- 28.) a.) Let $u \in \mathbb{R}$ be an upper bound of S, thus $u \ge x$ for all $x \in S$, thus $-u \le -x$ for all $x \in S$, thus $-u \le y$ for all $y \in -S$, thus -u is a lower bound of -S, thus -S is bounded below. Q.E.D.
 - b.) Let $u = \sup(S)$. Since u is an upper bound of S, -u is a lower bound of -S. For the sake of establishing a contradiction, suppose there exists $v \in \mathbb{R}$ such that -u < v and v is a lower bound of -S, thus u > -v. Since v is a lower bound of -S, $v \le y$ for all $y \in -S$, thus $-v \ge -y$ for all $y \in -S$, thus $-v \ge x$ for all $x \in S$, thus -v is an upper bound of S, but since u > -v, $u \ne \sup(S) \Rightarrow \leftarrow$, thus $-\sup(S) = -u = \inf(-S)$. Q.E.D.
- 30.) a.) For unbounded sets, infinite suprema and infima make sense, as for all $x \in \mathbb{R}$, $-\infty < x < \infty$. In addition, there exists no $y \in \mathbb{R}$ such that $y < -\infty$ or $y > \infty$, thus $\sup(S) = \infty$ and $\inf(S) = -\infty$.
 - b.) ***
- 33.) Let $x, y \in \mathbb{R}$. From the triangle inequality, we know that

$$|x+y| \le |x| + |y|$$

- 36.) When learning the various integration techniques taught in calculus 2, I noticed that some of them involved manipulating the dx term. I initially found this confusing, as I though that $\frac{d}{dx}$ was a single operator that could not be separated. I later found out that this was not the case, and that it can often be treated just like a fraction. What helped me to realize this was when I watched a video series that explained calculus in a more intuitive, less purely algebraic way. In this context, dx being a separate variable simply made sense.
- 39.) a.) A sequence is defined as a function x(n) such that $x: \mathbb{N} \to \mathbb{R}$.
 - b.) The sequence $\{x_n\}_{n=1}^{\infty}$ converges to $L \in \mathbb{R}$ if and only if

$$\forall \epsilon > 0 : \exists k \in \mathbb{N} : n \ge k \implies |x_n - L| < \epsilon$$