Visconti A., et al., *Total serum N-glycans associate with response to immune checkpoint inhibition therapy and survival in patients with advanced melanoma*, BMC Cancer, 2023 doi:10.1186/s12885-023-10511-3

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3	2 (2.3%)
ICI therapy	
Ipilimumab	1 (1.1%)
Pembrolizumab	20 (22.7%)
Nivolumab	30 (34.1%)
Ipilimumab + Nivolumab	37 (42.0%)

Exercize #5

? Which sex is more frequent?

Table 1 Patient characteristics.

	All cohorts
N (pre-treatment)	88
Sex	
Male	57 (64.8%)
Female	31 (35.2%)

Visconti A., et al., Total serum N-glycans associate with response to immune checkpoint inhibition therapy and survival in patients with advanced melanoma, BMC Cancer, 2023 doi:10.1186/s12885-023-10511-3

00:30

Exercize #5 -- Solution

? Which sex is more frequent?

Table 1 Patient characteristics.

	All cohorts
N (pre-treatment)	88
Sex	
Male	57 (64.8%)
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Visconti A., et al., Total serum N-glycans associate with response to immune checkpoint inhibition therapy and survival in patients with advanced melanoma, BMC Cancer, 2023 doi:10.1186/s12885-023-10511-3

Contingency table

Study Objectives: Persistent insomnia, although very common in general practice, often proves problematic to manage. This study investigates the clinical effectiveness and the feasibility of applying cognitive behavior therapy (CBT) methods for insomnia in primary care.

Design: Pragmatic randomized controlled trial of CBT versus treatment as usual.

Setting: General medical practice.

Participants: Two hundred one adults (mean age, 54 years) randomly assigned to receive CBT ($n = 107$; 72 women) or treatment as usual ($n = 94$; 65 women).

Exercise #6

- Complete the table with the correct absolute and relative frequencies using the information contained in the abstract

Participants: Two hundred one adults (mean age, 54 years) randomly assigned to receive CBT ($n = 107$; 72 women) or treatment as usual ($n = 94$; 65 women).

	CBT	Standard	Total
Males			
Females			
Total			

Exercize #6 -- Solution

- Complete the table with the correct absolute and relative frequencies using the information contained in the abstract

Participants: Two hundred one adults (mean age, 54 years) randomly assigned to receive CBT ($n = 107$; 72 women) or treatment as usual ($n = 94$; 65 women).

	CBT	Standard	Total
Males			
Females	72	65	
Total	107	94	201

Exercize #6 -- Solution

- Complete the table with the correct absolute and relative frequencies using the information contained in the abstract

Participants: Two hundred one adults (mean age, 54 years) randomly assigned to receive CBT ($n = 107$; 72 women) or treatment as usual ($n = 94$; 65 women).

	CBT	Standard	Total
Males	35	29	
Females	72	65	
Total	107	94	201

Exercize #6 -- Solution

- Complete the table with the correct absolute and relative frequencies using the information contained in the abstract

Participants: Two hundred one adults (mean age, 54 years) randomly assigned to receive CBT ($n = 107$; 72 women) or treatment as usual ($n = 94$; 65 women).

	CBT	Standard	Total
Males	35	29	64
Females	72	65	137
Total	107	94	201

Abbiamo completato la nostra Tabella di Contingenza (con frequenze assolute)

Exercize #6 -- Solution

- Complete the table with the correct absolute and relative frequencies using the information contained in the abstract

Participants: Two hundred one adults (mean age, 54 years) randomly assigned to receive CBT ($n = 107$; 72 women) or treatment as usual ($n = 94$; 65 women).

	CBT	Standard	Total
Males	35 (35/107)	29 (29/94)	64 (64/201)
Females	72 (72/107)	65 (65/94)	137 (137/201)
Total	107	94	201

Option 1: let's divide "by columns", that is, calculate the percentage of males and females in each arm of the experiment

Exercize #6 -- Solution

- Complete the table with the correct absolute and relative frequencies using the information contained in the abstract

Participants: Two hundred one adults (mean age, 54 years) randomly assigned to receive CBT ($n = 107$; 72 women) or treatment as usual ($n = 94$; 65 women).

	CBT	Standard	Total
Males	35 (32.7%)	29 (30.9%)	64 (31.8%)
Females	72 (67.3%)	65 (69.1%)	137 (68.2%)
Total	107	94	201

Option 1: let's divide "by columns", that is, calculate the percentage of males and females in each arm of the experiment

Exercize #6 -- Solution

- Complete the table with the correct absolute and relative frequencies using the information contained in the abstract

Participants: Two hundred one adults (mean age, 54 years) randomly assigned to receive CBT ($n = 107$; 72 women) or treatment as usual ($n = 94$; 65 women).

	CBT	Standard	Total
Males	35 (35/64)	29 (29/64)	64
Females	72 (72/137)	65 (65/137)	137
Total	107 (107/201)	94 (94/201)	201

Option 2: let's divide "by rows", that is, calculate the percentage of subjects in each arm of the experiments that is either male or female

Exercize #6 -- Solution

- Complete the table with the correct absolute and relative frequencies using the information contained in the abstract

Participants: Two hundred one adults (mean age, 54 years) randomly assigned to receive CBT ($n = 107$; 72 women) or treatment as usual ($n = 94$; 65 women).

	CBT	Standard	Total
Males	35 (54.7%)	29 (45.3%)	64
Females	72 (52.6%)	65 (47.4%)	137
Total	107 (53.2%)	94 (46.8%)	201

Option 2: let's divide "by rows", that is, calculate the percentage of subjects in each arm of the experiments that is either male or female

Exercize #7

- ? Is the proportion of men and women similar?
 - a) True
 - b) False
 - c) I need more elements to decide

- ? Comparing the two arms, is the proportion of men and women similar?
 - a) True
 - b) False
 - c) I need more elements to decide

	CBT	Standard	Total
Males	35 (32.7%)	29 (30.9%)	64 (31.8%)
Females	72 (67.3%)	65 (69.1%)	137 (68.2%)
Total	107	94	201

Exercize #7 -- Solution

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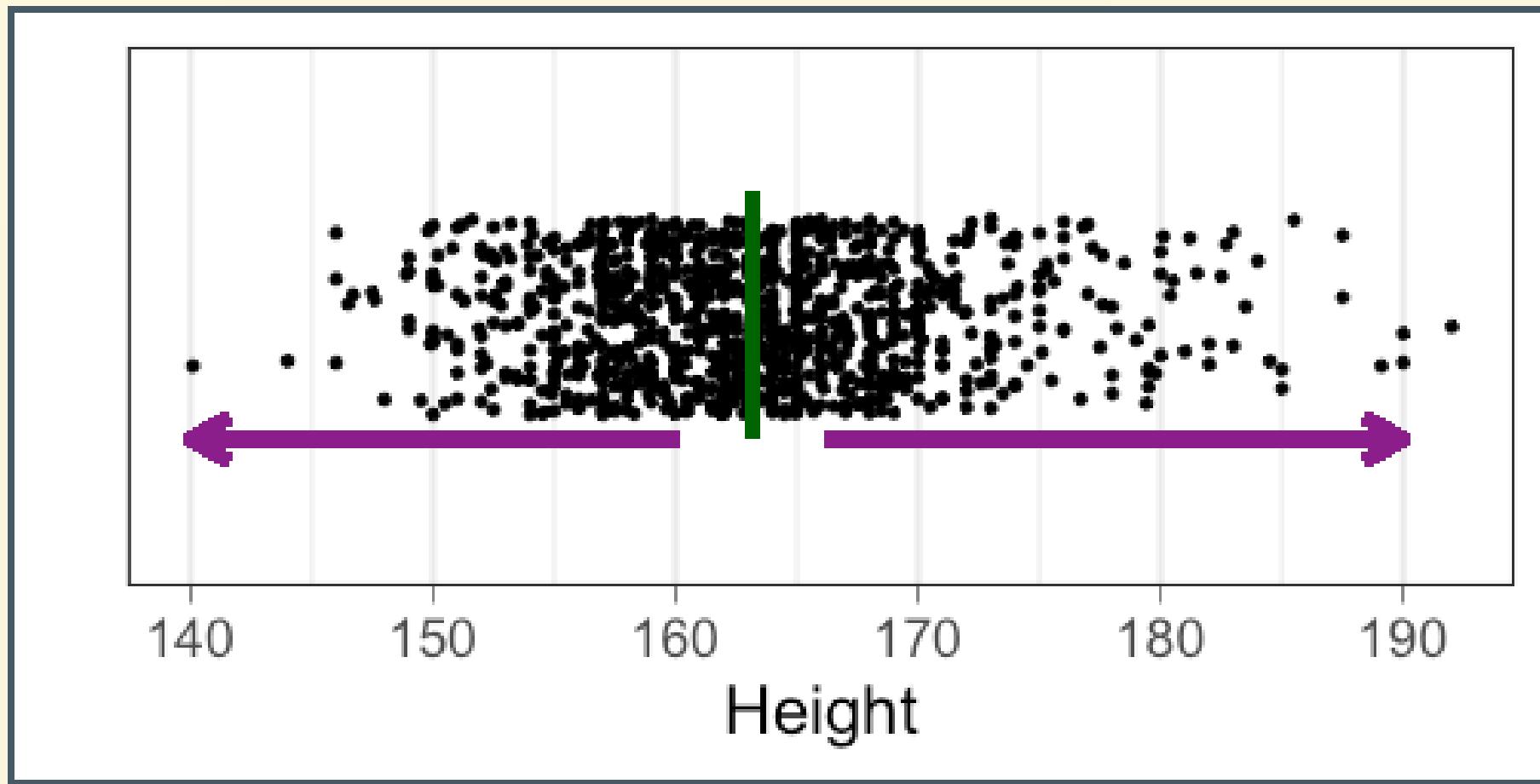
Exercize #7 -- Solution

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	CBT	Standard	Total
Males	35 (32.7%)	29 (30.9%)	64 (31.8%)
Females	72 (67.3%)	65 (69.1%)	137 (68.2%)
Total	107	94	201

Measures of central tendency and dispersion



Measure of central tendency: mode

- 🎯 The most frequent item

- 📌 $x = \{1, 1, 1, 3, 4, 4, 7, 8, 8, 9, 9\}$
 $\text{moda}(x) = 1$

Exercise #8

? Calculate the mode of the following data sets

$$y = \{1, 1, 1, 3, 4, 4, 4, 7, 8, 8, 9, 9\}$$

$$\text{moda}(y) = ?$$

$$z = \{1, 3, 4, 7, 8, 9, 11, 17, 21, 42\}$$

$$\text{moda}(z) = ?$$

00:30

Exercise #8 -- Solution

? Calculate the mode of the following data sets

$$y = \{1, 1, 1, 3, 4, 4, 4, 7, 8, 8, 9, 9\}$$

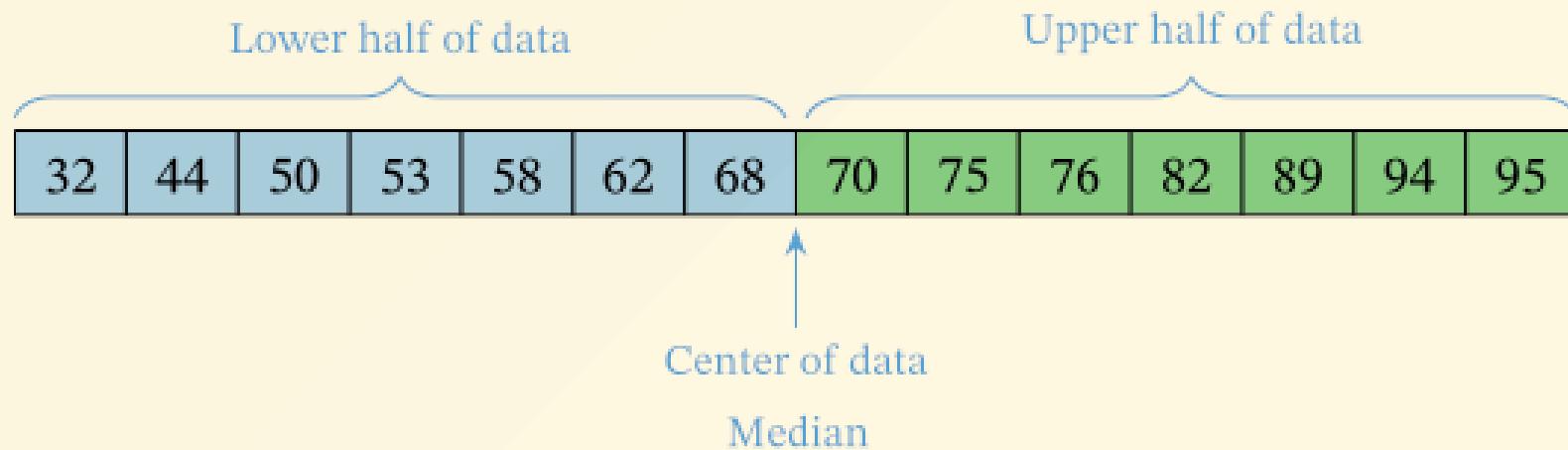
$$\text{moda}(y) = 1 \text{ & } 4$$

$$z = \{1, 3, 4, 7, 8, 9, 11, 17, 21, 42\}$$

$$\text{moda}(z) = \text{It doesn't exist}$$

Measure of central tendency: median

- 🎯 The "middle" value



⚠️ Data should be sorted!

Measure of central tendency: median

🎯 The "middle" value

📌 $n = 7, x = \{1, 3, 3, 6, 7, 8, 9\}$

$$\text{median}(x) = x_{(n+1)/2} = x_{(7+1)/2} = x_4 = 6$$

📌 $n = 8, x = \{1, 2, 3, 4, 5, 6, 8, 9\}$

$$\begin{aligned}\text{median}(x) &= \frac{x_{(n/2)} + x_{((n/2)+1)}}{2} = \frac{x_{(8/2)} + x_{((8/2)+1)}}{2} \\ &= \frac{x_4 + x_5}{2} = \frac{4+5}{2} = 4.5\end{aligned}$$

⚠️ Data should be sorted!

Exercise #9

? Calculate the median of the following data sets

$$y = \{6, 34, 40, 55, 75\}$$

$$\text{median}(y) = ?$$

$$z = \{6, 34, 40, 55, 175\}$$

$$\text{median}(z) = ?$$

Exercise #9 -- Solution

? Calculate the median of the following data sets

$$y = \{6, 34, 40, 55, 75\}$$

$$\text{median}(y) = y_3 = 40$$

$$z = \{6, 34, 40, 55, 175\}$$

$$\text{median}(z) = ?$$



Data should be sorted!

