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# Software Quality Assurance Đảm bảo chất lượng phần mềm

## Lecture 2: Software Metrics

# Contents

- Motivation of Software Metrics
- Lines of code
- Halstead's metrics
- McCabe Cyclomatic Number
- Maintainability Index (MI)
- OOP Software metrics

# 2.1. Motivation of Software Metrics

# How to achieve a successful software project?

- In order to conduct a successful software project we must understand
  - the scope of work to be done
  - the risks incurred
  - the resources required
  - the tasks to be accomplished
  - the milestones to be tracked
  - the cost
  - the schedule to be followed

# Project Management

- Before a project can be planned
  - objectives and scope should be established
  - alternative solutions should be considered
  - technical and management constraints should be identified
- This information is required to estimate costs, tasks, and a schedule

# Software Metrics

- Metrics help us understand the technical process that is used to develop a product
  - The process is measured to improve it and the product is measured to increase its quality
- Measuring software projects is still controversial
  - Not yet clear which are the appropriate metrics for a software project
  - whether people, processes or products can be compared using such metrics

# Why use metrics?

- Without measurements there is no real way to determine if the process is improving
- They allow the establishment of meaningful goals for improvement
- Metrics allow an organization to identify the causes of defects that have the greatest effect on software development



# Applying metrics

- When metrics are applied to a product they help identify
  - which user requirements are likely to change
  - which modules are most error prone
  - how much testing should be planned for each module

# Direct measurements

- Measurements can be either direct or indirect
- Direct measures are taken from a feature of an item (e.g., length)
  - Lines of code, execution speed, memory size, defects reported

# Indirect Measurements

- Indirect measurements associate a measure to a feature of the object being measured (e.g., quality is based upon counting rejects)
  - functionality, quality, complexity, efficiency, reliability and maintainability

# Code Complexity Measurements

## Các độ đo độ phức tạp mã nguồn

- Code complexity correlates with the defect rate and robustness of the application program
- Code complexity measurement tools
  - Testwell CMT++ for C, C++ and C#
  - Testwell CMTJava for Java
- Code with good complexity
  - contains less errors
  - is easier to understand
  - is easier to maintain

# How to use code complexity measurements

- Code complexity metrics are used to locate complex code
- To obtain a high quality software with low cost of testing and maintenance, the code complexity should be measured as early as possible in coding --> developers can adapt their code when recommended values are exceeded

# Code complexity metrics

- Metrics shown by Testwell CMT++/CMTJava
  - Lines of code metrics
  - McCabe Cyclomatic number
  - Halstead Metrics
  - Maintainability Index

## 2.2. Lines of code

# Lines of code metrics

- Most traditional measures used to quantify software complexity
- Simple, easy to count and very easy to understand
- Do not take into account the intelligence content and the layout of the code
- Testwell CMT++/CMTJava calculates the following lines of code metrics
  - LOCphy: number of physical lines
  - LOCbl: number of blank lines (a blank line inside a comment block is considered to be a comment line)
  - LOCpro: number of program lines (declarations, definitions, directives and code)
  - LOCcom: number of comment lines



# Lines of code metrics - Recommendations

## Những giá trị khuyên dùng cho chiều dài mã nguồn

- **Function length**

- Function length should be 4 to 40 program lines
- A function definition contains at least a prototype, one line of code, a pair of braces, which makes 4 lines
- A function longer than 40 program lines probably implements many functions
- Exception: functions containing one selection statement with many branches) --> decomposing them into smaller functions often decreases readability

# Lines of code metrics - Recommendations

## Những giá trị khuyên dùng cho chiều dài mã nguồn

- **File length**

- File length should be 4 to 400 program lines
- The smallest entity that may reasonably occupy a whole source file is a function and the minimum length of a function is 4 lines
- Files longer than 400 program lines (10..40 functions) are usually too long to be understood as a whole

# Lines of code metrics - Recommendations

## Những giá trị khuyên dùng cho chiều dài mã nguồn

- **Comments**

- At least 30% and at most 75% of a file should be comments
- If less than one third of a file is comments the file is either very trivial or poorly explained
- If more than 75% of a file are comments, the file is not a program but a document
- Exception: in a well-documented header file percentage of comments may sometimes exceed 75%

## 2.3. Halstead's Metrics

# Halstead's Metrics

- Developed by Maurice Halstead
- Introduced in 1977
- Used and experimented extensively since that time
- One of the oldest measures of program complexity
- Strong indicators of code complexity
- Often used as a maintenance metric

# Halstead's Metrics (cont.)

- Based on interpreting the source code as a sequence of tokens and classifying each token to be an operator or an operand
- **Operator: toán tử – Operand: toán hạng**
- Then is counted
  - number of unique (distinct) operators ( $n_1$ )
  - number of unique (distinct) operands ( $n_2$ )
  - total number of operators ( $N_1$ )
  - total number of operands ( $N_2$ )
- All other Halstead measures are derived from these four quantities with certain fixed formulas as described later

# Operators and Operands

- Operators
  - traditional: +, -, \*, /, ++, --, etc.
  - keywords: return, if, continue, break, try, catch etc.
- Operands
  - identifiers
  - constants

