



# Analyzing the Economic Impact of Decentralization on Users

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## Abstract

We model the ultimate price paid by users of a decentralized ledger as resulting from a two-stage game where Miners (/Proposers/etc.) first purchase blockspace via a Tullock contest, and then price that space to users. When analyzing our distributed ledger model, we find:

- A characterization of all possible pure equilibria (although pure equilibria are not guaranteed to exist).
- A natural sufficient condition, implied by Regularity (à la [34]), for existence of a “market-clearing” pure equilibrium where Miners choose to sell all space allocated by the Distributed Ledger Protocol, and that this equilibrium is unique.
- The *market share of the largest miner* is the relevant “measure of decentralization” to determine whether a market-clearing pure equilibrium exists.
- Block rewards do not impact users’ prices at equilibrium, when pure equilibria exist. But, higher block rewards can cause pure equilibria to exist.

We also discuss aspects of our model and how they relate to blockchains deployed in practice. For example, only “patient” users (who are happy for their transactions to enter the blockchain under any miner) would enjoy the conclusions highlighted by our model, whereas “impatient” users (who are interested only for their transaction to be included in the very next block) still face monopoly pricing.

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## 1 Introduction

Following Nakamoto’s creation of Bitcoin in 2008 [35], adoption of blockchain technology for various purposes has steadily grown.<sup>1</sup> More relevant to this paper is ongoing interest in so-called “Web3” or “Decentralized Apps”, for which an estimated \$5.4B USD in VC funding was raised in 2024.<sup>2</sup> This paper seeks contributions to a theoretical foundation for

<sup>1</sup> For example, Forbes reports a cryptocurrency market cap of \$3.27T USD at time of writing. Source: <https://www.forbes.com/digital-assets/crypto-prices/>

<sup>2</sup> Source: <https://cointelegraph.com/news/vc-roundup-web3-funding-5-4-billion-2024>. Crunchbase further estimates a cumulative \$111 B USD in VC funding raised for Web3: <https://news.crunchbase.com/web3-startups-investors/>.

37 why users might (or might not) ultimately find value in decentralized services in comparison  
38 to centralized alternatives.

39 **Classic vs. Modern Pitches for Decentralized Services.** Aside from financial specu-  
40 lation, perhaps the dominant ‘real’ use case of blockchain technology is as a currency for  
41 users with no viable alternative. While compelling applications, the economic case for such  
42 users is relatively straight-forward because the competing product<sup>3</sup> is so dysfunctional that  
43 concerns about (say) Bitcoin’s transaction fees, volatility, and UI become very second-order.  
44 A classical pitch for decentralization therefore emphasizes simply that decentralized services  
45 make it more challenging for authoritarian leaders (and law enforcement) to deny access, and  
46 this pitch is plenty convincing in comparison to the (functionally non-existent) alternatives.

47 A modern discussion on blockchain technology, however, includes applications targeting  
48 users in developed economies with highly developed alternatives. For example, the pitch for  
49 stablecoins to users with a hyper-inflating local currency looks very different than to users  
50 with access to Venmo, Paypal, and credit cards. Consider also decentralized services such  
51 as file storage (for which centralized services such as Dropbox are a reasonable substitute),  
52 social networks (for which centralized services such as Facebook or Twitter are a reasonable  
53 substitute), or gaming (for which centralized gaming services produced by Riot or Blizzard  
54 are a reasonable substitute) – what would cause users to prefer decentralized services over  
55 highly-developed centralized alternatives?

56 A natural answer is that perhaps the decentralized service might somehow be ‘better’  
57 than the centralized competitor.<sup>4</sup> But it is initially confusing how that might possibly arise  
58 as centralized services can optimally coordinate to lower internal costs, whereas decentralized  
59 services must additionally manage incentives/trust across distributed entities.

60 **Decentralizing Natural Monopolies.** One well-understood source of inefficiency in  
61 centralized services is deadweight loss caused by a monopolist.<sup>5</sup> That is, a decentralized  
62 service might plausibly be desirable to a highly-developed centralized alternative simply  
63 because the decentralized service results in different prices, and this can still be the case even  
64 if the centralized infrastructure is more efficient. Therefore it is natural to target domains  
65 with a “natural monopoly” aspect (such as social networks, payment systems, marketplaces,  
66 etc.).

67 Indeed, independently of any blockchain discussions, [48] highlights natural monopolies  
68 for digital services as a growing challenge, and further poses several possible approaches  
69 (each with drawbacks). One approach is described as follows: “An alternative approach to  
70 full-scale regulation consists in insulating a natural monopoly (or bottleneck or essential  
71 facility) segment, as became popular in the late twentieth century. This segment remains  
72 regulated and is constrained to provide a fair and nondiscriminatory access to competitors  
73 in segments that do not exhibit natural monopoly characteristics and therefore can sustain  
74 competition.”<sup>6</sup> One of two key drawbacks of this approach is as follows: “...one wants

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<sup>3</sup> For example: a currency likely to be frozen by an authoritarian government, a hyperinflating currency, or a currency that can be tracked by law enforcement critical of your illicit activity

<sup>4</sup> See here for an example of this pitch: <https://a16zcrypto.com/posts/article/how-stablecoins-will-eat-payments/>.

<sup>5</sup> The holdup problem is another – see Section 1.3 for a brief discussion.

<sup>6</sup> [48] cites several examples: electricity markets might insulate the natural monopoly (the grid) and enable open competition on generation, or rail travel might insulate the natural monopoly (the tracks/stations) and enable open competition on train operation. A prevalent digital example is Local Loop Unbundling, where many countries insulate the natural monopoly (the “local loop” – physical copper wires servicing telecommunications) by requiring its owners to lease access at nondiscriminatory prices to service providers.

to break up the incumbent without destroying the benefits of network externalities. For example, breaking a social network into two or three social networks might not raise welfare.”<sup>7</sup>

One interpretation of Bitcoin is exactly through this lens, and [29] are the first to make this point.<sup>8</sup> Indeed, when viewed as a payment system, the natural monopoly segment is ‘ledger maintenance’ (where a consistent record of transactions is maintained), while the user-facing ‘transaction processing’ segment is not a natural monopoly. In the language of Bitcoin, substantial network effects arise from having consensus on a single consistent ledger, but minimal network effects arise from users transacting within the same block (or with the same miner). In the language of payment systems, substantial network effects arise from users transacting in the same ‘currency’, but minimal network effects arise from users using the same app to process those transactions.<sup>9</sup> Perhaps shockingly, this insulation is maintained without regulation,<sup>10</sup> and therefore provides a novel approach to insulating natural monopolies.

**But does Decentralization Actually Help?** The preceding paragraph highlights blockchain-style decentralization an innovative approach to insulate natural monopolies from derivative services, but should we expect users to ultimately be better off? How would the answer depend on market primitives? Moreover, how do we even draw conclusions on users’ utility from decentralized services? Surprisingly few answers are known to questions like these, and surprisingly fewer frameworks are known to even approach them. The goal of this paper is therefore to provide a framework towards such questions in the core domain of distributed ledgers, with an emphasis on connecting users’ ultimate utility to properties of the decentralized ledger.

## 1.1 Overview of Results

We consider the core setting of a ledger. Ultimately, users desire the service of writing their transaction to the ledger, and have some value for doing so. Inspired by the preceding discussion, we separate this service into an Upstream segment which is a natural monopoly, and a Downstream segment which is not.<sup>11</sup>

A centralized ledger would simply provide the entire service in a vertically integrated

<sup>7</sup> The second key challenge highlighted is identifying a core bottleneck to insulate. We argue in Section 4 that for many domains of interest, such a bottleneck can be identified and (in theory, at least) insulated. A final challenge highlighted is the actual process of unbundling an existing product, which is unrelated to our work.

<sup>8</sup> “We model this novel economic structure and show that the BPS’s [Bitcoin Payment System’s] decentralized design offers a prototype of a payment system in which users are protected from monopoly harm even if the payment system were a monopoly. . . Standard economic arguments suggest that weak competition among monopolistic firms calls for regulation to mitigate monopoly harm. Under the BPS, users are protected from abuses of monopoly power even without competition from other payment systems. Thus, the BPS addresses potential antitrust concerns in a novel, even revolutionary, way.”

<sup>9</sup> The preceding sentence is necessarily clunky, as it is somewhat unnatural to imagine separating a centralized payment system into a back-end transaction processor (that stores data and moves money around, where network effects arise) and front-end transaction processor (that interfaces directly with users, and minimal network effects arise). One high-level contribution of the “Decentralized view” is as a lens to dis-integrate services without an obvious dis-integration.