Exercise #9 -- Solution

- ? Calculate the median of the following data sets

$$y = \{6, 34, 40, 55, 75\}$$

$$\text{median}(y) = y_3 = 40$$

$$z = \{6, 34, 40, 55, 175\}$$

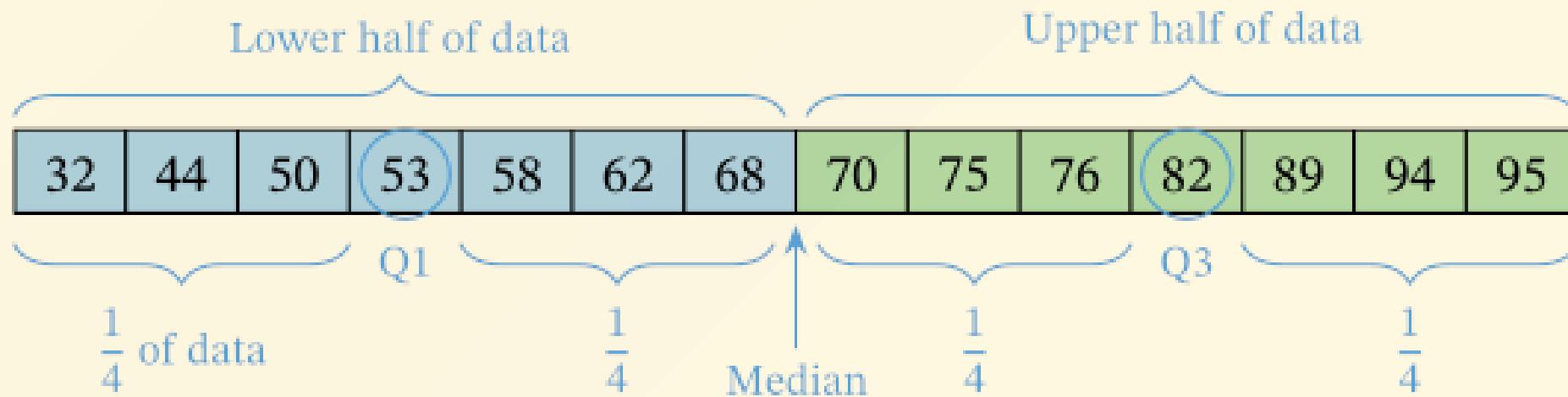
$$\text{median}(z) = z_3 = 40$$

⚠ Data should be sorted!



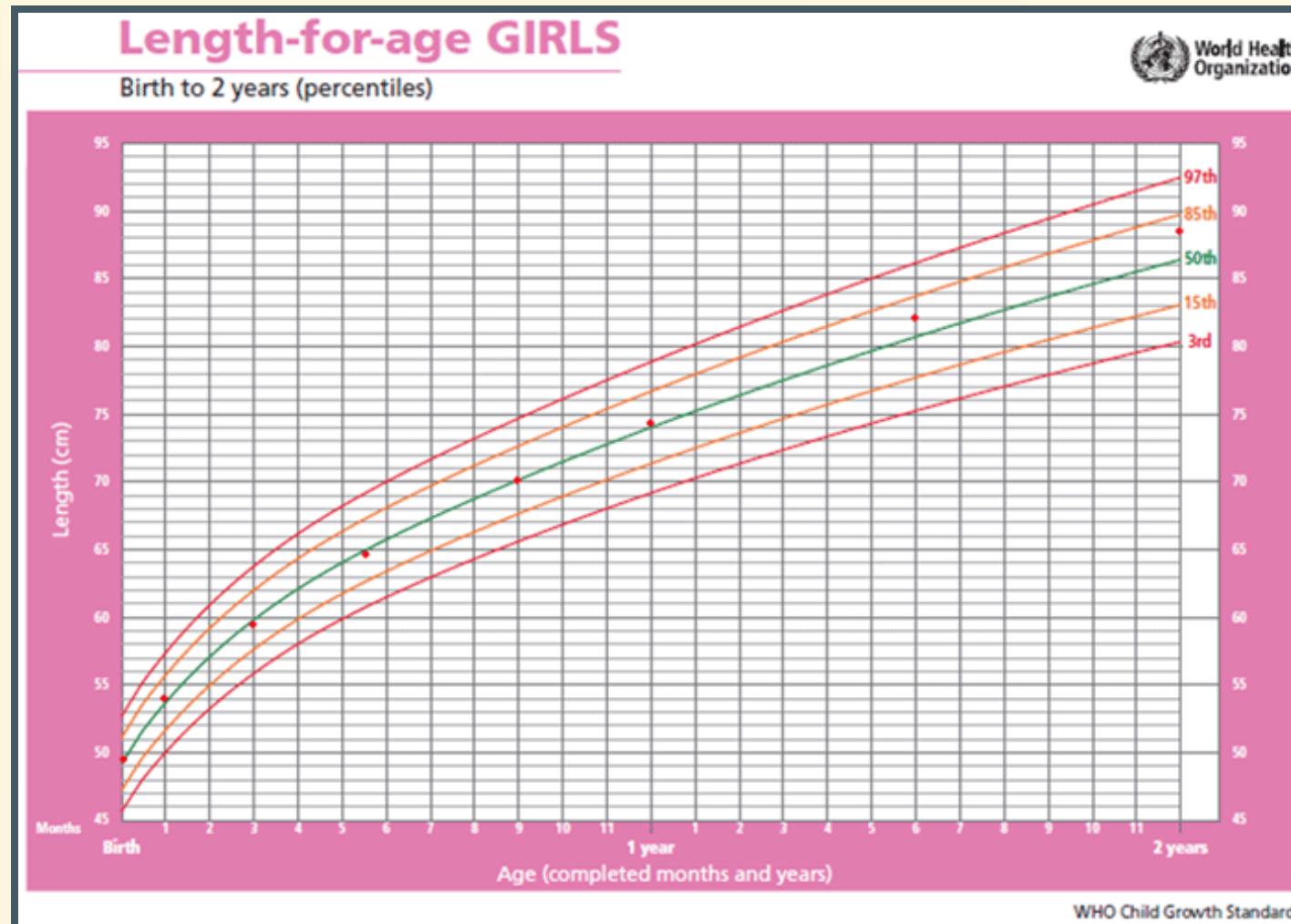
Robust to outliers

Quartiles



⚠ Data should be sorted!

Percentiles



Measure of central tendency: mean

- 🎯 Arithmetic mean

$$\bar{x} = \frac{1}{n} \left(\sum_{i=1}^n x_i \right) = \frac{x_1 + x_2 + \cdots + x_n}{n}$$

- 📌 $x = \{4, 36, 45, 50, 75\}$

$$\bar{x} = \frac{1}{n} \left(\sum_{i=1}^n x_i \right) = \frac{4+36+45+50+75}{5} = 42$$

Exercise #10

? Calculate the mean of the following data sets

$$y = \{6, 34, 40, 55, 75\}$$

$$\bar{y} = ?$$

$$z = \{6, 34, 40, 55, 175\}$$

$$\bar{z} = ?$$

02:00

Exercise #10 -- Solution

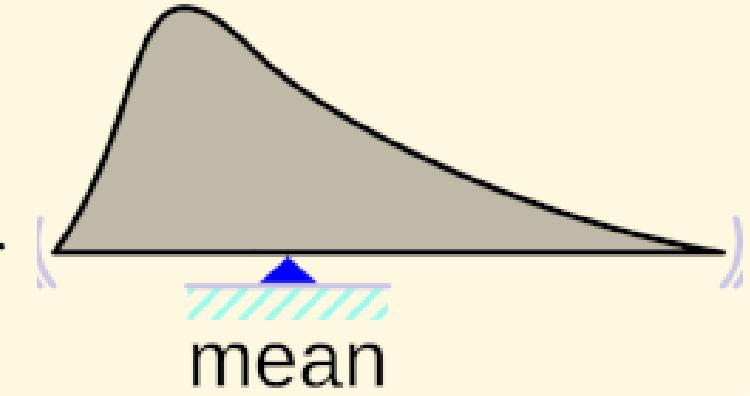
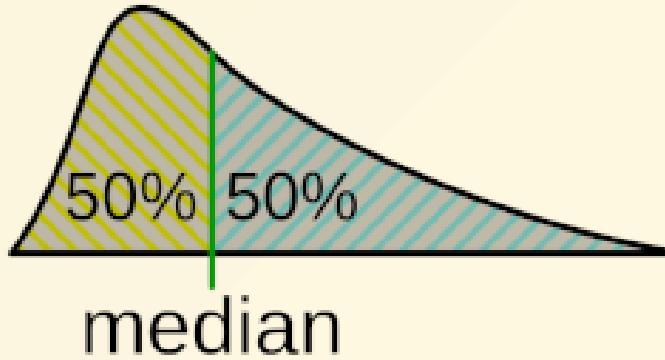
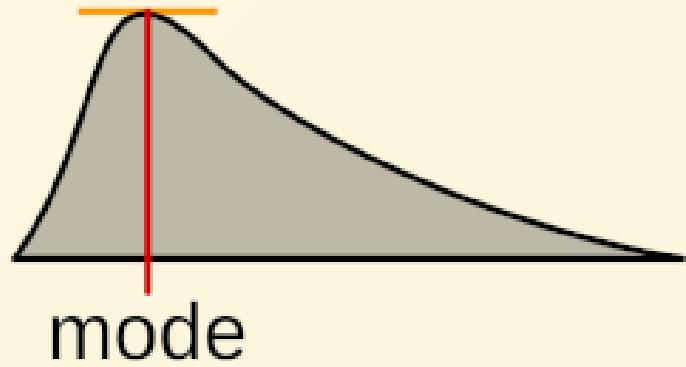
- ? Calculate the mean of the following data sets

$$y = \{6, 34, 40, 55, 75\}$$
$$\bar{y} = \frac{1}{n} \left(\sum_{i=1}^n y_i \right) = \frac{6+34+40+55+75}{5} = 42$$

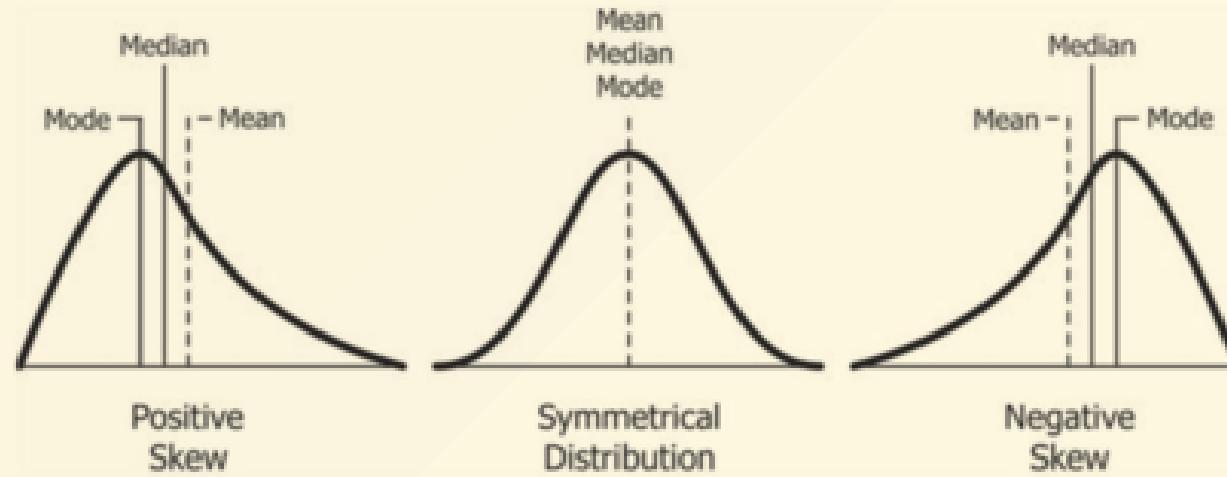
$$z = \{6, 34, 40, 55, 175\}$$
$$\bar{z} = \frac{1}{n} \left(\sum_{i=1}^n z_i \right) = \frac{4+36+45+50+175}{5} = 62$$

- 🎯 Not robust to outliers

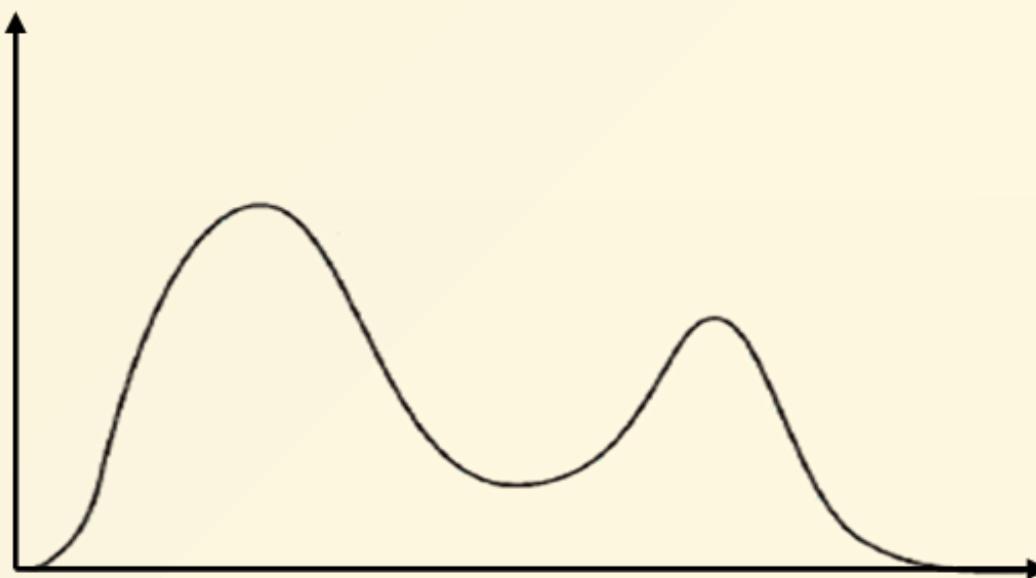
Mode vs median vs mean



The shape of a distribution



The shape of a distribution



Exercise 11

- ? In the results section, the authors reported the following

The mean length of stay was 22.4 days (median: 14 days).

The shape of the distribution is...