# Halstead's Metrics

## Một số độ đo của Halstead

- **Program length (N):** the program length is the sum of the total number of operators and operands in the program:
  - $N = N_1 + N_2$
- **Vocabulary size (n):** the vocabulary size is the sum of the number of unique operators and operands
  - $n = n_1 + n_2$
- **Program volume (V):** information content of the program
  - $V = N * \log_2(n)$
- **Halstead's volume** describes the size of the implementation of an algorithm



# Halstead's metrics - Recommendations

## Một số khuyến cáo về giá trị độ đo Halstead

- The volume of a function should be at least 20 and at most 1000
  - The volume of a parameter less one-line function that is not empty is about 20
  - A volume greater than 1000 tells that the function probably does too many things
  - The volume of a file should be at least 100 and at most 8000
  - These limits are based on volumes measured for files whose LOCpro and  $v(G)$  are near their recommended limits

# Other Halstead's metrics

- **Difficulty level (D)**

- The difficulty level or error proneness (D) of the program is proportional to the number of unique operator in the program
- D is also proportional to the ration between the total number of operands and the number of unique operands
  - i.e., if the same operands are used many times in the program, it is more prone to errors
- $D = (n_1/2) * (N_2 / n_2)$

- **Program level (L)**

- The program level (L) is the inverse of the error proneness of the program
- i.e., A low level program is more prone to errors than a high level program
- $L = 1 / D$

# Other Halstead's metrics

- **Effort to implement (E)**

- The effort to implement or understand a program is proportional to the volume and to the difficulty level of the program
- $E = V * D$

- **Time to implement (T)**

- The time to implement or understand a program (T) is proportional to the effort
- Halstead has found that dividing the effort by 18 give an approximation for the time in seconds
- $T = E / 18$

# Other Halstead's metrics

- **Number of delivered bugs (B)**

- The number of delivered bugs (B) correlates with the overall complexity of the software
- $B = (E^2/3)/3000$
- Estimates for the number of errors in the implementation
- Delivered bugs in a file should be less than 2
- Experiences have shown that when programming with C or C++, a source file almost always contains more errors than B suggests
- B is an important metric for dynamic testing
- The number of delivered bugs approximates the number of errors in a module
- As a goal at least that many errors should be found from the module in its testing

# Halstead's metric Example

## Ví dụ về độ đo Halstead

- Given a source code in C/C++
- Calculate some basic metrics of Halstead
  - $n_1$
  - $n_2$
  - $N_1$
  - $N_2$
- What are the operators/operands in this source code?

```
void sort ( int *a, int n ) {  
    int i, j, t;  
  
    if ( n < 2 ) return;  
    for ( i=0 ; i < n-1; i++ ) {  
        for ( j=i+1 ; j < n ; j++ ) {  
            if ( a[i] > a[j] ) {  
                t = a[i];  
                a[i] = a[j];  
                a[j] = t;  
            }  
        }  
    }  
}
```

$V \approx 80 \log_2(24) \approx 392$

# Halstead Example (cont.)

- Step 1:

- List all the operands and operators in the source file
- Count the number of distinct operands and distinct operators

- Step 2:

- Calculate V, D, E...

```
void sort ( int *a, int n ) {
int i, j, t;
```

```
    if ( n < 2 ) return;
    for ( i=0 ; i < n-1; i++ ) {
        for ( j=i+1 ; j < n ; j++ ) {
            if ( a[i] > a[j] ) {
                t = a[i];
                a[i] = a[j];
                a[j] = t;
            }
        }
    }
}
```

$$V = 80 \log_2(24) \approx 392$$

- Ignore the function definition
- Count operators and operands

```
3 < 3 {
5 = 3 }
1 > 1 +
1 - 2 ++
2 , 2 for
9 ; 2 if
4 ( 1 int
4 ) 1 return
6 []
```

```
1 0
2 1
1 2
6 a
8 i
7 j
3 n
3 t
```

	Total	Unique
Operators	N1 = 50	n1 = 17
Operands	N2 = 30	n2 = 7

## 2.4. McCabe Cyclomatic Number

# McCabe Cyclomatic Number

## Chỉ số phức tạp của McCabe

- The cyclomatic complexity  $v(G)$  has been introduced by Thomas McCabe in 1976
- Measures the number of linearly-independent paths through a program module (Control Flow)
- The McCabe complexity is one of the more widely-accepted software metrics, it is intended to be independent of language and language format
- Considered as a broad measure of soundness and confidence for a program



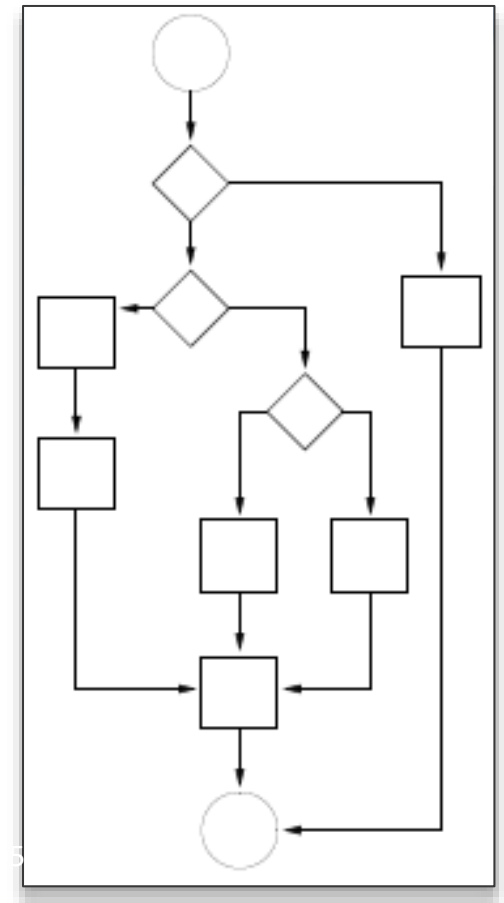
# McCabe Cyclomatic Number – $v(G)$

- $v(G)$  is the number of conditional branches
- $v(G) = 1$  for a program consisting of only sequential statements
- For a single function,  $v(G)$  is one less than the number of conditional branching points in the function
- The greater the cyclomatic number is, the more execution paths there are through the function, and the harder it is to understand

