

The effects of planetary obliquity on the Hadley cell

Alexander Paterson*

University of Exeter, Exeter, UK

Geoffrey Vallis

University of Exeter, Exeter, UK

*Corresponding author address: CGAFD, University of Exeter, Exeter, United Kingdom

E-mail: ap587@exeter.ac.uk

ABSTRACT

8 Placeholder abstract text.

9 1. Introduction

10 Note to assessors: This is an incomplete draft of a paper that I am actively working on. Before
11 you read through (if it's a while since the upload) I may have a more up-to-date copy available if
12 you email me! I am currently working on wrangling the data into a conclusion, with some more
13 heavy duty analysis and engagement with some theory. Thank you! - Alex

14 2. Model

15 We aim to use a simple, flexible GCM to simulate variations in planetary and atmospheric pa-
16 rameters, with emphasis on obliquity. We then wish to use this model to study how the Hadley
17 cell responds to these conditions, which could plausibly be found on an exoplanet in the coming
18 years. To this end we use Isca, a derivative of GFDL's FMS idealized aquaplanet model (cite
19 model paper). Within this framework, we use a dry atmosphere forced by Newtonian relaxation to
20 a prescribed equilibrium temperature field. The forcing we use is a new method following a more
21 physically motivated path than is typically used [cite].

22 This method involves 5 main steps:

- 23 1. Calculation of the incoming solar radiation at each latitude. We use a diurnally averaged solar
24 flux, S , following the method of ?:

$$S(\phi) = \frac{q_0}{\pi} (H \sin \phi \sin \delta + \cos \phi \cos \delta \sin H), \quad (1)$$

25 where q_0 is the bolometric solar flux. H is the radian half-day length which is 0 for perpetual
26 night and π for perpetual day. ϕ is the latitude and δ is solar declination, in the range $-\delta_0 <$
27 $\delta < \delta_0$ where δ_0 is the planet's obliquity.

- 28 2. Use the insolation at each latitude to calculate a top-of-atmosphere temperature. This uses
29 a simple radiative equilibrium model for the vertical temperature structure. The balance of

albedo adjusted incoming shortwave with outgoing longwave results in a top-of-atmosphere temperature of:

$$T_t(\phi) = \left(\frac{S(\phi)(1-A)}{2\sigma} \right)^{\frac{1}{4}}, \quad (2)$$

where σ is the Stephan-Boltzmann constant and the factor of 2 on the denominator is the difference between emitting and top-of-atmosphere temperature.

3. The vertical structure is simplified into two layers: a troposphere with a uniform lapse rate, and a stratosphere with no change in temperature. The height of the boundary between these layers is determined by performing a convective adjustment to the radiative equilibrium profile, see ?.

——— More detail about this derivation ———

We assume that convection is efficient such that it establishes a convectively neutral lapse rate, Δ , and that it equalizes the ground and surface layer temperatures. We can then solve numerically for the tropopause height, or use the following approximate analytic solution:

$$H_T(\phi) = \frac{1}{16\Gamma} \left(CT_T(\phi) + \sqrt{C^2 T_T(\phi)^2 + 32\Gamma\tau_s H_a T_T(\phi)} \right) \quad (3)$$

where T_T is the tropopause/top of atmosphere temperature, $C = \log 4$, Γ is the lapse rate, τ_s is the optical depth at the surface, and H_a is the scale height of the absorber in the atmosphere (water vapour on Earth). Typical Earth values of these parameters are: $\Gamma = 6.5 K km^{-1}$, $\tau_s = 5$, and $H_a = 2 km$. The full derivation of this equation is available in ? [GV2017].

4. A constant lapse rate is used to calculate troposphere temperatures down to the surface, with a stratosphere of constant temperature at each latitude.
5. The effects of surface heat capacity are modelled by using the flux from the insolation direct temperature, T_{insol} , to force the equilibrium temperature, T_{eq} . The heat capacity, c , is defined

by a certain depth of a global mixed layer ocean.

$$c \frac{\partial T_{eq}(\phi)}{\partial t} = \sigma (T_{insol}(\phi)^4 - T_{eq}(\phi)^4). \quad (4)$$

The entire atmospheric column temperature is therefore shifted to simulate the moderating effect of a heat absorbing surface layer. The entire column is shifted for simplicity, with the assumption that convection quickly brings the temperature profile in the troposphere back to the specified lapse rate.

The stratosphere is left at a constant temperature as to not make assumptions about its structure, while keeping some delineation at the tropopause. The constant temperature approximates the vertical structure in the upper atmosphere from a grey radiative balance model.

a. Experimental setup

Details about my particular experiments aka how i got the results below.

3. Results

Obliquity only effects the seasonal distribution of incoming solar radiation. The total energy received by the planet remains constant throughout these experiments. As obliquity is increased, the planet experiences stronger seasons, until at 90 degrees obliquity where each hemisphere sees a 'polar winter' where the sun never rises for many days. Figure c shows the annual mean and seasonally averaged incoming solar radiation. Of note is the change from the location of peak insolation being at the equator to the poles at 54 degrees obliquity. Due to the strong seasonal effects on planets with high obliquities it is necessary to look at the seasonal rather than annual mean to avoid washing out the true behaviour. Figure cb) shows the mean insolation over the solstice period, defined as one month either side of the solstice. This strong effect of the polar day

70 is clearly seen. At an obliquity of 75 degrees the insolation peaks at xxW/M^2 at the pole rather
71 than xxW/m^2 at the equator for an Earth-like obliquity.

72 *a. Obliquity climatology*

73 Now we will examine the effects of this on the basic climatology of the planet. First looking at
74 the annual mean followed by the solstice mean for full eddy-permitting and axisymmetric models.

75 At an obliquity of 30 degrees we observe a regime similar to that of the Earth (Fig: c). There is a
76 wide equatorial region of relatively constant temperature, before dropping 20K to the poles. This
77 temperature gradient is part of the the observed circulation structure. There are Hadley cells reach
78 to around 30 degrees of latitude off the equator and weaker eddy-driven Ferrel cells extending from
79 there to around 70 degrees. We also observe a small, weak polar cell in the lower atmosphere.
80 In the zonal wind field we see a westerly jet in each hemisphere with two peaks. The first, a
81 thermally driven jet, located higher in the troposphere and centered at the edge of the Hadley cell.
82 The second, an eddy driven jet, in the middle of the Ferrel cell which reaches down towards the
83 surface at approximately 60 degrees latitude. The jets are not vertically bounded as this model
84 does not include a temperature gradient reversal in the stratosphere.

85 If we increase the obliquity to 60 degrees we see a very different temperature structure. The
86 annual mean equator-to-pole temperature gradient is reversed, and much lower as the poles are
87 now the warmest latitudes. The lower branch of the Hadley cell has weakened compared with the
88 lower obliquity case. The Ferrel cells have narrowed, now ending at approximately 50 degrees
89 latitude. Overall the circulation in the annual mean is significantly weaker, the meridional mean
90 mass overturning streamfunction is half as intense across the atmosphere. There are no westerly
91 jets present as the strong seasonal effects are masking the jets when the annual mean is taken.

92 We have also run the same planet under axisymmetric conditions. Here we only allow wave
93 number zero in the spectral model, so no eddies are permitted. In this model the climate differs in
94 a few key ways. [][]

95 *b. Seasonal effects*

96 To actually understand how the changing obliquity is affecting the climate, we need to examine
97 the seasonal effects in more detail. Figure c shows the solstice mean for the experiments detailed
98 in Figure c. The solstice period here is defined as the time period one month either side of the
99 solstice. In our 30 degree obliquity experiment the offset heating results in a temperature field
100 maxima offset from the equator by approximately 25 degrees. This is caused by the heat capacity
101 of the model moderating the seasonal shift. The mass streamfunction shows a cross-equatorial
102 winter Hadley cell paired with a very weak summer cell. The latitude of the ascending branch
103 of the winter Hadley cell does not align with the latitude of maximum temperature; we explore
104 the reasons behind this in section xx. The westerly jet latitudes are fairly unchanged from the
105 annual mean case, the main difference between them being their relative strengths. The winter
106 hemisphere jet is much stronger, associated with the strong Hadley and Ferrel cells. The 30 degree
107 obliquity experiment produces a seasonal climate similar to that of other idealised models of Earth
108 xx. At 60 degrees obliquity, Figure cb), the temperature maxima is now located at the pole. This is
109 consistent with predictions from the insolation equation. Past 21 degrees obliquity the insolation
110 maxima for the season is at the pole. There is now one global circulation cell, the winter cross-
111 equatorial Hadley cell. Interestingly it is of similar size and intensity as the Hadley cell at 30
112 degrees obliquity, while the temperature structure has changed significantly. We look in detail at
113 the reasons for this in section xx. An eddy driven westerly jet is not present at higher obliquities.
114 Instead we only see the thermally driven upper jet centered at the edge of the Hadley cell. In the

115 summer hemisphere we see an easterly jet with a maxima on the up-welling branch of the Hadley
116 cell. This is a thermal jet caused by the reversed, now pole-equator, temperature gradient.

