

Digital Signal Processing

Summary of Matlab Signal processing Toolbox

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Important for exam

- Theoretically, you can finish the exam without Matlab. But Matlab is strongly recommended in the exam.
- You need to install ‘Observer’ (not ‘exam monitor’ anymore).
- **You have to disable Matlab copilot before the exam!**
- **Using copilot in the exam, detected by ‘Observer’, will be considered as cheating.**
- But you are allowed to use ‘**help ...**’ in Matlab to consult the use of function.

Computation

conv(x,h,'same')	convolution multiplication
real()	Get the real part of a number
imag()	Get the imagine part of a number
log10()	Calcultion of ln()
root()	Calculate roots of a polynomial
[r,p,k]=residue(b,a)	Partial fraction decomposition (s)
[r,p,k]=residuez(b,a)	Partial fraction decomposition (z^{-1})
syms s	Symbolic notation
subs(eq, var, num)	Substitute a var in equation by number

Fourier transform & Z transform

fft()	Compute Fast Fourier Transform (FFT)
ifft()	Compute inverse Fast Fourier Transform (IFFT)
fftshift()	Shift zero-frequency component to the center
ifftshift()	Inverse zero-frequency shift
ztrans()	Z transform of a symbolic section
iztrans()	Inverse Z transform of a symbolic section

Spectrum analysis

abs()	Magnitude spectrum
angle()	Phase angle
bode()	Bode plot

Transfer function and response

$H_s = \text{tf}(b, a)$	Create an analog filter (s-domain)
$H_z = \text{tf}(b, a, Ts)$	Create a digital filter (z-domain)
$y = \text{impulse(sys,t)}$	Impulse response
$y = \text{freqs}(b,a,w)$	Frequency response for analog filter
$y = \text{freqz}(b,a,n)$	Frequency response for digital filter
$[num,den] = \text{zp2tf}(z,p,k)$	Convert(z,p,k) to transfer function's numerator and denominator
$[z,p,k] = \text{tf2zp}(b,a)$	From transfer function to find its zeros, poles and gain
$[p,z] = \text{pzmap(sys)}$	Zero-pole plot, also receive the zeros and poles values
pzplot(sys)	Zero-pole plot
$y = \text{lsim(sys, x, t)}$	Simulate an input signal passing through filter
$y = \text{filter}(b,a,x)$	Filtered result with input x and transfer function (b,a)

Second order sections (SOS)

[sos,g] = tf2sos(b,a)

Transfer function coefficients, specified as vectors. Express the transfer function in terms of b and a as

$$H(z) = \frac{B(z)}{A(z)} = \frac{b_1 + b_2 z^{-1} + \dots + b_{n+1} z^{-n}}{a_1 + a_2 z^{-1} + \dots + a_{m+1} z^{-m}}.$$

Second-order section representation, returned as a matrix. sos is an L -by-6 matrix

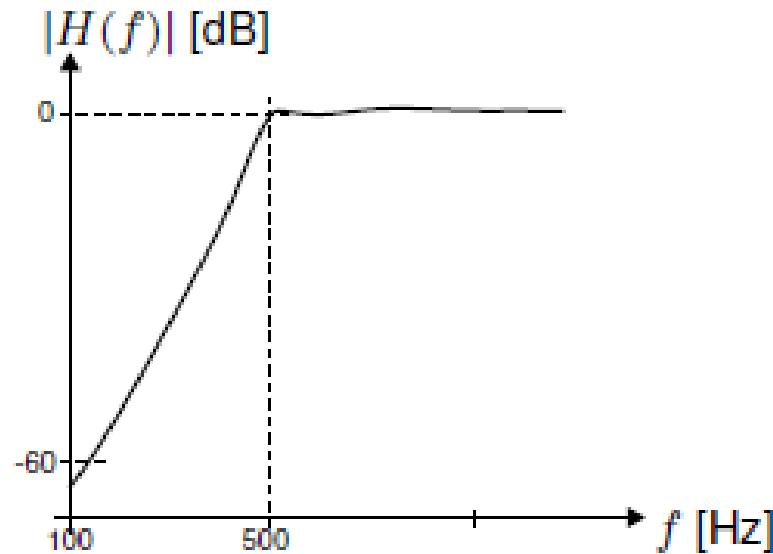
$$\text{sos} = \begin{bmatrix} b_{01} & b_{11} & b_{21} & 1 & a_{11} & a_{21} \\ b_{02} & b_{12} & b_{22} & 1 & a_{12} & a_{22} \\ \vdots & \vdots & \vdots & \vdots & \vdots & \vdots \\ b_{0L} & b_{1L} & b_{2L} & 1 & a_{1L} & a_{2L} \end{bmatrix}$$

whose rows contain the numerator and denominator coefficients b_{ik} and a_{ik} of the second-order sections of $H(z)$:

$$H(z) = g \prod_{k=1}^L H_k(z) = g \prod_{k=1}^L \frac{b_{0k} + b_{1k} z^{-1} + b_{2k} z^{-2}}{1 + a_{1k} z^{-1} + a_{2k} z^{-2}}.$$