# McCabe Cyclomatic Number

## Công thức tính chỉ số McCabe

- Describes the structural complexity
  - Control flow
  - Data flow
- Graph based metrics
  - Number of vertices
  - Number of edges
  - Maximum length (depth of graph)
- In general:  $v(G) = \#edges - \#vertices + 2$
- For control flow graphs
  - $v(G) = \#binaryDecision + 1$
  - $v(G) = \#IFs + \#LOOPS + 1$



# McCabe Cyclomatic Number

## Ý nghĩa của chỉ số McCabe

- For dynamic testing, the cyclomatic number  $v(G)$  is one of the most important complexity measures
- Because the cyclomatic complexity describes the control flow complexity
  - it is obvious that modules and functions having high cyclomatic number need more test cases than modules having a lower cyclomatic number
  - Rule: each function should have at least as many test cases as indicated by its cyclomatic number

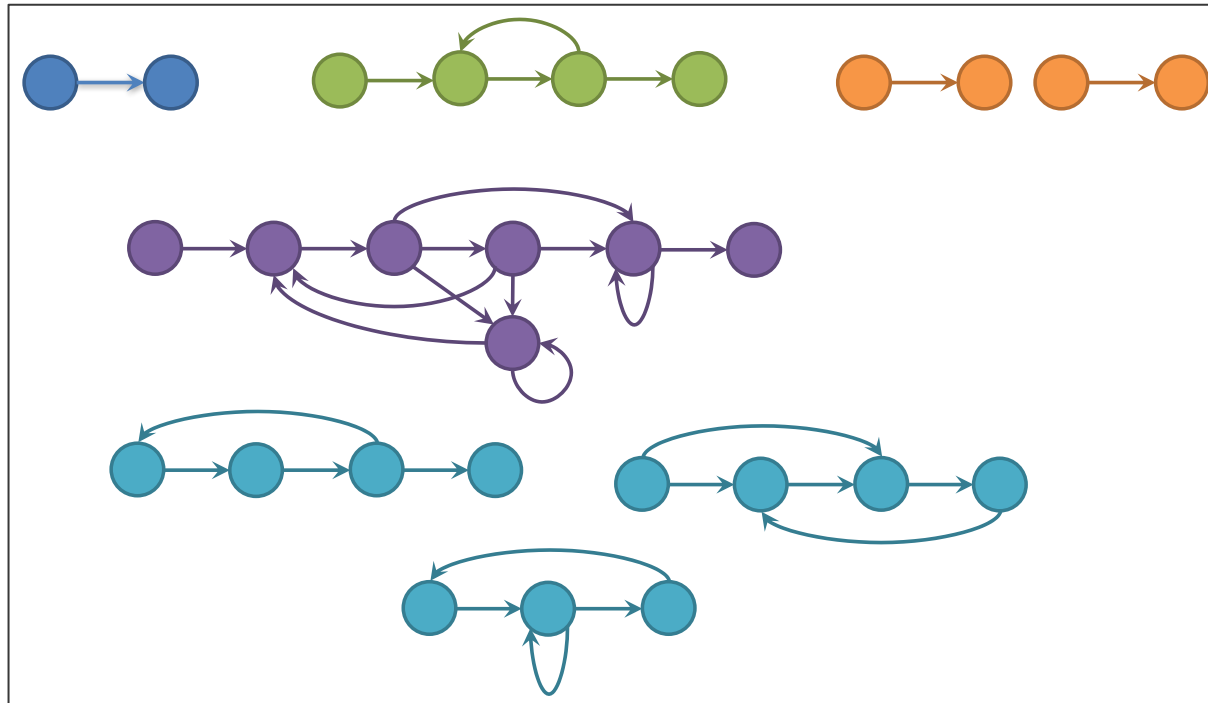
# McCabe Cyclomatic Number - Example

- Count IFs and LOOPS