117 Axisymmetric solstice description

118 *c. Surface temperature effects*

119 Figure c shows the annual mean equator-to-pole temperature difference for eddy permitting and
120 antisymmetric models. Both cases feature a clear negative relationship between these values. At
121 smaller obliquities the axisymmetric runs have a much larger equator-to-pole difference as there
122 are no eddies providing poleward heat transport. Past 54 degrees in the 3D case, we see a negative
123 temperature gradient. Here the poles are warmer than the equator, as we saw in the field slices
124 (Fig c). At very high obliquities, greater than 60 degrees, we see the axisymmetric model and
125 3D have essentially the same values. This is further evidence to the reduced role of eddies at high
126 obliquities - with the climate dominated by a single thermally direct overturning Hadley cell.

127 The strength of the solstice Hadley cell is observed to increase consistently from 0 to 90 degrees
128 obliquity. This is in contrast with the annual mean cell which decreases in strength, with an ex-
129 ception at 30 degrees. At 30 degrees there is a strong winter cell which is still largely concentrated
130 in the winter hemisphere. At high obliquities, this winter cell is centered over the equator, and so
131 in the annual mean is largely cancelled out.

132 *Acknowledgments.* Start acknowledgments here.

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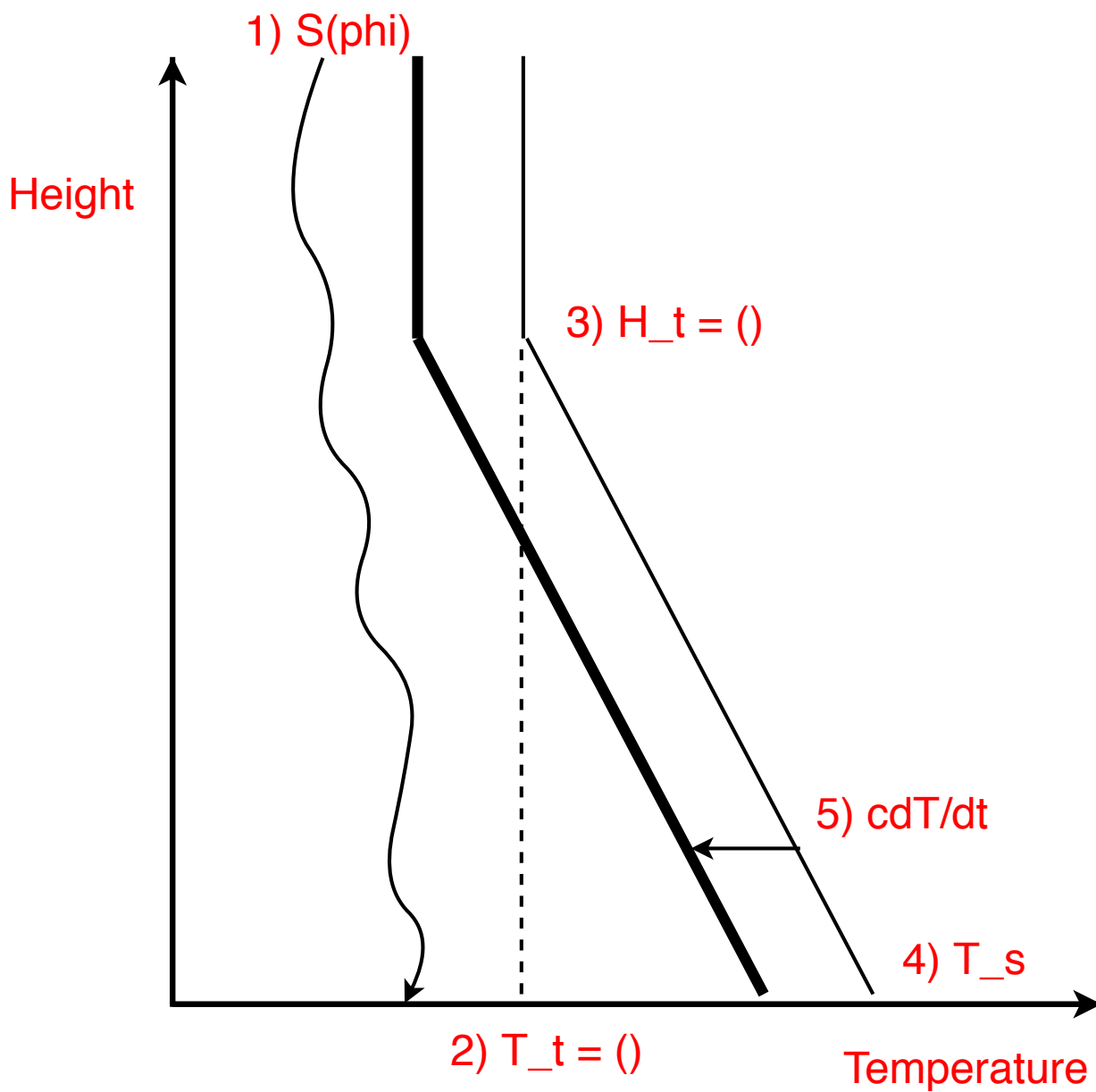


FIG. 1. Diagram of model method

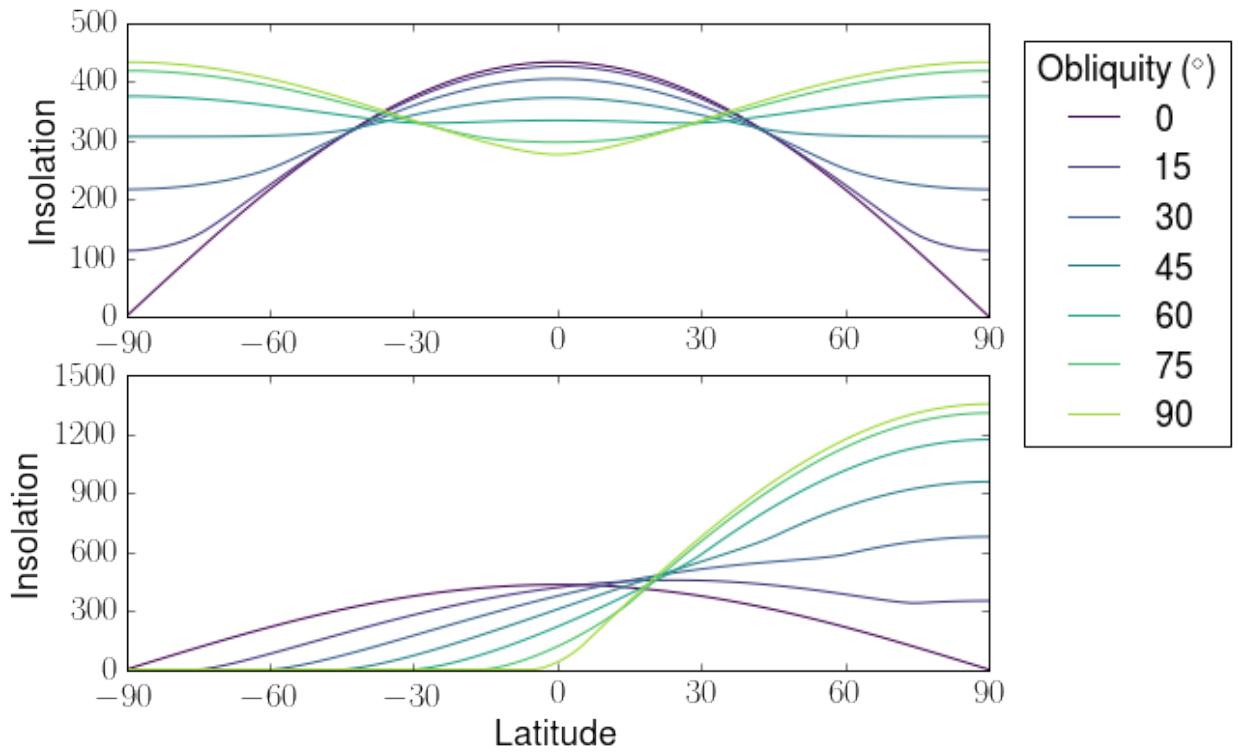


FIG. 2. Top: Annual mean top of atmosphere insolation for obliquities from 15 degrees to 90 degrees. Bottom:
Top of atmosphere insolation on the solstice for the same planetary obliquities.