- a) symmetric
- b) positive skew
- c) negative skew
- d) I need more information to answer

Exercise 11 -- Solution

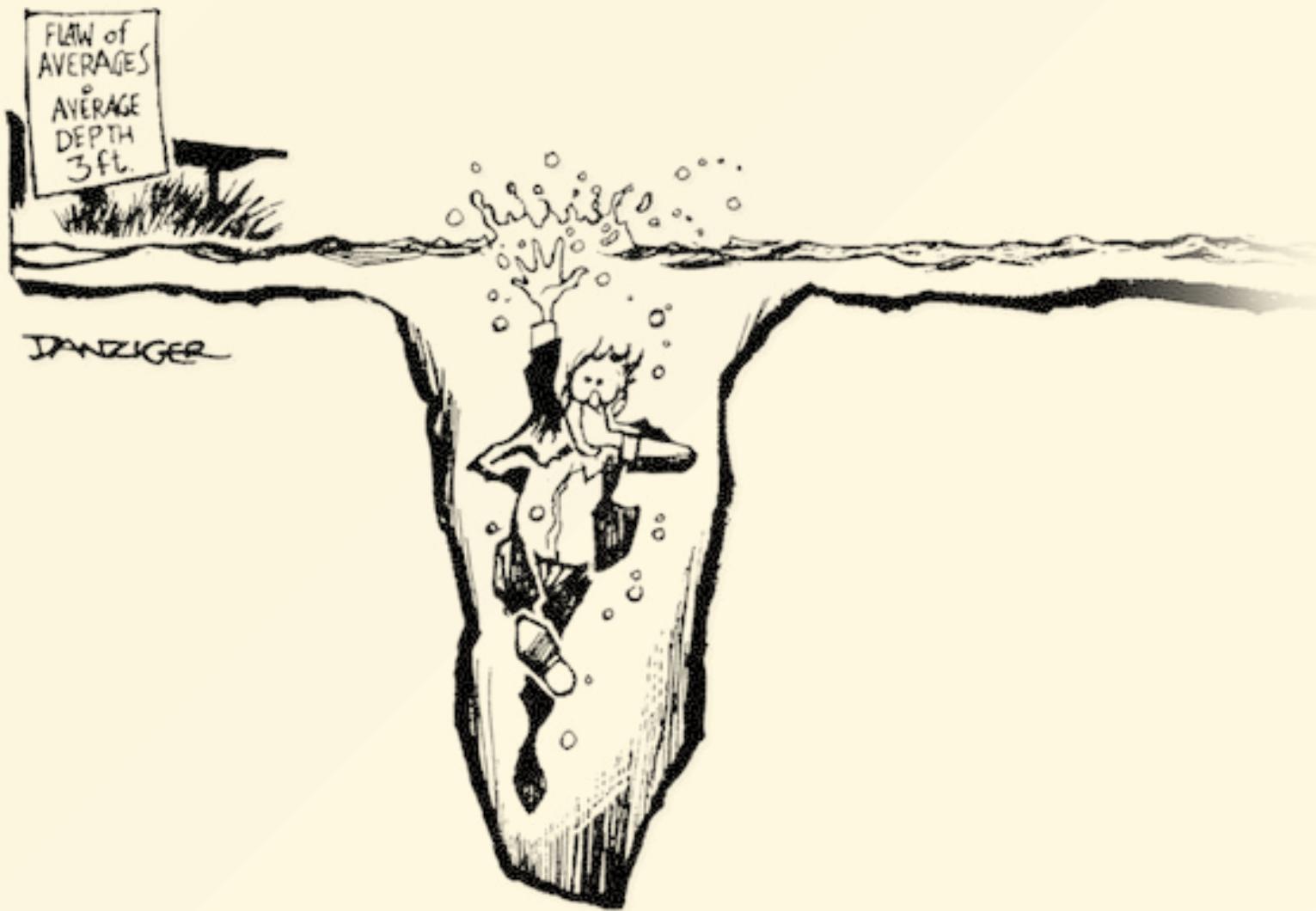
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The mean length of stay was 22.4 days (median: 14 days).

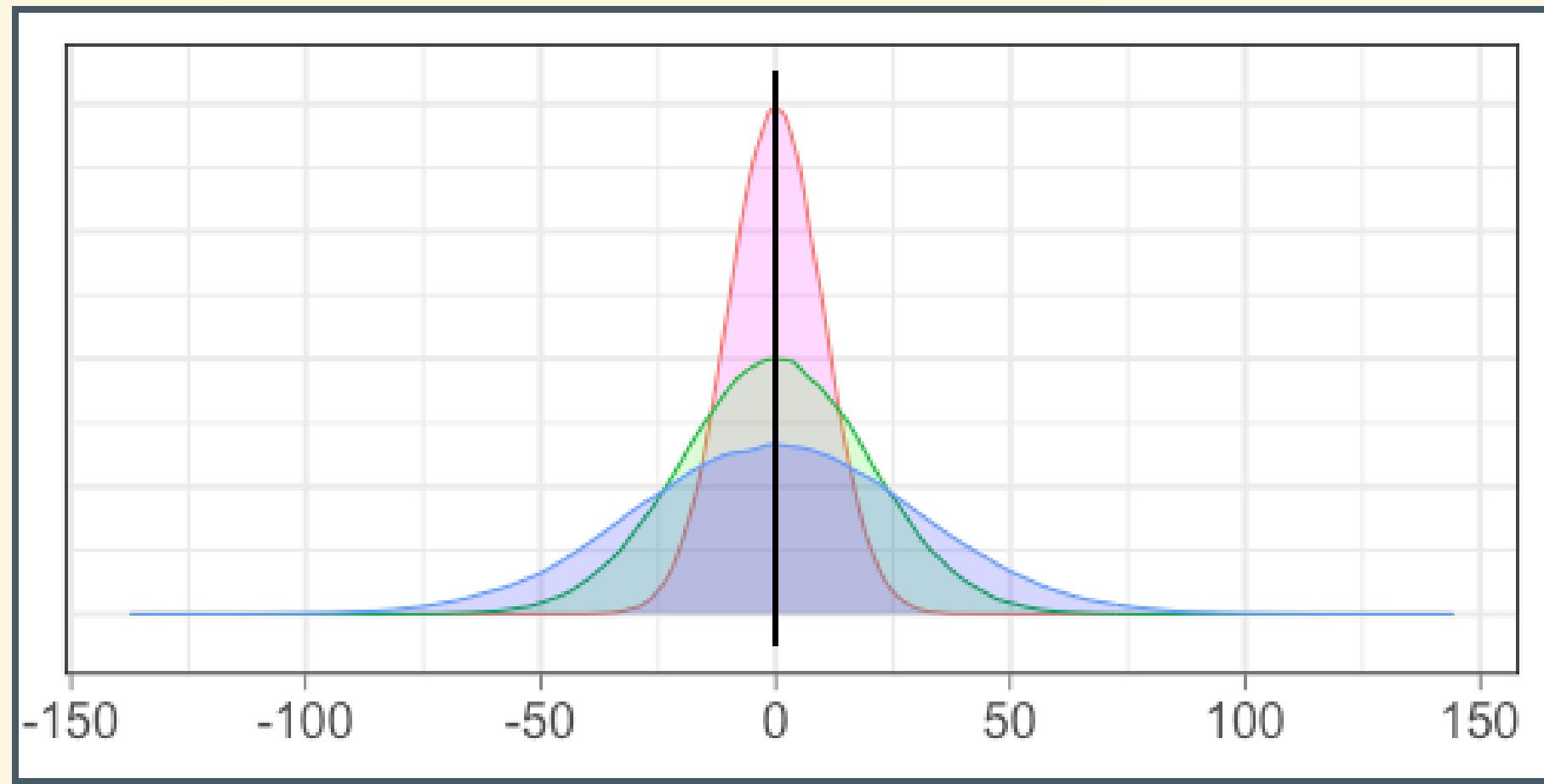
The shape of the distribution is...

- a) symmetric
- b) positive skew
- c) negative skew
- d) I need more information to answer

Measures of dispersion

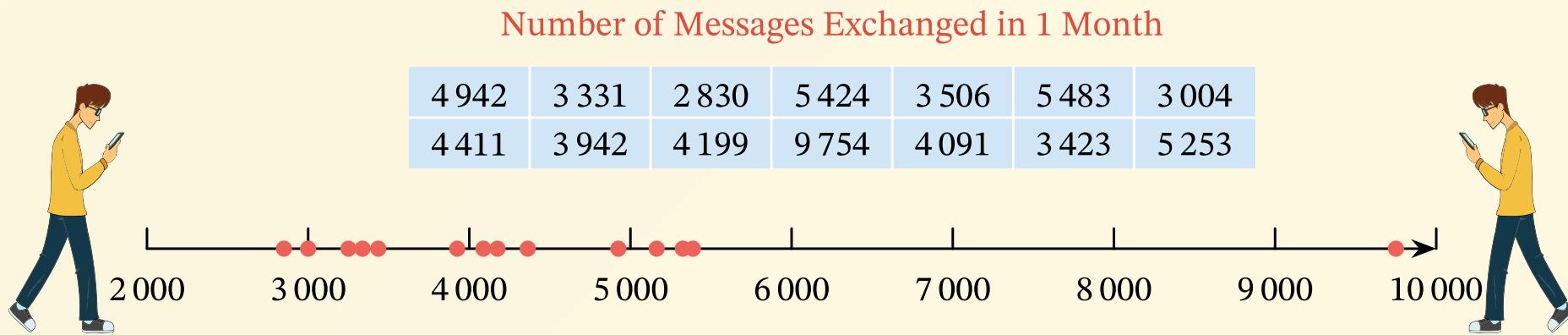


Measures of dispersion



Measure of dispersion: range

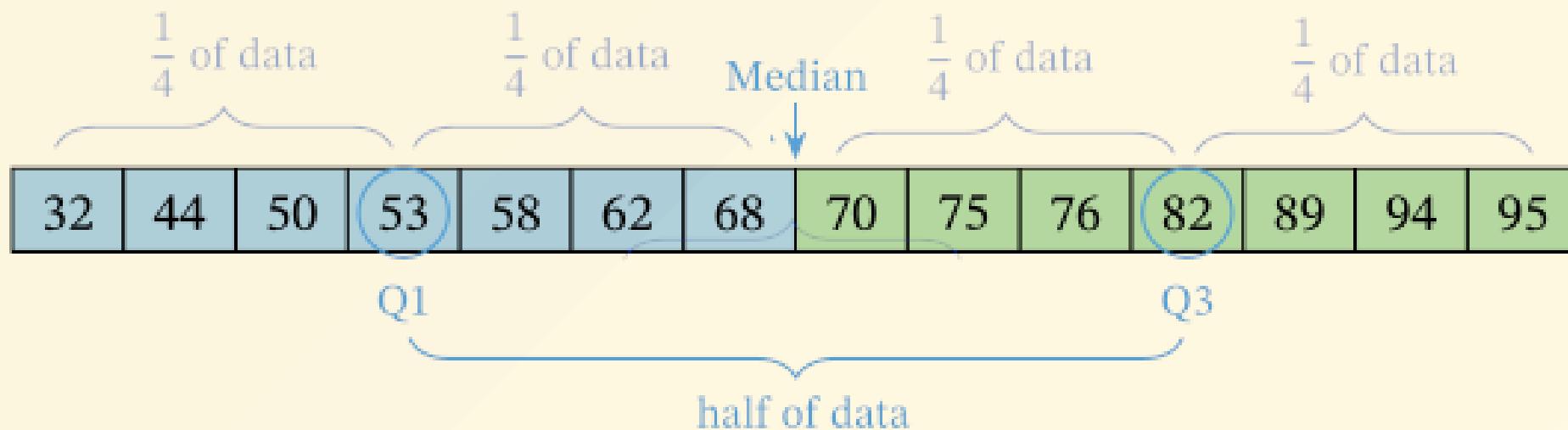
🎯 $\text{range}(x) = \max(x) - \min(x)$



$$\text{range}(x) = \max(x) - \min(x) = 9,754 - 2,830 = 6,924$$

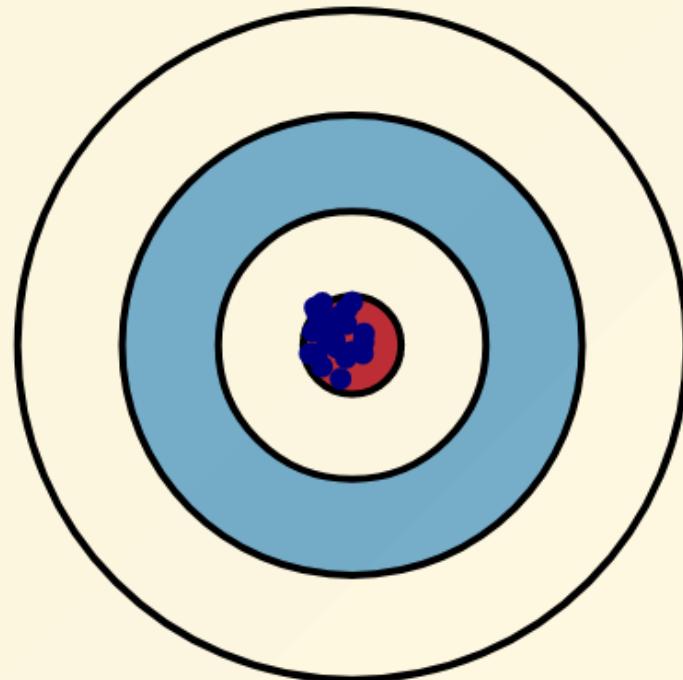
Measure of dispersion: interquartile range


$$\text{IQR}(x) = \text{Q3}(x) - \text{Q1}(x)$$

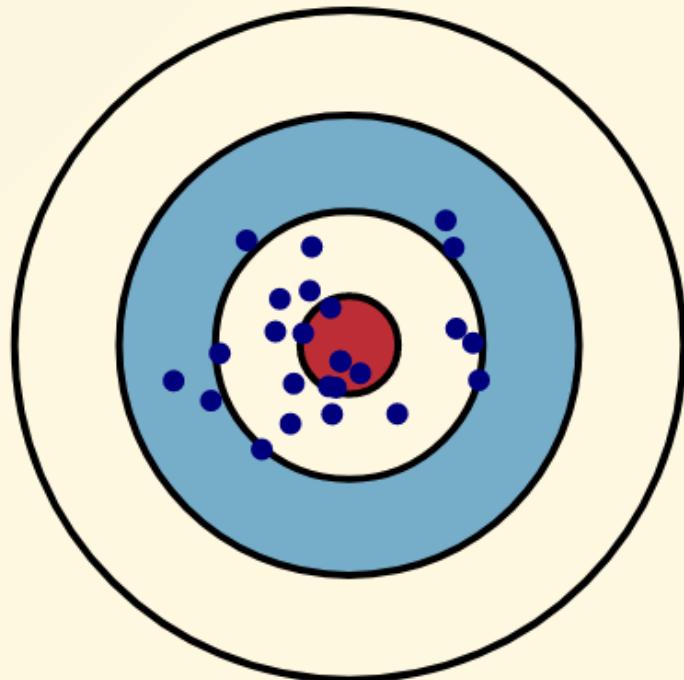


Measure of dispersion: variance

Low Variance



High Variance



Measure of dispersion: variance


$$s^2 = \frac{1}{n-1} \sum_{i=1}^n (x_i - \bar{x})^2$$

where $\bar{x} = \frac{1}{n} \left(\sum_{i=1}^n x_i \right)$


$$x = \{1, 2, 3\} \quad \bar{x} = \frac{1+2+3}{3} = 2$$

$$\begin{aligned} s &= \frac{1}{3-1} \times [(1-2)^2 + (2-2)^2 + (3-2)^2] = \\ &= \frac{1}{2} \times [1^2 + 0^2 + 1^2] = \frac{1}{2} \times 2 = 1 \end{aligned}$$

Measure of dispersion: standard deviation


$$s = \sqrt{s^2} = \sqrt{\frac{1}{n-1} \sum_{i=1}^n (x_i - \bar{x})^2}$$

where $\bar{x} = \frac{1}{n} (\sum_{i=1}^n x_i)$


$$x = \{1, 2, 3\} \quad \bar{x} = \frac{1+2+3}{3} = 2$$

$$\begin{aligned} s &= \sqrt{\frac{1}{3-1} \times [(1-2)^2 + (2-2)^2 + (3-2)^2]} = \\ &= \sqrt{\frac{1}{2} \times [1^2 + 0^2 + 1^2]} = \sqrt{\frac{1}{2} \times 2} = \sqrt{1} = 1 \end{aligned}$$

Centrality, dispersion, and data types

Data type	Centrality Measure	Dispersion Measure
Nominal	Mode	-
Ordinal	Mode, Median	Range, IQR
Numeric	Mode, Median, Mean	Range, IQR, standard deviation

Exercise #12

- ? In the results section, the authors reported the following

Coronary-artery calcium scores averaged 68.9 ± 244.2 (range 0 to 1526) in patients and 8.8 ± 41.8 (range 0 to 243.4) in controls.

