

# TRANSFORMATIONS

- Transformations in 3D (rotation, scale, shear) can be expressed as 3x3 matrix multiplications
- Translations cannot
- *Homogeneous coordinates*
  - 3x3  $\rightarrow$  4x4
  - Translation by x,y,z  $\rightarrow$

$$\begin{array}{cccc} 1 & 0 & 0 & x \\ 0 & 1 & 0 & y \\ 0 & 0 & 1 & z \\ 0 & 0 & 0 & 1 \end{array} * \begin{array}{c} a \\ b \\ c \\ 1 \end{array} = \begin{array}{cc} a + x & \\ b + y & \\ c + z & \\ 1 & \end{array} = w$$

- Division by w (*perspective division*) to retrieve inhomogeneous point
- The *Model matrix* defined the result of a number of transformations that are unique for an object

# VIEW & PROJECTION MATRIX

- Per default: OpenGL's camera is at (0,0,0) looking towards the -z direction
- Everything in *normalized device coordinates* (NDC) in range [-1,1]
- View matrix modifies the location of the OpenGL's camera
- Projection Matrix
  - Projects a 3D scene onto the 2D rendering surface
  - Projection methods
    - Orthographic projection (parallel lines remain parallel)
    - Perspective projection (parallel lines converge)
- Each vertex  $v$  is modified by model  $M$ , view  $V$ , and projection  $P$  matrices:  
$$x = P * V * M * v$$