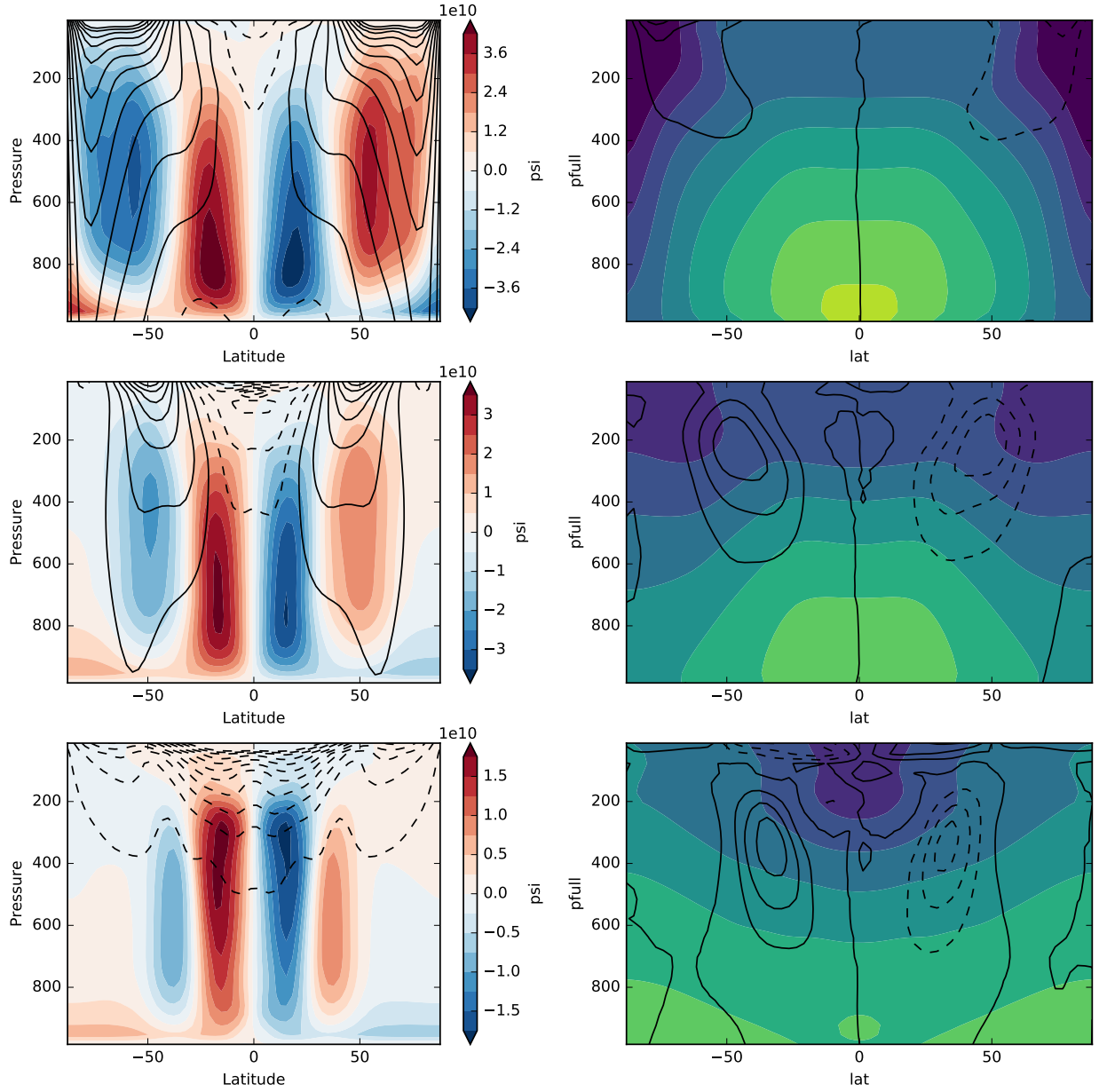
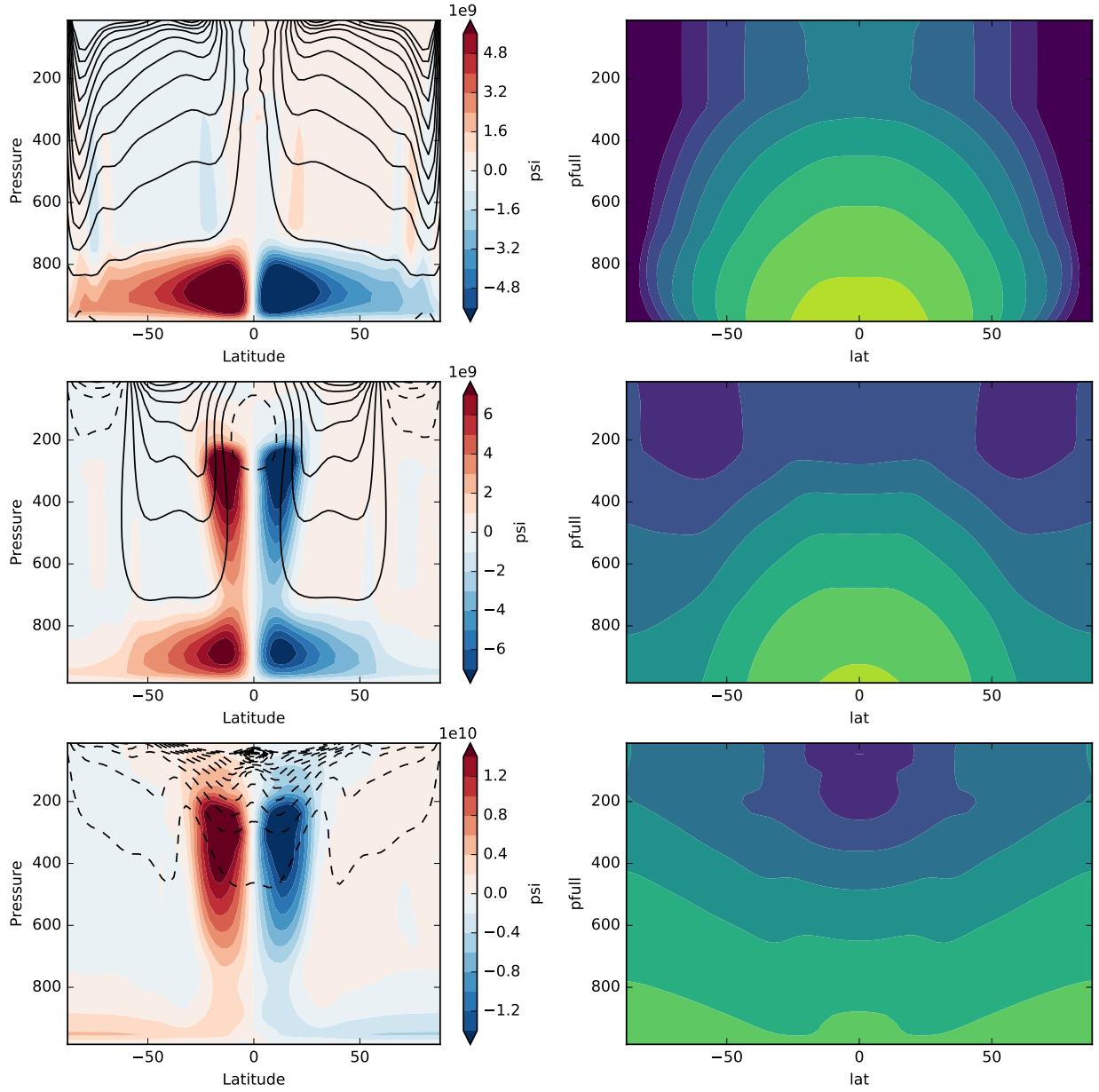


FIG. 3. Zonal, annual mean circulation for a series of model runs with obliquity 0° (top), 30° (middle) and 60° (bottom). Left: Mass streamfunction (colours) and zonal wind (contours). Right: Temperature (colours) and meridional eddy-momentum flux, $u'\bar{v}'$ (contours).



