# Assignment 5

# $Computational\ Intelligence,\ SS2018$

Team Members		
Last name	First name	Matriculation Number
Lee	Eunseo	11739623
Shadley	Alex	11739595
Lee	Dayeong	11730321

## 1 Classication/ Clustering

#### 1.1 2 dimensional feature

#### 1.1.1 Perform all of the above-mentioned tasks for the EM algorithm.

In the process of initializing the parameters, we used random function to select m points for calculating means. Therefore, the result is different for each process. We selected the best results from 10 trials.

• Compare the result with the labeled data set (i.e., consider labels as well). Make a scatter plot of the data and plot the Gaussian mixture model over this plot.

Figure 1: label data

First array is EM algorithm classification. Second array is answer classification. Three points are mis-classified.

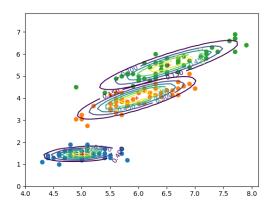


Figure 2: Three gaussian with scatter data points

EM algorithm succeeded to find three gaussian model and classified the data points well.

• For your tests, select the correct number of components (K = 3), but also check the result when you use more or less components. How do you choose your initialization  $\theta$ 0? Does this choice have an inuence on the result

When the number of components is 2, the result is the following figure.

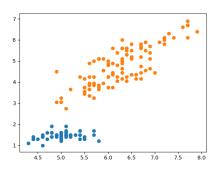


Figure 3: K = 2

When the number of components is 4, the result is the following figure.

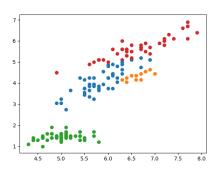


Figure 4: K = 4

For initialization  $\theta 0$ , we referred to the class pdf. The following figure is the reference class pdf.

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4.2.1 Initialisierung Eine Möglichkeit \Theta^0 zu initialisieren ist: 1. \ \alpha_m^0 \ \text{auf uniforme Verteilungsfunktion} \ \alpha_m^0 = \frac{1}{M} 2. \ \Sigma_m^0 \ \text{wird auf die Kovarianzmatrix} \ \Sigma \ \text{der Daten X gesetzt d.h.} \ \Sigma = \frac{1}{N} \sum_{n=1}^N (\mathbf{x}_n - \boldsymbol{\mu}) (\mathbf{x}_n - \boldsymbol{\mu})^T \ \text{wobei} \boldsymbol{\mu} = \frac{1}{N} \sum_{n=1}^N x_n. 3. \ \text{Für } \boldsymbol{\mu}_m^0 \ \text{wählt man } m \ \text{Samples zufällig aus oder man verwendet den k-means Algorithmus.}
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Figure 5: The initialization process in the class pdf

The initialization process influences the EM algorithm result. When the randomly selected points, for calculating mean value, is well chosen, the result is accurate. That is, the result is accurate when the first random selected points are from first answer label group, the second random selected points are from second answer label group and the third random selected points are from third answer label group.

• plot the log-likelihood function over the iterations! What is the behavior of this function over the iterations?

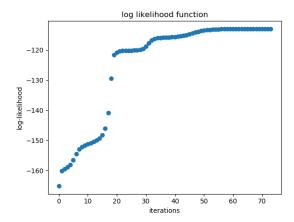


Figure 6: The log-likelihood function over iterations

As shown in Figure 4, the log-likelihood increases over iterations. That is, likelihood increased over iterations. And about 50th iteration, the function looks convering to the value, -112.96270776709655. Therfore, the process stops even though it didn't reach the max iteration number.

• Make a scatter plot of the data that shows the result of the soft-classication that is done in the E-step

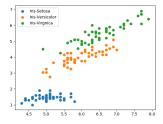


Figure 7: The EM algorithm soft-classification

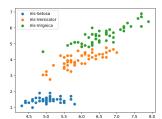


Figure 8: The answer classification

The EM algorithm classifies well the points when it is compared with the answer classification. EM algorithm fails to classify the points near the boundary of iris-Versicolor and iris-Virgnica.

- 1.1.2 Perform all of the above-mentioned tasks for the K-means algorithm
- 1.1.3 You may additionally choose any other pair of features; how would this change the classication accuracy
- 1.2 4 dimensional feature
- 1.2.1 How do the convergence properties and the accuracy of you classication change in comparison to scenario 2.1?
- 1.2.2 Within your EM-function conne the structure of the covariance matrices to diagonal matrices! What is the inuence on the result.
- 1.3 Processing the data with PCA
- 1.3.1 How much of the variance in the data is explained this way?
- 1.3.2 How does the performance of your algorithms compare to scenario 2.1 and scenario 2.2?
- 1.3.3 Apply PCA with whitening, so that the transformed data has zero mean and a unit covariance matrix. How does this inuence the choice of your initialization?

### 2 Samples from a Gaussian Mixture Model

- 2.1 Write a function Y = sample-GMM(alpha, mu, cov, N)
- 2.2 Using a GMM of your choice (K > 3), demonstrate the correctness of your function