- IF: 2, LOOP: 2
- $v(G) = 5$

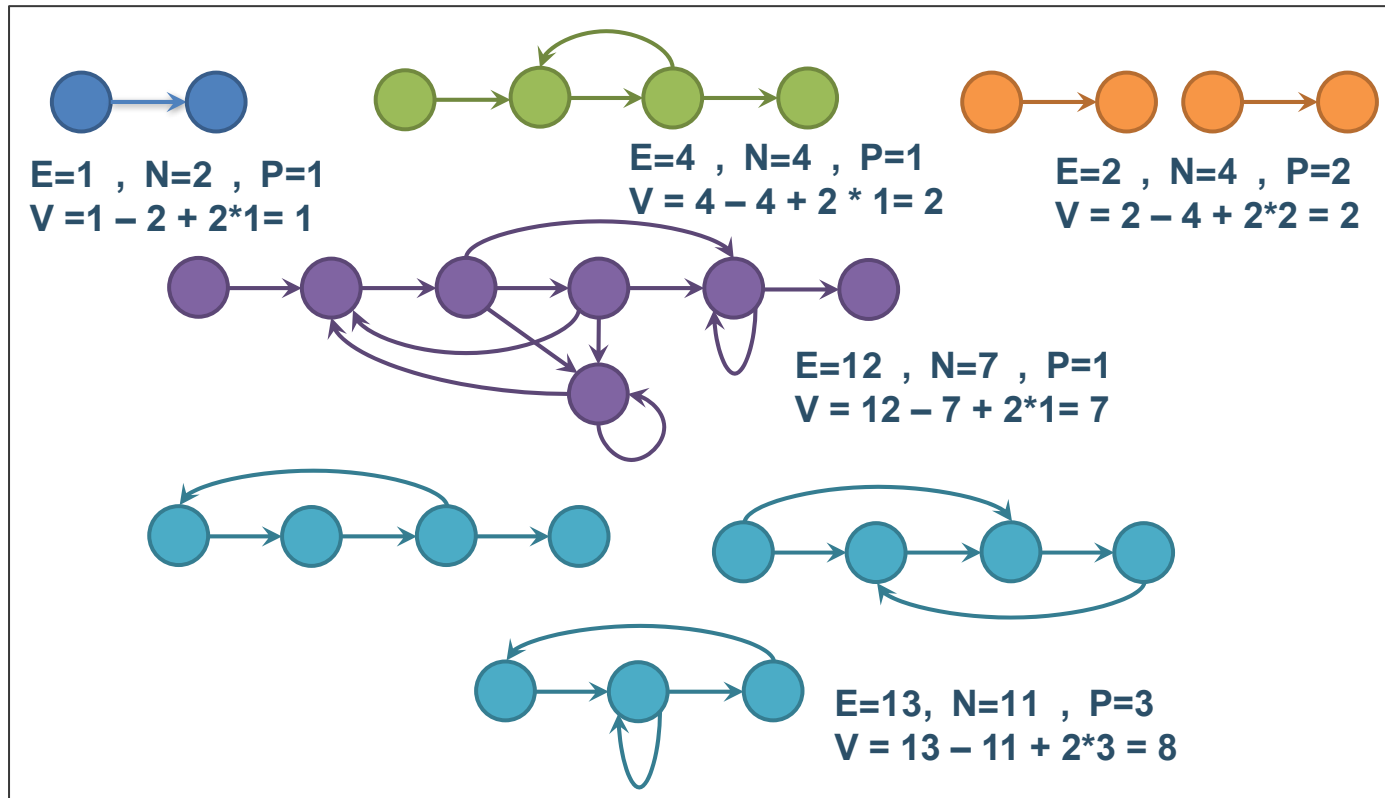
```
void sort ( int *a, int n ) {  
    int i, j, t;  
  
    if ( n < 2 ) return;  
    for ( i=0 ; i < n-1; i++ ) {  
        for ( j=i+1 ; j < n ; j++ ) {  
            if ( a[i] > a[j] ) {  
                t = a[i];  
                a[i] = a[j];  
                a[j] = t;  
            }  
        }  
    }  
}
```

$V = 80 \log_2(24) \square 392$

# Other examples based on CFG



# Other examples based on CFG

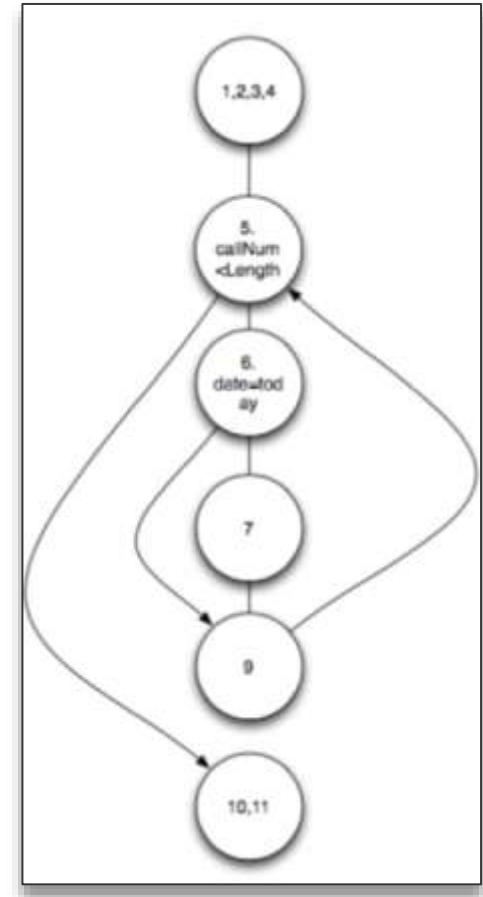


# Other examples based on source code

```
1  procedure SpeakingTimeToday (in listOfCalls; out speakingTime);
2  begin
3      callNum = 0
4      speakingTime = 0
5      while (callNum < listOfCalls.Length)
6          if listOfCalls[callNum].date = today
7              speakingTime = speakingTime + listOfCalls[callNum].time
8          end
9          callNum = callNum + 1
10 end
11 end
```