175 FIG. 4. Zonal, annual mean circulation for a series of axisymmetric model runs with obliquity 0° (top), 30°
 176 (middle) and 60° (bottom). Left: Mass streamfunction (colours) and zonal wind (contours). Right: Temperature
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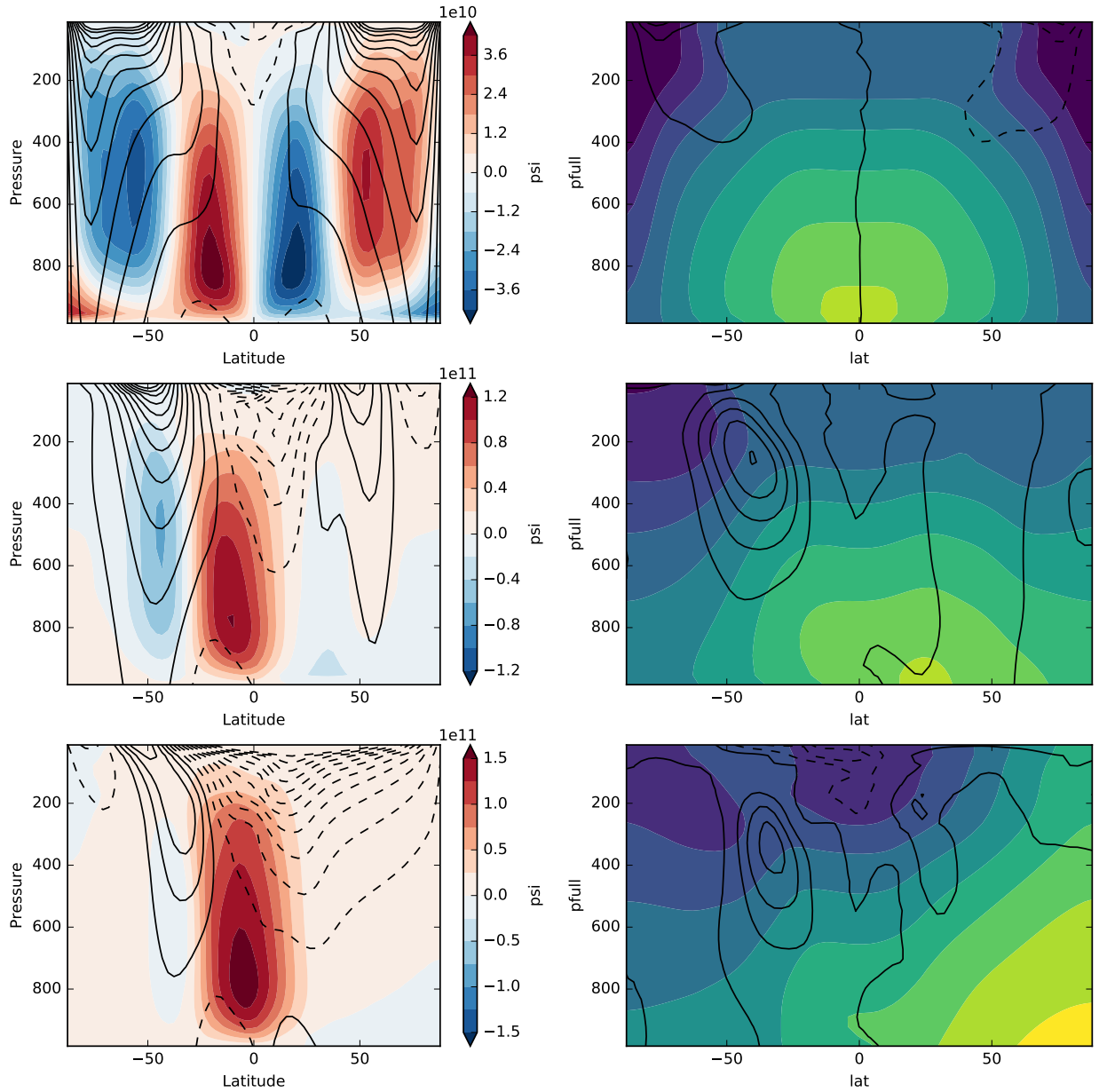
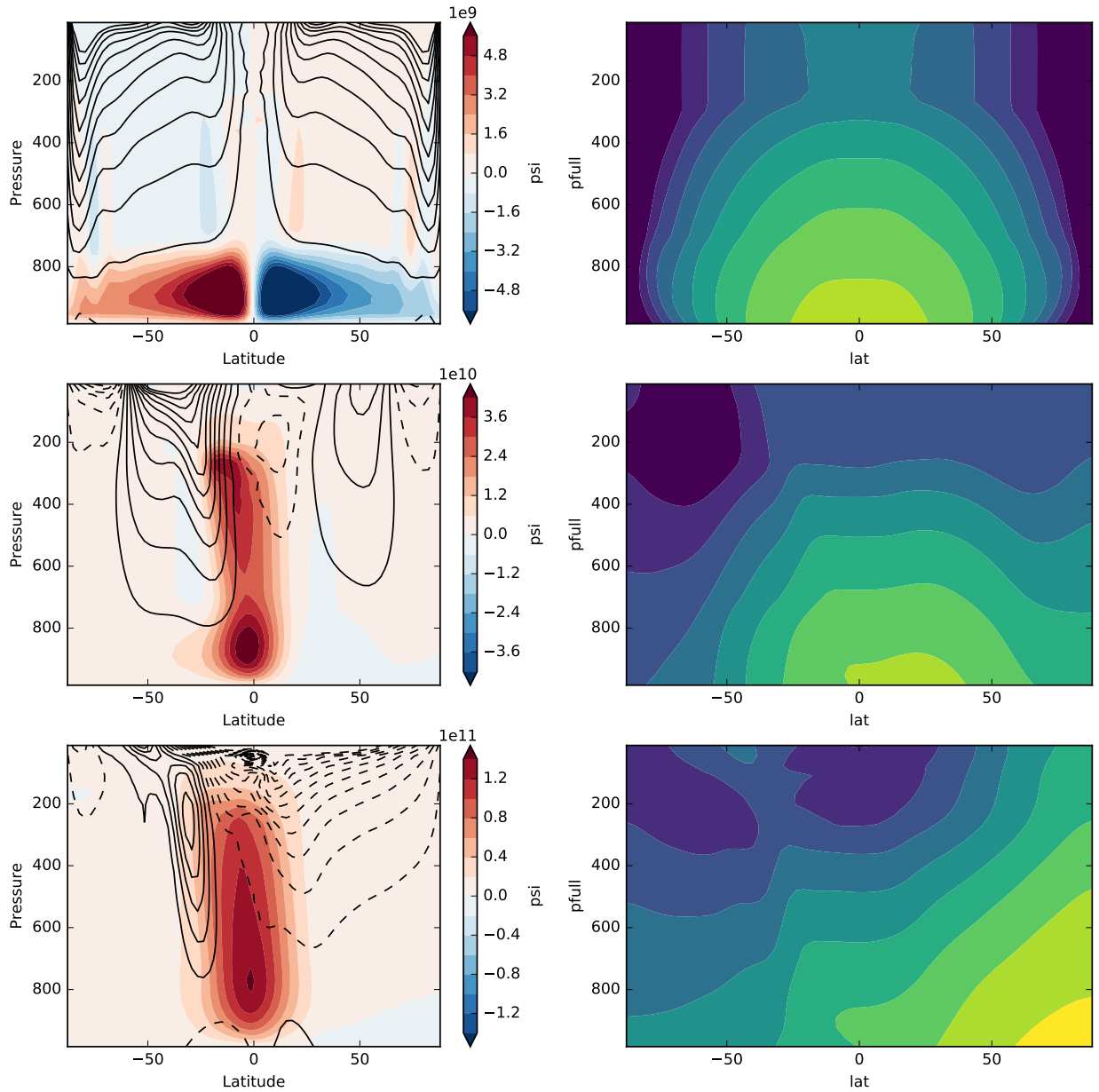


FIG. 5. Zonal, solstice mean circulation for a series of model runs with obliquity 0° (top), 30° (middle) and 60° (bottom). Left: Mass streamfunction (colours) and zonal wind (contours). Right: Temperature (colours) and meridional eddy-momentum flux, $u'\bar{v}'$ (contours).



