

Section 1.1

1.) **Problem:** Evaluate the following:

$$(1 + 2i)^3, \quad \frac{5}{-3 + 4i}, \quad \left(\frac{2 + i}{3 - 2i} \right)^2, \quad (1 + i)^n + (1 - i)^n$$

Solutions:

a.) $(1 + 2i)^3 = (-3 + 4i)(1 + 2i) = -11 - 2i$

b.) We have that

$$\frac{5}{-3 + 4i} = \frac{5}{-3 + 4i} \cdot \frac{-3 - 4i}{-3 - 4i} = \frac{-15 - 20i}{25} = -\frac{3}{5} - \frac{4}{5}i$$

c.) We have that

$$\begin{aligned} \left(\frac{2 + i}{3 - 2i} \right)^2 &= \frac{2 + i}{3 - 2i} \cdot \frac{2 + i}{3 - 2i} = \frac{3 + 4i}{5 - 12i} = \frac{3 + 4i}{5 - 12i} \cdot \frac{5 + 12i}{5 + 12i} = \frac{-33 + 56i}{169} \\ &= -\frac{33}{169} + \frac{56}{169}i \end{aligned}$$

d.) Awd