

LECTURE 7: RISK ADJUSTMENT + QUALITY COMPETITION

① GILBERT + MCGUIRE (2000):

- consumer types i.e. $\{H, L\}$
 $\begin{matrix} \uparrow & \uparrow \\ \lambda & 1-\lambda \\ (\text{sick}) & (\text{healthy}) \end{matrix}$
- two illnesses $j \in \{a, c\}$
 $\begin{matrix} \uparrow & \uparrow \\ \text{acute} & \text{chronic} \\ \downarrow & \\ \text{occurs with} & \\ (\text{normalized}) \text{prob. } 1 & \end{matrix}$
↳ This is where adverse selection enters: $P_h > P_c$
- costs to treat: $\{m_a, m_c\}$
- insurance premium: r

PATIENT

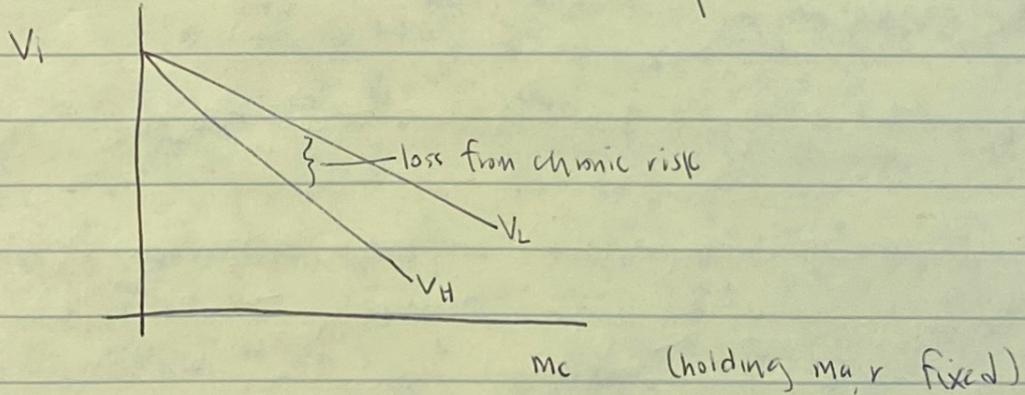
Then utility is: $V_i(m_a, m_c, r) = \underbrace{v_a(m_a)}_{\text{normalized}} + p_c v_c(m_c) - r$

to always happen

→ side note: why no risk aversion for patients?

NOTE: Who is better off with insurance?

What is the adverse selection problem here?

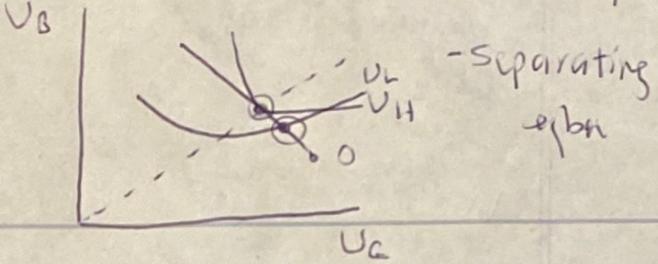


SOCIAL PLANNER

GOALS: ① Efficiency: $v'_a(m_a^*) = v'_c(m_c^*) \Rightarrow$ why?

* MC of treatment is 1 for both a and c! *

Recall the Rothschild + Stiglitz graph:



(2) (2) Equity in premiums:

$$r^* = m_a^* + [\lambda p_H + (1-\lambda)p_L] m_c^*$$

$\underbrace{m_a^*}_{\text{w/ } p_i=1} \quad \underbrace{[\lambda p_H + (1-\lambda)p_L] m_c^*}_{\text{Average } p(c=1)}$

Average $p(c=1)$
Expected insurer cost \Rightarrow goals 1 + 2 define ΦD

- what is the adverse selection problem here?

- Can you work out the math? [from patient perspective]

* without adjustment, what happens to market?

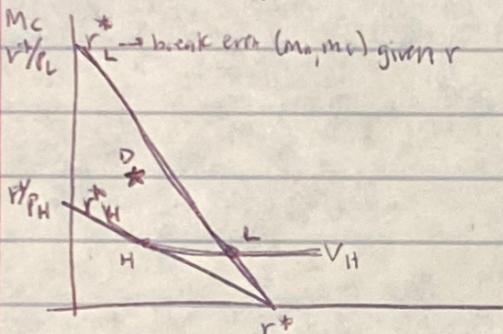
- low types will not have full insurance

- this is unfair as well as inefficient!

Premiums

Provider

Note H contracts are less generous in treating C.