Which measures do we use to describe this variable?

- a) mean and standard deviation
- b) median and interquartile range
- c) median and standard deviation
- d) I need more information to answer

Exercise #12 -- Solution

- ? In the results section, the authors reported the following

Coronary-artery calcium scores averaged 68.9 ± 244.2 (range 0 to 1526) in patients and 8.8 ± 41.8 (range 0 to 243.4) in controls.

Which measures do we use to describe this variable?

- a) mean and standard deviation
- b) median and interquartile range
- c) median and standard deviation
- d) I need more information to answer

Outliers in the wild

TABLE 3. Length of In-Patient Stay, by Surgical Procedure

Procedure	No. of procedures	Length of stay, d	
		Mean \pm SD	Median (IQR)
Breast surgery	1,338	3.3 \pm 4.4	3 (0-5)
Coronary artery bypass graft	570	9.6 \pm 15.2	8 (7-9)
Cesarean section	4,831	4.9 \pm 6.4	4 (3-5)
Repair of fractured neck of femur	2,303	13.8 \pm 12.2	10 (7-17)
Hip replacement	6,432	8.7 \pm 5.9	7 (6-9)
Abdominal hysterectomy	1,484	5.4 \pm 4.0	5 (4-6)
Knee replacement	4,483	8.2 \pm 5.0	7 (6-9)
Major vascular surgery	269	22.4 \pm 23.1	14 (8-30)
Overall	21,710	7.8 \pm 8.0	6 (4- 9)

The mean length of stay was 7.8 days but was greatly influenced by 2 patients with lengths of stay of almost 1 year. The median length of stay was 6 days, with 90% of patients discharged within 14 days after the procedure. Table 3 displays measures of central tendency (mean and median values) and dispersion (SDs and interquartile ranges) for the length of stay for each type of surgical procedure.

Parameters vs statistics

- Parameters: calculated on the population
- Statistics: calculated on the sample

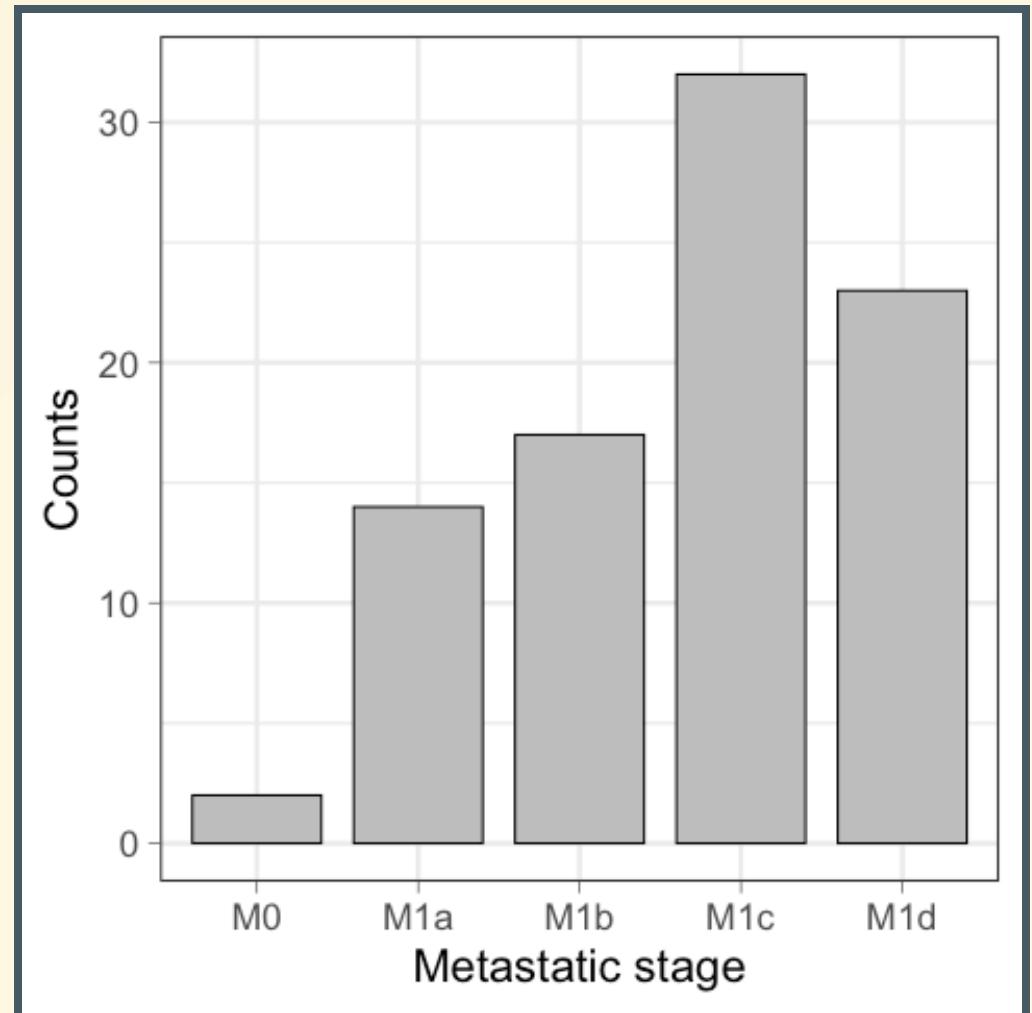
	Parameter	Statistic
Size	N	n
Mean	μ	\bar{x}
Standard deviation	σ	s
Proportion	π	p

Notes on data visualization

Bar chart

- categorical data
 - absolute frequency
 - relative frequency

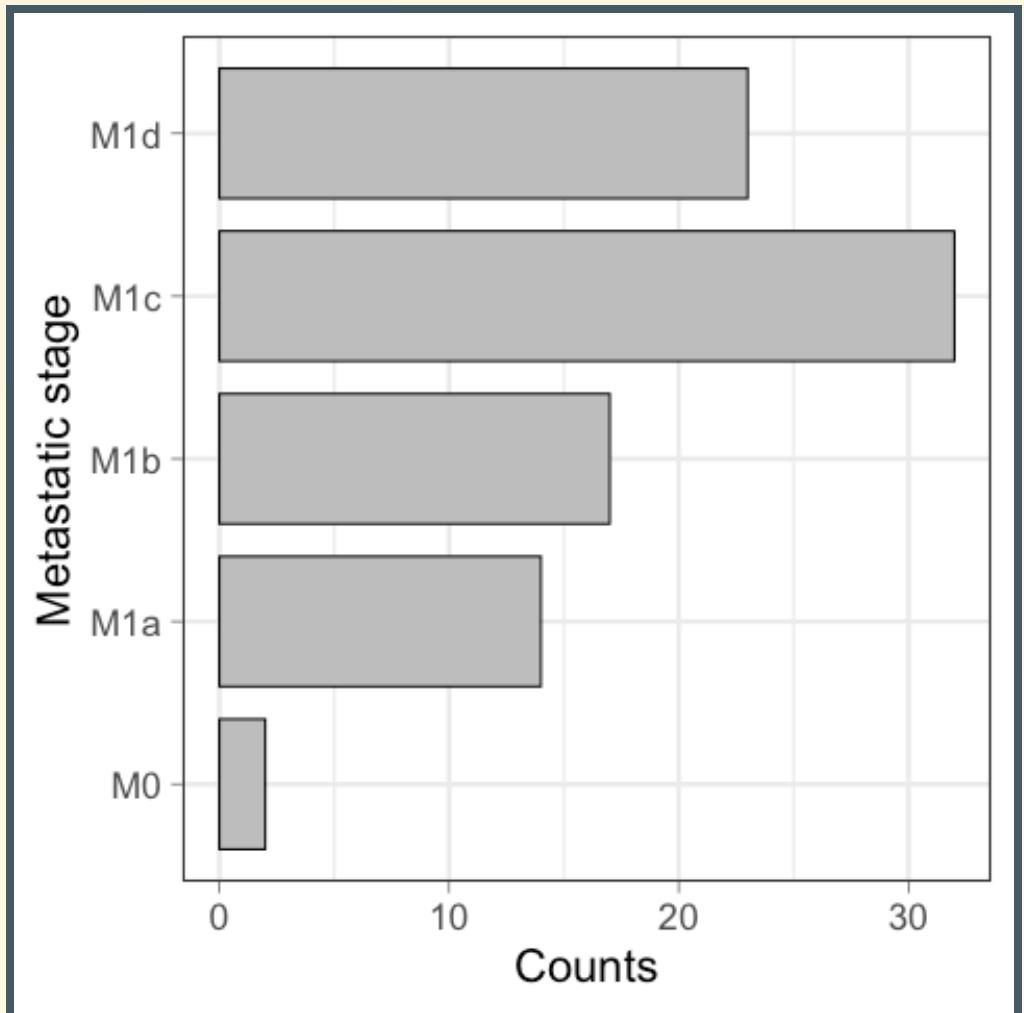
Visconti A., et al., Total serum *N*-glycans associate with response to immune checkpoint inhibition therapy and survival in patients with advanced melanoma, BMC Cancer, 2023 doi:10.1186/s12885-023-10511-3



Horizontal bar chart

- categorical data
 - absolute frequency
 - relative frequency

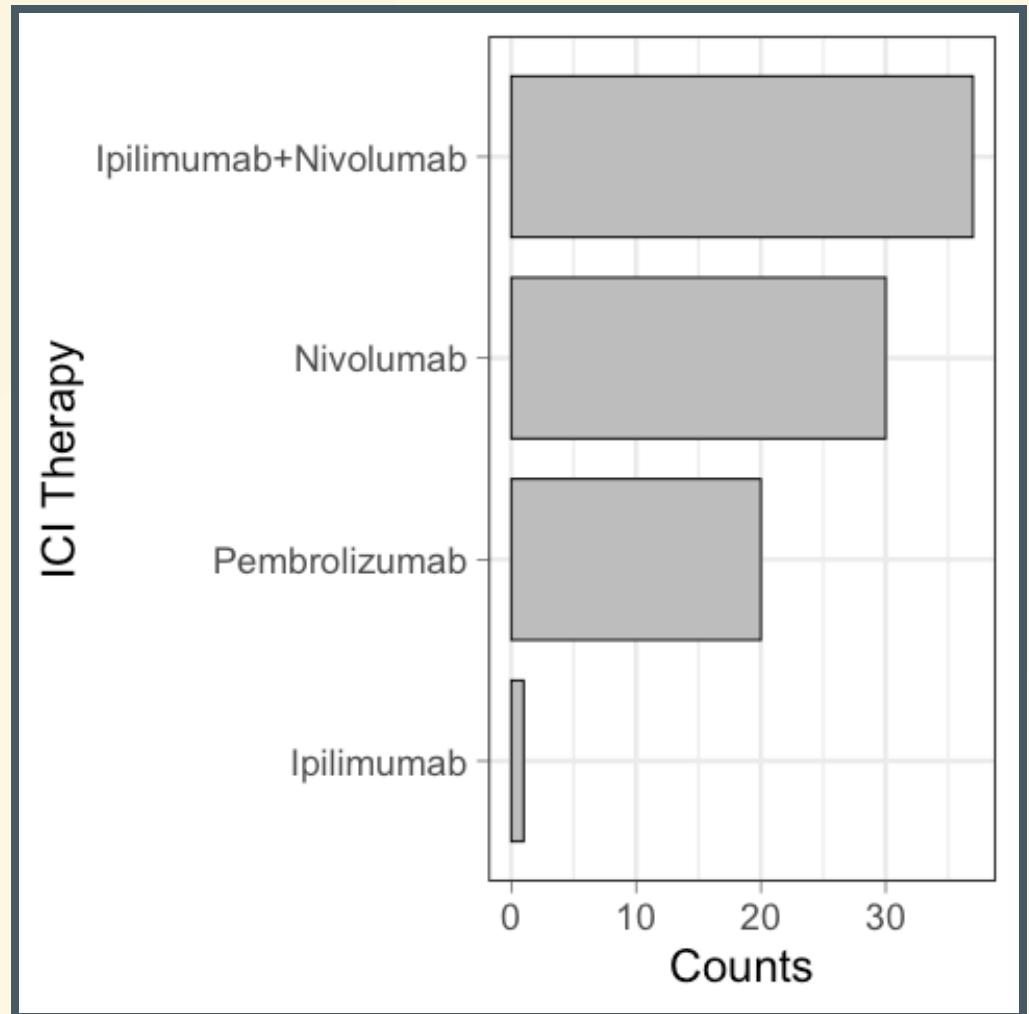
Visconti A., et al., *Total serum N-glycans associate with response to immune checkpoint inhibition therapy and survival in patients with advanced melanoma*, BMC Cancer, 2023 doi:10.1186/s12885-023-10511-3