# Other examples based on source code

```
1  procedure SpeakingTimeToday (in listOfCalls; out speakingTime);
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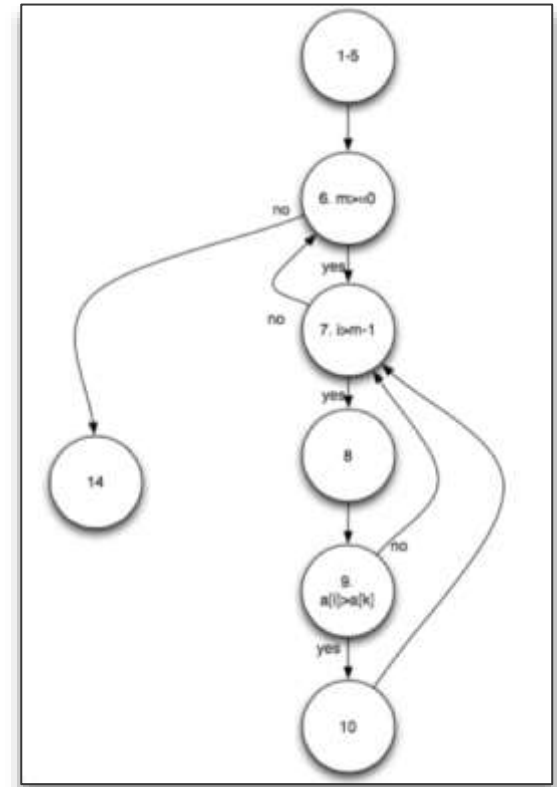


# Other examples based on source code

```
1 public class MyBubbleSort {
2
3     public static void bubble_srt(int array[]) {
4         int n = array.length;
5         int k;
6         for (int m = n; m >= 0; m--) {
7             for (int i = 0; i < m - 1; i++) {
8                 k = i + 1;
9                 if (array[i] > array[k]) {
10                     swapNumbers(i, k, array);
11                 }
12             }
13         }
14     }
15
16     private static void swapNumbers(int i, int j, int[] array) {
17         int temp;
18         temp = array[i];
19         array[i] = array[j];
20         array[j] = temp;
21     }
22 }
```

# Other examples based on source code

```
1 public class MyBubbleSort {
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3     public static void bubble_srt(int array[]) {
4         int n = array.length;
5         int k;
6         for (int m = n; m >= 0; m--) {
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8                 k = i + 1;
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10                     swapNumbers(i, k, array);
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12             }
13         }
14     }
15
16     private static void swapNumbers(int i, int j, int[] array) {
17         int temp;
18         temp = array[i];
19         array[i] = array[j];
20         array[j] = temp;
21     }
22 }
```



# McCabe Cyclomatic Number – Recommendations

## Khuyến cáo đối với chỉ số McCabe

- The cyclomatic number of a function should be less than 15.
  - i.e., if a function has a cyclomatic number of 15, there are at least 15 (but probably more) execution paths through it
- More than 15 paths are hard to identify and test
  - Functions containing one selection statement with many branches make up a exception
- A reasonable upper limit cyclomatic number of a file is 100

## 2.5. Maintainability Index

# Maintainability Index (MI)

## Chỉ số bảo trì được của chương trình

- Calculated with certain formulas from lines of code measures, McCabe measure and Halstead measures
- Indicates when it becomes cheaper and/or less risky to rewrite the code instead to change it
- Two variants of Maintainability Index:
  - One that contains comments (MI) and one that does not contain comments (MIwoc)
- Actually there are three measures:
  - MIwoc: Maintainability Index without comments
  - Mlcw: Maintainability Index comment weight
  - MI: Maintainability Index = **MIwoc + Mlcw**

# MI's formula

## Công thức tính chỉ số MI

- $MI_{woc} = 171 - 5.2 * \ln(\text{aveV}) - 0.23 * \text{aveG} - 16.2 * \ln(\text{aveLOC})$ 
  - $\text{aveV}$  = average Halstead Volume  $V$  per module
  - $\text{aveG}$  = average extended cyclomatic complexity  $v(G)$  per module
  - $\text{aveLOC}$  = average count of lines  $LOC_{phy}$  per module
  - $\text{perCM}$  = average percent of lines of comments per module
- $MI_{cw} = 50 * \sin(\sqrt{2,4} * \text{perCM})$

# MI Recommendations

## Các khuyến cáo đối với chỉ số MI

- Maintainability Index (MI, with comments) values:
  - 85 and more: good maintainability
  - 65-85: Moderate maintainability
  - < 65: Difficult to maintain with really bad pieces of code
  - big, uncommented, unstructured module can lead to a MI value can be event negative

# Maintainability Index Example

- Halstead's  $V = 392$
- McCabe's  $v(G) = 5$
- LOC = 14
- MI = 96 --> easy to maintain!