Example: Design of high pass filter

Design a 0.5 dB Chebyshev highpass filter with cutoff frequency 500Hz, sampling frequency 8kHz.



```
% construct analog filter  
[b,a] = cheby1(4,0.5,2*pi*500,'high','s');  
Hs=tf(b,a);  
  
% convert it to digital filter (bilinear)  
Hz = c2d(Hs, 1/8000,'tustin');  
bode(Hz)  
  
% convert to second order sections  
bb =cell2mat(Hz.Numerator);  
aa = cell2mat(Hz.Denominator);  
[ss,g] = tf2sos(bb,aa);  
Hz1 = tf(ss(1,1:3), ss(1,4:6), 1/8000);  
Hz2 = tf(ss(2,1:3), ss(2,4:6), 1/8000);  
Hz_csc = g*Hz1*Hz2;  
bode(Hz_csc)
```

Analog filter design

[b,a] = butter(N, wa, 's')	Analog Butterworth filter
[b,a] = cheby1(N, Rp, wa, 's')	Analog Chebyshev type I filter
[b,a] = besself(N, wa)	Analog Bessel filter
[z,p,k] = buttap(n)	Butterworth frequency-normalized filter
[z,p,k] = cheb1ap(n,Rp)	Chebyshev type I frequency-normalized filter
[z,p,k] = besselap(n)	Bessel frequency-normalized filter
[bt, at] = lp2lp(b,a,Wo)	Transform lowpass analog filters to lowpass
[bt, at] = lp2hp(b,a,Wo)	Transform lowpass analog filters to highpass
[bt, at] = lp2bp(b,a,Wo,Bw)	Transform lowpass analog filters to bandpass
[bt, at] = lp2bs(b,a,Wo,Bw)	Transform lowpass analog filters to bandstop

Digital Filter

`fir1(n,Wn,ftype>window)`

`barlett(L)`

`hamming(L)`

`hanning(L)`

`kaiser(L, beta)`

Generate a n_order FIR filter with window

Barlett window length L

Hamming window length L

Hanning window length L

Kaiser window length L

`Hz = c2d(Hs, Ts, method)`

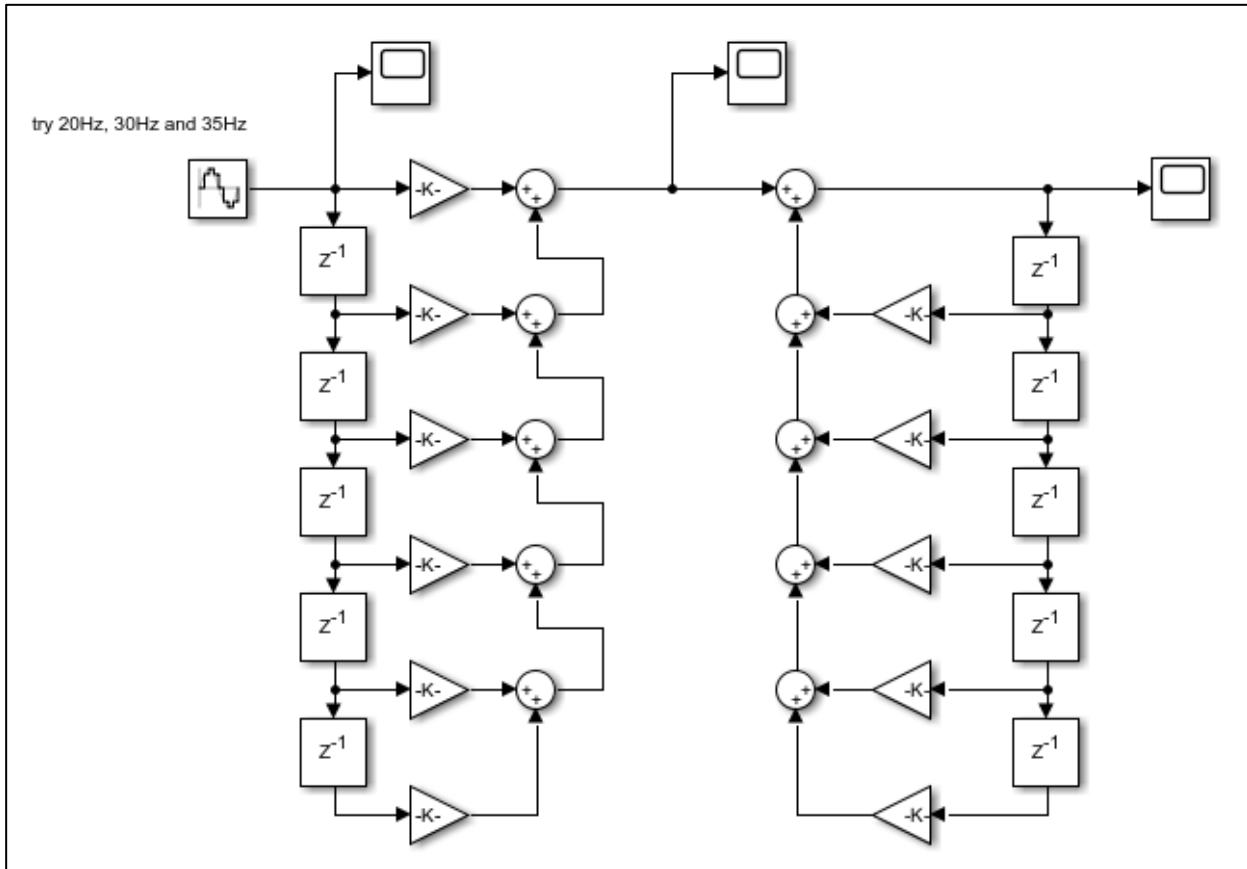
Convert analog filter Hs to digital filter Hz (method: 'matched', 'impulse', 'tustin')

