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Nusa Zidaric

Nusa Zidaric Email: email Homepage: http://

# **Abstract**

The GAP package FSR ...

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# Acknowledgements

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# **Contents**

1	Preface	4
2	Output formatting functions and TEX drawing functions 2.1 Output formatting functions	<b>5</b> 5
3	FSR (Feedback Shift Register) 3.1 Common functionality	7 7 10 13
4	misc - helper functions 4.1 misc - helper functions	<b>17</b> 17
Re	eferences	18
Index		

# **Preface**

The GAP package FSR implements Feedback Shift Registers

# Output formatting functions and TEX drawing functions

# 2.1 Output formatting functions

There are two types of functions: ones that return the input in a human friendly version (as strings or list of strings), and ones that write the human friendly version of the input into a file (txt or tex)

## 2.1.1 IntFFExt

```
        ▷ IntFFExt([B, ]ffe)
        (method)

        ▷ IntVecFFExt([B, ]vec)
        (method)

        ▷ IntMatFFExt([B, ]M)
        (method)
```

IntFFExt takes the *ffe* and writes it as an integer of the prime field if *ffe* is an element of the prime field (same as Int(ffe)), or writes it as a vector of integers from the prime subfield if *ffe* is an element of an extension field, using the given basis *B* or canonical basis representation of *ffe* if no basis is provided.

IntVecFFExt takes the vector vec of FFEs and writes it in a human friendly version: as a vector of integers from the prime field if all components of vec belong to a prime field, or as a vector of vectors of integers from the prime subfield, if the components belong to an extension field, using the given basis B or canonical basis representation of ffe, if no basis is provided. (note: all components are treated as elements of the largest field).

IntMatFFExt takes a matrix M and returns its human friendly version: a matrix of vectors of integers from the prime field if all components of M belong to a prime field, or a vector of row vectors, whose elements are vectors of integers from the prime subfield, if the components belong to an extension field, using the given basis B or canonical basis representation of components of M.

NOTE: the non-basis versions return a representation in the smallest field that contains the element. for representation in a specific field, use the basis version with desired basis.

## 2.1.2 VecToString

VecToString([B, ]vec)

(method)

Writes a FFE verctor or matrix as string or list of strings using the given basis *B* or canonical basis representation of *ffe* if no basis is provided. This mathod calls methods IntFFExt, IntVecFFExt and IntMatFFExt from section LINK. The list of strings is more practically useful: we wish to have the components as srings, therefore the human friendly version of a matrix is not an actual string.

NOTE: the non-basis versions return a representation in the cononical basis of the smallest field that contains the element. For representation in a specific field, use the basis version with desired basis.

## 2.1.3 WriteVector (for a FFE and given basis)

```
▷ WriteVector(output, B, vec)
```

(function)

Writes the human friendly version of vector *vec* represented in basis *B*, to the output file *output*. Also works if *vec* is an integer or FFE.

NOTE: the basis MUST be provided.

Also works for writing matrices, but writes them as a row vector, not as a rectangle.

# 2.1.4 WriteMatrix (for a matrix of FFE and given basis)

```
▷ WriteMatrix(output, B, M)
```

(function)

Writes the human friendly version of matrix M represented in basis B to the output file output nicely formatted (rectangular, each row in a new line).

NOTE: the basis MUST be provided.

# 2.1.5 WriteMatrixTEX

▷ WriteMatrixTEX(output, M)

(function)

Writes the TEX code for matrix M over a prime field to the output file output.

NOTE: Only works for matrices over a prime field !!!

# 2.2 TEX drawing functions

# FSR (Feedback Shift Register)

# 3.1 Common functionality

We define an object FSR (Feedback Shift Register), which can come in two flavours: with linear feedback LFSR (3.2.1) and nonlinear feedback NLFSR (3.3.2). Because of many similarities between the two, the basic common functionality can be found here, while specialized functions (such as LFSR and NLFSR object creation) in corresponding sections.

#### **3.1.1** IsFSR

▷ IsFSR (filter)

This is the category of FSR objects. Objects in this category are created using functions LFSR (3.2.1) or NLFSR (3.3.2).

# 3.1.2 FieldPoly

FieldPoly of the fsr stores the irreducible polynomial used to construct the extension field or 1 in case of a prime field.