<sup>10</sup> Our analysis does rely on Miners treating core aspects of the consensus protocol as exogenous, which bears conceptual similarity to regulation.

<sup>11</sup> See Section 2 for further discussion. Intuitively, the Upstream segment directly edits the ledger, which is a natural monopoly due to network effects of multiple users sharing access to the same ledger. The Downstream segment directly interfaces with users to solicit their transactions and pass to the Upstream segment, and exhibits minimal network effects.

manner.<sup>12</sup> A classic Industrial Organization exercise might consider dis-integrating the Upstream monopolist from separate Downstream firms that compete with one another.<sup>13</sup> A distributed ledger removes centralized control entirely – the Upstream segment is provided by a hard-coded Protocol with exogenously set parameters. Competitive Downstream providers then ‘purchase’ the Upstream resource according to the rules of the protocol and use it to process users’ transactions.<sup>14</sup> We analyze this in Section 3, and in particular include a discussion of why the model captures key aspects of distributed ledgers.

We then draw the following conclusions in our model:

- To the extent that a quantitative “measure of decentralization” impacts the price faced by users, it is the *size of the largest miner*.<sup>15</sup>
- Block rewards have limited impact on users. Specifically, block rewards cannot impact the ultimate price users would face in equilibrium (provided equilibria exist),<sup>16</sup> but can cause equilibria to exist.<sup>17</sup>
- We also characterize all possible equilibria (Theorem 10) and provide sufficient conditions for desirable equilibria to exist (Theorem 11).
- Our model applies only to *patient* users (who are happy to have their transaction included in any block), whereas *impatient* users (who want their transaction included in the next block or not at all) instead face miners with monopoly power over the contents of that block.

## 1.2 Roadmap

In Section 1.3, we discuss related work. Section 2 overviews our model. We include a section that provides technical preliminaries for equilibria of simultaneous first-Price auctions in our full version.<sup>18</sup> Section 3 describes our Distributed Ledger Model, highlights key distinctions to a Centralized provider, highlights its connection to distributed ledgers in practice, and provides our main analysis. Section 4 concludes.

## 1.3 Related Work

**Modeling Economic Impact of Decentralized Technologies.** The most closely related works in terms of motivation also seek to understand potential economic benefits of aspects of decentralized technologies (although there is no technical overlap between our work and any of these). By far the most related in terms of motivation is [29], who also view distributed ledgers through the lens of insulating a natural monopoly. [29] considers users with a simple value for service (either High or Low), and who prefer not to wait for their transactions to be included. In their model, a monopolist excludes all Low users, but immediately processes

<sup>12</sup>Venmo is a good example to have in mind for this model – the Venmo backend is the Upstream segment, and the Venmo app is the Downstream segment. Users enjoy network effects due to the backend database, and minimal network effects from opening the same app on their phones.

<sup>13</sup>The authors are not aware of a live example matching this model. A hypothetical example to have in mind would be if Venmo allowed third-party apps to access its ledger, and charged access fees to those apps.

<sup>14</sup>In the language of Bitcoin, miners are Downstream providers. Miners solicit transactions from users, and ‘purchase’ the right to include transactions in a Bitcoin block by ‘paying’ in hashes.

<sup>15</sup>See Theorems 10 and 11 for precise statements.

<sup>16</sup>See Theorem 10 for a precise statement.

<sup>17</sup>See Propositions 12 and 13 for precise statements.

<sup>18</sup>Due to space constraints, we prioritize presentation of our model, statements of results, and implications in the body. This technical analysis is useful primarily for technical intuition, and so is moved to the full version due to space constraints.

all High transactions, causing deadweight loss. Bitcoin, on the other hand, processes all users, but with delay cost.<sup>19</sup> So their work highlights a tradeoff between a monopolist (deadweight loss) and Bitcoin (delay cost). In comparison, our work (a) focuses exclusively on the monetary cost paid by users, and (b) considers a richer model of user preferences (i.e. an arbitrary demand curve, sometimes subject to a standard regularity condition).

Other works analyze the economic impact of aspects of decentralized technologies from an orthogonal viewpoint. For example, [46, 41] view decentralization/tokenization as a commitment device by which a platform can cede control to users. In addition, [25] similarly view tokenization as a commitment device to future competitive pricing. These works address a similar high-level challenge (platforms with network effects), and also through novel approaches that arose recently alongside blockchain technology. However, these works still involve a rent-seeking platform (in comparison to our exogenous protocol), and cede control to users or external investors (in comparison to changing the market structure).

**Tullock Contests.** At a technical level, our work studies equilibria of a two-part game, one of which is a Tullock Contest and the second of which is an auction (see Section 3 for a precise specification). As such, much of our technical analysis concerns Tullock Contests [8, 28, 27], which are commonly used to capture the game played by Bitcoin miners to produce blocks (and also to capture related aspects of blockchain ecosystems) [3, 2, 16, 4]. The key technical distinction between our work and these works lies in our second-stage auction game, which will become clear in Section 3.

**Industrial Organization Theory.** Our model is inspired by ‘textbook’ Industrial Organization Theory models [47, 44]. Our model focuses on textbook settings (without demand uncertainty, and without costly marketing) to isolate the impact of the novel blockchain-inspired market structure. This may a fruitful aspect to consider as future work develops. In classical language, we model downstream producers that sell identical products (because the users are patient, and therefore indifferent to which block they get in). Impatient users (which are not the focus of our work, as they simply face a downstream monopolist) would instead be captured by perfectly differentiated downstream products (because impatient users want only to enter the next block).

**Other Economic Aspects of Blockchains.** Numerous other works consider economic aspects of blockchains. Several consider the economic incentives of protocol participants [18, 17, 12, 30, 43, 7, 22, 26, 37, 38, 10, 36, 20, 52, 39, 51, 54, 1, 5, 11, 19, 9]. These works uncover reasons why participants may not be incentivized to follow the protocol specifications. In comparison to these works, we assume the underlying blockchain protocol functions as intended. Several consider “transaction fee mechanism design” – the auction specified by the protocol for users to purchase transactions from miners [31, 42, 45, 50, 53, 23, 21, 15, 14, 13, 6, 32, 33, 24]. We model miners running a first-price auction with reserve, and discuss briefly in Section 3 the connection between our modeling decision and blockchains with alternate TFMs (such as Ethereum’s EIP-1559).<sup>20</sup> Finally, [40] considers the pricing dynamics of serial monopolists selling blockspace to patient buyers. In comparison to our work, [40] considers Miners who produce only a single block and aim to maximize their revenue from that block in isolation, whereas our work considers Miners who aim to optimize their joint revenue from multiple blocks (and also models the Tullock contest by which Miners earn the right to

<sup>19</sup> [29] further analyze the delay as a function of Bitcoin protocol parameters.

<sup>20</sup> Briefly, what really matters for our model is the cost of including a transaction on-chain (which in EIP-1559 is the base fee, and in Bitcoin is zero), and how a profit-maximizing miner would choose to sell block space (given that cost) to users who can choose to instead purchase from other miners.

180 produce those blocks).

## 181 **2 Preliminaries**

182 **Running Story.** Our model is motivated by the concept of a ledger. Ultimately, the product  
 183 consumed by an end-user is the ability to write information to the global ledger (which we  
 184 call a WRITE).<sup>21</sup> That is, each end-user has a message they would like to write on the ledger,  
 185 and purchases a WRITE to do so.

186 The entire value proposition of a global ledger is that there is ultimately a single consistent  
 187 ledger. It is therefore crucial that *some* aspects of ledger maintenance are performed via a  
 188 single entity/protocol/etc. (for example, centralized ledgers should maintain a single consistent  
 189 back-end database. Decentralized ledgers should have a single protocol from which observers  
 190 can conclude a single consistent ledger). Intuitively, these are operations that directly edit  
 191 content in the ledger (and because there is a single consistent ledger, these operations must be  
 192 carefully coordinated by a single entity/protocol/etc.). Other aspects of ledger maintenance  
 193 can in principle be performed by competing entities (for example, end-users can in principle  
 194 face different User Interfaces, pricing schemes, etc.). We abstract away precise details of  
 195 the ledger maintenance process, and simply refer to operations that directly edit the single  
 196 consistent ledger as *Upstream* (and refer to one unit of these operations as an APPEND), and  
 197 those that could in principle be performed by competing entities *Downstream*.