181 FIG. 6. Zonal, solstice mean circulation for a series of axisymmetric model runs with obliquity 0° (top), 30°
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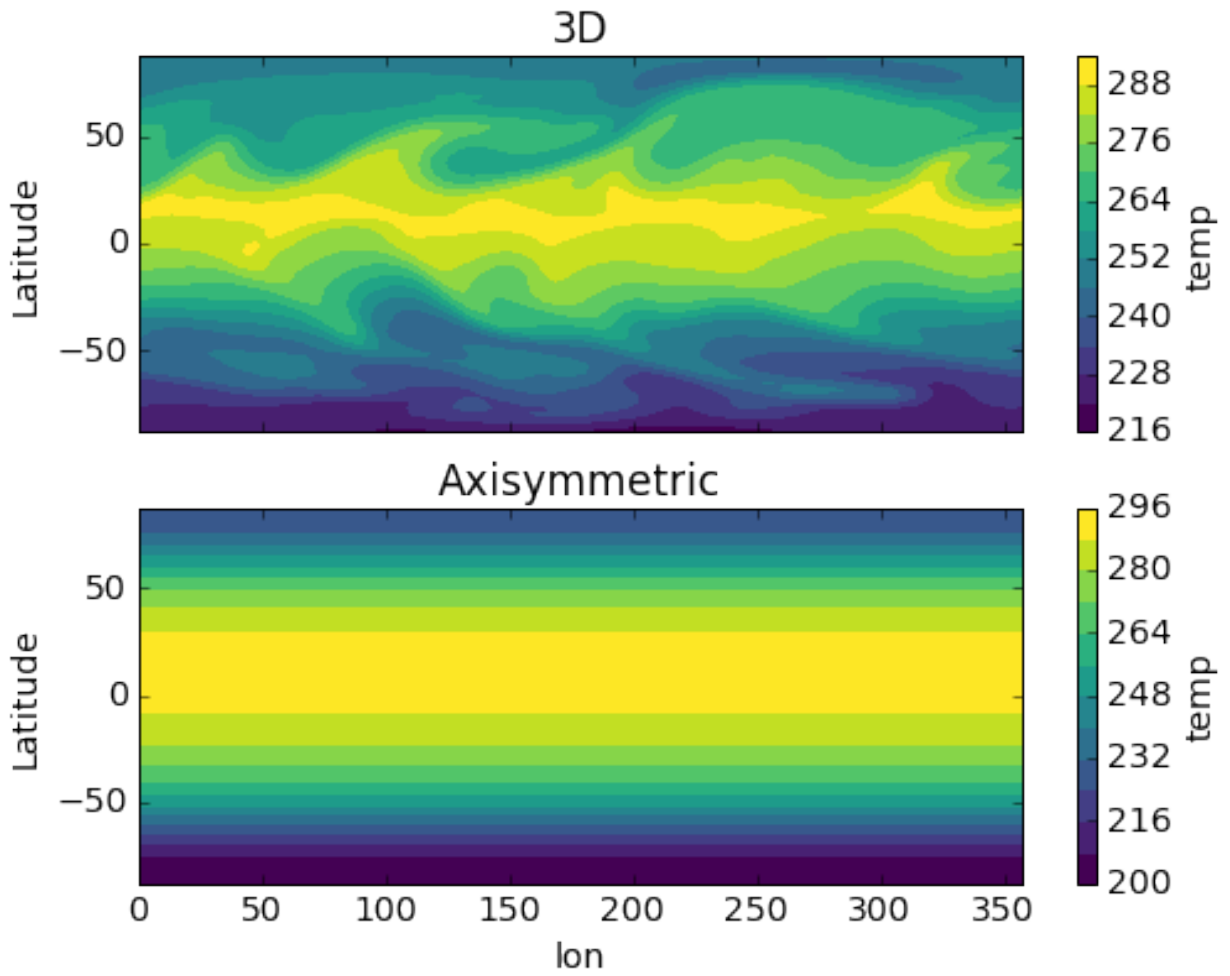


FIG. 7. Surface temperatures at the solstice for 3D and axisymmetric model runs at 15° obliquity.

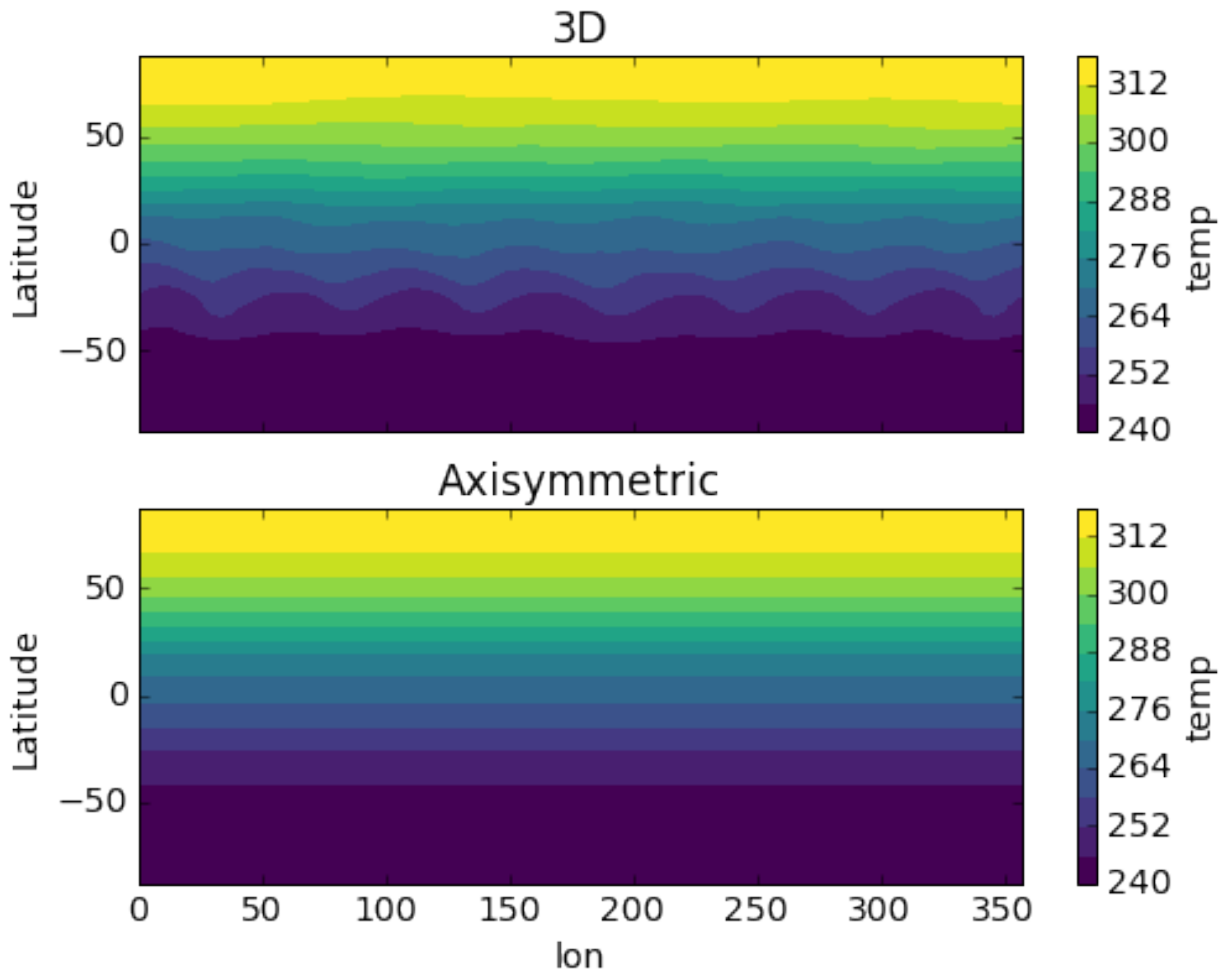


FIG. 8. Surface temperatures at the solstice for 3D and axisymmetric model runs at 60° obliquity.

