

$$\Delta_0^{\tilde{\varphi}}:=S_0^{\tilde{\varphi}_0}$$