198 It may help to have a few examples in mind. Imagine breaking a centralized ledger  
 199 (i.e. Venmo) into its back-end database maintenance and front-end User Interface. The  
 200 back-end database must ensure consistency on a single global ledger, and so is Upstream.  
 201 Edits to the back-end database must be reliable and consistent (even if the database is  
 202 replicated, distributed, etc.). One APPEND constitutes the resources necessary to add one  
 203 entry to the back-end database (maintaining consistency, availability, etc.). The front-end  
 204 User Interface is Downstream – the front-end UI interacts directly with consumers, and  
 205 turns communication with end-users into a query to the Upstream back-end database. The  
 206 front-end UI consumes APPENDS in order to produce WRITES, and sells WRITES to users.  
 207 Note that, in principle, the centralized ledger could offer different front-end UIs to different  
 208 consumers (with different pricing schemes, different communication protocols, different app  
 209 layout, etc.) – doing so does not in principle interfere with the ability to maintain a single,  
 210 consistent back-end database.

211 One could imagine instead a centralized back-end database that provides an API for  
 212 third-party app access. The centralized back-end database again is a producer of APPENDS.  
 213 Each third-party app is a consumer of APPENDS and a producer of WRITES. End-users  
 214 purchase WRITES from a third-party app (who incurs costs both from interacting with the  
 215 end-user, and from purchasing APPENDS). Again, each third-party app could in principle  
 216 differ in pricing schemes, communication protocols, app layouts, etc., and purchase APPENDS  
 217 from the same back-end database (that interacts with each third-party app in a manner that  
 218 maintains a single consistent ledger).

219 One could also imagine a decentralized consensus protocol maintaining a decentralized  
 220 ledger, allowing participation from “miners”, “stakers”, “proposers”, etc.<sup>22</sup> The decentralized

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<sup>21</sup> In order to focus on the relevant market primitives, we do not explicitly model ledger maintenance, consensus, cryptography, privacy, or reading. The service purchased by an end-user gets their message onto the ledger, and in a manner that can be read by the desired recipients.

<sup>22</sup> Throughout this paper, we adopt the language of Bitcoin and refer to these participants as miners.

protocol outlines a costly procedure by which miners receive APPENDS.<sup>23</sup> Each miner is a consumer of APPENDS (that they “purchase” by completing the costly procedure specified in the decentralized protocol), and a producer of WRITES. End-users purchase WRITES from a miner (who incurs costs both from interacting with the end-user, and “purchasing” an APPEND). The consensus protocol structures its “sale” of APPENDS so that all ledger updates contribute to a single consistent ledger.<sup>24</sup>

The subsequent paragraphs formalize our model in the abstract – the running story provides intuition for each concept.

**Market Resources.** We consider two types of resources. The Downstream resource, WRITE, is consumed by end-users. The Upstream resource, APPEND, is required to produce WRITES (in one-to-one ratio). Production of the Upstream resource is a natural monopoly, and therefore will be produced by a single entity/protocol. Production of the Downstream resource is not a natural monopoly, therefore we model a Downstream market with multiple competing participants.

**Market Participants.** There are two types of market participants. End-users are the ultimate consumers, who desire WRITES. Each end-user wants a single WRITE, and has some value  $v$  should they receive one. Downstream producers produce WRITES, which necessitates consumption of APPENDS. The protocol (which is hard-coded and has no objective function or strategic decisions) produces APPENDS.

**Market Primitives.** There is a continuum of end-users, with  $D(p)$  denoting the mass of consumers with value at least  $p$  for a WRITE.

We assume that  $D(\cdot)$  provides finite revenue to a monopolist (that is,  $\sup_p \{p \cdot D(p)\} < \infty$ ). Our main results require a standard regularity assumption on  $D(\cdot)$ .

► **Definition 1 (Regular).** A demand curve  $D(\cdot)$  is Regular if:

- $D(\cdot)$  is differentiable and strictly decreasing. In this case, we use  $-d(\cdot) := D'(\cdot)$ .
- The function  $\varphi_D(x) := x - \frac{D(x)}{d(x)}$  is monotone non-decreasing in  $x$ .

**Structure of the Game.** We model the interactions between the Upstream protocol, Downstream providers, and End-Users as a three-stage game. First, the Upstream protocol sets the dynamics for selling APPENDS to Downstream providers. Next, with this protocol fixed, Downstream providers set their strategies both for purchasing APPENDS and for selling WRITES to End-Users. Finally, with these strategies fixed, End-Users set their strategies for purchasing WRITES from Downstream providers.

**Equilibrium Analysis.** Let DP denote the set of Downstream providers, EU denote the set of End-Users, and  $P_i(\vec{a})$  denote the payoff to Player  $i$  when the action profile is  $\vec{a}$ .

An End-User Equilibrium fixes some actions  $\vec{a}_{DP}$  by the Downstream providers, and is a Nash Equilibrium of the End-User game induced by  $\vec{a}_{DP}$  (with payoff  $P_i(\vec{a}_{DP}; \vec{a}_{EU})$  to Player  $i \in EU$  on action profile  $\vec{a}_{EU}$ ).

A Downstream Equilibrium<sup>25</sup> specifies, for each possible action profile  $\vec{a}_{DP}$  of the Downstream providers, an End-User Equilibrium  $E(\vec{a}_{DP})$  for the end-user game induced by  $\vec{a}_{DP}$ , and then (together with  $E(\cdot)$ ) is a Nash Equilibrium among Downstream providers for the Downstream game induced by  $E(\cdot)$  (which awards payoff  $P_i(\vec{a}_{DP}, E(\vec{a}_{DP}))$  to Player  $i \in DP$

<sup>23</sup>For example, Bitcoin miners receive APPENDS by repeated hashing (which costs electricity and hardware). Ethereum stakers receive APPENDS by locking up ETH in the Ethereum protocol (which costs capital).

<sup>24</sup>That is, this paper assumes that the consensus protocol functions as intended. See Section 1.3 for a brief discussion on related work surrounding this assumption.

<sup>25</sup>We will sometimes simply call this an Equilibrium.

on action profile  $\vec{a}_{\text{DP}}$ ). When  $E(\cdot)$  is unique (or otherwise clear from context), we will abuse notation and simply refer to  $\vec{a}_{\text{DP}}$  as a Downstream Equilibrium. Moreover, we will also abuse notation and say that a Downstream Strategy  $\alpha_i$  dominates  $\alpha'_i$  if  $\alpha_i$  dominates  $\alpha'_i$  in the game among Downstream providers induced by  $E(\cdot)$ .

**Notation.** For a (not necessarily continuous) monotone non-increasing function  $F(\cdot)$ , we let  $F^{-1}(y) := \{x \mid \lim_{z \rightarrow x^+} F(z) \leq y \leq \lim_{z \rightarrow x^-} F(z)\}$ ,  $F_{\inf}^{-1}(y)$  denote the infimum of  $F^{-1}(y)$ , and  $F_{\sup}^{-1}(y)$  denote the supremum of  $F^{-1}(y)$ . Observe that if  $F(\cdot)$  is left-continuous, then  $F(x) \geq y$  for any  $x \in F^{-1}(y)$ .<sup>26</sup> If  $F(\cdot)$  is continuous and strictly decreasing, we simplify notation and define  $F^{-1}(y) := F_{\inf}^{-1}(y) = F_{\sup}^{-1}(y)$ .

**First-Price Auction with Reserve.** First-Price Auctions with Reserves are a common subgame in our market structures. With a continuum of bidders and a total supply of  $Q$ , a first-price auction with reserve  $r$  concludes as follows. First, let  $B(q)$  denote the mass of bidders who submit a bid at least as large as  $q$ .<sup>27</sup> Next, if  $B(r) < Q$ , then every bidder who submits a bid at least as large as  $r$  wins and pays their bid. If  $B(r) \geq Q$ , then every bidder who submits a bid strictly exceeding  $B_{\sup}^{-1}(Q)$  wins and pays their bid, every bidder who submits a bid strictly below  $B_{\sup}^{-1}(Q)$  loses, a mass of  $B(B_{\sup}^{-1}(Q)) - Q$  bidders who submit a bid of exactly  $B_{\sup}^{-1}(Q)$  lose and the remainder win and pay their bid (and in this case a total mass of  $Q$  bidders win).<sup>28</sup> <sup>29</sup> Observe that every bid profile induces an effective price of  $b := \max\{B_{\sup}^{-1}(Q), r\}$  – every bidder who submits a bid exceeding  $b$  certainly wins (and pays their bid) and every bidder who submits a bid below  $b$  certainly loses.

**Equilibria of Simultaneous First-Price Auctions.** Simultaneous First-Price Auctions are another common subgame in our market structures. Below we overview Simultaneous First-Price Auctions and technical lemmas helpful to understand our results – full analyses and proofs are in the full version.