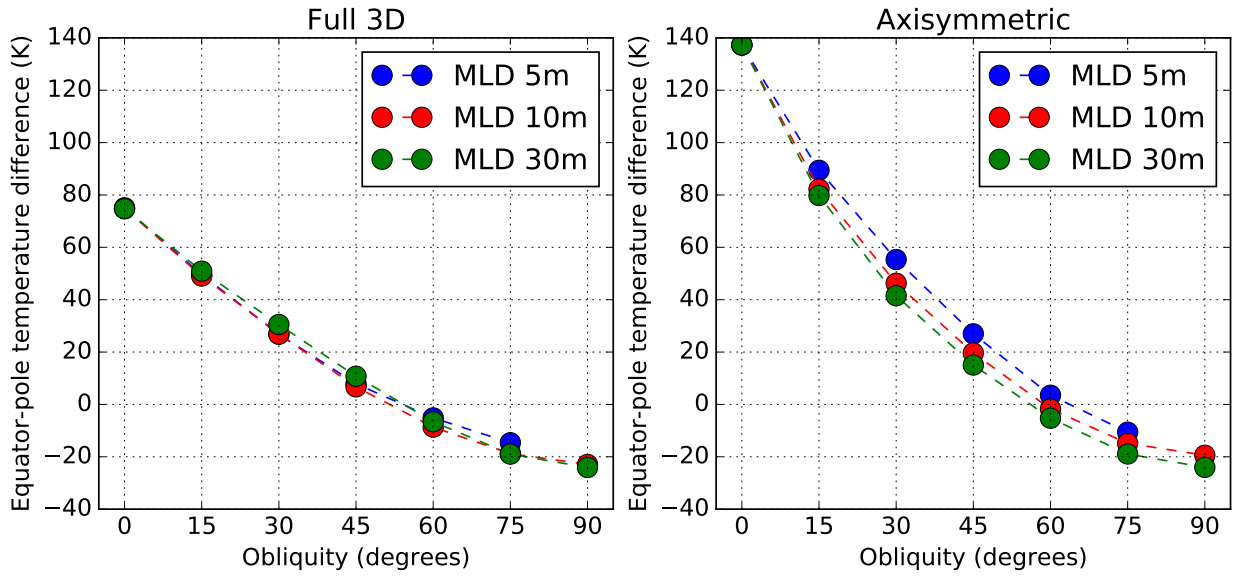
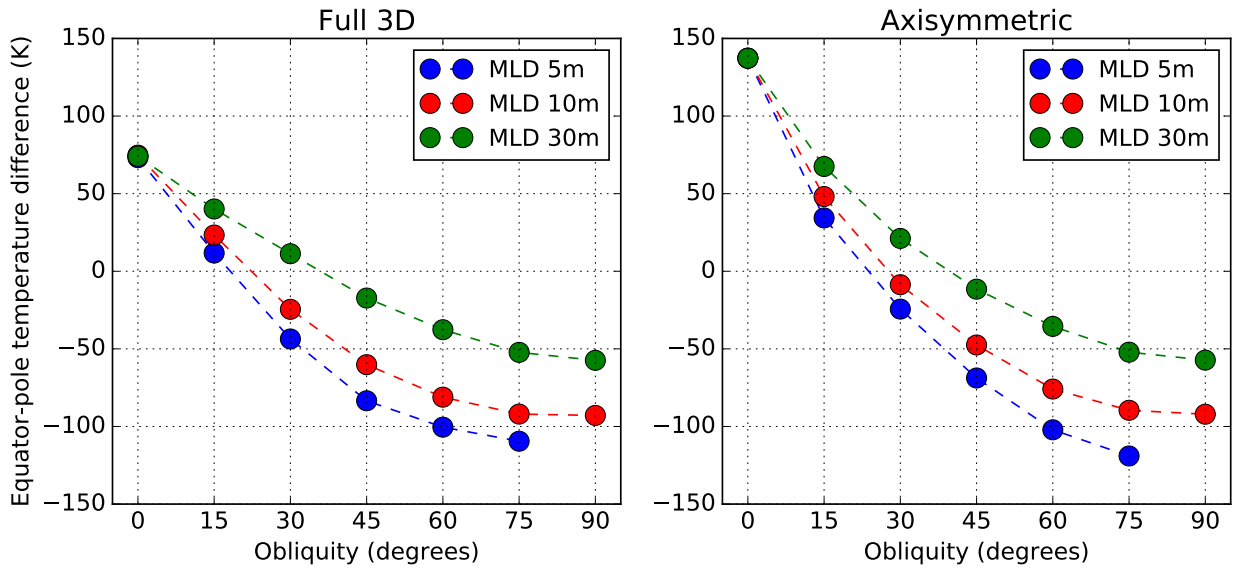


FIG. 9. Annual mean equator-to-pole temperature difference for full 3D eddy permitting, and axisymmetric obliquity variations. Note that the temperature difference is negative for obliquities greater than around 50 degrees. Past this point the poles are warmer than the equator due to the intense polar summer.



186 FIG. 10. Solstice equator-pole temperature difference in the summer hemisphere, for full 3D eddy permitting,
 187 and axisymmetric obliquity variations.

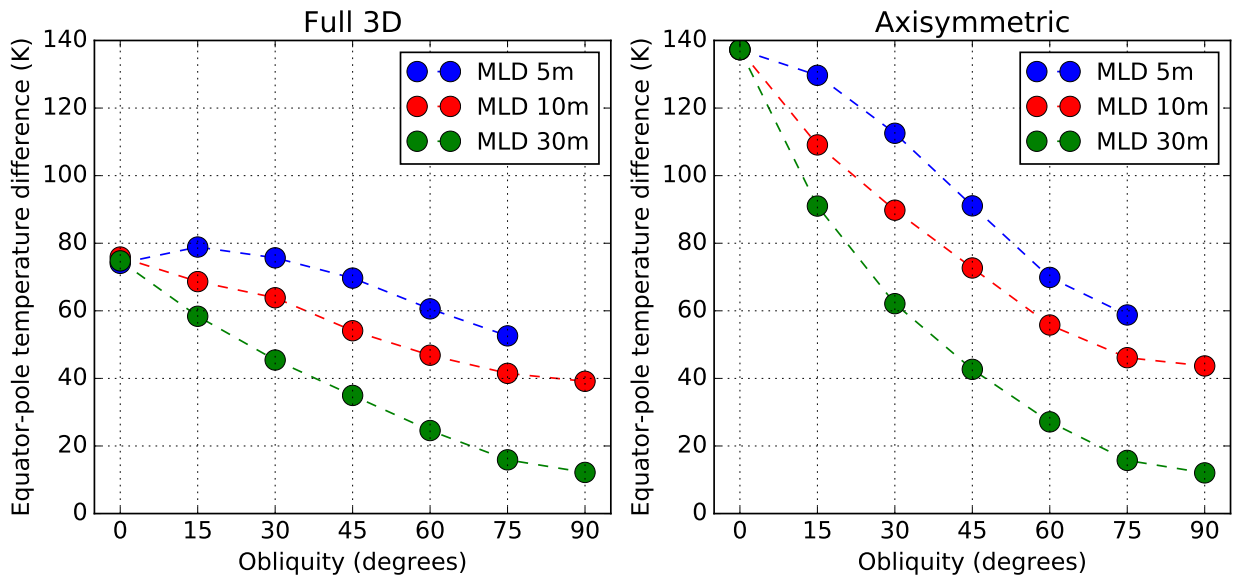


FIG. 11. Solstice equator-pole temperature difference in the winter hemisphere for full 3D eddy permitting,
and axisymmetric obliquity variations.