Horizontal bar chart

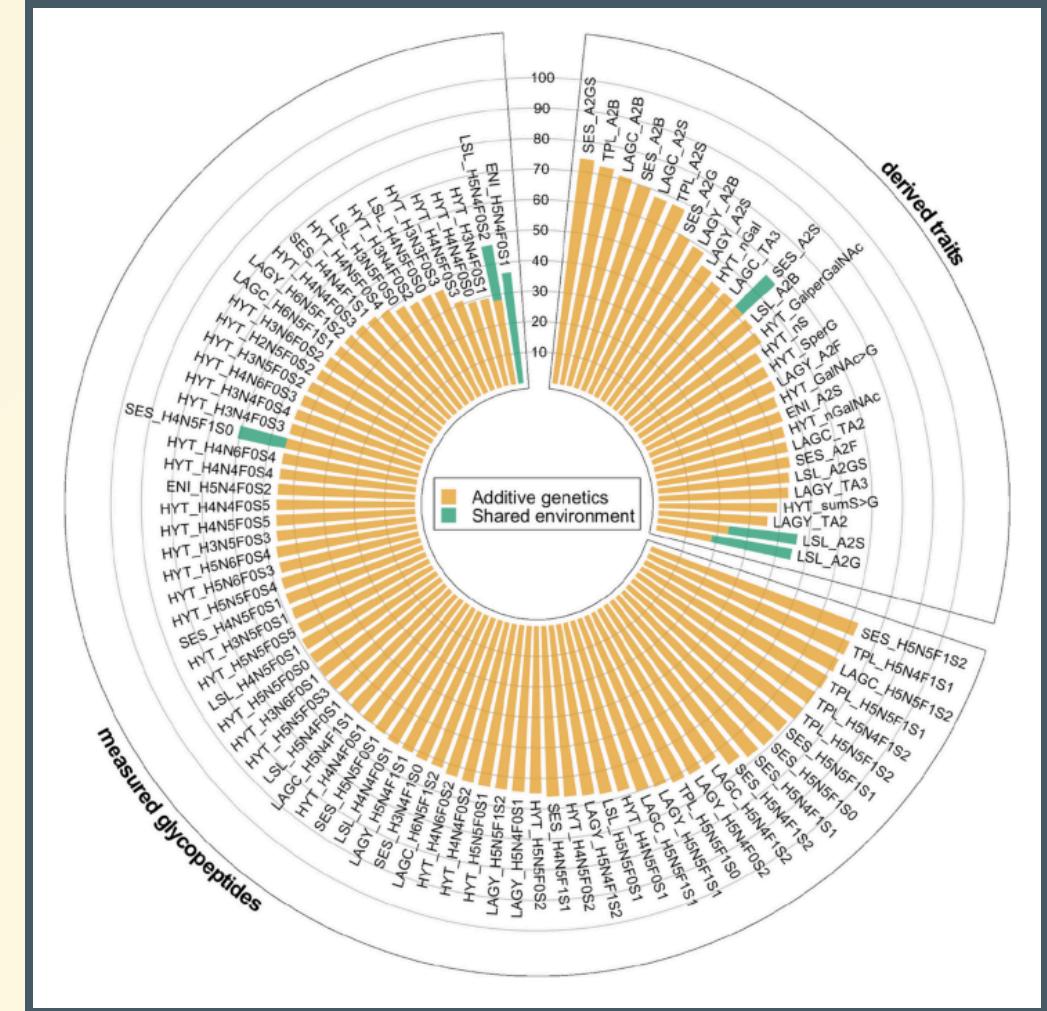
- categorical data
 - absolute frequency
 - relative frequency

Visconti A., et al., *Total serum N-glycans associate with response to immune checkpoint inhibition therapy and survival in patients with advanced melanoma*, BMC Cancer, 2023 doi:10.1186/s12885-023-10511-3



Circular bar chart

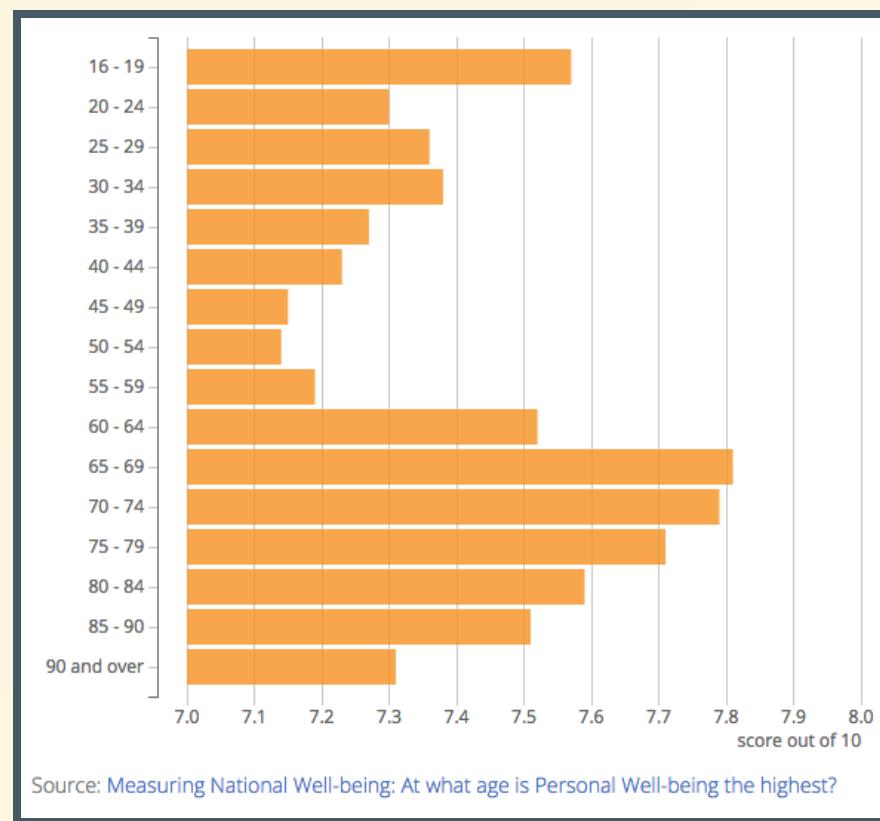
- categorical data
 - absolute frequency
 - relative frequency



Visconti, A., et al.. *The genetics and epidemiology of N-and O-immunoglobulin A glycomics.*, 2024, doi:10.1186/s13073-024-01369-6

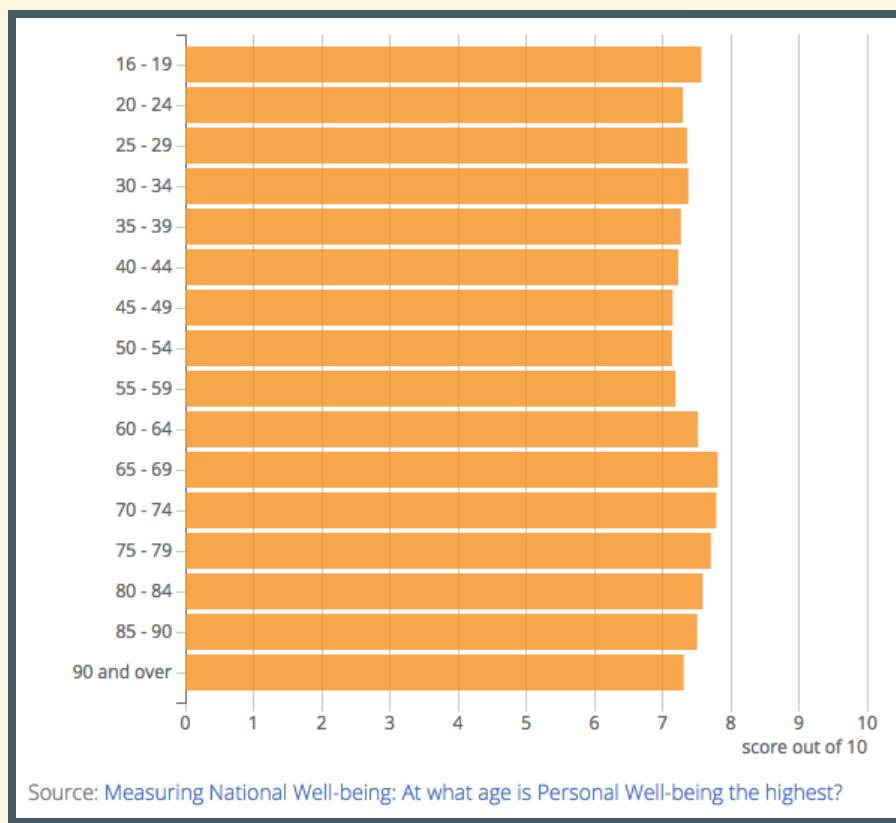
What does this graph tell us?

- From 1 to 10, how happy were you yesterday?



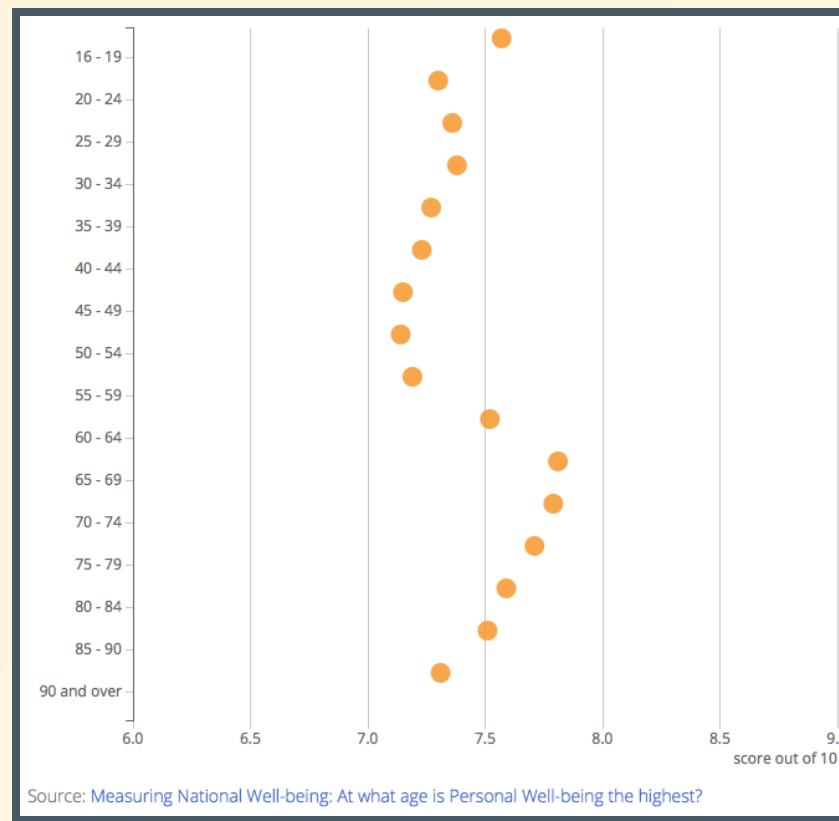
What does this graph tell us?

- From 1 to 10, how happy were you yesterday?



What does this graph tell us?

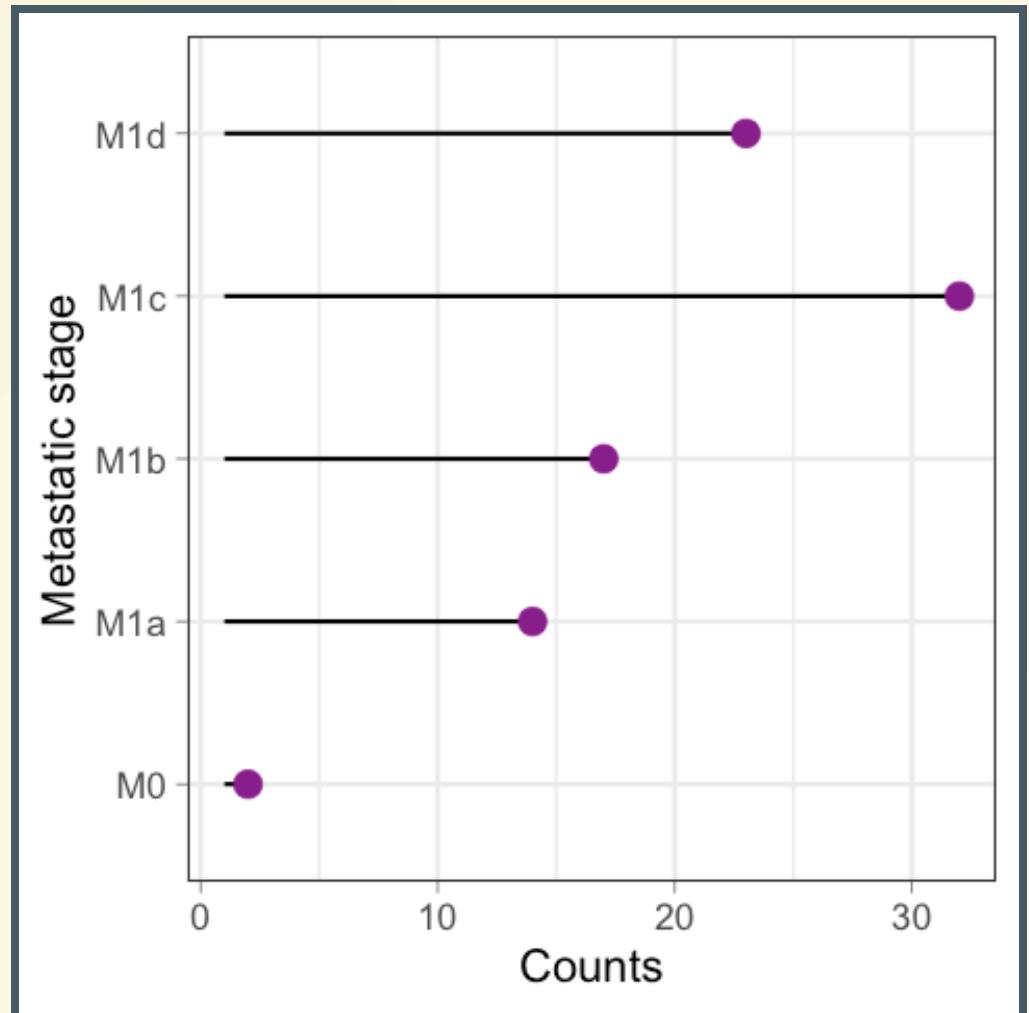
- From 1 to 10, how happy were you yesterday?



