

A Neural Network that Guides Stochastic Search

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Abstract. Typically in a genetic algorithm, the variability operators, i.e. the way that a parent generates offspring, is not modified during the evolutionary run. Here we adaptively learn an exploration distribution by training a denoising autoencoder online at each generation to reconstruct a slowly decaying memory of the best genotypes so far encountered. By using a compressed hidden layer, the autoencoder is forced to learn hidden features in the training set that may generalise to novel problems. It's output neurons define a probability distribution that we sample from to produce offspring solutions. The algorithm outperforms a canonical genetic algorithm on several combinatorial problems, including the multidimensional 0/1 knapsack problem, MAXSAT and the Hierarchical If and Only If, and on some parameter optimisation algorithms such as the Rastrigin and Rosenbrock functions. The neural network is able to learn hidden structure in the fittest genotypes, whilst sampling from the network using a Bernoulli distribution or with Gaussian noise maintains diversity, enabling optimal solutions to be found on NP-hard problems.

1 Introduction

Estimation of distribution algorithms (EDAs) are a growing subfield in evolutionary computation. They attempt to statistically model sections of a search space in order to uncover underlying structure and guide search towards optimal solutions in an efficient manner [1]. At the heart of any EDA lies a model-building algorithm. Examples include Bayesian Networks [2], Markov Networks [?] and K-Means clustering [?]. In this paper we introduce a novel neural-based method for modelling; a denoising autoencoder. An autoencoder is a feed forward neural network, consisting of at least one hidden layer, which is trained to reproduce its inputs from its outputs. Over the course of training the hidden layer forms a compressed representation of the inputs, which can be used for reconstructing missing data [?] and dimensionality reduction [?]. Throughout the evolutionary run we train a single autoencoder with the currently best solutions in the population, allowing a compressed hidden layer to extract features in the genotypes by backpropagation. Our work differs from traditional EDAs such as PBIL [?] or ECGA [?] because an explicit statistical model of a distribution of genotypes is not produced. Results presented in Section 5 show that the autoencoder based genetic algorithm is able to outperform a canonical genetic algorithm (GA) across a range of combinatorial optimisation and parameter optimisation problems.

2 Background

EDAs (also known as Probabilistic-Model-Building Genetic Algorithms) are population based optimisers, that typically replace genetic operators with a statistical model. The rationale behind the model building and related linkage learning approach is that dependencies between variables can be captured and preserved. Early work on EDAs concentrated on methods that explicitly modelled the probabilities of features occurring independently in a population of genotypes. These include the compact Genetic Algorithm [?], PBIL [?] and Univariate Marginal Probability methods[?]. Improved success was found by modelling multivariate dependencies using clustering algorithms (ECGA) [?], Bayesian Networks [2], Markov Networks [?] and tree structures [?], among others.

Our use of the autoencoder model is motivated by its potential to learn high-dimensional non-linear dependencies in data, while maintaining a low computational cost in terms of training time. Recently there has been interest in neural-based methods in an EDA context for multi-objective optimisation. A Growing Neural Gas (GNG) was used as a model in [?], employing a competitive Hebbian learning rule to cluster data without having to pre specify the number of groups. A shallow Restricted Boltzmann Machine (RBM) was used to model high dimensional data in [?], beating the state-of-the-art on several multi-objective continuous benchmark problems. An autoencoder is another neural-based method for the unsupervised learning of features and has hitherto not been applied to combinatorial or continuous optimisation.

A second motivation for this approach is to investigate methods in which evolutionary algorithms can be implemented using neural structures. The *Neural Replicator Hypothesis* [?] proposes that evolutionary dynamics could operate in the brain at ontogenetic timescales. In [3], a (1+1)-ES is implemented in a network of spiking neurons. Adding Hebbian learning enabled linkages to be found between features, and the 128-bit HIFF problem to be solved significantly faster than by a genetic algorithm.

3 Methods

3.1 The Autoencoder

In this paper, we present a system that uses a denoising autoencoder (dA) to model the structure of the best solutions at each generation. New solutions at each generation are produced by sampling from the dA. Therefore, the two primary uses of the dA are for model building and sampling new solutions.