Realization

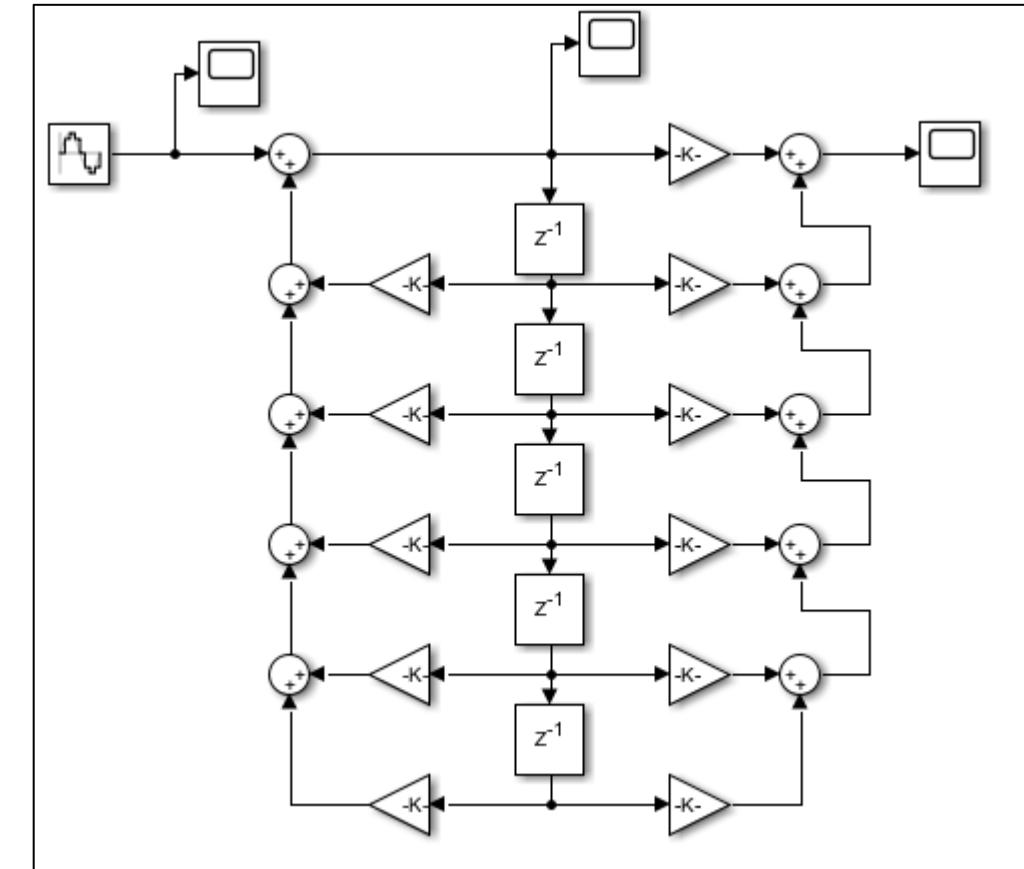
Set time (how long)



Click it to run
the simulation



Direct Type I



Direct Type II

APP in Matlab- GUI