UnderlyingField of the fsr is the finite field over which the fsr is defined (all indeterminates and constants are from this field).

NOTE: it may seem redundant to sore both FieldPoly and UnderlyingField, however, they are used by other functions in the package.

FeedbackVec of the *fsr* stores the coefficients of the CharPoly without its leading term in case of LFSR, and coefficients of the nonzero monomials present in the multivariate function defining the feedback in case of NLFSR.

 ${\tt OutputTap}$  holds the output tap position(s): the sequence elements are taken from the stage(s) listed in  ${\tt OutputTap}$ .

# **3.1.3** Length

Length of the fsr is the number of its stages.

InternalStateSize of the fsr is size in bits needed to store the state  $length \cdot width$ , where width = DegreeOverPrimeField(UnderlyingField(fsr))

## 3.1.4 LoadFSR

 $\triangleright$  LoadFSR(fsr, ist) (method)

Loading the fsr with the initial state ist, which is a FFE vector of same length as fsr and with elements from its underlying finite field. If either of those two requirements is violated, loading fails and error message appears. At the time of loading the initial sequence elements (ie zeroth elements) are obtained and numsteps is set to 0.

# 3.1.5 StepFSR

▷ StepFSR(fsr[, elm]) (method)

Perform one step the fsr, ie. compute the new state and update the numsteps, then output the elements denoted by OutputTap. If the optional parameter elm is used then the new element is computed as a sum of computed feedback and elm. Elemen elm must be an element of the underlying finite field.

As this is a way to destroy the linearity of an LFSR, we refer to StepFSR with the optiomal nonzero elm as nonlinear step. Similarly, the NLFSR can also have an extra element added to the (already nonlinear) feedback.

Returns an error if the fsr is not loaded!

## 3.1.6 RunFSR

▷ RunFSR(fsr[, B, ist, num, pr]) (method)

**Returns:** A sequence of elements generated by FSR.

The fsr will be run for a certain (num or threshold) number of steps: there is a threshold value, currently set to  $2^{\sim}Length(fsr) + Length(fsr)$ , which is used by all versions without explicit num and enforced when num exceeds threshold. There is an optional printing switch pr, with default set to false; if true then the state and the output sequence element(s) are printed in GAP shell on every step of the fsr (we call this output for RunFSR), and the given basis B is used for representation of elements. Note that having both a pint switch and a basis is redundant, however, the additional boolean helps the method selection to distinguish between calls with basis and calls with both initial state ist and the evector of FFE elements elmvec to be used for nonlinear steps (because all three vectors return true for IsFFECollection).

- RunFSR(fsr[, B, num, pr] ) run fsr for num/threshold steps with/without output
- RunFSR(fsr, [B,] ist[, num, pr]) load fsr with ist, then run fsr for num/threshold steps with/without output (ie. linear version)

• RunFSR(fsr, [B,] elm[, num, pr]) - run fsr for num/threshold steps, whereby the SAME element elm is added to the feedback at each step, with/without output (ie. non-linear version)

• RunFSR(fsr, [B,] ist, elmvec[, pr]) - load fsr with ist, then run fsr for Length(elmvec) steps, whereby one element of elmvec is added to the feedback at each step (starting with elmvec[1]), with/without output (ie. non-linear version). NOTE: the sequence returned has length Length(elmvec)+1, because the zeroth sequence element is returned at the time of loading the FSR.

For the load and run versions, element seq<sub>0</sub> is a part of the output sequence, hence the output sequence has the length num+1/threshold+1/Length(elmvec)+1.

For versions without the loading of ist, calling RunFSR returns an error if the fsr is not loaded! The ouput of RunFSR is:

- sequence of FFEs: seq<sub>0</sub>, seq<sub>1</sub>, seq<sub>2</sub>, ..., for Length(OutputTap)=1
- sequence of vectors, each of them with t FFEs:  $seq_0$ ,  $seq_1$ ,  $seq_2$ , ..., where  $seq_i = (seq_{i1}, ..., seq_{it})$  for Length(OutputTap)=t

