

# a2q4q5\_\_YOU

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## 1 A2: Q4 and Q5

```
[29]: import numpy as np
      from scipy.sparse import dok_matrix
      from copy import deepcopy
      import matplotlib.pyplot as plt
```

## 2 A2Q4a: SparseMatMult

```
[30]: def SparseMatMult(G, x):
      '''
          y = SparseMatMult(G, x)

          Multiplies a vector (x) by a sparse matrix G,
          such that  $y = G @ x$  .

          Inputs:
              G is an  $N \times M$  dictionary-of-keys (dok) sparse matrix
              x is an  $M$ -vector

          Output:
              y is an  $N$ -vector
      '''
      rows, cols = G.nonzero()
      Nrows, Ncols = np.shape(G)
      y = np.zeros(Nrows)

      # === YOUR CODE HERE ===
      size = len(rows)
      for n in range(size):
          i = rows[n]
          j = cols[n]
          y[i] += x[j]*G[i,j]

      return y
```

```
[31]: # Simple test
#      [1  0  0]      [ 0.1 ]
# A = [0  1 -1]  b = [ 0.2 ]
#      [0  2  0]      [ 0.3 ]
A = dok_matrix((3,3), dtype=np.float32)
A[0,0] = 1
A[1,2] = -1
A[1,1] = 1
A[2,1] = 2
b = np.array([0.1, 0.2, 0.3])
y = SparseMatMult(A, b)
print(f'y = {y}')
print(f'Answer should be [ 0.1 -0.1  0.4]')
```

```
y = [ 0.1 -0.1  0.4]
Answer should be [ 0.1 -0.1  0.4]
```

### 3 A2Q4b: PageRank

```
[77]: def PageRank(G, alpha):
    '''
        p, iters = PageRank(G, alpha)

        Computes the Google Page-rank for the network in the adjacency matrix G.

        Note: This function never forms a full R×R matrix, where R is the number
              of node in the network.

        Input
        G      is an R×R adjacency matrix, G[i,j] = 1 iff node j projects to node i
        ↪ i

        Note: G must be a dictionary-of-keys (dok) sparse matrix
        alpha is a scalar between 0 and 1

        Output
        p      is a probability vector containing the Page-rank of each node
        iters   is the number of iterations used to achieve a change tolerance
              of 1e-8 (changes to elements of p are all smaller than 1e-8)
    '''
    R = np.shape(G)[0]
    rows, cols = G.nonzero()
    iters = 0

    # === YOUR CODE HERE ===
    # calculate degrees
    deg = np.zeros(R)
```

```

for j in range(R):
    for x in cols:
        if (x == j):
            deg[j] += 1
#print(f'degs: {deg}')
# make P
P = G
for n in range(len(rows)):
    i = rows[n]
    j = cols[n]
    P[i,j] = 1/deg[j]
    #print(f'value at {i},{j} = {P[i,j]}')
# make initial p
p = np.zeros(R)
for i in range(R):
    p[i] = 1/R
#print(f'p = {p}')

# iterate
diff = 1
iters = 0
while (abs(diff) > 0.00000001):
    oldp = np.zeros(R)
    for i in range(R):
        oldp[i] = p[i]
    #print(f'{oldp}')
    degtimesp = np.zeros(R)
    for i in range(R):
        if (deg[i] == 0):
            degtimesp[i] = (p[i])/R
        else:
            degtimesp[i] = 0
    ptimesp = SparseMatMult(P, p)
    #print(f'd times p = {degtimesp}')
    #print(f'P times p = {ptimesp}')
    # generate new p
    for i in range(R):
        p[i] = (ptimesp[i]+degtimesp[i])*alpha + (1-alpha)/R
    #print(f'    new p = {p}')
    # compare
    diffs = np.zeros(R)
    for i in range(R):
        diffs[i] = abs(p[i]-oldp[i])
        #print(f'diffs[{i}] = abs({p[i]}-{oldp[i]}) = {diffs[i]}')
    diff = max(diffs)
    iters += 1

```

```
return p, iters
```

```
[78]: A = dok_matrix((6,6), dtype=np.float32)
A[1,0] = 1
A[0,3] = 1
A[0,5] = 1
A[2,1] = 1
A[3,1] = 1
A[3,2] = 1
A[4,2] = 1
A[5,2] = 1
A[5,4] = 1
# its the example from the lecture
alph = 0.85
p, iters = PageRank(A, alph)
print(f'p = {p}, {iters} iterations')
```

```
p = [0.26752809 0.25239887 0.13226952 0.16974589 0.06247637 0.11558128], 38
iterations
```