Lollipop chart

- categorical data
 - absolute frequency
 - relative frequency

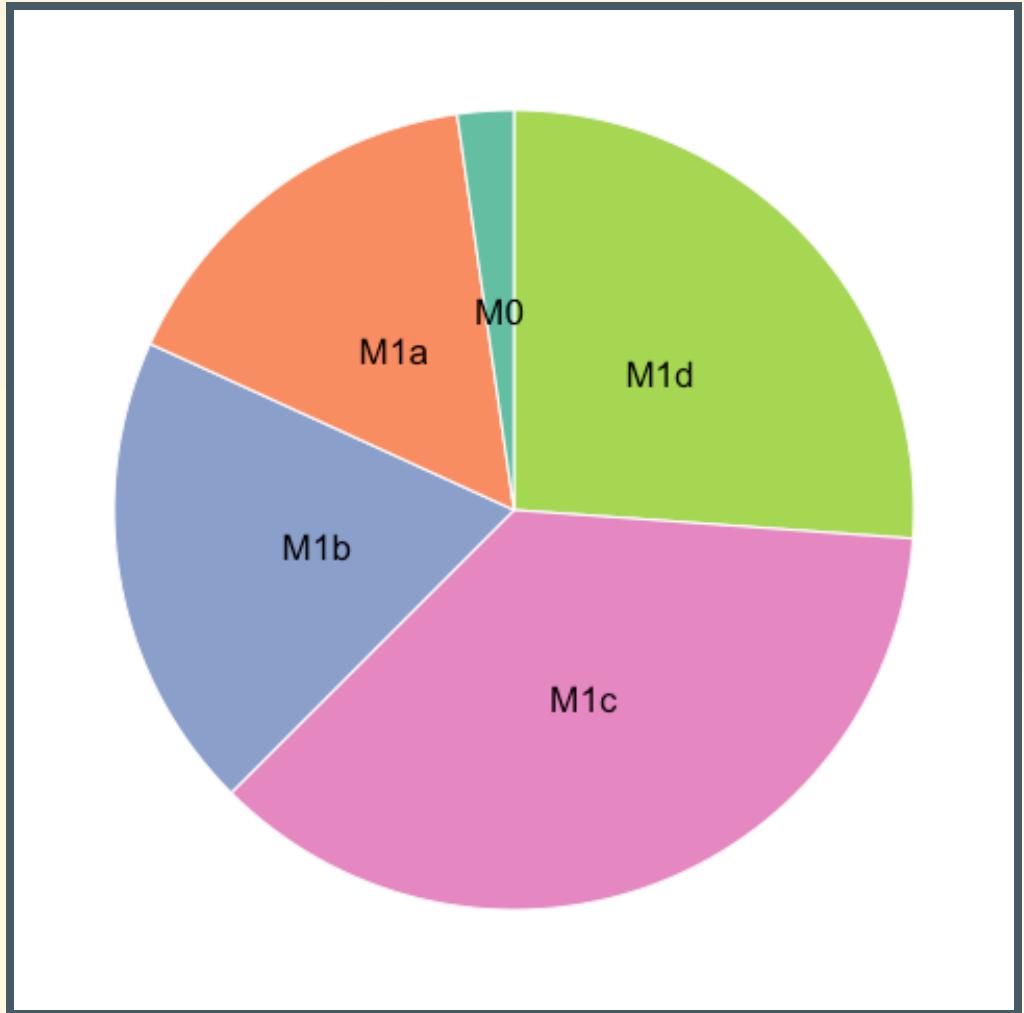
Visconti A., et al., *Total serum N-glycans associate with response to immune checkpoint inhibition therapy and survival in patients with advanced melanoma*, BMC Cancer, 2023 doi:10.1186/s12885-023-10511-3



Pie chart

- categorical data
 - relative frequency

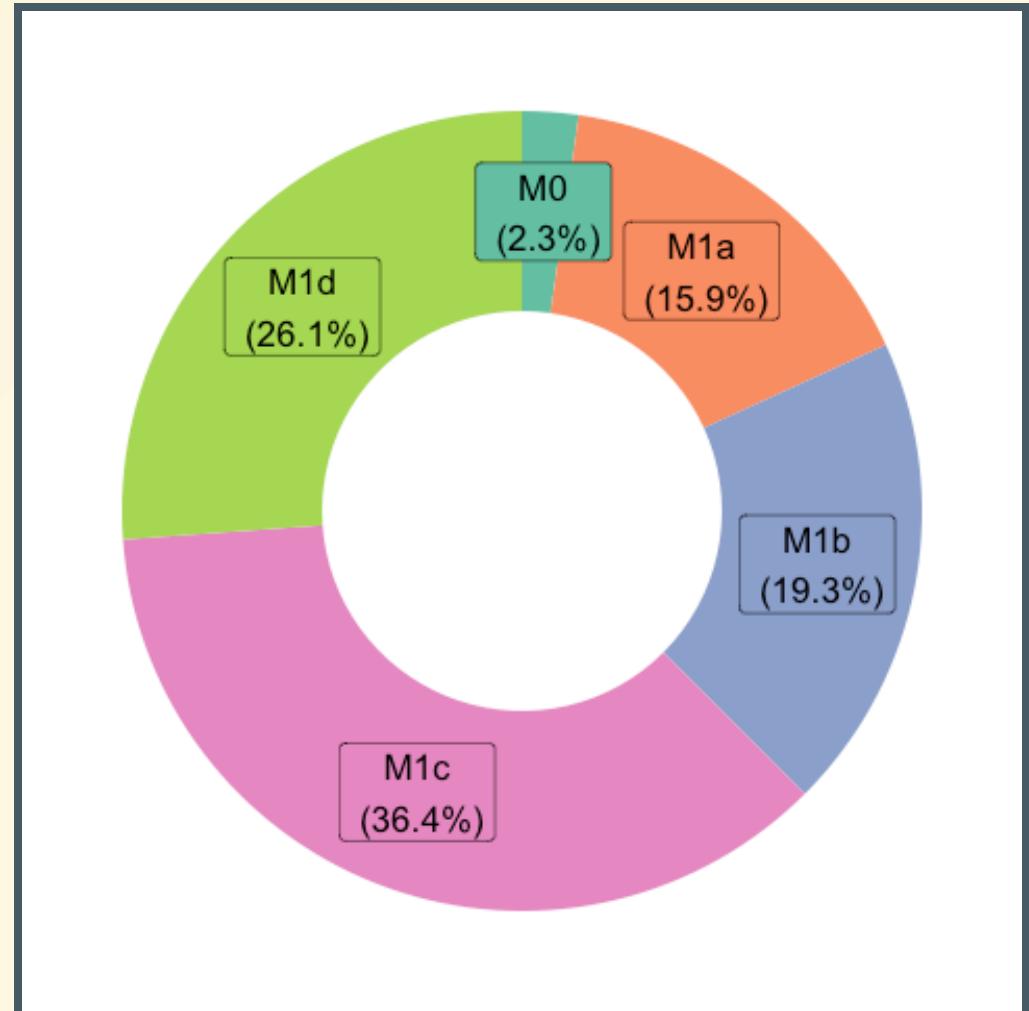
Visconti A., et al., *Total serum N-glycans associate with response to immune checkpoint inhibition therapy and survival in patients with advanced melanoma*, BMC Cancer, 2023 doi:10.1186/s12885-023-10511-3



Donut chart

- categorical data
 - relative frequency

Visconti A., et al., *Total serum N-glycans associate with response to immune checkpoint inhibition therapy and survival in patients with advanced melanoma*, BMC Cancer, 2023 doi:10.1186/s12885-023-10511-3



Waffle chart

- categorical data
 - relative frequency

Visconti A., et al., Total serum N-glycans associate with response to immune checkpoint inhibition therapy and survival in patients with advanced melanoma, BMC Cancer, 2023 doi:10.1186/s12885-023-10511-3



Infographics

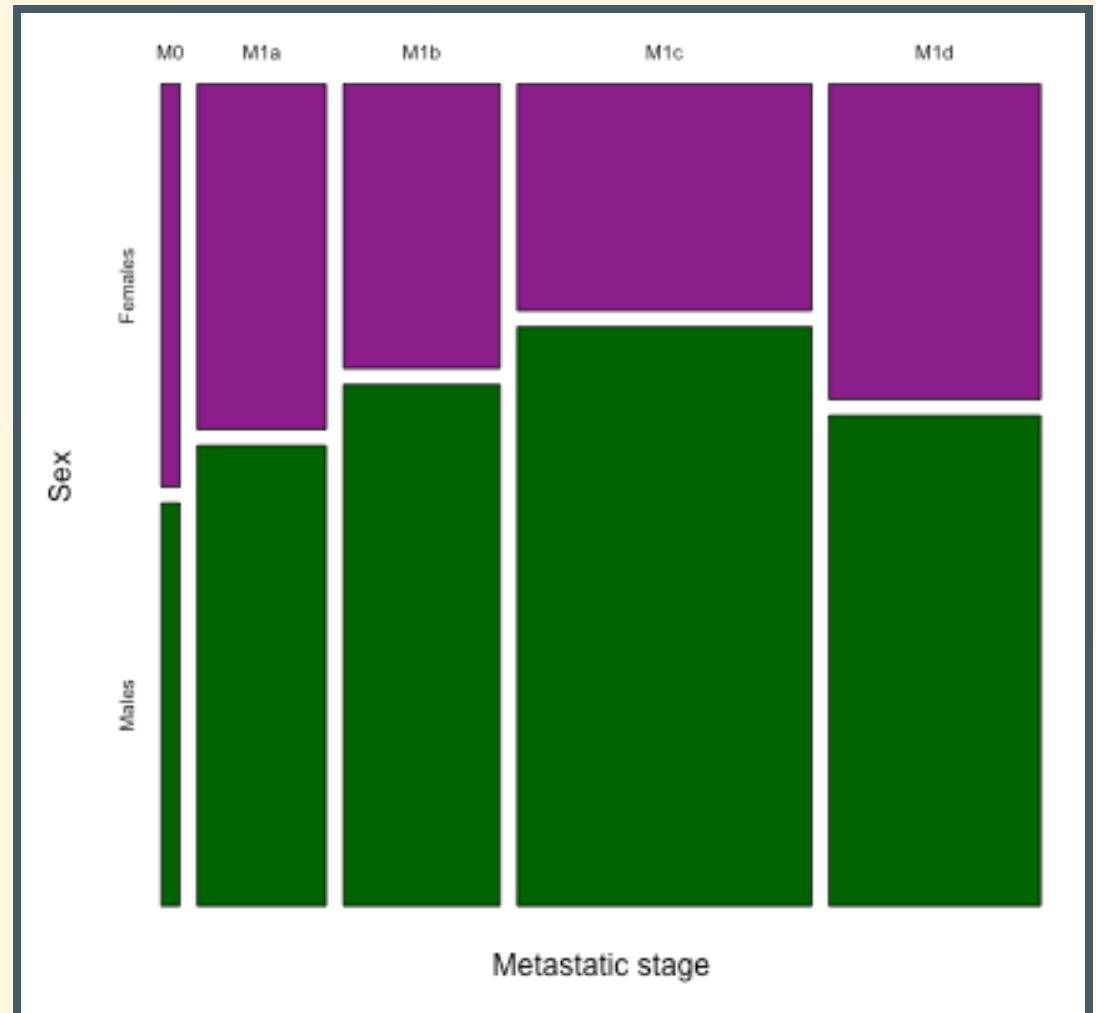


Spiegelhalter, D., *The Art of Statistics: Learning From Data*, Pelican, 2019

Mosaic plot

- categorical data
 - relative frequency

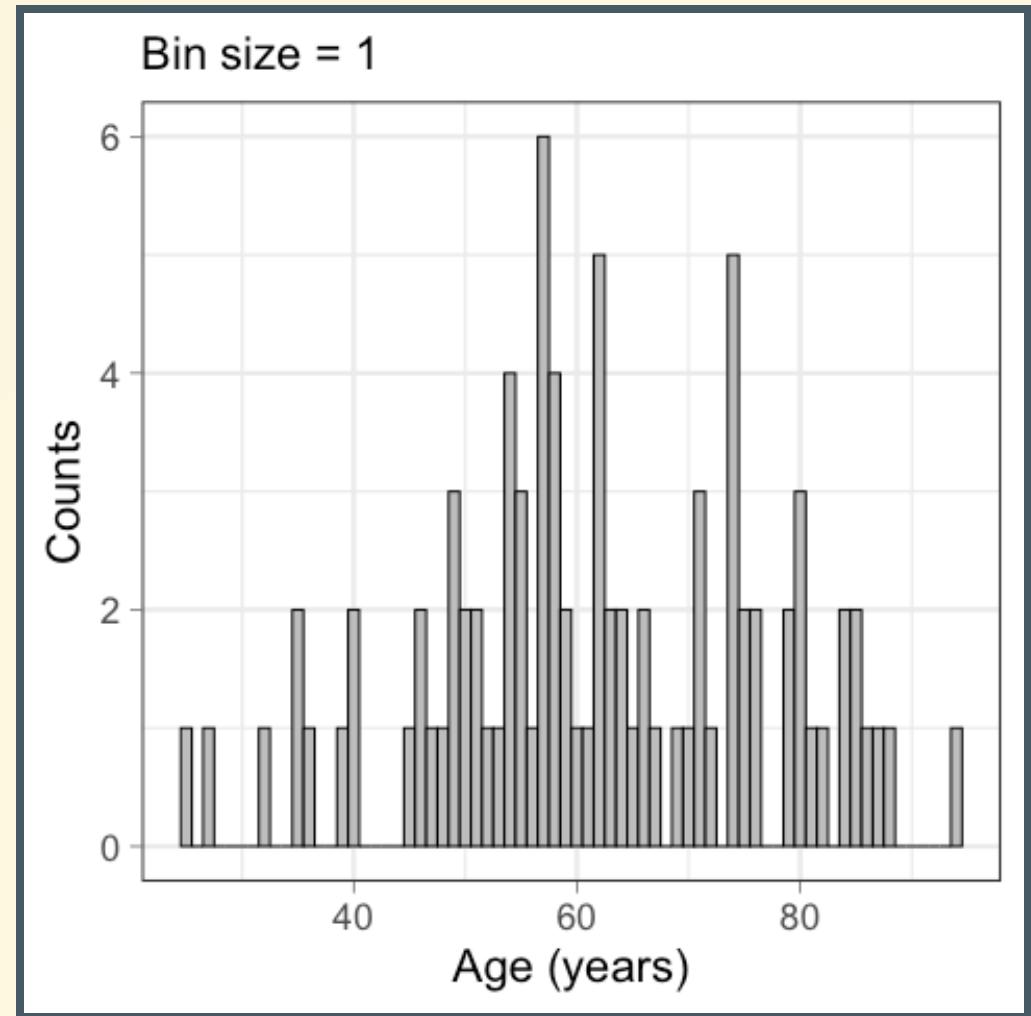
Visconti A., et al., Total serum N-glycans associate with response to immune checkpoint inhibition therapy and survival in patients with advanced melanoma, BMC Cancer, 2023 doi:10.1186/s12885-023-10511-3