Example of RunFSR called for an lfsr *test* over  $F_{2^4}$ , with initial state *ist*, print switch *true* for basis B, with run length 5:

```
\_ Example \_
gap> K := GF(2);; x := X(K, "x");;
gap> f := x^4 + x^3 + 1;; F := FieldExtension(K, f);; B := Basis(F);;
gap> y := X(F, "y");; 1 := y^4 + y + Z(2^4);;
gap> test := LFSR(K, f, 1);;
< empty LFSR given by CharPoly = y^4+y+Z(2^4)>
gap> ist :=[0*Z(2), Z(2^4), Z(2^4)^5, Z(2)^0];;
gap> RunFSR(test, B, ist, 5, true);
using basis B := [ Z(2)^0, Z(2^4)^7, Z(2^4)^14, Z(2^4)^6 ]
                  [3,....,0] with taps [0]
              [[0,0,0,0],[0,1,1,0],[1,1,0,1],[1,0,0,0]]
              [[1, 0, 1, 1], [0, 0, 0, 0], [0, 1, 1, 0], [1, 1, 0, 1]]
              [[0, 1, 1, 1], [1, 0, 1, 1], [0, 0, 0, 0], [0, 1, 1, 0]]
              [[1,0,1,1],[0,1,1],[1,0,1,1],[0,0,0,0]
              [[1, 0, 1, 1], [1, 0, 1, 1], [0, 1, 1, 1], [1, 0, 1, 1]]
              [[1, 1, 0, 1], [1, 0, 1, 1], [1, 0, 1, 1], [0, 1, 1, 1]]
[ Z(2)^0, Z(2^2), Z(2^4), 0*Z(2), Z(2^4)^2, Z(2^4)^{11} ]
```

Example of RunFSR called for an lfsr *test* over  $F_{24}$ , with initial state *ist*, print switch *true* for basis B, with 5 nonlinear inputs :

In both examples above the there is a column *elm*, which is in first case empty, because we are not adding nonlinear inputs to the feedback, while in the second example, this column shows the element being added at each step (empty in first row - the loading step). Also note that the two examples above use the call LoadFSR, which adds the elm seq<sub>0</sub> to the sequence, so both sequences above are of length num+1/Length(elmvec)+1, ie 6. The last row in both examples is the actual sequence obtained from this run, and is kept in Zechs logarithm representation.

```
Example

gap> RunFSR(test, ist); Length(last);

[ Z(2)^0, Z(2^2), Z(2^4), 0*Z(2), Z(2^4)^2, Z(2^4)^11, Z(2^4)^2, Z(2^4)^2, Z(2^2), Z(2^4)^7, Z(2^2)^2, Z(2^2)^2, Z(2^4)^14, Z(2^4)^8, Z(2^4)^3, Z(2^2)^2, Z(2^4)^2, Z(2^4), Z(2^4)^2, Z(2^4)^9 ]

21
```

Last example above shows a sequence of length 21, ie *threshold+1*, getting first sequence element from LoadFSR followed by *threshold* iterations of StepFSR.

# 3.2 LFSR specific funcionality

#### 3.2.1 LFSR

Returns: An empty LFSR with components init, state and numsteps

Different ways to create an LFSR oblject, main difference is in creation of the underlying finite field.

Inputs:

- F the underlying finite field (either an extension field or a prime field)
- charpol LFSR dfining polynomial
- fieldpol defifning polynomial of the extension field (must be irreducible)
- p characteeristic
- m degree of extension (degree of fieldpol)
- *n* length of LFSR (degree of *charpoly*)
- tap optional parameter: the output tap (must be a positive integer or a list of positive integers) and will be changed to the default S\_0 if the specified integer is out of LFSR range.

# Compoents:

- init FFE vector of length n=deg(charpol), storing the initial state of the LFSR, with indeces from n-1, ..., 0
- state FFE vector of length n=deg(charpol), storing the current state of the LFSR, with indeces from n-1, ..., 0
- numsteps the number of steps performed thus far (initialized to -1 when created, set to 0 when loaded using LoadFSR (3.1.4) and incremented by 1 with each step (using StepFSR (3.1.5)))

Attributes FieldPoly (3.1.2), UnderlyingFied (??), CharPoly, FeedbackVec (3.1.2), Length (3.1.3) and OutputTap (3.1.2) and the property IsLinearFeedback are set during the construction of anLFSR.