The population of good solutions at each generation can be assumed to be a sample from a data generating distribution. Data generating distributions for high-dimensional data often have complex structure that cannot be modelled accurately by simple probabilistic models. Models such as RBMs, Bayesian nets and Helmholtz machines have been used in the past to this end [4–6].

A standard autoencoder consists of an encoder and a decoder. The encoder performs an affine transformation followed by an element-wise non-linear operation. The mapping performed by the encoder is deterministic and can be described as:

$$h_{\theta}(\mathbf{x}) = f(\mathbf{W}\mathbf{x} + \mathbf{b})$$

The decoder is also a deterministic network and operates on the encoded input $h_{\theta}(x)$ to produce the reconstructed input:

$$r_{\theta'}(\mathbf{h}) = g(\mathbf{W}'\mathbf{h} + \mathbf{b}')$$

The autoencoder learns the distribution of the training data by means of the layer of hidden variables. The encoder network is a non-linear generalisation of PCA [?]. The autoencoder learns interactions between the input attributes and maps it to the hidden layer via a non-linear transformation, making it a powerful model for learning and exploiting structure present in the best individuals.

We interpret the outputs of the decoder network as parameters for a conditional distribution $p(X|Z = \mathbf{z})$ over the outputs of the network given an input \mathbf{z} . For binary optimization problems, the outputs \mathbf{z} are considered to be parameters for the distribution $X|\mathbf{z} \sim \mathcal{B}(\mathbf{z})$ where \mathcal{B} is the bernoulli distribution. For continuous parameter-optimisation problems, the outputs \mathbf{z} parameterise a multi-variate normal distribution $X \sim \mathcal{N}(\mathbf{z}, \sigma^2)$, where the covariance matrix is assumed to be diagonal and the standard deviation along the diagonal is a tuneable parameter.

In our algorithm we use a denoising autoencoder (dA) which is a variant of the standard autoencoder [?]. The dA tries to recreate the input \mathbf{x} from ‘corrupted’ or ‘noisy’ versions of the input, which are generated by a stochastic corruption process $\tilde{\mathbf{x}} = \mathbf{q}(\tilde{\mathbf{x}}|\mathbf{x})$. Autoencoders are trained along with strong regularisation in order to impose an information bottleneck on the model. If this is not done carefully, it would be very easy for the autoencoder to learn the identity transformation which would not be very useful. Adding the denoising criterion to the model forces the autoencoder to learn more robust representations which are invariant to perturbations of the input. Although denoising was introduced in order to encourage the learning of more robust representations, in our system we employ the denoising criterion to widen the basins of attraction around the best individuals in every generation. During training, we train the autoencoder on the most promising solutions, and by increasing corruption we encourage individuals that are far away from the training set to move towards the nearest high quality solution. By making use of the corruption noise as a tuneable parameter, the extent of the basins of attraction can be controlled, with high corruption giving rise to large basins of attraction.

We present a toy example in order to validate our hypothesis. We train an autoencoder on a 6-bit problem where the target vectors are all ones, all zeros, and the 3 least significant bits set to 1. Fig 2 shows matrix of transition probabilities for all possible pairs of genomes. There are 64 possible genomes for the 6-bit problem. The indices of the X and Y axes are labelled as the sequence of binary numbers: the 0-index corresponds to the string of all 0s and the 63rd

index corresponds to the string of all ones. Each point (a,b) in the figure denotes the probability of transition from genome a to b. From the figure we observe that there are bands of high probabilities along $Y = 0, 7, 63$. This implies that for most input genomes, the autoencoder has a high probability of producing a genome that is close to one of the target solutions. In figure 3, we plot the marginalised probabilities of each of the target genomes. We observe peaks at the location of the three target vectors. We also notice that there is a band of high probability between the vectors 000000 and 000111. This demonstrates that the autoencoder learns the structure of the best solutions and yields outputs that are closer to the best solutions. The fact that the new population has probability peaks around all three target solutions demonstrates that the autoencoder learns a complex non-linear mapping from input to output and is capable of retaining information about several classes of solutions, thus enabling more effective search.