Histogram

- numerical data

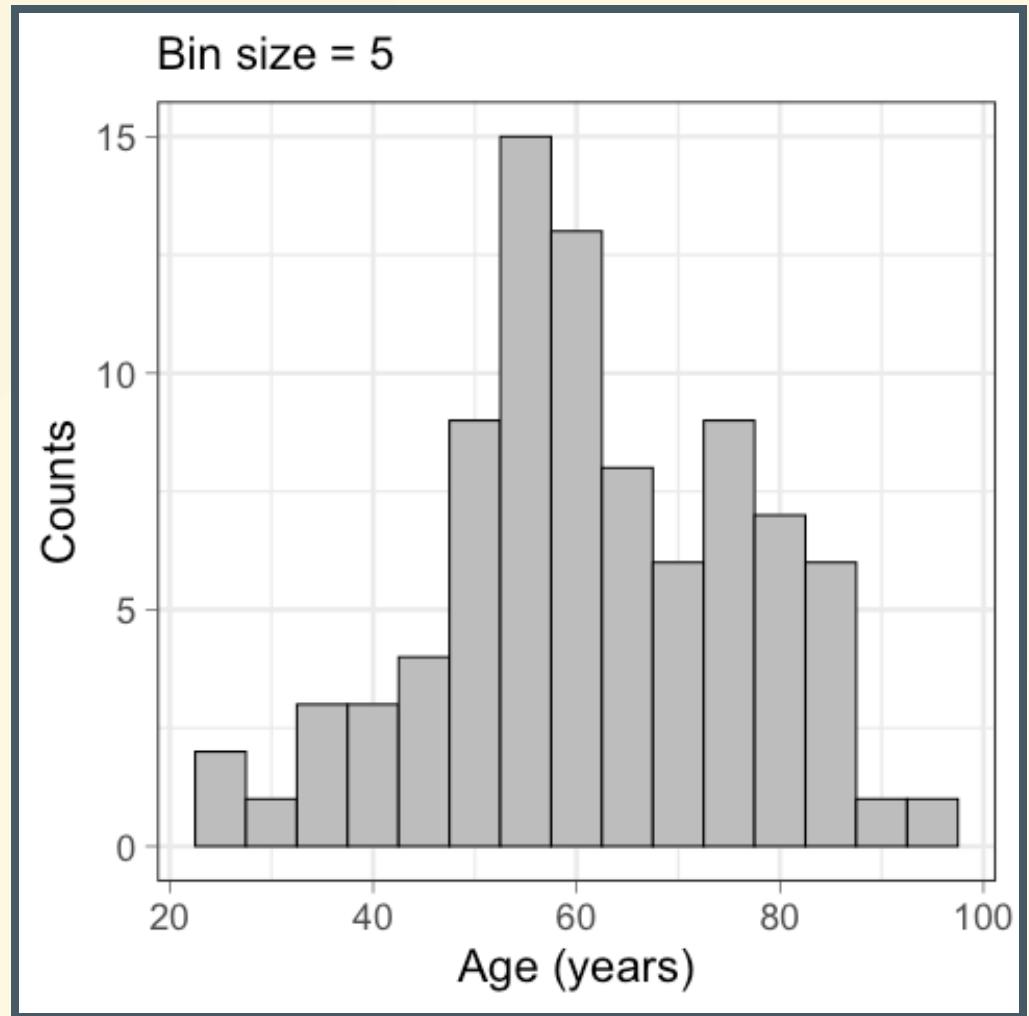
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Histogram

- numerical data

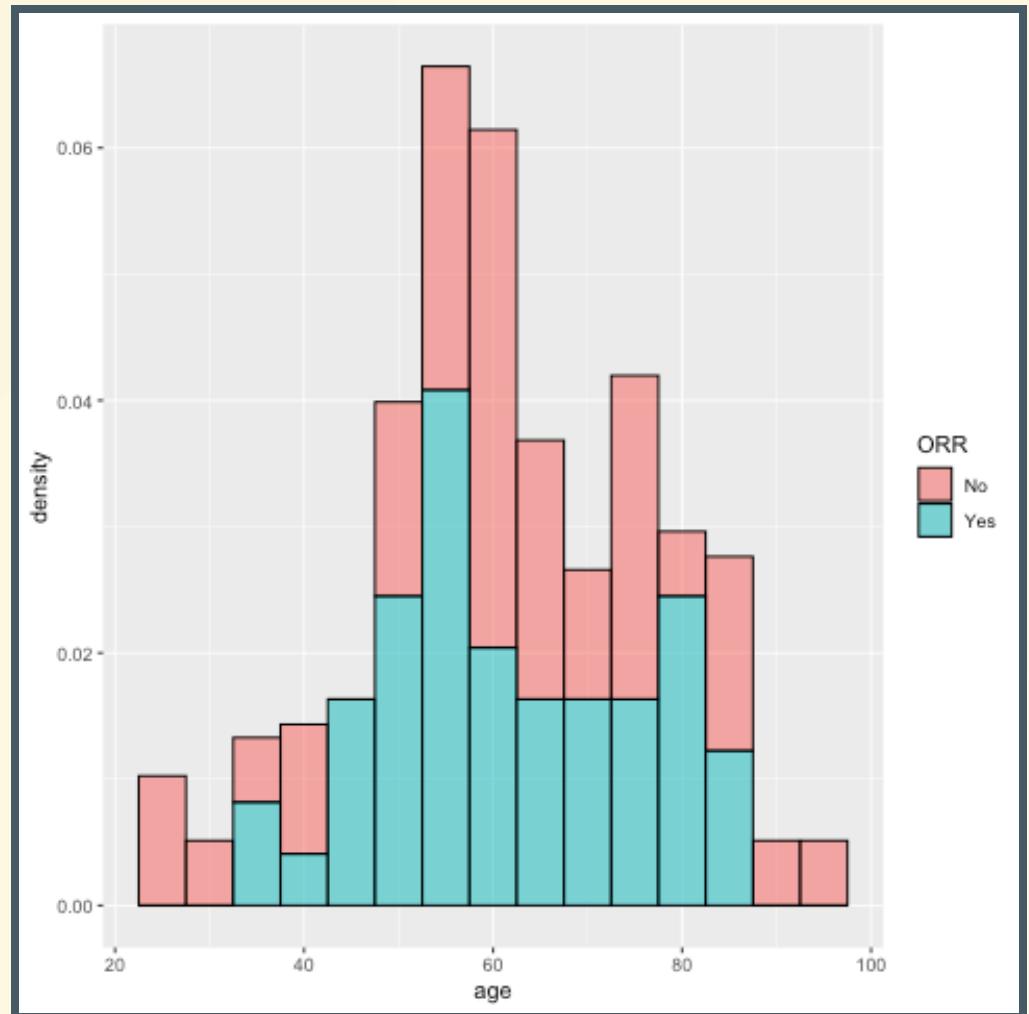
Visconti A., et al., Total serum N-glycans associate with response to immune checkpoint inhibition therapy and survival in patients with advanced melanoma, BMC Cancer, 2023 doi:10.1186/s12885-023-10511-3



Histogram

- numerical data

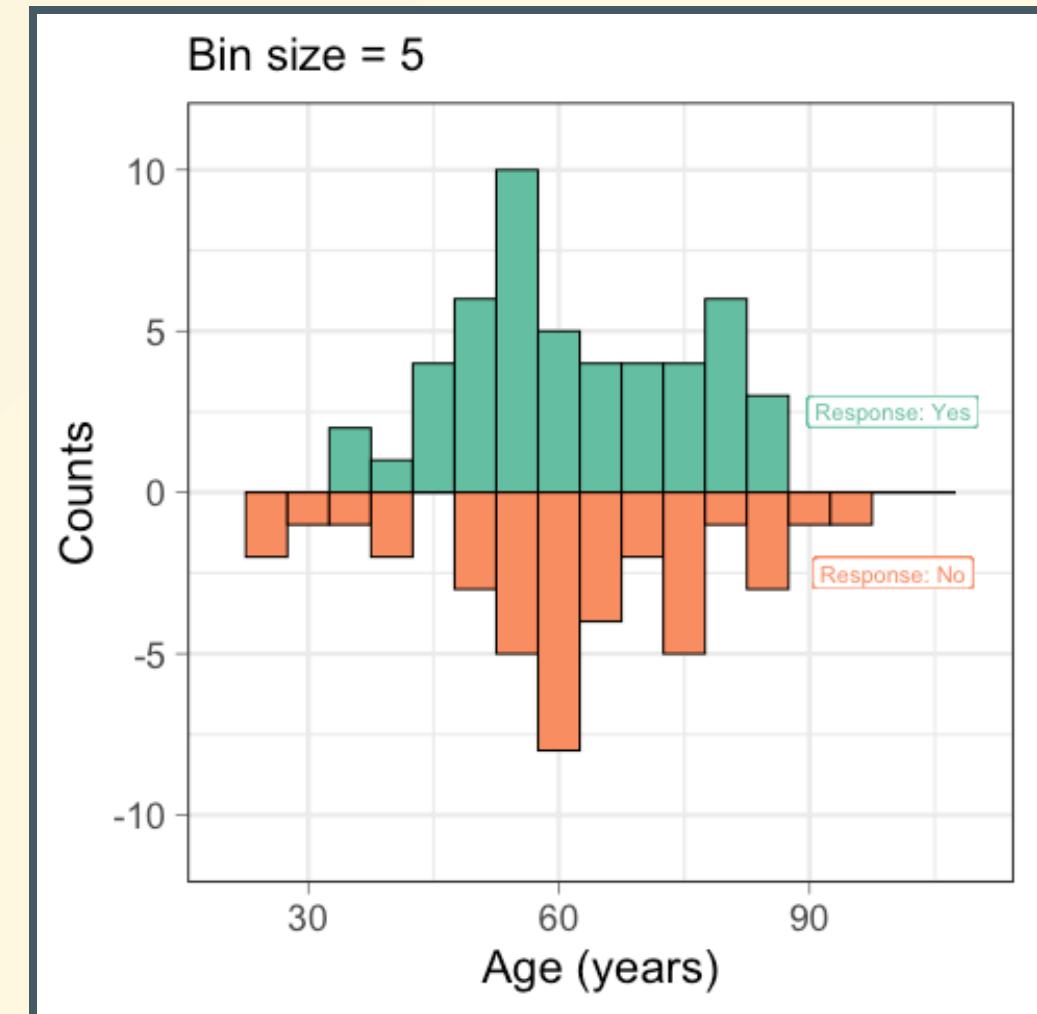
Visconti A., et al., Total serum N-glycans associate with response to immune checkpoint inhibition therapy and survival in patients with advanced melanoma, BMC Cancer, 2023 doi:10.1186/s12885-023-10511-3



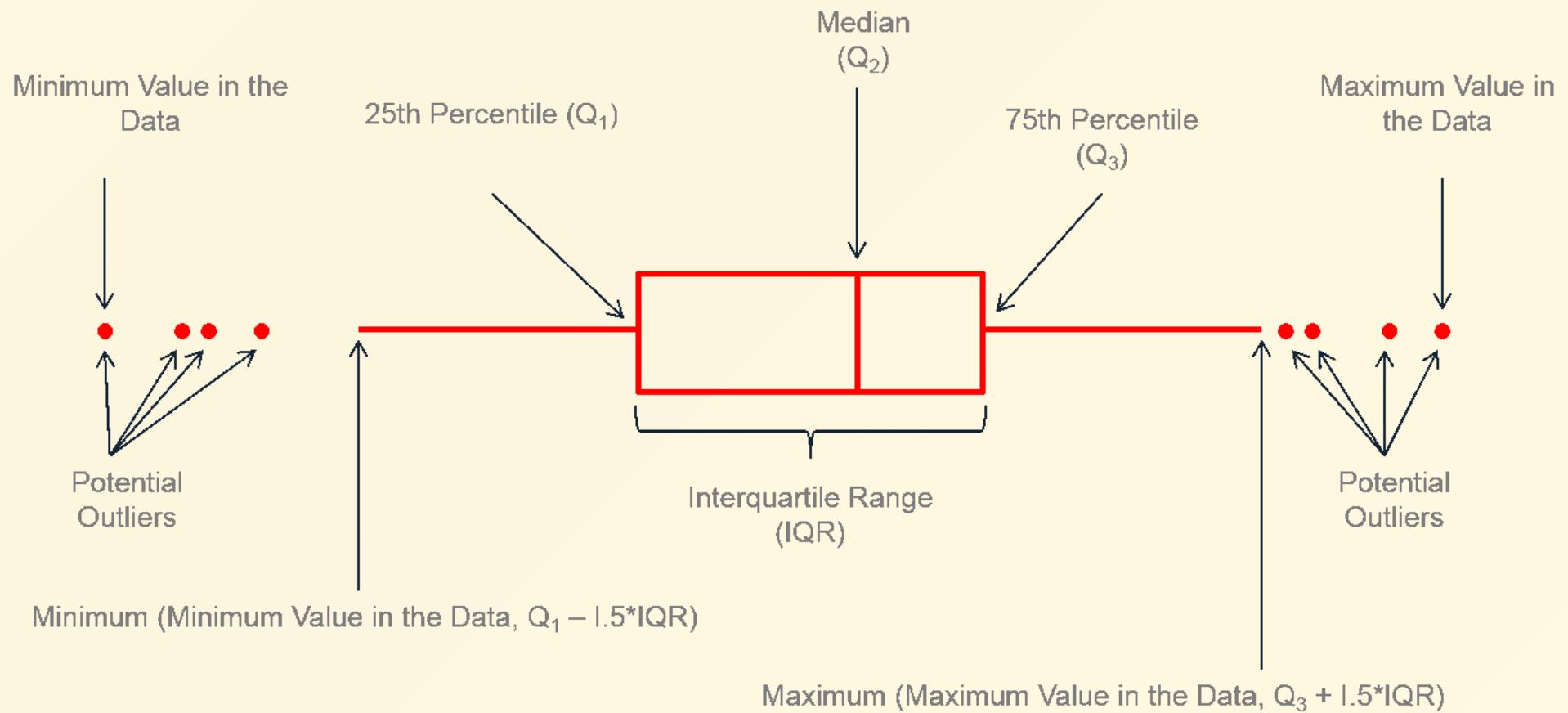
Miami plot/Mirror histogram

- numerical data

Visconti A., et al., Total serum N-glycans associate with response to immune checkpoint inhibition therapy and survival in patients with advanced melanoma, BMC Cancer, 2023 doi:10.1186/s12885-023-10511-3