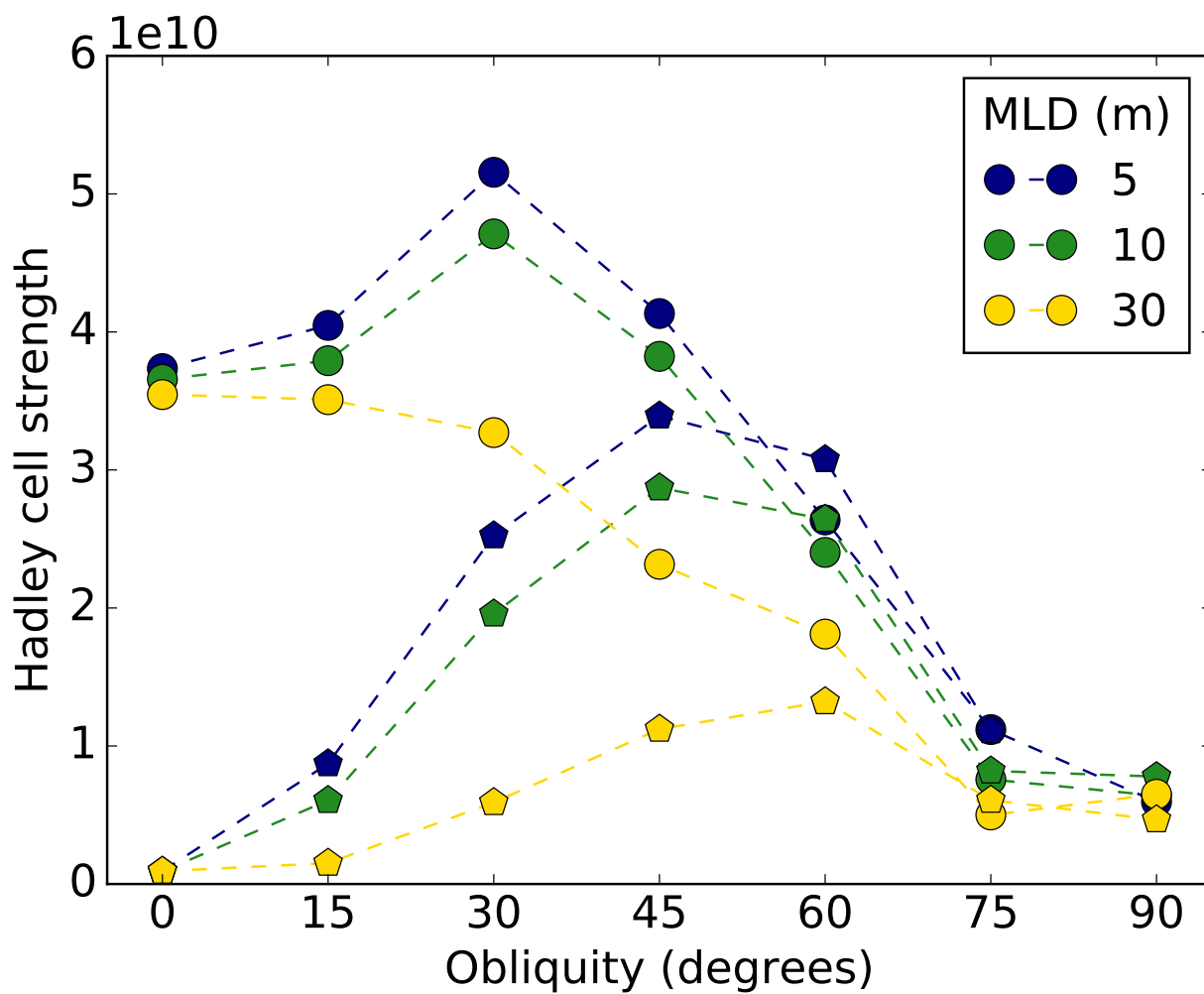


FIG. 12. Annual mean Hadley cell strength for mixed layer depth 5, 10, 30m.

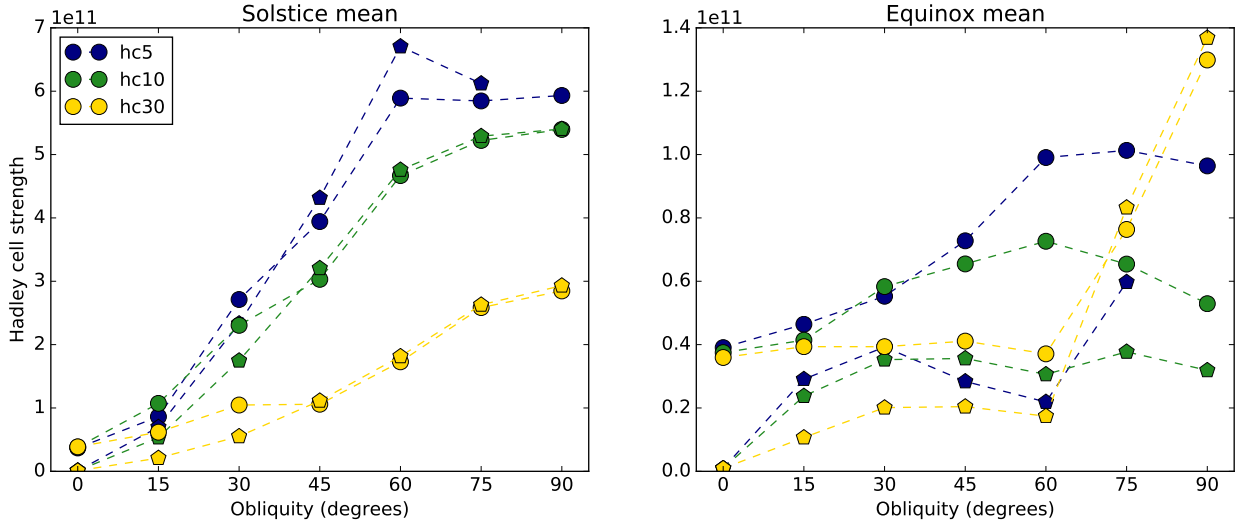


FIG. 13. Seasonal mean Hadley cell strengths for mixed layer depth 5, 10, 30m.