```
void sort ( int *a, int n ) {  
    int i, j, t;  
  
    if ( n < 2 ) return;  
    for ( i=0 ; i < n-1; i++ ) {  
        for ( j=i+1 ; j < n ; j++ ) {  
            if ( a[i] > a[j] ) {  
                t = a[i];  
                a[i] = a[j];  
                a[j] = t;  
            }  
        }  
    }  
}
```

$V = 80 \log_2(24) \approx 392$



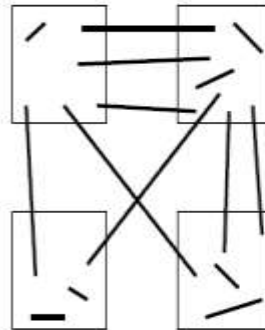
## 2.6. OOP Software Metrics

# What about modularity?

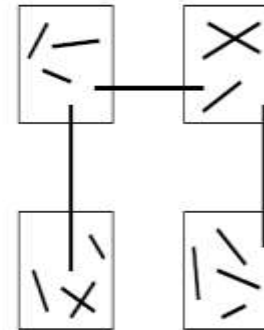
## Thế nào là tính mô đun hoá của chương trình

- Generally, modularity is the degree to which a system may be separated and recombined
- High cohesion and Low coupling is a good design

**Design A**



**Design B**



- **Cohesion:** calls inside the module
- **Coupling:** calls between the modules

	A	B
Cohesion	Lo	Hi
Coupling	Hi	Lo

- Squares are modules, lines are calls, ends of the lines are functions.
- Which design is better?

# Modularity metrics: Fan-in and Fan-out

## Chỉ số về tính mô đun hoá

- Fan-in of M: number of modules calling functions in M
- Fan-out of M: number of modules called by M
- Modules with fan-in = 0
  - deadcode
  - outside of the system boundaries
- Henry and Kafura's information flow complexity
- Fan-in and fan-out can be defined for procedures and functions
  - HK: take global data structures into account:
    - fan-in: flow of information into procedures
    - fan-out: flow of information out of procedures
  - $HK = SLOC \times (\text{fan-in} \times \text{fan-out})^2$ 
    - SLOC: the length (in lines of code) of the procedure without comments and blank lines

# Object-oriented metrics

- Object-oriented metrics measure the structure or behaviour of an object-oriented system
- The system is viewed as a collection of objects rather than as functions/procedures with messages passed from object to object
- Some traditional metrics can be adapted to work within the OO-domain:
  - LOC, percentage of comments, Cyclomatic complexity
  - These metrics are applied within methods

# Chidamber and Kemerer's metrics

## Độ đo của Chidamber và Kemerer

- Weighted methods per class (WMC)
- Response for a class (RFC)
- Lack of cohesion of methods (LCOM)
- Coupling between objects (CBO)
- Depth of inheritance tree (DIT)
- Number of children (NOC)

# Weighted Methods per Class (WMC)

## Phương thức trên một lớp

- WMC is a count of the methods implemented within a class or the sum of the complexities of the methods
  - method complexity is measured by cyclomatic complexity
- The number of methods and their complexity is a predictor of how much time and effort is required to develop and maintain the class
- The larger the number of methods in class, the greater the potential impact on children
  - children inherit all of the methods defined in the parent class
- Classes with large number of methods are likely to be more application specific, limiting the possibility of reuse

# Response for a Class (RFC)

## Phản hồi của một lớp

- The RFC is the count of the set of all methods that can be invoked in response to a message to an object of the class or by some method in the class
  - This includes all methods accessible within the class hierarchy
- This metric looks at the combination of the complexity of a class through the number of methods and the amount of communication with other classes
- The larger the number of methods that can be invoked from a class through messages, the greater the complexity of the class