If there is something wrong with the arguments (e.g. attempting to create an extension field using a reducible poynomial), an error message appears and the function returns fail.

Example below shows how to create an empty LFSR over  $F_{24}$  created as extension of  $F_2$ , called *test*:

```
gap> K := GF(2);; x := X(K, "x");;
gap> f := x^4 + x^3 + 1;; F := FieldExtension(K, f);;
gap> y := X(F, "y");; 1 := y^4+ y+ Z(2^4);;
gap> test := LFSR(K, f, 1);
< empty LFSR given by CharPoly = y^4+y+Z(2^4)>
```

## 3.2.2 IsLinearFeedback

```
▷ IsLinearFeedback(1fsr) (property)
▷ IsLFSR(1fsr) (filter)
```

If we were to represent the *lsfr* with a multivariate polynomial, DegreeOfPolynomial would return 1 - the feedback polynomial is linear and *lsLinearFeedback* is set to *true*. (ie. only linear terms are present: monomials with only one variable)

Filter IsLFSR is defined as and-filter of IsFSR and IsLinearFeedback.

#### 3.2.3 CharPoly

Attribute holding the characteristic polynomial (the feedback polynomial).

# 3.2.4 IsPeriodic

```
▷ PeriodReducible(lfsr)
```

(method)

Properties, attributes and methods concerning the periodicity of the output sequence(s), generated by the *lsfr*.

Properties:

- IsPeriodic: true if constant term of CharPoly != 0 (8.11 lidl, niederreiter)
- IsUltPeriodic: true if IsLFSR is true (8.7 lidl, niederreiter)
- IsMaxSeqLFSR: true if CharPoly is primitive (ref???)

Attributes:

• Period: holds the period of the UNKNOWNEntity(LFSR)

Methods to compute the period:

- PeriodIrreducible:
- PeriodReducible:

# 3.2.5 ViewObj

Different detail on the *lfsr* created by LFSR (3.2.1):

- Display/View: show the CharPoly and wheter or not the lsfr is empty
- Print: same as Display/View if *lsfr* is empty, otherwise it also shows the values of the three components init, state and numsteps
- PrintAll: same as Print if *lsfr* is empty, otherwise it also shows the values of the three components init, state and numsteps with additional information about the underlying field and the tap positions.

Both Print and PrintAll can be used with optional parameter basis B for desiered output format. Below are examples of output

```
gap> K := GF(2);; x := X(K, "x");;
gap> f := x^4 + x^3 + 1;; F := FieldExtension(K, f);; B := Basis(F);;
gap> y := X(F, "y");; 1 := y^4+ y+ Z(2^4);;
gap> test := LFSR(K, f, 1);;
gap> Print(test);
Empty LFSR given by CharPoly = y^4+y+Z(2^4)
gap> LoadFSR(test, ist);
Z(2)^0
gap> Print(test);
LFSR given by CharPoly = y^4+y+Z(2^4)
```

```
with initial state = [0*Z(2), Z(2^4), Z(2^2), Z(2)^0]
with current state = [0*Z(2), Z(2^4), Z(2^2), Z(2)^0]
after 0 steps
gap> RunFSR(test,5);
[ Z(2^2), Z(2^4), 0*Z(2), Z(2^4)^2, Z(2^4)^1]
gap> Print(test);
LFSR given by CharPoly = y^4+y+Z(2^4)
with initial state = [0*Z(2), Z(2^4), Z(2^2), Z(2)^0]
with current state = [Z(2^2), Z(2^4)^2, Z(2^4)^2, Z(2^4)^1]
after 5 steps
gap> PrintAll(test);
LFSR over GF(2^4) given by CharPoly = y^4+y+Z(2^4)
with feedback coeff = [0*Z(2), 0*Z(2), Z(2)^0, Z(2^4)]
with initial state = [0*Z(2), Z(2^4), Z(2^2), Z(2)^0]
with current state = [Z(2^2), Z(2^4)^2, Z(2^4)^2, Z(2^4)^{11}]
after 5 steps
with output from stage S_0
gap> PrintAll(test, B);
LFSR over GF(2^4) defined by FieldPoly=x^4+x^3+Z(2)^0 given by CharPoly = y^4+y+Z(2^4)
with feedback coeff =[ [ 0, 0, 0, 0 ], [ 0, 0, 0, 0 ], [ 1, 0, 0, 0 ], [ 0, 1, 1, 0 ] ]
with initial state =[ [ 0, 0, 0, 0 ], [ 0, 1, 1, 0 ], [ 1, 1, 0, 1 ], [ 1, 0, 0, 0 ] ]
with current state =[[1, 1, 0, 1], [1, 0, 1, 1], [1, 0, 1, 1], [0, 1, 1, 1]]
after 5 steps
with output from stage S_0
```