► **Definition 2 (Simultaneous First-Price Auctions).** *In Simultaneous First-Price Auctions, there are  $n$  sellers. Each seller  $i$  has a  $Q_i$  mass of items for sale, and sets reserve  $r_i$ . We define  $Q^{\leq}(r) := \sum_{i, r_i \leq r} Q_i$  to be the total mass of items for sale at reserve at most  $r$ ,<sup>30</sup>  $Q^{<}(r) := \sum_{i, r_i < r} Q_i$  to be the total mass of items for sale at reserve strictly less than  $r$ ,<sup>31</sup> and  $Q^=(r) := Q^{\leq}(r) - Q^{<}(r)$  to be the total mass of items for sale at reserve exactly  $r$ .*

*A continuum of unit-demand buyers each submit a (possibly 0) bid to each first-price auction. Each first-price auction executes exactly as defined in Section 2. An equilibrium of Simultaneous First-Price Auctions is simply a strategy profile where each bidder best responds.*

For equilibria among bidders, fixing all  $Q_i, r_i$ , we establish in the full version that all winning bidders pay the same price in equilibrium, and define the value of this as *clearing price*.

<sup>26</sup> Because for any  $x \in F^{-1}(y)$ ,  $y \leq \lim_{z \rightarrow x^-} F(z) = F(x)$ .

<sup>27</sup> Observe that  $B(\cdot)$  is left-continuous. To see this, observe that all bidders who bid at least  $b - \varepsilon$  contribute to  $B(b - \varepsilon)$ . So the bidders that contribute to  $B(b - \varepsilon)$  for all  $\varepsilon > 0$  are exactly those who bid at least  $b$  – the same bidders that contribute to  $B(b)$ .

<sup>28</sup> Recall that  $B(B_{\sup}^{-1}(Q)) - Q \geq 0$  as  $B$  is left-continuous.

<sup>29</sup> All of our analysis holds no matter how ties are broken to select the winning bidders among those who bid  $B(B_{\sup}^{-1}(Q))$ .

<sup>30</sup> Observe that  $Q^{\leq r}$  is monotone non-decreasing, and right-continuous everywhere. To see this, observe that seller  $i$  contributes  $Q_i$  to  $Q^{\leq}(r)$  if and only if  $r_i \leq r$ , and to  $Q^{\leq}(r + \varepsilon)$  for all  $\varepsilon > 0$  if and only if  $r_i \leq r$ . Therefore all sellers contribute the same to both  $Q^{\leq}(r)$  and  $\lim_{\varepsilon \rightarrow 0} Q^{\leq}(r + \varepsilon)$ .

<sup>31</sup> Observe that  $Q^{<}(r)$  is monotone non-decreasing, and left-continuous everywhere. To see this, observe that seller  $i$  contributes to  $Q^{<}(r)$  if and only if  $r_i < r$ , and to  $Q^{<}(r - \varepsilon)$  for some  $\varepsilon > 0$  if and only if  $r_i < r$ . Therefore, all sellers contribute the same to both  $Q^{<}(r)$  and  $\lim_{\varepsilon \rightarrow 0} Q^{<}(r - \varepsilon)$ .

► **Definition 3** (Clearing Price and Canonical Equilibrium). For an equilibrium  $E$  of Simultaneous First-Price Auctions, we refer to its clearing price  $c(E)$  as the single bid such that every winning bidder wins exactly one item at bid  $c(E)$ , or loses. We say an equilibrium is canonical if (i) a total supply of  $\min\{D(c(E)), Q^{\leq}(c(E))\}$  items are sold,<sup>32</sup> and (ii) the clearing price is minimal across all equilibria.<sup>33</sup> Note that if  $D(\cdot)$  is continuous and strictly decreasing, all equilibria are canonical.

Downstream Equilibria in our market structures concern the behavior of sellers in Simultaneous First-Price Auctions (i.e. choosing a quantity  $Q_i$  according by participating in the Upstream protocol, and setting a reserve  $r_i$ ). We refer to the reserve-setting aspect as a *price-setting equilibrium* (noting that a Downstream Equilibrium must both induce a price-setting equilibrium for fixed  $\vec{Q}$ , and be a joint equilibrium when considering both investment and reserves).

► **Definition 4** (Price-Setting Game). A Price-Setting Game has the following structure:  
**Players.** There are  $n > 0$  sellers. Seller  $i$  has quantity  $Q_i$  of items.  
**Action Space.** Each seller picks a reserve  $r_i$  to set in a first-price auction.  
**Costs.** Each seller pays a cost of  $c_i$  per item sold.  
**Payoffs.** On strategy profile  $\vec{r}$ , a continuum of buyers with values according to  $D(\cdot)$  bids in equilibrium of the simultaneous first-price auctions with quantities  $\vec{Q}$  and reserves  $\vec{r}$ , which induces a clearing price of  $p(\vec{Q}, \vec{r})$ . If Seller  $i$  sells a mass of  $Q'_i$  items in this equilibrium, their payoff is  $Q'_i \cdot (p(\vec{Q}, \vec{r}) - c_i)$ .

Note that if  $D(\cdot)$  is continuous and strictly decreasing, the clearing price  $p(\vec{Q}, \vec{r})$  is unique. We refer to a Price-Setting Game as canonical if the equilibrium selected by buyers is canonical.

A concept throughout our analyses is whether a seller clears their entire inventory, and whether they determine the price at which the bidding equilibrium clears.

► **Definition 5.** We say that Seller  $i$  is saturated in a strategy profile  $\vec{r}$  if either (i) Seller  $i$  sells a mass of  $Q_i$  items or (ii) the clearing price  $p(\vec{Q}, \vec{r}) \leq c_i$ . We further say that an equilibrium is saturated if all sellers are saturated. Finally, we refer to Seller  $i$  as a price-setter in the strategy profile  $\vec{r}$  if  $Q_i > 0$  and the clearing price  $p(\vec{Q}, \vec{r}) = r_i > c_i$ .

Finally, Proposition 6 characterizes that all potential price-setting equilibria are either a “market-clearing equilibrium” where no seller is sufficiently large to profit from price-setting, or have a unique price-setter.

► **Proposition 6.** Let  $Q := \sum_i Q_i$ . Then every price-setting equilibrium takes one of two forms:

■ Every seller is saturated and the clearing price is  $D_{\sup}^{-1}(Q)$ . An equilibrium of this form exists if and only if  $Q_i \leq \frac{(x - c_i)(Q - D(x))}{x - D_{\sup}^{-1}(Q)}$  for all  $i$  and all  $x > D_{\sup}^{-1}(Q)$ .

<sup>32</sup>That is, there does not exist a non-zero mass of buyers with value  $D(c(E))$  and an unsaturated auction with reserve  $c(E)$ .

<sup>33</sup>Intuitively, what happens is the following. There is a demand curve  $D(\cdot)$  defined by the users’ demand. The sellers  $\{(Q_i, r_i)\}$  jointly define a supply curve, with  $S(q)$  denoting the quantity of WRITES sold in some auction with reserve at most  $q$ . The supply curve has jump discontinuities, and so the demand may “meet” supply in a discontinuity. Still, any point where supply meets demand can be the effective price, and if  $D(\cdot)$  is continuous and strictly decreasing there is a unique such point.

333 ■ There is a single price-setter  $i$ , who sets price  $r_i^* := \arg \max_{x \geq D_{\text{sup}}^{-1}(Q)} \{(x - c_i)(D(x) +$   
 334  $Q_i - Q)\}$ . If an equilibrium of this form exists, it certainly exists with  $i^* := \arg \max_i \{r_i^*\}$   
 335 as the price-setter (but equilibria with other price-setters are possible). Moreover, if  
 336  $c_i = c_j$  for all  $i, j$ , then  $\arg \max_i \{Q_i\} = i^*$ .