- If a large number of methods can be invoked in response to a message, the testing and debugging of the class becomes complicated since it requires a greater level of understanding on the part of the tester

# Lack of cohesion (LCOM)

## (Sự thiếu độ kết dính)

- Lack of cohesion measures the dissimilarity of methods in a class by instance variables or attributes
- A highly cohesive module should stand alone
  - High cohesion indicates
    - a good class subdivision
    - simplicity and high reusability
- $LCOM(C) = P - Q$  if  $P > Q$  and  $= 0$  if otherwise
  - P: #pairs of distinct methods in C that do not share variables
  - Q: #pairs of distinct methods in C that share variables
- Lack of cohesion or low cohesion increases complexity, thereby increasing the likelihood of errors during the development process
- Classes with low cohesion could probably be subdivided into two or more subclasses with increased cohesion



# Coupling between object classes (CBO)

## Sự kết nối giữa các đối tượng của các lớp

- CBO is a count of the number of other classes to which a class is coupled
  - measured by counting the number of distinct non-inheritance related class hierarchies on which a class depends
- Excessive coupling is detrimental to modular design and prevents reuse
  - the more independent class is, the easier it is reused in another application
- The larger the number of couples, the higher the sensitivity to changes in other parts of the design
  - therefore maintenance is more difficult
- Strong coupling complicates a system since a class is harder to understand, change or correct
- Complexity can be reduced by designing systems with the weakest possible coupling between classes
  - This improves modularity and promotes encapsulation

# Depth of Inheritance Tree (DIT)

## Độ sâu cây kế thừa

- The depth of a class within the inheritance hierarchy is the maximum number of steps from the class node to the root of the tree and is measured by the number of ancestor classes
- The deeper a class is within the hierarchy, the greater the number of methods it is likely to inherit making it more complex to predict its behavior
- Deeper trees constitute greater design complexity
  - More methods and classes are involved
  - But the greater the potential for reuse of inherited methods

# Number of Children (NOC)

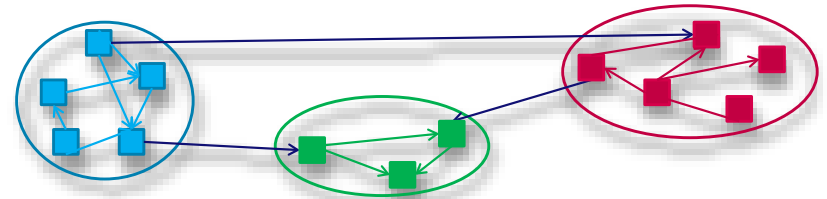
## Số lượng lớp con

- The number of children is the number of immediate subclasses subordinate to a class in the hierarchy
- If a class has a large number of children, it may require more testing of the methods of that class, thus increasing the testing time
- NOC is an indicator of the potential influence a class can have on the system
  - The greater the NOC, the greater the likelihood of improper abstraction of the parent
  - But the greater the NOC, the greater the reuse since inheritance is a form of reuse

# Package-level Metrics

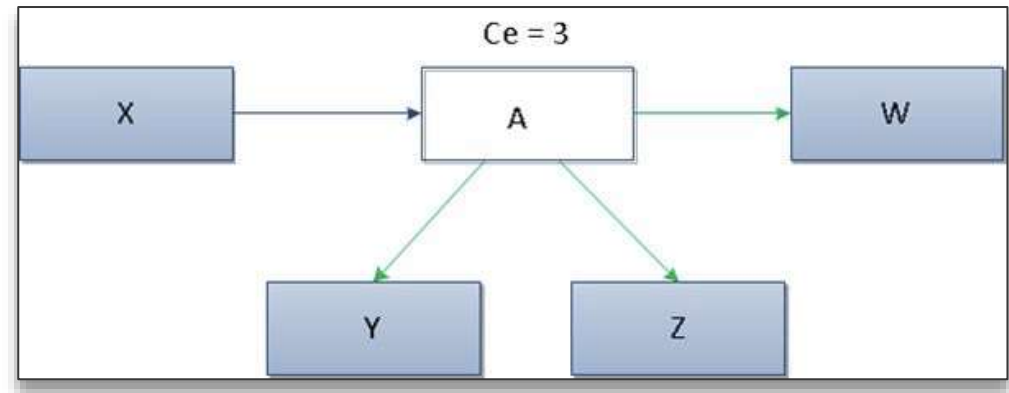
## Các độ đo ở mức gói

- Proposed by Robert Cecil Martin (Uncle Bob)
- Focus on the relationship between packages in the project
- Martin's metrics include
  - Efferent Coupling (Ce)
  - Afferent Coupling (Ca)
  - Instability (I)
  - Abstractness (A)
  - Normalized Distance from Main Sequence (D)



# Efferent Coupling (CE)

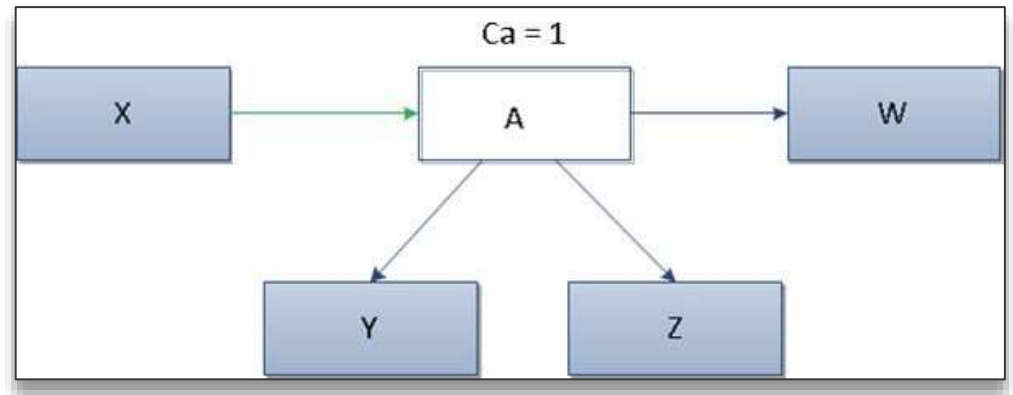
- This metric is used to measure interrelationship between classes (outgoing dependencies)