We perform another experiment to test the effect of corruption noise on the outputs of the dA. We argue that increasing corruption noise widens the basin of attraction around the training examples. In this experiment, we train the GA on a 20-bit MaxOnes problem. The choice of the problem was motivated by the fact that MaxOnes has a unique optimum solution and the hamming distances from the optimal solution are easy to interpret. We allow the GA to run for 10 iterations and train the autoencoder on the best solutions at every iteration. The inputs to the dA are corrupted by a binary corruption process that stochastically flips a fixed proportion of bits for each example. The autoencoder is then trained to reconstruct the true targets from the corrupted inputs. After 10 iterations we present a set of randomly generated input vectors and sample a new population from the dA. We repeat this experiment with different corruption rates and the same set of input vectors and plot the hamming distances of the new population from the optimum solution. From figure 3 we observe that increasing the corruption rate leads to a decrease in the hamming distances. This shows that as corruption noise is increased, the outputs of the dA are more likely to be closer to an example in the training set. ?

3.2 Optimisation Algorithm

The pipeline of the *Denoising Autoencoder Genetic Algorithm* (DAGA) is similar to other EDAs and is inspired by methods in HBOA [2]. A population of solutions is maintained, P_t , and updated at each iteration, t . An initial population of solutions, P_0 , is drawn from a uniform distribution. These solutions are evaluated and the fittest unique $x\%$ are selected (i.e. truncation selection) to be in the training set, \hat{P}_t . The Denoising Autoencoder, D_t , is then trained with \hat{P}_t for e epochs. Following training, a new set of solutions, S_t , is selected from P using tournament selection (with replacement). Each member of S_t is inputted to D_t , and the output vector, y , is sampled from using a binomial distribution, to produce a new solution. This solution is included in P_{t+1} if it is better than its closest neighbour according to Restricted Tournament Selection (RTR) [2]. Pseudocode for DAGA is presented in Algorithm 1.

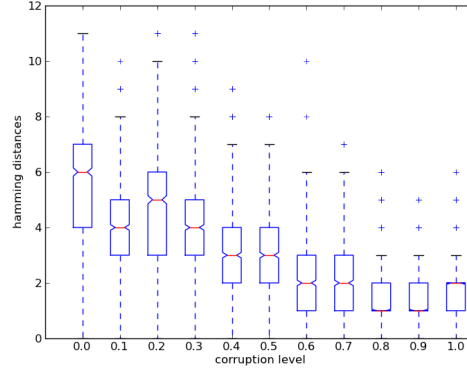


Fig. 1: Hamming distances to optimal solution on MaxOnes with different corruption levels.

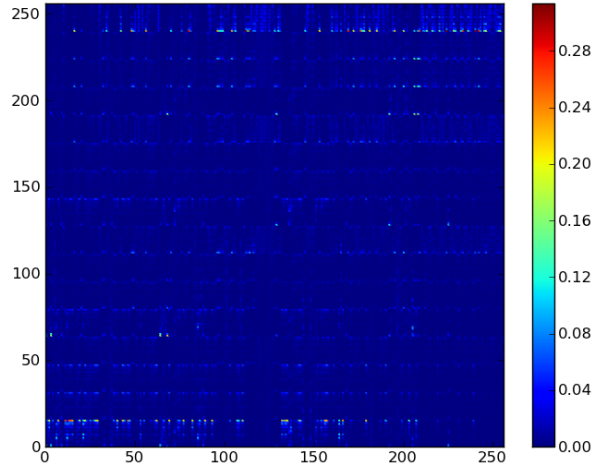


Fig. 2: 8-bit HIFF transition matrix.

4 Experiments

DAGA is tested on three sets of experiments: (1) discrete, (2) continuous and (3) accumulation of adaptation problems.