### 3 Distributed Ledger Model

337 We now formally present our Distributed Ledger model. After formally specifying the model,  
 338 we overview key differences to classical market structures, and its connection to distributed  
 339 ledgers in practice.  
 340

341 ► **Definition 7** (Distributed Ledger Model). *The Distributed Ledger Model has the following*  
 342 *properties. We refer to the Upstream provider as Protocol and to the Downstream providers*  
 343 *as Miners.*

344 *UPSTREAM*  
 345 **Protocol.** *The Upstream protocol produces a fixed amount of  $Q_A$  APPENDs and maintains*  
 346 *consensus. The protocol runs a Tullock Contest [49] in some Resource to distribute the*  
 347 *supply of APPENDs, with a block reward  $B \geq 0$ . Specifically, Miner  $i$  who invests  $q_i$  of*  
 348 *Resource receives a fraction of the total APPEND supply proportional to their investment*  
 349 *(i.e.,  $Q_A \cdot \frac{q_i}{\sum_j q_j}$ ). Miner  $i$  also receives  $B \cdot Q_A \cdot \frac{q_i}{\sum_j q_j}$  payment.*

350 **Payoffs.** *Upstream protocol has no payoffs – it simply maintains consensus on the*  
 351 *ledger.<sup>34 35</sup>*

352 *DOWNSTREAM*

353 **Players.** *There is a set of  $n$  Miners.*

354 **Action Space.** *Each Miner  $i$  chooses a quantity of investment  $q_i$  in the Upstream Tullock*  
 355 *Contest, and a reserve price  $r_i$  for a first-price auction they will run among end-users.*

356 **Costs.** *Miner  $i$  pays cost  $c_i^R$  per unit of Resource, and  $c^W$  per WRITE. That is, if Miner*  
 357  *$i$  wishes to invest  $q_i$  in the Upstream game, they pay cost  $q_i \cdot c_i^R$ . If Miner  $i$  eventually*  
 358 *sells  $Q'_i \leq \frac{q_i}{\sum_j q_j} \cdot Q_A$  WRITES, Miner  $i$  pays cost  $Q'_i \cdot c^W$ . W.l.o.g. we let  $c_i^R \leq c_{i+1}^R$  for*  
 359 *all  $i \in [n - 1]$ .*

360 **Payoffs.** *For a Miner  $i$  who invests  $q_i$  in the Upstream game and eventually sells  $Q'_i$*   
 361 *WRITES, their total cost is  $c_i^R \cdot q_i + Q'_i \cdot c^W$ . They receive a block reward of  $B \cdot Q_A \cdot q_i / \sum_j q_j$ ,*  
 362 *plus any additional revenue earned in their first-price auction. Therefore, if Miner  $i$  earns*  
 363 *revenue  $R_i$  from their first-price auction, invests  $q_i$  in the upstream game, and sells  $Q'_i$*   
 364 *WRITES, their payoff is  $R_i - Q'_i \cdot c^W - q_i \cdot c_i^R + B \cdot Q_A \cdot \frac{q_i}{\sum_j q_j}$ .*

365 *END-USER*

<sup>34</sup>In the case of Bitcoin (and Ethereum, and most other Decentralized Ledgers), Miners are also participants in a consensus protocol. It may be helpful to think of Upstream providers as nodes that pass messages, verify authenticity, etc. in roles that would not also result in the ability to sometimes dictate contents of a block.

<sup>35</sup>We have intentionally modeled the decisions of the consensus protocol as exogenous to the game we study. Of course, *someone* decides on  $Q_A$ ,  $B$ , and to use a Tullock Contest in the first place. In practice, these decisions happen on a *much* slower time scale than the game we model. For example, both Bitcoin and Ethereum (and all permissionless blockchains the authors are aware of) have used Tullock Contests since their creation. Bitcoin has never changed the formula for its block reward, and Bitcoin has technically not changed its blocksize either (although ‘soft forks’ have occasionally increased Bitcoin’s functional blocksize). Still, it is also worthwhile for future work to study the processes by which protocol parameters are set.

***Players.** There is a continuum of End-Users who follow a demand curve  $D(\cdot)$  for WRITES.*

***Action Space.** Each end-user submits a bid to each First-Price Auction.*

***Payoffs.** An end-user with value  $v$  has payoff  $v - q$  for receiving at least one WRITE and paying total price  $q$ ,<sup>36</sup> and payoff 0 if they do not get a WRITE.*

Before proceeding to analysis, some discussion is warranted on why the above model captures popular distributed ledgers, and what differentiates it from classic market structures.

**Key Differences.** One key difference between the Distributed Ledger Model and traditional market structures is the presence of a non-strategic protocol. Specifically, the Upstream game is hard-coded in the Distributed Ledger Model rather than endogenously optimized by a profit-maximizing Monopolist. This distinction is key.<sup>37</sup> Additionally, the decision to fix the quantity  $Q_A$  of APPENDS and run a Tullock contest is material, and meaningfully affects the analysis.<sup>38</sup> Finally, the decision to have a block reward (which directly rewards miners for purchasing APPENDS, even if they do not ultimately sell WRITES) is material, although our analysis shows limited impact on end-users (see Section 3.3.3).

### Connecting the Distributed Ledger Model to Distributed Ledgers in Practice.

First, we map aspects of Bitcoin onto the Distributed Ledger Model. Assuming that the Bitcoin protocol functions as intended,<sup>39</sup> let us first describe the interaction between Miners and Protocol. In order to produce a valid block, Miners must solve a “proof-of-work cryptopuzzle.” Specifically, Miners trade one hash computation for one independent Bernoulli trial to create a valid block.<sup>40</sup> Moreover, the success rate of each Bernoulli trial is dynamically adjusted by the Bitcoin protocol so that one block is created amongst the entire network every ten minutes. Each block provides 1 MB of space for the Miner to include transactions, and awards the miner a block reward (currently 3.125 BTC). So in our model, the interaction between Miners and Protocol captures the following aspect: Resource is hash computations. Each Miner  $i$  has some cost  $c_i^R$  to perform one hash computation.<sup>41</sup> APPENDS are units of space in a valid block, and Protocol has hard-coded that  $Q_A = 1$  MB per ten minutes are awarded in total and that each Miner receives a fraction of 1 MB blocks proportional to their hash computations (because the success probability of each hash dynamically adjusts to enforce a total quantity of 1 MB per ten minutes). Finally, the protocol hardcodes  $B = 3.125$  BTC per 10 minutes as the total block reward,<sup>42</sup> which is also distributed proportionally to miners according to their hash computations.

Aside from its interaction with Miners, Protocol simply maintains consensus on the contents of the ledger. For example, Protocol verifies validity of contents of the ledger, resolves any conflicts using “Nakamoto consensus” [35], and widely disseminates the ledger

<sup>36</sup>That is, End-Users are unit-demand and only want a single WRITE – if they win multiple auctions they do not get additional utility. Still, they make a payment in any auction they win.

<sup>37</sup>As noted above, it is *certainly* relevant to *also* study the meta-game by which protocol rules are formed, but the game induced by a fixed protocol would still be relevant for the entirety of Bitcoin’s existence.

<sup>38</sup>For example, conclusions would change if instead the protocol set a price  $p_A$  for APPENDS and sold whatever is demanded, even if  $p_A$  were determined exogenously. As previously noted, all blockchain protocols the authors are aware of run an Upstream Tullock contest, and it is not clear how to implement alternate Upstream market structures with a secure protocol.

<sup>39</sup>See Section 1.3 for a small subset of works describing manners by which the protocol may not function as intended.

<sup>40</sup>With extremely low probability of success – roughly  $2^{-78}$  at the time of writing.

<sup>41</sup>This includes electricity, operational costs, amortized hardware costs, etc.

<sup>42</sup>Note that this quantity halves every four years, as pre-specified by the Bitcoin protocol.

401 itself. In particular, the protocol rules suffice to identify a unique consistent ledger to  
 402 disseminate.

403 End-users get their transactions in a Bitcoin block by broadcasting to Miners. Each  
 404 transaction includes a transaction fee, which is paid to whichever Miner includes that  
 405 transaction in their block. Processing a transaction induces costs such as checking validity,  
 406 and maintaining network connectivity (to hear about transactions in the first place), which  
 407 are captured by  $c^W$  in our model. Miners are typically revenue-maximizing, and typically  
 408 fill their blocks with transactions paying the highest fees (and, to the best of the authors’  
 409 knowledge, typically without reserves). For a *patient* end-user, who wants their transaction  
 410 in the Bitcoin ledger eventually but not necessarily immediately, each Miner is a potential  
 411 seller running their own First-Price Auction, and the service offered by distinct miners is  
 412 indistinguishable.

413 It is also worth highlighting which of these aspects are key to fit our model, and which  
 414 are not. All permissionless distributed ledgers the authors are aware of run a Tullock Contest  
 415 in *some* Resource. Some (including Bitcoin Cash, Litecoin, Ethereum Classic) also use hash  
 416 computations as Resource (“proof-of-work”). Others (including Ethereum, Solana, Cardano)  
 417 use locked capital as Resource (“proof-of-stake”).<sup>43</sup> It is not material to our analysis which  
 418 Resource is used, only that the Protocol ultimately awards block space proportional to that  
 419 resource.

