

The code takes a positive integer N_i as input and computes the upper bound

$$\mathbb{E}_i(N'_t) \leq \min_{J \in \{1, \dots, N_i\}} \left(J + (N_i - J) \left(1 - \mathbb{P}_i(\hat{A}_i^J \in C_i^J) \right) \right)$$

for the conditional expectation $\mathbb{E}_i(N'_t)$ of the number N'_t of shots in the i th round of the outer loop in the Accelerated Quantum Amplitude Estimation (AQAE) algorithm, that is, Algorithm 2 in the paper *Accelerated Quantum Amplitude Estimation without QFT* by Alet Roux and Tomasz Zastawniak. This is used in the paper to obtain an upper bound for the expectation $\mathbb{E}(M)$ of the quantum computational complexity M of the AQAE algorithm.

The function `PCi(E_N_i, N)` computes the conditional probability

$$\mathbb{P}_i(\hat{A}_i^J \in C_i^J) = \mathbb{P}_i(E_i^N \leq e(\hat{A}_i^N))$$

for given values of E_i^N and N , where \hat{A}_i^J , C_i^J , and $e(\hat{A}_i^N)$ are defined in the paper.

The function `PCi(E_N_i, N)` uses repeatedly the formula

$$\begin{aligned} \mathbb{P}(X \in [a, b]) &= \mathbb{P}(X \leq b) - \mathbb{P}(X < a) \\ &= \mathbb{P}(X \leq \lfloor b \rfloor) - \mathbb{P}(X \leq \lceil a \rceil - 1) \\ &= F_X(\lfloor b \rfloor) - F_X(\lceil a \rceil - 1), \end{aligned}$$

where X is a random variable with the binomial distribution $B(N, p)$, N is a positive integer, $p \in (0, 1)$, $a, b \in [0, N]$, $\lceil a \rceil$ is the ceiling of a (that is, the smallest integer greater than or equal to a), $\lfloor b \rfloor$ is the floor of b (that is, the largest integer smaller than or equal to b), and $F_X(x) = \mathbb{P}(X \leq x)$ is the cumulative distribution function of X .