# 3.3 NLFSR specific funcionality

## 3.3.1 ChooseField

```
\triangleright ChooseField(F) (function)
```

Workaround for the NLFSR object definition: we need to fix the chosen underlying finite field and prepare indeterminates in the chosen field. The indeterminates will be used for the multivariable polynomial, which will define the NLFSR feedback. Current threshold is set by global MaxNLFSRLen = 100.

#### **3.3.2 NLFSR**

```
▷ NLFSR(K, clist, mlist, len[, tap])

▷ NLFSR(K, fieldpol, clist, mlist, len[, tap])

(function)

(function)
```

Returns: An empty NLFSR with components init, state and numsteps

Different ways to create an NLFSR oblject, main difference is in creation of the underlying finite field.

NOTE: before creating the NLFSR, we must always create the indeterminates to be used for the feedback using ChooseField function call!!! please see example below

Inputs:

• F - the underlying finite field (either an extension field or a prime field)

- fieldpol defifning polynomial of the extension field (must be irreducible) TO DO
- clist list of coefficients for the monomials in mlist
- mlist list of monomials
- 1en length of NLFSR
- tap optional parameter: the output tap (must be a positive integer or a list of positive integers) and will be changed to the default S\_0 if the specified integer is out of NLFSRrange.

NOTE: clist and mlist must be of same length, all elements in clist must belong to the underlying field. Monomials in mlist must not include any indeterminates that are out of range specified by len: stages of NLFSR are represented by indeterminants and the feedback is not allowed to use a stage that doesnt exist. A second constraint on mlist requires that it must contain at least one monomial of degree > 1, otherwise we must create an LFSR.

#### Compoents:

- init FFE vector of length n=deg(charpol), storing the initial state of the NLFSR, with indeces from n-1, ..., 0
- state FFE vector of length n=deg(charpol), storing the current state of the NLFSR, with indeces from n-1, ..., 0
- numsteps the number of steps performed thus far (initialized to -1 when created, set to 0 when loaded using LoadFSR (3.1.4) and incremented by 1 with each step (using StepFSR (3.1.5)))

Attributes FieldPoly (3.1.2), UnderlyingFied (??), MultivarPoly, FeedbackVec (3.1.2), IndetList (3.3.4), Length (3.1.3) and OutputTap (3.1.2) and the property IsNonLinearFeedback are set during the construction of an NLFSR.

If there is something wrong with the arguments (e.g. attempting to create an extension field using a reducible poynomial), an error message appears and the function returns fail.

```
gap> F := GF(2);; clist := [One(F), One(F)];; mlist := [x_0*x_1, x_2];;
Error, Variable: 'x_0' must have a value
not in any function at line 2 of *stdin*
gap> test := NLFSR(F, clist, mlist, 3);
Error, Variable: 'mlist' must have a value
not in any function at line 3 of *stdin*
gap> ChooseField(F);
You can now create an NLFSR with up to 100 stages
with up to 100 nonzero terms
gap> mlist := [x_0*x_1, x_2];;
gap> test := NLFSR(F, clist, mlist, 3);
< empty NLFSR of length 3,
given by MultivarPoly = x_0*x_1+x_2>
```

## 3.3.3 IsNonLinearFeedback

```
▷ IsNonLinearFeedback(nlfsr) (property)
▷ IsNLFSR(nlfsr) (filter)
```

For the multivariate polynomial given by *clist* and *mlist*, DegreeOfPolynomial greter than 1 sets IsNonLinearFeedback to *true*. otherwise it prints out a warning that you need to use the LFSR constructor instead.

Filter IsNLFSR is defined as and-filter of IsFSR and IsNonLinearFeedback.