420 We note that [3] also model blockchain investment games as a Tullock contest, while  
 421 other works [29] instead model it as perfect competition with free entry. We briefly note that  
 422 free entry can also be captured arbitrarily well in our model by taking  $n \rightarrow \infty$  Miners with  
 423 identical  $c_i^R$  (see Theorem 11, for example).<sup>44</sup>

424 On the other hand, it is crucial for our model to accurately capture end-users that they  
 425 are *patient* and therefore equally happy to be included in any valid block. *Impatient* users  
 426 (such as those primarily motivated by DeFi applications) are not captured by our model.  
 427 Instead, impatient users view the particular block offered by the next Miner as the only  
 428 resource of interest, and therefore that Miner faces no competition. Therefore, a Miner selling  
 429 blockspace primarily to impatient users is instead a monopolist.

430 Additionally, observe that Miners(/Stakers) are free to use whatever “off-chain” auction  
 431 they like in order to sell space in their created blocks, independent of whatever “on-chain”  
 432 mechanism is hardcoded. For example, it is immaterial to our model that Bitcoin’s on-  
 433 chain mechanism is pay-your-bid, whereas Ethereum’s is a posted-price mechanism, because  
 434 Miners(/Stakers) in both protocols can run a first-price auction with reserve off-chain to  
 435 determine which transactions are included in the first place. On the other hand, the fact  
 436 that Ethereum’s EIP-1559 *burns*<sup>45</sup> revenue from the posted-price mechanism is material, and  
 437 can be captured in our model via  $c^W$ . That is, our model adopts the perspective of [24] that  
 438 EIP-1559 is really specifying a WRITE cost per included transaction (the burned base fee)  
 439 on each *Proposer*, and the Proposer is then free to run whatever off-chain auction they like  
 440 to build their block (rather than that EIP-1559 specifies *the* auction that Proposers *must*  
 441 run when facing users).

442 Finally, while all mainstream protocols the authors are aware of currently have a single  
 443 Proposer at each time slot, some protocols are now experimenting with “Multiple Concurrent

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<sup>43</sup>That is, Miners are now called Stakers, who trade one unit of locked capital per Bernoulli trial.

<sup>44</sup>Specifically, the final bullet concludes that the natural “market clearing equilibrium” becomes an equilibrium with sufficiently-many identical Miners.

<sup>45</sup>That is, transactions included in an Ethereum pay a posted-price (set by the Ethereum protocol) that is destroyed, and not awarded to the miner.

Proposer (MCP)” protocols. In these protocols, there is no longer a monopolist for each block slot. Instead, multiple Proposers have the opportunity to insert transactions. Interestingly, our model also captures MCP protocols with either patient or impatient users.<sup>46</sup>

In summary, the Distributed Ledger Model captures key aspects of many mainstream blockchain protocols (they are Tullock contests, and the protocol can impact  $c^W$ ), while not capturing others (such as impatient end-users, or blockchains with a heavy MEV ecosystem<sup>47</sup>). Indeed, this is in line with the motivation for our paper: Decentralization does not uniformly impact all users identically in all domains, and so our model necessarily picks one canonical domain of focus.

Throughout this section, we abuse notation and use  $(\vec{q}, \vec{r})$  to refer to the Downstream Equilibrium  $(\vec{q}, \vec{r})$  together with the mapping  $E(\cdot)$  that takes  $(\vec{q}, \vec{r})$  to the canonical End-User Equilibrium. We repeat the key takeaways of this section below:

- While Equilibria may not always exist, Proposition 8 establishes an upper bound on the price any Miner will set: any strategy that sets a price exceeding the monopoly reserve for  $D(\cdot)$  is a dominated strategy.
- Theorem 10 characterizes all potential Equilibria. In particular, there exists a single  $\vec{Q}$  such that Miner  $i$  wins  $Q_i$  APPENDS in all pure equilibria. From here, there is a unique “market-clearing” potential equilibrium (where each miner sets reserve at most  $D^{-1}(Q_A)$ ), and for each  $i$  a unique potential equilibrium where Miner  $i$  is a price-setter.
- Theorem 11 provides necessary and sufficient conditions for the “market-clearing” potential equilibrium to be an equilibrium.<sup>48</sup> Importantly, the condition *depends only on*  $D(\cdot)$ ,  $Q_A$ , and  $\max_i \{Q_i\}$ . That is, to the extent that a “measure of decentralization” impacts the ultimate price paid by end-users, the correct “measure of decentralization” is the market share of the largest miner.
- The magnitude of the block reward (or whether there is a block reward at all) *does not impact*  $\vec{Q}$ , *nor any of the potential Equilibria identified by Theorem 10*. But, a larger block reward makes Equilibria more likely to exist (see Proposition 12).

### 3.1 Higher-than-Monopolist Reserves are Dominated Strategies

Before reasoning about equilibria, we first reason about what reserves a Miner might set in an undominated strategy. Formally, we say that Downstream Strategy  $(q_i, r_i)$  dominates  $(q'_i, r'_i)$  if *in the game among Downstream Providers*,  $P_i((q_i, \vec{q}_{-i}), (r_i, \vec{r}_{-i})) \geq P_i((q'_i, \vec{q}_{-i}), (r'_i, \vec{r}_{-i}))$  for all  $\vec{q}_{-i}, \vec{r}_{-i}$ .

► **Proposition 8.** *Let  $r^*(D, Q_A) := \arg \max_{r \geq D_{\inf}^{-1}(Q_A)} \{(r - c^W) \cdot D(r)\}$ . Then for all Miners  $i$ , all  $q_i > 0$ , and all  $r_i > r^*(D, Q_A)$ ,  $(q_i, r^*(D, Q_A))$  dominates  $(q_i, r_i)$ .*

<sup>46</sup>To be extra clear, our model verbatim captures an MCP protocol where the block space in each block is partitioned according to stake (i.e. a 10% staker gets 10% of every block). Most MCP proposals instead sample a discrete number of Proposers proportional to stake, and allow each such Proposer an equal fraction of the block. Our model does not capture this verbatim, as the sampling process would meaningfully complicate analysis, but it would be a natural direction for follow-up work to modify our model to capture these MCP protocols verbatim.

<sup>47</sup>In blockchains with a heavy MEV ecosystem, the process of turning APPENDS into WRITES itself is cost-intensive and meaningfully asymmetric.

<sup>48</sup>In addition, we extend the necessary and sufficient conditions for the “market-clearing” equilibrium (when they exists) to the scenario where different Miners having different cost per WRITE in the full version.

Proposition 8 establishes an upper bound on what price could possibly arise, even out of equilibrium – it can be no worse than the price that would be set by a single Miner who produces all blocks.

### 3.2 Characterizing Equilibria (when they exist)

End-User Equilibria are analyzed in *Equilibria of Simultaneous First-Price Auctions* of Section 2, which describes how to determine the clearing price as a function of the Miners' strategies. This section focuses on analyzing Downstream Equilibria. While Pure Equilibria do not always exist (even when  $D(\cdot)$  is Regular – see Section 3.3.1), we are able to cleanly characterize all *potential* Pure Equilibria. Below, we outline the characterization.