D is socially desired point (on pricing line M_A where $MB = MC = 1$)

Competitive form: An equilibrium requires that we stipulate contracts (p_m^*, m_a^*, r^*)

such that:

- consumers maximize expected utility
- insurers make 0 profits

Our competitive rfa is not efficient - can risk adjustment help?

Risk Adj.

- Signals of is type (H, L) are shown to regulators + plans:

so $\{0, 1\}$ where $P(S=1|H) > P(S=1|L)$
↑ ↙ good signal bad signal

- signals are "noisy": $q_i = P(S=1 | i \in \{H, L\})$ [so $q_H > q_L$]

- Then posterior beliefs $\lambda_i = P(i=H | S=1) = \frac{P(S=1 | i=H) \cdot P(i=H)}{P(S=1)}$

so $\lambda_H \approx \lambda \cdot q_H$ and $\lambda_L \approx (1-\lambda) \cdot q_L$

GLAZER + MCGUIRE (2000) continue

- Signals give information on contracting C
- Is this a separating equilibrium? \Rightarrow ~~not if design of plans is similar.~~
— Yes B.V.T...

Now model looks like:

1. Everyone pays r^*
2. Plans choose (m_a^*, m_c^*) for r^*
3. Consumers buy plans
4. Regulator pays plans: $\tilde{r}^* = m_a^* + [p_H \lambda_s + (1-\lambda_s) p_L] m_c^*$
for $s \in \{0, 1\}$

Now two contracts exist:

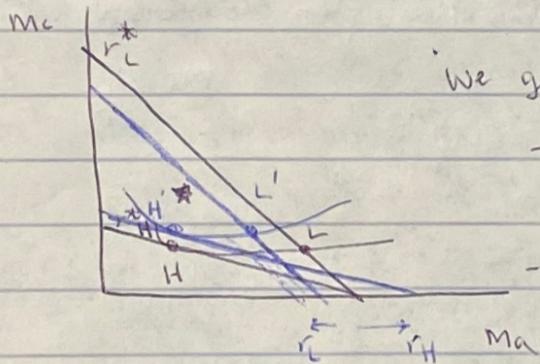
$$\textcircled{1} \text{ for H types: } (m_{aH}, m_{cH}) = \underset{\text{argmax}}{\left[v_a(m_a) + p_H v_c(m_c) \right]}$$

\rightarrow same

$$\text{s.t. } m_a + p_H m_c - \tilde{r}_H = 0$$

\hookrightarrow risk-adjusted payment

$$\textcircled{2} \text{ for L types: } (m_{aL}, m_{cL}) = \underset{\text{argmax}}{\left[v_a(m_a) + p_L v_c(m_c) \right]} \text{ s.t. } m_a + p_L m_c - \tilde{r}_L = 0$$



we get closer to D!

- conventional risk adjustment helps,
- but does not resolve issues.
- How does this affect goals $\textcircled{1} + \textcircled{2}$?

OPTIMAL RISK ADJUSTMENT

\hookrightarrow compensate a weak signal with a tax/subsidy transfer

- what if we "over" or "under" paid based on signals?

$$\text{Table } r_H^* = m_a^* + p_H m_c^*$$

$$r_L^* = m_a^* + p_L m_c^*$$

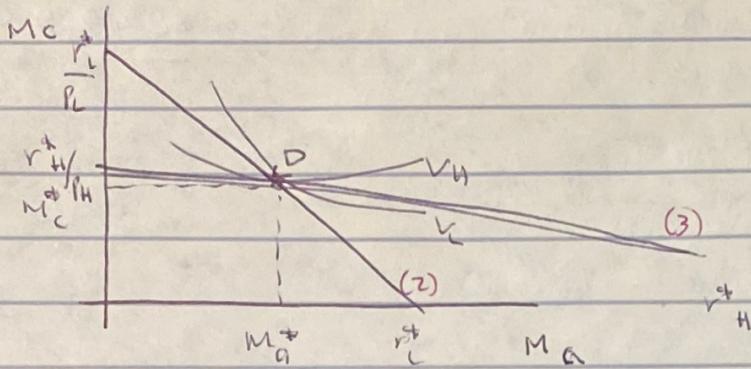
$$\Leftrightarrow r_H^* = q_H r^* + (1-q_H) r_o^*$$

$$r_L^* = q_L r^* + (1-q_L) r_o^* \leftarrow \begin{array}{l} \text{what you} \\ \text{pay for} \\ \text{what you pay for} = 1 \end{array}$$

We want to implement this

this does so

NOW WE GET A POOLING EQUILIBRIUM:



key insight: $r_0^* + r_1^*$
more around slopes of (2)
and (3)