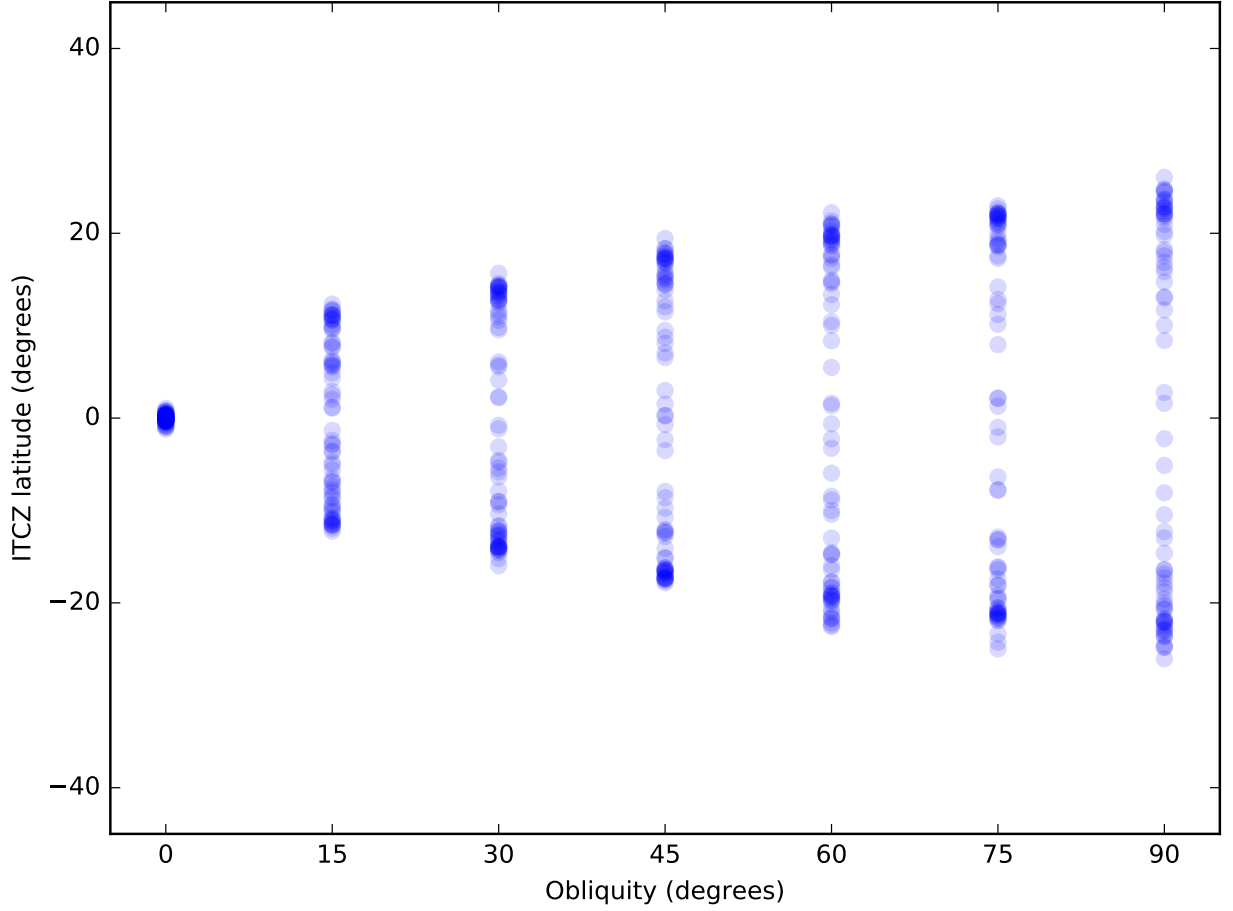


FIG. 14. 5-day mean latitude of the ITCZ for experiments with a mixed layer depth of 10m. We see a strong initial trend when obliquity is first introduced, and slow growth in the outer limit of the ITCZ for any further obliquity. This outer limit is also much less than the obliquity of the planet, only reaching 25 degrees with a 90 degree obliquity.

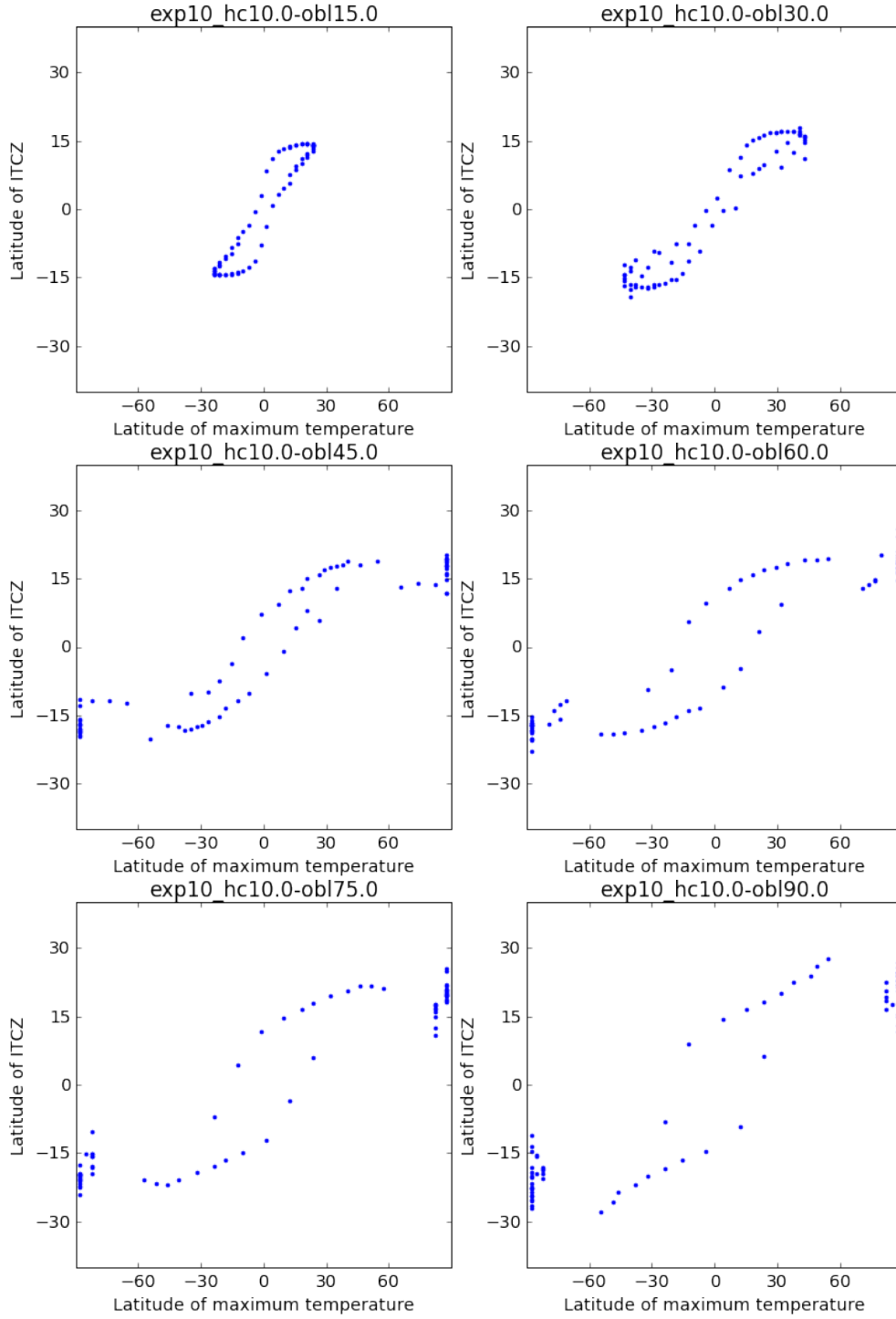


FIG. 15.

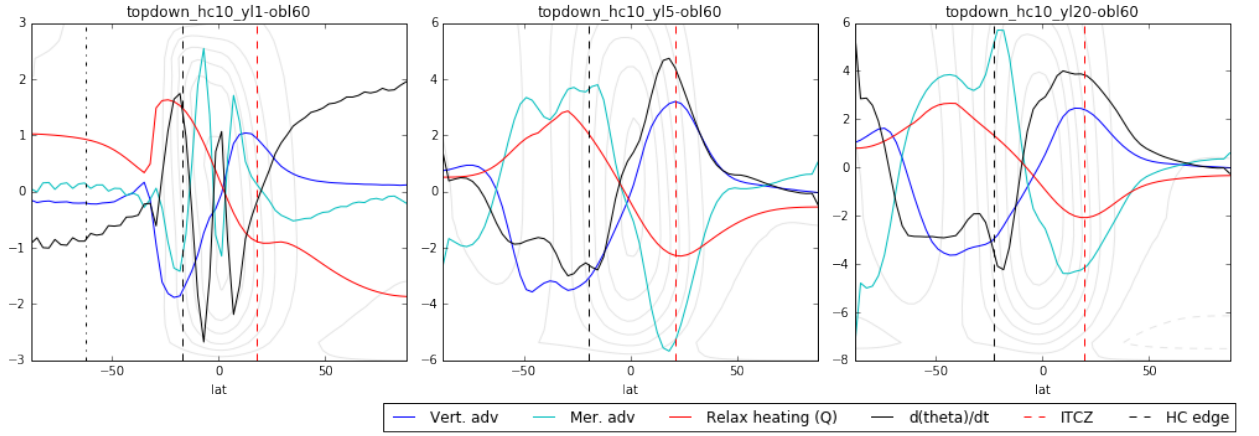


FIG. 16. Solstice mean thermodynamic breakdown of year length varying experiments.