- Taking investments  $\vec{q}$  as fixed, Miners have quantities  $\vec{Q}$ , which necessarily satisfy  $\sum_i Q_i = Q_A$  (as  $Q_A$  is exogenously set). In any Pure Equilibrium, it therefore must be that  $\vec{r}$  is a price-setting equilibrium for  $\vec{Q}$ .
- Taking reserves  $\vec{r}$  as fixed and the total quantity  $Q_A$  as fixed,  $\vec{q}$  must be an investment equilibrium. Knowing from previous analysis that any price-setting equilibrium has at most one price-setter, we can instead study: taking the clearing price  $r$ , the price-setter  $i$ , and the total quantity  $Q_A$  as fixed,  $\vec{q}$  must be an investment equilibrium. This is *almost* like asking for an equilibrium in the Tullock contest defined by costs  $c_i^R$  and total reward  $(r - c^W) \cdot D(r) + B \cdot Q_A$ .
  - But, the game is not *exactly* a Tullock contest. Indeed, no one gets reward  $((r - c^W) \cdot D(r) + B \cdot Q_A) \cdot q_i / \sum_j q_j$  – all  $j \neq i$  receive reward  $(r - c^W + B) \cdot Q_A \cdot q_i / \sum_j q_j$ , and the price-setter  $i$  receives reward  $(r - c^W + B) \cdot Q_A \cdot q_i / \sum_j q_j - (r - c^W) \cdot (Q_A - D(r))$ . However, after inspecting both reward formulas, *the marginal change in each Miners' payoff is identical to the marginal change in  $(r - c^W + B) \cdot Q_A \cdot q_i / \sum_j q_j$* . Therefore, the same local optimality conditions that must be satisfied by an equilibrium of a Tullock contest with total reward  $(r - c^W + B) \cdot Q_A$  must be satisfied by any equilibrium with clearing price  $r$ .
  - Importantly, however, while the equilibrium *investments* in a Tullock contest certainly depends on the total reward split, the equilibrium *resulting market shares* do not.
- The previous two bullets suggest the following as necessary conditions for a pure equilibrium:
  - The resulting market share of APPENDS won must match those in equilibrium of a Tullock contest where Miner  $i$  incurs cost  $c_i^R$  per Resource. Importantly, this equilibrium is unique and well-defined. Call this vector of quantities  $\vec{Q}^*(\vec{c})$ .
  - Let  $Q_i^{\text{OPT}} := \arg \max_{Q \in [\sum_{j \neq i} Q_j^*, Q_A]} \{(Q - \sum_{j \neq i} Q_j) \cdot D^{-1}(Q)\}$ . Then some Miner  $i$  is a price-setter at  $D^{-1}(Q_i^{\text{OPT}})$  (this includes the possibility that  $Q_i^{\text{OPT}} = Q_A$  for all  $i$ , and the unique possible Pure Equilibrium saturates all Miners).
  - Indeed, Theorem 10 confirms these characterize all potential Pure Equilibria.
- Ultimately, in order to be a Pure Equilibrium, the question is whether the pair  $(q_i, r_i)$  which can be changed in tandem is a best-response to  $\vec{q}_{-i}, \vec{r}_{-i}$ . The previous bullets expound upon necessary conditions for this to plausibly occur – if  $(q_i, r_i)$  is to be a best response to  $(\vec{q}_{-i}, \vec{r}_{-i})$ ,  $q_i$  must be a best response to  $(\vec{q}_{-i}, \vec{r}_{-i}; r_i)$ , and  $r_i$  must be a best response to  $(\vec{q}_{-i}, \vec{r}_{-i}, q_i)$ . Section 3.3.1 contains an example demonstrating the possibility of no Pure Equilibria.

We execute this outline in our full version – Theorem 10 characterizes all possible Pure Equilibria.

523 ► **Definition 9.** Define  $c^*(\bar{c}^R)$  to be the unique solution to  $\sum_{i=1}^n \max\{0, 1 - \frac{c_i^R}{c^*(\bar{c}^R)}\} = 1$ .<sup>49</sup>  
 524 Further define  $x_i^*(\bar{c}^R) := \max\{0, 1 - \frac{c_i^R}{c^*(\bar{c}^R)}\}$ .

525 ► **Theorem 10.** Let  $(\vec{q}, \vec{r})$  be an Equilibrium in the Distributed Ledger Model, and let the  
 526 clearing price for End-Users be  $r$ . Then:

527 ■  $\sum_j q_j = Q_A \cdot (r + B - c^W) / c^*(\bar{c}^R)$ .

528 ■ For all Miners  $i$ ,  $\sum_j \frac{q_j}{c_j} = x_i^*(\bar{c}^R)$ .

529 Moreover,  $r \geq D_{\sup}^{-1}(Q_A)$ , and:

530 ■ If  $r = D_{\sup}^{-1}(Q_A)$ , then  $Q_A \cdot x_i^*(\bar{c}^R) \leq \frac{(x - c^W)(Q_A - D(x))}{x - r}$  for all  $i$  and all  $x > r$ .

531 ■ If  $r > D_{\sup}^{-1}(Q_A)$ , then there is a single price-setter  $i^*$ , who sets a price equal to  $r_{i^*} :=$   
 532  $\arg \max_{x > D_{\sup}^{-1}(Q_A)} \{(x - c^W) \cdot (D(x) + Q_A \cdot x_{i^*}^*(\bar{c}^R) - Q_A)\}$ . If an equilibrium of this  
 533 form exists, one certainly exists with  $i^* = 1$  as the price-setter (equilibria with other  
 534 price-setters are possible).

535 Importantly, observe in Theorem 10 that:

536 ■ Block rewards play no role in the ultimate clearing price, nor the resulting market share  
 537 of each Miner.<sup>50</sup>

538 ■ A necessary condition for an equilibrium to exist with clearing price  $D_{\sup}^{-1}(Q_A)$  (the  
 539 smallest possible clearing price) is only a function of  $x_1^*$ ,  $Q_A$ , and  $D(\cdot)$ . That is, to the  
 540 extent that a quantitative measure of decentralization plays a role in the ultimate price  
 541 paid by end-users, it is the size of the largest Miner. Moreover,  $x_1^*$  can be determined  
 542 only as a function of  $\bar{c}^R$ .

543 ■ That is, there is one term that depends only on  $\bar{c}^R$  ( $x_1^*(\bar{c}^R)$ ), and another that depends  
 544 only on  $c^W$  and  $D(\cdot)$  ( $\sup_{x > r} \{\frac{(x - c^W) \cdot (Q_A - D(x))}{x - r}\}$ ), and an Equilibrium that clears all  
 545  $Q_A$  WITNESSES made available by the protocol can plausibly exist if and only if  $x_1^*(\bar{c}^R) \leq$   
 546  $\sup_{x > r} \{\frac{(x - c^W) \cdot (Q_A - D(x))}{x - r}\}$ .

### 547 3.3 A Sufficient Condition for Pure Equilibria

548 Theorem 10 characterizes all possible pure Equilibria, and so it is tempting to proceed  
 549 with equilibrium analysis under these conditions. Unfortunately, pure Equilibria are not  
 550 guaranteed to exist in the Distributed Ledger Model. In Section 3.3.1 we provide an example  
 551 demonstrating this, and identify the barrier. This motivates a natural sufficient condition  
 552 that we analyze in Section 3.3.2. Along the way, we also discuss the impact of block rewards  
 553 on equilibria in Section 3.3.3.

#### 554 3.3.1 An Example with with Non-Existence

555 Consider a demand curve  $D(\cdot)$  with  $D(x) = 1 - x$  for all  $x \in [0, 1]$ ,  $Q_A = 1$ ,  $B = 0$ , and  
 556  $c^W = 0$ . Consider also  $n = 3$  miners each with  $c_i^R = 1$ . Then Theorem 10 concludes:

557 ■ In any potential equilibrium, it must hold that  $Q_i(\vec{q}, \vec{r}) = 1/3$  for all  $i$ .

558 ■ Fixing  $Q_1 = 1/3$ ,  $\arg \max_{x \geq 0} \{x \cdot (1/3 - x)\} = 1/6$ . Therefore, it is not possible to have  
 559 an equilibrium with clearing price  $r = D^{-1}(1) = 0$ .<sup>51</sup>

<sup>49</sup> [3] establish that  $c^*(\bar{c}^R)$  is well-defined – the proof is straight-forward.

<sup>50</sup> As noted previously, Block rewards do play a role in determining whether Pure Equilibria exist – see Section 3.3.3.

<sup>51</sup> Because in such an equilibrium, all three Miners earn profit zero, whereas any Miner could deviate to set a price of  $1/6$  and instead earn profit  $1/36$  (letting the other Miners earn profit  $1/18$ ).

- 560 ■  $c^*(1, 1, 1) = 3/2$ . Therefore, the only potential equilibria have one Miner as a price-setter
- 561 at price  $1/6$ , with  $\sum_j q_j = \frac{1/6}{3/2} = 1/9$  (and therefore each Miner has  $q_i = 1/27$ ).
- 562 ■ However, this is not an equilibrium. In this strategy profile, the price-setter earns revenue
- 563  $1/36$  from the simultaneous first-price auctions, but pays  $1/27$  in Resource cost, yielding
- 564 negative payoff. The price-setter would be better off not investing at all.

565 In particular, what stands out about this example is that a fully-saturated equilibrium  
 566 has absolutely no shot (because such an equilibrium would generate zero revenue in total).  
 567 This suggests a natural sufficient condition: that the fully-saturated equilibrium generate  
 568 *some* fraction of the optimal revenue a monopolist could earn.

### 569 3.3.2 A Sufficient Condition

570 Theorem 11 below states an interpretable sufficient condition for an equilibrium with clearing  
 571 price  $r = D^{-1}(Q_A)$ , and a technical condition that is necessary and sufficient when  $B = 0$ .