4.1 Discrete

Multi-dimensional Knapsack Problem Here we wish to choose of subset of N items to maximise the total value of items, z , while satisfying m constraints. We wish to maximise:

$$z = \sum_{j=1}^N v_j x_j, \text{ subject to } \sum_{j=1}^N w_{ij} x_j \leq c_i, i = 1, \dots, m$$

$$x_i \in \{0, 1\}, j = 1, \dots, N.$$

Two different instances are used in the results presented below. The first is the Weing8 instance [?], which has 105 items and two constraints (optimal solution is 602,319), and the second is a randomly generated instance with 500 items and one constraint (optimal solution is 100,104). Both instances are available in the supplementary material. If any of the m constraints are violated, the total value of chosen items is multiplied by -1 .

Hierarchical If and only If The Hierarchical If and only If (HIFF) problem was created by Watson et al., as an example of a function which is not separable [?]. It is a pathological function for a hill climber because of a very large number of local optima. The HIFF is structured as a balanced binary tree [2], where at each lower level a transfer function is applied to consecutive non-overlapping 2-bit partitions, $00 \rightarrow 0$, $11 \rightarrow 1$, anything else \rightarrow null, to define the string in the layer above. At each level, 00 and 11 blocks contribute to the fitness by 2^{level} . Two global optima exist, a string of all 1s and all 0s. In the results section, DAGA is applied to the 128-bit HIFF. In order to remove any possible bias towards an all 1s solution, solutions from DAGA have a random bit mask (fixed before each trial) applied to them before evaluating fitness.

Royal Road The Royal Road function as defined by Mitchell et al. [?], divides a bit string, x , into a number of equally sized, non-overlapping partitions, $z_i \in [x_i, \dots, x_{i+n}]$. If all of the bits in the partition match a predefined pattern, s_i , then the partition's fitness contribution is added to the overall fitness. The existence of these "Building blocks" was meant to act as a "royal road" for GAs compared to hill-climbers but bad alleles hitchhiking to good partial solutions slows down convergence speed. The 128-bit problem with 8-bit partitions is defined as,

$$f(x) = \sum_{i=1}^{16} \delta_i(x) o(s_i), \text{ where } \delta_i(x) \begin{cases} 1, & \text{if } x \in s_i \\ 0, & \text{otherwise} \end{cases}$$

If a string contains two instances of s , a fitness of 16 is achieved. If all instances are found, fitness = 128. s_i instances are blocks of all 1s but as with the HIFF, a random mask is applied to the output of DAGA before fitness evaluation.

MAXSAT

4.2 Continuous

Sphere

Rosenbrock

Rastrigin

4.3 Accumulation of Adaptation

To answer the question of whether solving previous problems can speedup convergence on unseen problems in the same class, a new task was devised that was influenced by Watson et al [?]. DAGA is applied to solve three problems in sequence, without reinitialising the weights of the DA. The problems consist of minimising the hamming distance to a target string. The algorithm is evaluated on the difference in the number of iterations needed to solve the third problem after solving the first two, compared to solving the third problem on its own. The first and second solutions are a square and cross pattern. The third solution is a pattern made by recombining quarters from the original patterns. As each new solution can inherit a quarter from either the cross or the square pattern, there are 2^4 unique solutions. DAGA is tested on training on the cross and the square and then on one of the 16, as well as the square and the cross and then on of the other, leading to 32 experiments.

5 Results

On the discrete and continuous problems, DAGA is compared to a canonical generational Genetic Algorithm (GA). On the continuous problems it is additionally compared to a (1+1)-ES with the 1/5 rule [?]. The GA employs tournament selection, two point crossover (with probability p_c) and on the discrete problems there is a probability, p_m , of a bit flip mutation at each allele, while on the continuous problems there is probability, p_m , of adding Gaussian noise to each component of the vector from $N(0, \delta)$. Programming code is available in the online supplementary material. For each experiment a large parameter sweep was performed on both DAGA and the GA and the best found configurations were chosen for comparison. Due to the stochastic nature of the algorithms each experiment is repeated 10 times.