PROOF SKETCH:

goal: need to show that (r_H^*, r_L^*) is (1) an eqbm

(2) the socially optimal eqbm

STEP 1: construct candidate eqbm: $(m_A^*, m_C^*, r^*) \mid r_H^*, r_L^*$ (1)

STEP 2: rule out alternate paths

1. A Pareto-improvement \rightarrow does not exist since (1) is efficient

2. A "cream-skimming" plan } does not exist: no other profit-maximizing

3. A "H-type, profit-making" plan } solution given slope of (2) + (3)



What are r_0^* , r_1^* ?

$$r_0^* = [q_H r_L^* - q_L r_H^*] / [q_H - q_L]$$

$$r_1^* = [(1-q_L)r_H^* - (1-q_H)r_L^*] / [q_H - q_L]$$

Intuitively:

- if signal is imprecise ($q_H \rightarrow 0$), then payment differences get large ($r_1^* \rightarrow \infty$, $r_0^* \rightarrow -\infty$)

What is actually provided?

PROVIDERS

First, no risk adjustment:

$$V(e, m) = \tilde{\lambda}_0(e) \pi_L + (1 - \tilde{\lambda}_0(e)) \pi_H - e - m + \tilde{\lambda}_1(e, m) \pi_L + (1 - \tilde{\lambda}_1(e, m)) \pi_H$$

Providers choose (e, m) to maximize:

- note $\pi_L > \pi_H$ (easier to treat healthier patients)
- hence, what happens in e, m ? Focus on L types

Now, what about risk adjustment?

- if risk adjustment is perfect, $\pi_L - \pi_H \rightarrow 0$
- then

$$V(e, m) = \tilde{\lambda}_0(e) \pi - e - m + \pi$$

* what is optimum now? $e^* = 0$ (good!)

$m^* = 0$ (bad!)

How can we fix this? Pay-for-prevention

- give providers a bonus $\alpha [x(m) - x(0)]$

L average prevention

- now $V(e, m) = \pi - e - m + \alpha [x(m) - x(0)]$

so m^* solves: $\alpha [x'(m)] = 1$

- provider chooses α s.t. $\alpha = \tilde{\lambda}_0(e) \left[\frac{(B_L - B_H)(\alpha - \alpha_0)}{(\alpha - \alpha_0) - (B_L - B_H)} \right]$

$$\times [(B_L - C_L) - (B_H - C_H)]$$

- is this feasible?

(2)

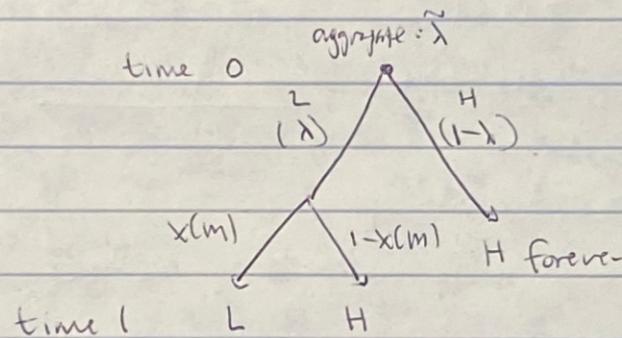
EAGLETON, ELLIS + LU (2012) : Risk adjustment + prevention

- dynamic distortions from RA:

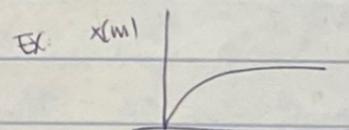
- still have $i \in \{L, H\}$ with costs $c_L < c_H$

\uparrow \uparrow
 $1-\lambda$ λ

- but patient risk can change over time!



m (~~represents~~) represents health investment
and $x(m)$ $\Pr(i=L|m)$.



Suppose $\tilde{\lambda}(e, m)$ where $\tilde{\lambda}_e = \tilde{\lambda}_0(e)x(m)$.

Can we implement m^* ?

SOCIALPLANNER

m^* is defined based on: $W = B(m) - m - e$

$$B(m) = \tilde{\lambda}_0(e)x(m) \left\{ [B_L - c_L] - [B_H - c_H] \right\}$$

net benefit from m for L

$\rightarrow e=0$ (why?)

\rightarrow Hence the FOC is given by

$$\frac{dB(m)}{dm} = 0 \text{ or } \tilde{\lambda}_0(e) [B_L - c_L] - [B_H - c_H] x'(m) = 1.$$

note $B_L > B_H$ and $c_L < c_H$

\rightarrow Notes on comparative statics:

- As $\tilde{\lambda}_0 \uparrow$ (lower aggregate risk), $x'(m) \downarrow \Rightarrow$ more investment in prevention
- As relative benefits \uparrow , same response.