

We allow collaboration on homework assignments, and **encourage you to work in study groups of at most 4 students**. You should turn one **assignment** for each study group. We will **not accept late assignments**.

**Homework 2 (1 Exercise)**  
**Handed Out on 9/3/2021**  
**Due on 9/9/2021**

There is one product, say a soup, and is being offered at one location of a city, which only has one road. The city is represented by the interval  $[0,1]$ . Along the line is distributed uniformly a mass 1 of consumers ( $M=1$ ). Then, the density of consumers at each location is 1 (loosely, there is 1 consumer at each location). Each consumer wishes to buy at most one unit.

The firm is located at  $\frac{1}{2}$ . The firm is called FIRM 1.

The willingness to pay for the good produced at the restaurant FIRM 1 is  $R_I$ .

The consumer can also not buy any soup, and the utility in that case would be 0.

The transportation cost for a consumer located at  $x$  who travels is  $Tx$  per unit of distance if traveling from 0 to  $x$ . The transportation cost for a consumer located at  $x$  who travels is  $T(1-x)$  per unit of distance if traveling from  $x$  to 1.

The production costs for FIRM 1 are zero (so  $c_I=0$ ).

- a) (5 points). What price should FIRM 1 charge to maximize its profit? What would the profit be equal to?
- b) (5 points). How would your answer change if the firm is located at  $\frac{1}{4}$ ?
- c) (5 points). How would your answer change if the firm is located at 1?

Be careful in discussing how your answers to questions 5.a; 5.b; 5c depend on the parameters  $R_I$  and  $T$ .

- d) (5 points) Where would the firm be rather located? What is the basic economic intuition?