5.1 Discrete

Table ?? presents details of the best solution in the population at quarter intervals of a run for DAGA and the GA on the 6 problems described above in 4.1. The table shows that DAGA finds either significantly better solutions, or optimal solutions significantly faster than the GA. On three of the five experiments

Experiment	Algorithm	Min	Max	Mean 1Q	Mean 2Q	Mean 3Q	Mean 4Q	Success %
MAXSAT	GA	424.0	429.0	425.9	426.2	426.3	426.5	0%
	AE	429.0	430.0	429.1*	429.56*	429.67*	429.78*	70%
HIFF	GA	832.0	1024.0	505.2	756.6	915.2	940.8	50%
	AE	1024.0	1024.0	568.4*	992.0*	1024.0*	1024.0	100%
Knapsack Weing8	GA	619568.0	621086.0	609728.9	619170.1	619856.0	620099.2	0%
	AE	621086.0	624319.0	617593.2*	621446.8*	622056.4*	623124.3*	80%
Knapsack 500	GA	10047.0	10093.0	9637.7	10011.8	10055.8	10074.2	0%
	AE	10096.0	10104.0	10020.0*	10101.4*	10102.7*	10102.7*	70%
RR	GA	120.0	128.0	120.0	124.0	127.2	127.2	90%
	AE	128.0	128.0	122.4	128.0	128.0	128.0	100%

Table 1: Results for DAGA and the GA on the 5 problems. Showing the value of the minimum and maximum solution returned at the end of search, and the mean best solution in the population after 25%, 50%, 75% and 100% of evaluations had been completed, across 10 trials. Stars indicate that the mean result for DAGA is significantly different from the GA according to a Wilcoxon Rank Sum test ($p < 0.05$).

(both knapsacks and MAXSAT), DAGA finds significantly better solutions than the GA, within the given evaluation limits. On the Weing8 knapsack instance DAGA reaches the optimum solution 8 out of 10 attempts, and on the 500-item instance 7 out of 10 attempts. On the MAXSAT instance, DAGA also reaches the optimum 70% of the time. On all three of these problems the GA is unable to locate the optimal solution a single time. On the 128-bit HIFF, DAGA locates the optimal solution every time, while the GA locates it on only half of the trials. On the Royal Road, DAGA again locates the global optima on every trial, while the GA finds it on 9 out of 10. These results show that on a wide range of discrete problems DAGA is able to find higher quality solutions and more consistently locate the optimum compared to a GA.

As well as frequently obtaining better quality solutions at the end of the optimisation process, DAGA also finds significantly better solutions than the GA at earlier stages in the optimisation process on a number of the tested problems. Table ?? shows the mean best solution found after different numbers of function evaluations have passed. From this we see that on all of the problems, apart from RR, DAGA finds significantly better solutions than the GA after a quarter of function evaluations have passed. On the 128-bit HIFF and RR functions, the GA is able to locate optimal solutions eventually but not consistently. DAGA is statistically significantly better after 25%, 50% and 75% of evaluations have passed on the 128-bit HIFF. On this difficult problem, DAGA finds the optimum after 230,000 evaluations on average, with 200,000 in the fastest case and 285,000 in the slowest. At its fastest, the GA finds the optimum after 300,000 evaluations (mean 332,000 on the successful attempts), although on half the trials it fails to

Experiment	Algorithm	Min	Max	Mean 1Q	Mean 2Q	Mean 3Q	Mean 4Q
Sphere 50D	GA	0.065	0.101	25.178 \pm 10.900	0.165 \pm 0.088	0.125 \pm 0.032	0.088 \pm 0.016
	(1+1)-ES	0.000	0.000	0.000 \pm 0.000	0.000 \pm 0.000	0.000 \pm 0.000	0.000 \pm 0.000
	AE	0.026	0.033	0.376 \pm 0.016	0.055 \pm 0.004	0.037 \pm 0.002	0.029 \pm 0.003
Rosenbrock 10D	GA	0.547	0.800	5.092 \pm 1.371	2.026 \pm 0.930	0.830 \pm 0.133	0.659 \pm 0.106
	(1+1)-ES	0.000	0.000	0.003 \pm 0.000	0.000 \pm 0.000	0.000 \pm 0.000	0.000 \pm 0.000
	AE	0.018	0.082	0.117 \pm 0.033	0.058 \pm 0.022	0.049 \pm 0.019	0.042 \pm 0.018
Rastrigin 10D	GA	1.395	4.347	3.132 \pm 1.245	3.098 \pm 1.232	3.047 \pm 1.284	3.058 \pm 1.234
	(1+1)-ES	37.808	160.187	89.844 \pm 33.520	89.844 \pm 33.520	89.844 \pm 33.520	89.844 \pm 33.520
	AE	0.601	1.277	1.145 \pm 0.327	1.002 \pm 0.275	0.945 \pm 0.209	0.888 \pm 0.203