572 ► **Theorem 11.** *Consider a potential equilibrium  $(\bar{q}^*, \bar{r}^*)$  such that:*

- 573 ■ *The clearing price is  $r = D_{\sup}^{-1}(Q_A)$ .*
- 574 ■  *$\sum_j q_j^* = Q_A \cdot (r + B - c^W)/c^*(\bar{c}^R)$ .*
- 575 ■ *For all Miners  $i$ ,  $\sum_j \frac{q_i}{q_j} = x_i^*(\bar{c}^R)$ .*

576 *Then:*

- 577 ■ *If  $D(\cdot)$  is Regular and  $x_1^*(\bar{c}^R) \leq 1 - \frac{1}{D(0)/Q_A - 1}$ , then  $(\bar{q}^*, \bar{r}^*)$  is an Equilibrium.*
- 578 ■ *If  $B = 0$ , define  $k(z) := \frac{D_{\sup}^{-1}(z \cdot Q_A) \cdot z \cdot Q_A}{D_{\sup}^{-1}(Q_A) \cdot Q_A}$ . Then  $(\bar{q}^*, \bar{r}^*)$  is an Equilibrium if and only if*  
 579 
$$x_1^*(\bar{c}^R) \leq 1 - \sup_{z \in [0,1]} \left\{ \frac{k(z) - 1}{2 \cdot (\sqrt{k(z)/z} - 1)} \right\}$$

580 As previously noted, Theorem 11 provides interpretable sufficient conditions for  $Q_A$   
 581 WRITES to clear in Equilibrium (in Bullet One), and necessary and sufficient conditions  
 582 (when  $B = 0$ ) in Bullet Two. In both cases, the condition depends only on  $D(\cdot)$ ,  $Q_A$ , and  
 583  $x_1^*(\bar{c}^R)$ , highlighting the “size of the largest miner” (which can be computed as a function  
 584 only of  $\bar{c}^R$ ) as the relevant “measure of decentralization” for determining the economic impact  
 585 on end-users (in our model).

586 We can also use Theorem 11 to reason about modifications to the example in Section 3.3.1.  
 587 Consider the case of  $n$  Miners each with  $c_i^R = 1$ ,  $D(x) = 1 - x$  for all  $x \in [0, 1]$ ,  $B = 0$  and  
 588  $c^W = 0$ , but we will vary  $Q_A$ .

- 589 ■ Then Bullet One of Theorem 11 confirms it is an Equilibrium for  $Q_A$  WRITES to clear  
 590 (at price  $1 - Q_A$ ) as long as  $1/n \leq 1 - \frac{1}{1/Q_A - 1}$ , which can be rewritten as  $Q_A \leq \frac{n-1}{2n}$ .  
 591 For this particular example in Section 3.3.1, this is not particularly impressive, as even a  
 592 Miner controlling blockchain would sell all  $Q_A$  APPENDS as long as  $Q_A \leq 1/2$ .
- 593 ■ The more precise Bullet Two of Theorem 11 could be applied. In this case,  $k(z) =$   
 594  $\frac{z \cdot (1 - z \cdot Q_A)}{1 - Q_A}$ , and for example when  $Q_A = 3/4$ ,  $\sup_{z \in [0,1]} \left\{ \frac{k(z) - 1}{2 \cdot (\sqrt{k(z)/z} - 1)} \right\} = 2/3$ . There-  
 595 fore,  $n = 3$  identical Miners are sufficient in order for a Protocol with  $Q_A = 3/4$  to have  
 596 an Equilibrium where all  $Q_A$  WRITES are sold (whereas  $n = 1$  Miner is insufficient, as  
 597 such a Miner would choose to monopoly-price and sell only  $1/2$ ).

### 598 3.3.3 Block Rewards Support Existence of Pure Equilibria

599 In this section, we reason about the role of block rewards on equilibria. This section has two  
 600 main results, both below.

601 ► **Proposition 12.** *Let  $(\bar{q}^*, \bar{r}^*)$  induce a clearing price of  $r$ , and be an equilibrium of the*  
 602 *Distributed Ledger Model with Resource costs  $\bar{c}_R$ , WRITE cost  $c^W$ , demand curve  $D(\cdot)$ , and*  
 603 *block reward  $B$ . Then  $((1 + \frac{B' - B}{Q_A \cdot (r - c^W + B)}) \cdot \bar{q}^*, \bar{r}^*)$  is an equilibrium of the Distributed ledger*  
 604 *Model with Resource costs  $\bar{c}_R$ , WRITE cost  $c^W$ , demand curve  $D(\cdot)$ , and block reward  $B' > B$ .*

605 Proposition 12 establishes that higher block rewards support the existence of pure  
 606 equilibria (although Theorem 10 establishes that block rewards do not impact potential  
 607 pure equilibria themselves). This is of standalone interest for understanding the impact of  
 608 modeling parameters on end-users, and also a technical ingredient in the proof of Theorem 11.

609 Additionally, we show that if  $\bar{c}^R$  does not immediately rule out a market-clearing equilib-  
 610 rium, there is a sufficiently large block reward so that a market-clearing equilibrium exists.

611  
 612 ► **Proposition 13.** *Let  $\bar{c}^R, D(\cdot), Q_A, c^W, Q_A$  be such that  $Q_A \cdot x_i^*(\bar{c}^R) < \inf_{x > D_{\sup}^{-1}(Q_A)} \{ \frac{(x - c^W) \cdot (Q_A - D(x))}{x - D_{\sup}^{-1}(Q_A)} \}$ .*  
 613 *Then, there exists a sufficiently large  $B < \infty$  such that a market-clearing equilibrium exists*  
 614 *in the market defined by  $\bar{c}^R, D(\cdot), B, Q_A, c^W$ .*

## 615 4 Conclusion

616 We investigate decentralization as a means to insulate a natural monopoly from its derivative  
 617 services. We then draw conclusions regarding the ultimate utility of end-users as a function of  
 618 protocol parameters. We further highlight the impact of various aspects on our conclusions:  
 619 (a) our analysis applies to patient users (who are content with purchase from any miner)  
 620 and not impatient users (who view each miner as a monopolist anyway), (b) the relevant  
 621 “measure of decentralization” for impact on users’ price is the size of the largest miner (which  
 622 can be determined exclusively as a function of the profile of Resource investment costs, as in  
 623 a pure Tullock contest), (c) block rewards don’t impact users’ price at equilibrium, but can  
 624 influence whether equilibria exist.

625 Within distributed ledgers, our model considers the basic setup where users directly  
 626 interact with miners to include a transaction on the blockchain. Of course, many blockchain  
 627 ecosystems have evolved and now include additional parties (Builders and Layer-2s are two  
 628 notable examples). Our work provides a framework through which to ask: how does the  
 629 presence of these parties ultimately impact the service users receive?

630 Beyond our model, it is also important to endogenize aspects that our model treats as  
 631 exogenous. For example, our model treats as exogenous the fact that Bitcoin/Ethereum  
 632 run a Tullock contest in Computation/Stake. While this is an accurate representation of  
 633 all major blockchains since their inception, and Upstream protocol mechanics change *much*  
 634 more slowly than strategic Downstream decisions, these protocols are not truly exogenous –  
 635 protocol rules are set by some governance process (perhaps formally specified, perhaps not).  
 636 It is therefore an important direction for future work to additionally model the dynamics by  
 637 which protocol mechanics are determined. Additionally, our model treats the “lines” between  
 638 distinct miners/stakers as exogenous. While it is again the case that miners/stakers merge  
 639 at a *much* slower pace than adapting strategic Downstream decisions, miner/staker identities  
 640 are not exogenously fixed – parties might certainly merge and jointly strategize if they find  
 641 it beneficial. In particular, if all parties were to merge/collude or otherwise jointly strategize,  
 642 they could profit by setting monopoly prices, so it is important to additionally model the  
 643 process by which miners/stakers might merge, collude, or otherwise jointly strategize.

644 Beyond distributed ledgers, there are many natural monopolies for digital services that  
 645 pose challenges for traditional regulatory approaches [48]. Our results provide theoretical

foundations for exploring decentralized protocols as a tool that *might* prove useful to insulate such natural monopolies. Future work could, for example, consider decentralized protocols that manage marketplaces (allowing competition among matchmakers, search, etc.) or store social network data (allowing competition among UIs, content moderation, etc.). Our work motivates further investigation of decentralized protocols as a means to insulate natural monopolies in other domains in a detailed manner that can both (a) identify which natural monopolies might be amenable to insulation by a decentralized protocol, and (b) provide a complete analysis linking design choices of the decentralized protocol to impact on users.

Beyond insulating natural monopolies, our work contributes to an emerging line of works seeking theoretical foundations for the impact of decentralized systems on users [29, 46, 25, 41]. Significant further work along these lines is necessary in order to understand domains where decentralized systems have a shot at providing lasting value, even in the presence of highly-developed incumbents.

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