- It is a count for the number of classes in a given package which depend on the classes of other packages
- An indicator of the package's responsibility



- The high value of Ce indicates instability of a package
  - change in any of the numerous external classes can cause the need for changes to the package
- Preferred values for Ce are in the range of 0 to 20

# Afferent Coupling (CA)

- Another type of dependencies between packages, i.e., incoming dependencies
- It measures the number of classes and interfaces from other packages that depend on classes in the analysed package



# Instability (I)

- This metric is used to measure the relative susceptibility of class to changes
- $I = Ce / (Ce + Ca)$
- On the basis of value of I, we can distinguish two types of components
  - The ones having many outgoing dependencies and not many of incoming ones (value of I is close to 1), which are rather unstable due to the possibility of easy changes to these packages
  - The ones having many incoming dependencies and not many of outgoing ones (value of I is close to 0), therefore they are rather more difficult in modifying due to their greater responsibility

# Abstractness (A)

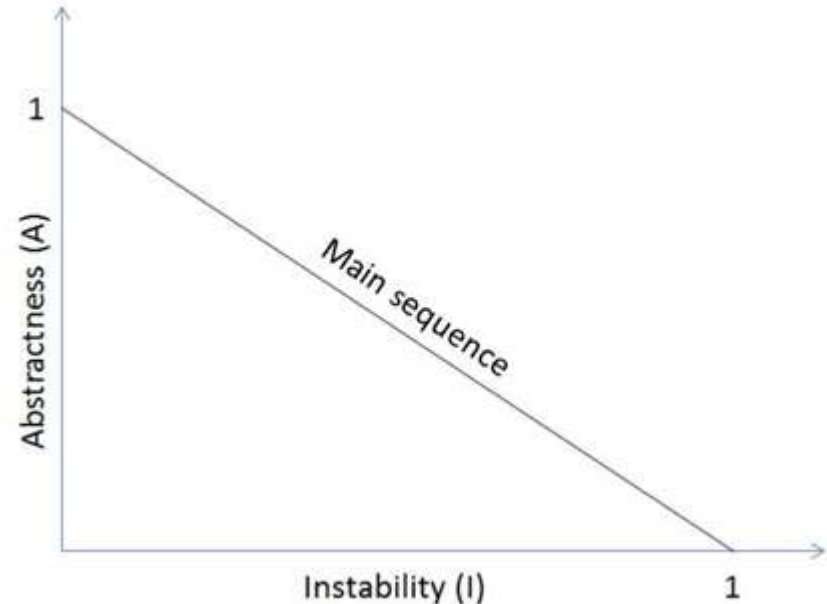
- This metric is used to measure the degree of abstraction of the package and is somewhat similar to the instability
- $A = T_a / (T_a + T_c)$ 
  - $T_a$ : number of abstract classes in a package
  - $T_c$ : number of concrete classes in this package
- Packages that are stable (metric I close to 0) should also be abstract (metric A close to 1)
- Packages that are unstable (metric I close to 1) should consists of concrete classes (metric A close to 0)



# Main Sequence

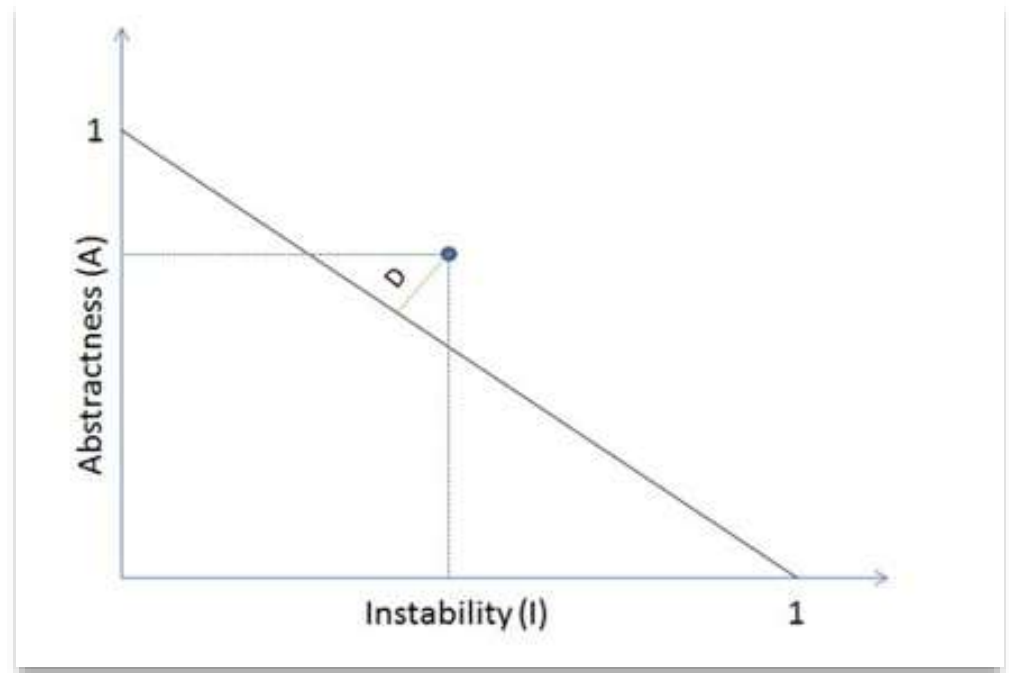
## Đường trình tự chính

- Combining A and I formulates the existence of main sequence
- Classes that were well designed should group themselves around the graph end points along the main sequence



# Normalized distance from main sequence (D)

- This metric is used to measure the balance between stability and abstractness and is calculated using the following formula
  - $D = |A + I - 1|$
  - If we put a given class on a graph of the main sequence, its distance from the main sequence will be proportional to the value of D



# Benefits of Normalized distance from main sequence (D)

## Ý nghĩa của chỉ số D

- The value of D should be as low as possible so that the components were located close to the main sequence
- $A = 0$  and  $I = 0$ , a package is extremely stable and concrete, the situation is undesirable because the package is very stiff and cannot be extended
- $A = 1$  and  $I = 1$ , rather impossible situation because a completely abstract package must have some connection to the outside, so that the instance that implements the functionality defined in abstract classes contained in this package could be created

# Summaries

## Tổng kết

- Students must understand the motivation of using software metrics to improve the quality of source code and also to improve the quality of software systems
- Give a general perspective about software metrics that are commonly used in software engineering
  - General metrics of lines of code
  - McCabe Cyclomatic Number
  - Halstead's metrics
  - Maintainability Index
  - OOP metrics



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Thank you  
for your  
attention!!!

