

1.)

$$\mathcal{L}[t \cos(3t)] = -\frac{d}{ds} \frac{s}{s^2 + 9} = -\frac{s^2 + 9 - 2s^2}{(s^2 + 9)^2} = -\frac{9 - s^2}{(s^2 + 9)^2}$$

2.)

$$\mathcal{L}[t \sin(5t)] = -\frac{d}{ds} \frac{5}{s^2 + 25} = -\frac{-10s}{(s^2 + 25)^2} = \frac{10s}{(s^2 + 25)^2}$$

3.)

$$\begin{aligned}\mathcal{L}[t^2 \sin t] &= (-1)^2 \frac{d^2}{ds^2} \frac{1}{s^2 + 1} = \frac{d}{ds} \frac{-2s}{(s^2 + 1)^2} \\ &= \frac{-2(s^2 + 1)^2 + 2s(2s)(s^2 + 1) + 2s(s^2 + 1)(2s)}{(s^2 + 1)^4} = \frac{-2(s^2 + 1)^2 + 4s + 4s}{(s^2 + 1)^3} \\ &= -\frac{2(s^2 + 1)^2 + 8s}{(s^2 + 1)^3}\end{aligned}$$

4.)

$$\mathcal{L}[te^{4t} \cos(3t)] = -\frac{d}{ds} F(s - 4) = -\frac{d}{ds} \frac{(s - 4)}{(s - 4)^2 + 9} =$$

5.)

6.)

7.)

8.)

9.)

10.)

11.)

12.)