NOTE: at the same time IsLinearFeedback is set to false (for coding purposes).

# 3.3.4 MultivarPoly

```
▷ MultivarPoly(nlfsr)

▷ IndetList(nlfsr)

(attribute)
```

MultivarPoly holds the multivariate function defining the feedback of the NLFSR. IndetList holds all the indeterminates that are present in MultivarPoly and FeedbackVec holds only the nonzero coefficients (as opposed to the LFSR, where this field holds coefficients for all stages of the FSR). The feedback element is computed from MultivarPoly, IndetList and state, and not from FeedbackVec.

```
gap> MultivarPoly(test); IndetList(test);
x_0*x_1+x_2
[ 0, 1, 2 ]
```

## 3.3.5 ViewObj

Different detail on nlfsr created by NLFSR (3.3.2):

- Display/View: show the MultivarPoly and wheter or not the *nlfsr* is empty
- Print: same as Display/View if *nlfsr* is empty, otherwise it also shows the values of the three components init, state and numsteps
- PrintAll: same as Print if *nlfsr* is empty, otherwise it also shows the values of the three components init, state and numsteps with additional information about the underlying field and the tap positions

Both Print and PrintAll can be used with optional parameter basis *B* for desiered output format.

```
gap> Print(test);
< empty NLFSR of length 3,</pre>
```

```
given by MultivarPoly = x_0*x_1+x_2>
gap> PrintAll(test, Basis(UnderlyingField(test)));
< empty NLFSR of length 3,
  given by MultivarPoly = x_0*x_1+x_2> with feedback coeff =[ [ 1 ], [ 1 ] ]
with initial state =[ [ 0 ], [ 0 ], [ 0 ] ]
with current state =[ [ 0 ], [ 0 ], [ 0 ] ]
after initialization
with output from stage S_0
```

# misc - helper functions

# 4.1 misc - helper functions

# 4.1.1 MonomialsOverField (for an NLFSR)

▷ MonomialsOverField(F, poly)

(method)

MonomialsOverField reduces takes a monomial or a list of monomials, and reduces all the exponents modulo (Size(F)-1) for all extension fields and prime fields except for F=(F)<sub>2</sub>. For (F)<sub>2</sub> all the exponents are set to 1.

# 4.1.2 DegreeOfPolynomial (DegreeOfPolynomial)

▷ DegreeOfPolynomial(F, poly)

(method)

DegreeOfPolynomial as follows for both monomial of form  $p = \prod x_i^{e_i}$  and polynomial of form  $P = \sum c_j \cdot_j$  where  $p_j = \prod_i x_i^{e_i}$  DegreeOfPolynomial for a monomial:  $= \sum e_i$ , where i runs through all indeterminates present in this monomial DegreeOfPolynomial for a polynomial:  $= \max(DegreeOfPolynomial(p_j))$ , where max runs through all monomials  $p_j$  present in this polynomial so an actual extra function called DegreeOfMonomial is not needed

# References

# Index

IntFFExt, 5	PeriodReducible, 12
IntMatFFExt, 5	PrintAll, 12, 15
IntVecFFExt, 5	PrintObj, 12, 15
CharPoly, 11	RunFSR, 8
ChooseField, 13	StepFSR, 8
DegreeOfPolynomial	200 <b>F</b> 2 211, 0
DegreeOfPolynomial, 17	UnderlyingField, 7
FeedbackVec, 7	VecToString, 5
FieldPoly, 7	ViewObj, 12, 15
fsr, 7	WriteMatrix
FSR package, 2	for a matrix of FFE and given basis, 6
IndetList, 15	$ ext{WriteMatrixTEX}, 6$
InternalStateSize, 8	$ ext{WriteVector}$
IsFSR, 7	for a FFE and given basis, 6
IsLFSR, 11	
IsLinearFeedback, 11	
IsMaxSeqLFSR, 11	
IsNLFSR, 15	
IsNonLinearFeedback, 15	
IsPeriodic, 11	
IsUltPeriodic, 11	
Length, 8	
LFSR, 10	
LoadFSR, 8	
MonomialsOverField	
for an NLFSR, 17	
MultivarPoly, 15	
NLFSR, 13	
outputs, 5	
OutputTap, 7	
Period, 11	
PeriodIrreducible.11	