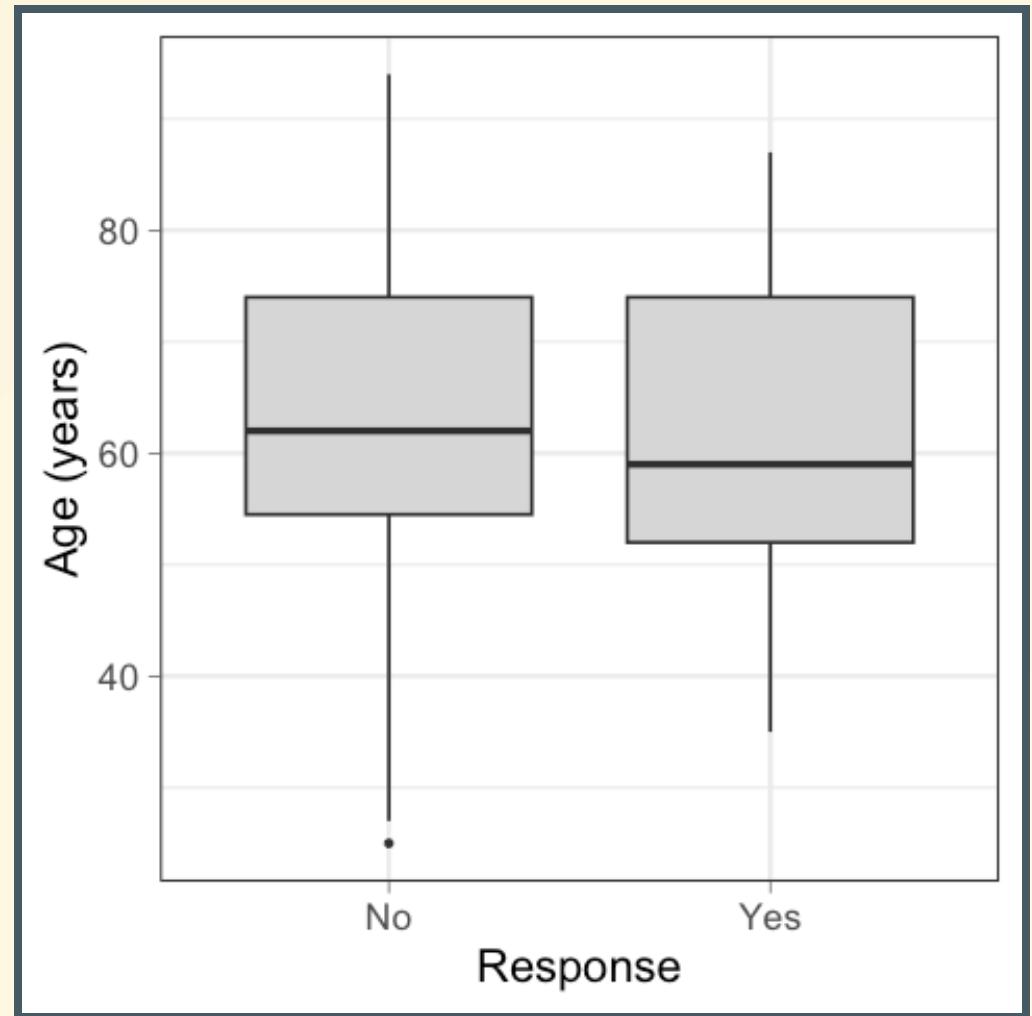
Boxplot



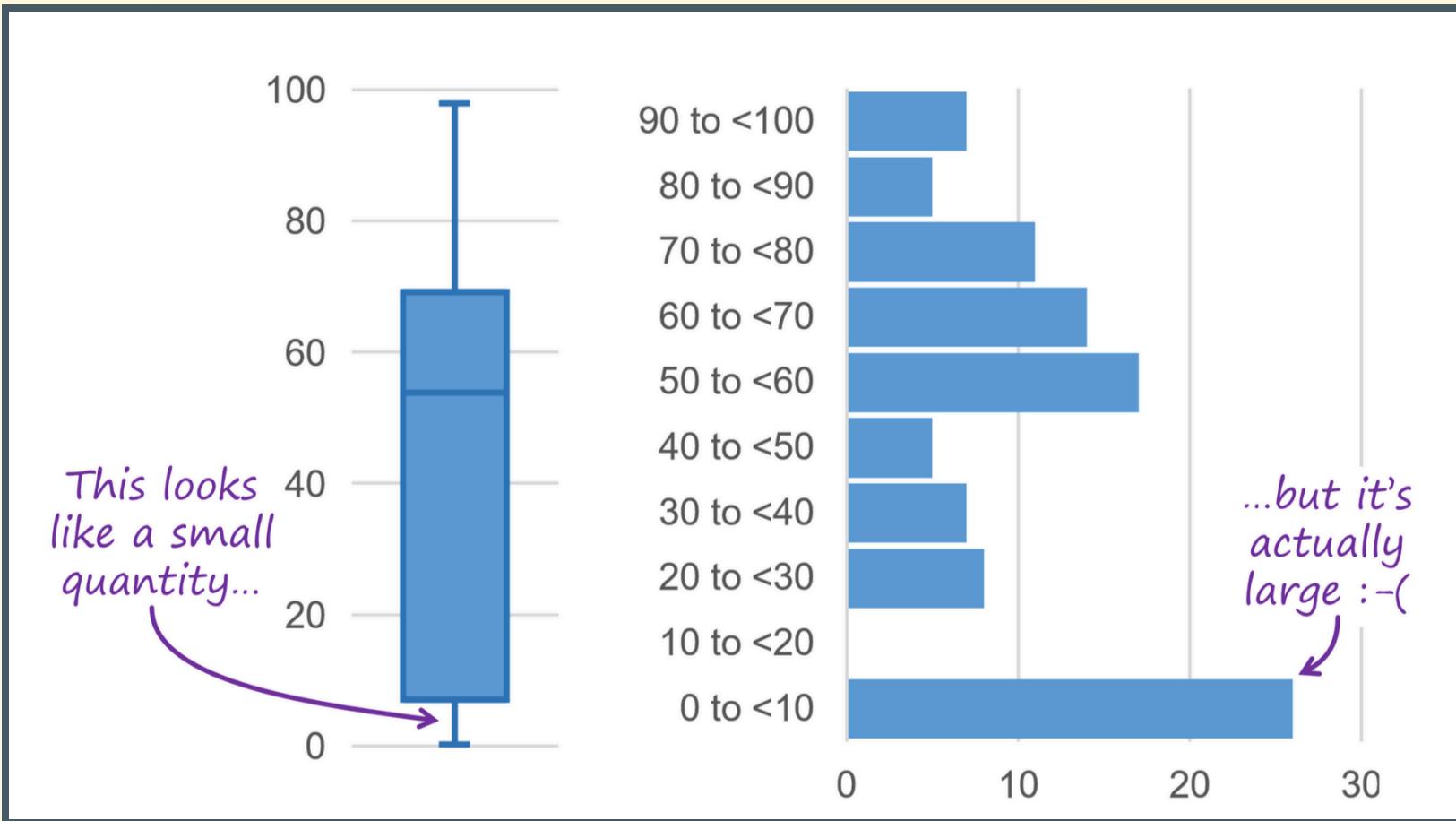
Boxplot

- numerical data

Visconti A., et al., Total serum *N*-glycans associate with response to immune checkpoint inhibition therapy and survival in patients with advanced melanoma, BMC Cancer, 2023 doi:10.1186/s12885-023-10511-3



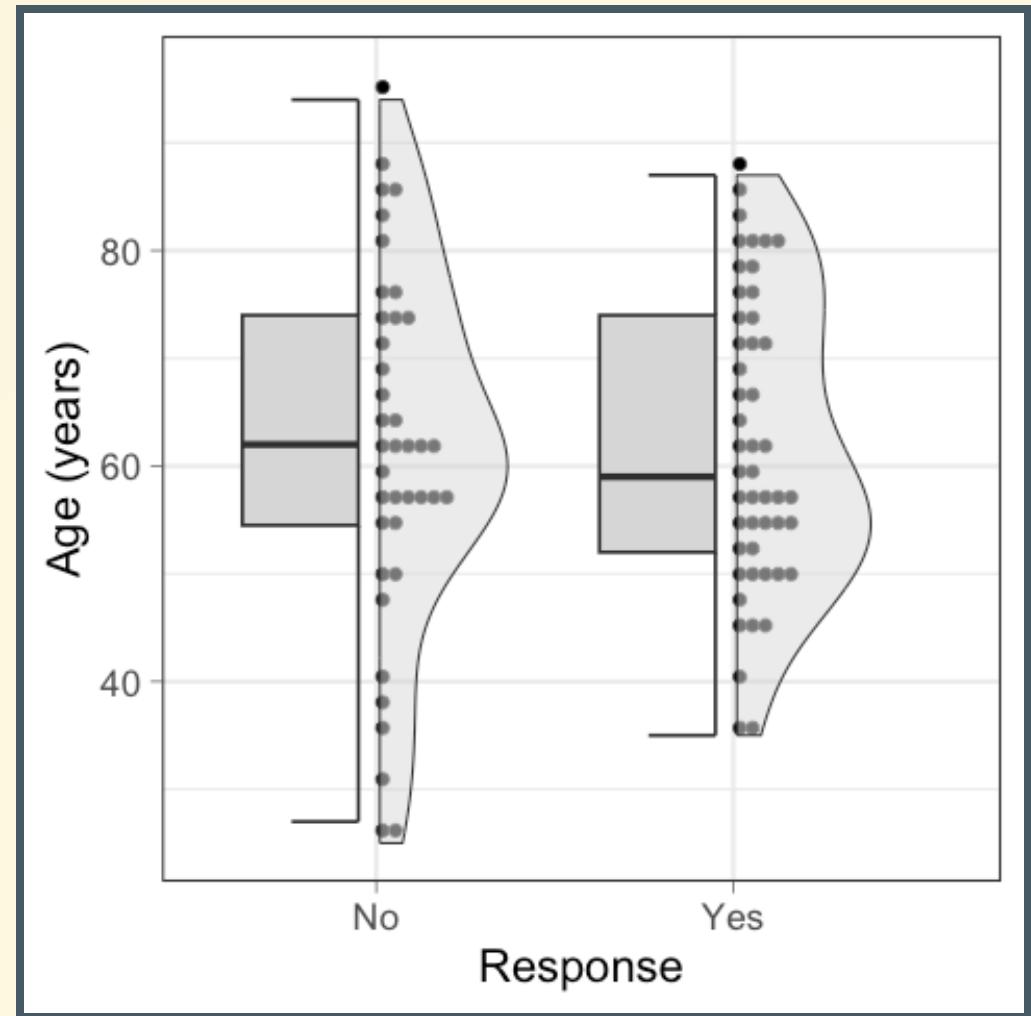
Boxplot



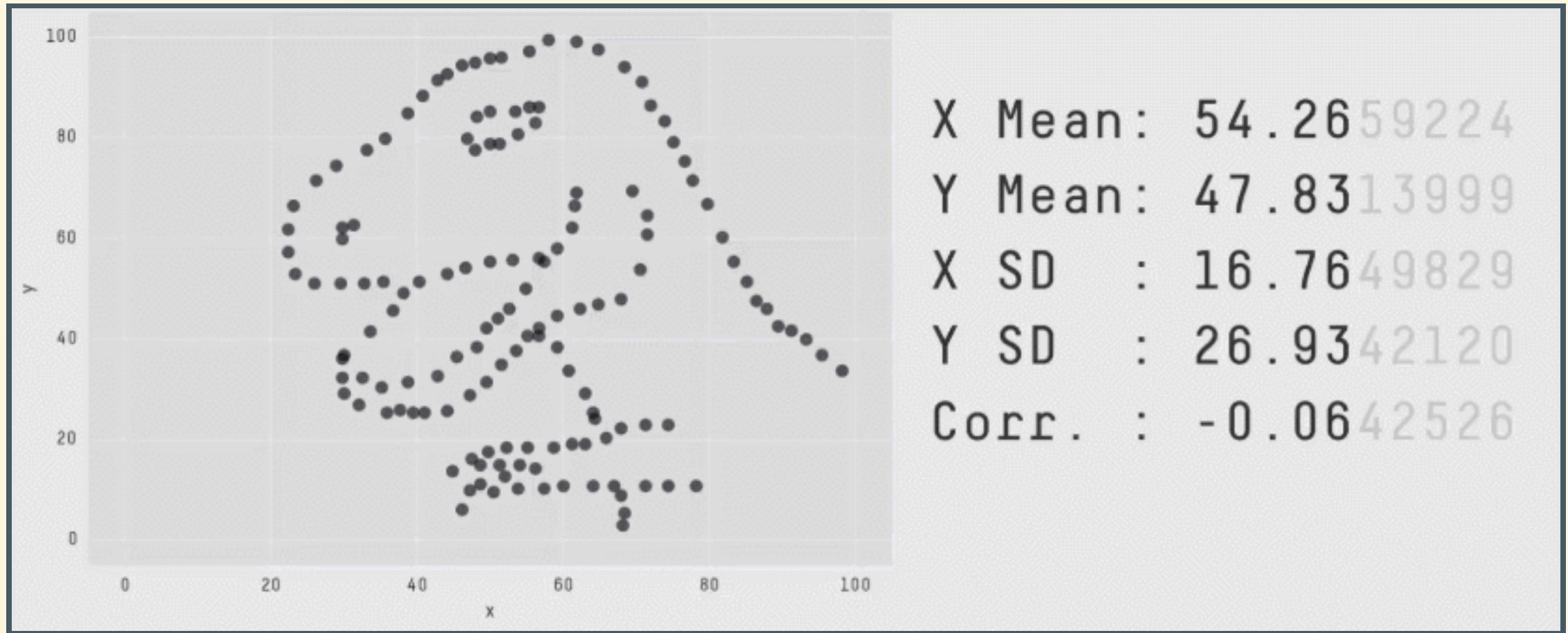
Boxplot

- numerical data

Visconti A., et al., Total serum N-glycans associate with response to immune checkpoint inhibition therapy and survival in patients with advanced melanoma, BMC Cancer, 2023 doi:10.1186/s12885-023-10511-3



Data visualisation: DataSaurus Dozen



Summary

- Data come in different types
- Data are described with measures of centrality and dispersion
- Visualising your data is always a good idea

See you tomorrow