Table 2: Results for DAGA, (1+1)-ES and the GA on 3 continuous problems. Showing the value of the minimum and maximum solution returned at the end of search, and the mean best solution in the population after 25%, 50%, 75% and 100% of evaluations had been completed, across 10 trials. A 100,000 evaluation limit is used on sphere and 300,000 is used on the other two. On each function results were found to have significant differences on a one way ANOVA ($p < 0.05$), post-hoc analysis with a t-test and the Bonferroni correction for multiple comparisons showed significant differences between all pairs ($p < 0.05$).

reach the optimum after 500,000. On RR, DAGA has a better mean score from the first quarter onwards, but the GA regularly reaches the optimum solution and their scores are not significantly different statistically ($p=0.13$ from 25% to 50%).

5.2 Continuous

Results for DAGA, (1+1)-ES and the GA are presented in for the sphere, Table ?? Rosenbrock and Rastrigin functions. On all three of these problems DAGA outperforms the GA, and is able to reach significantly better solutions with fewer evaluations. However, the (1+1)-ES is considerably better on the sphere and Rosenbrock functions, achieving significantly better solutions in the first quarter of evaluations (25,000 and 75,000 respectively) than DAGA can over the whole run (100,000 and 300,000). This implies that the (1+1)-ES is a much more efficient continuous optimiser on these search spaces. However, the (1+1)-ES performs extremely badly on the Rastrigin, which consists of many local optima. Here, the population-based GA and DAGA excel, getting much closer to the optimal solution of 0. DAGA is significantly better than the GA and the only algorithm to find solutions under 1.0.

5.3 Accumulation of Adaptations

Results for DAGA on the image generation task described in Section 4.3 are presented in Table x. The figure shows the difference in the average number of

	a	b	c	d	e	f	g	h	i	j	k	l	m	n	p
a then p	21.91	33.64	18.82	46.09	10.00	27.82	11.09	84.09	46.27	42.18	43.55	63.45	44.18	53.45	173.64
p then a	117.36	63.18	46.55	65.91	54.45	62.36	44.18	91.55	74.82	61.27	55.91	57.00	72.18	70.36	125.18

Table 3: Showing the difference between mean number of iterations taken to solve the image labelled on the top row without pre-learning and the mean number of iterations taken with pre learning on the two solutions labelled in the first column, averaged over 10 trials. All mean iterations are significantly different, Wilcoxon Rank Sum test ($p < 0.05$). NOTE: MISSING O!!!!

iterations taken to solve the third problem, between solving the third problem directly and solving it after using a dA that has been trained on solving the first two problems without reinitialisation. We see that in every case, there is a significant speed up when DAGA solves the first two problems before solving the third. Figure 4(a) shows the population created by sampling random inputs after solving the Cross and Box problems, while Figure 4(b) shows the same without training. There is a clear difference in the solutions created, with the dA after training showing box-like pattern, mixed with diagonals. This shows that it has learnt from both training patterns, and the large speed ups on the third task shows that is exploited to solve the latter problem considerably faster. Unsurprisingly, the largest speed ups occur when the third problem is identical to the second. For both initial training patterns, this speedup is considerably greater than the mean, although it is markedly greater on the Box-Cross (BC) set. Also notable on BC is that the speed up is much less on the Box pattern, even though it was solved in the first run of the algorithm. By training on the Cross pattern second, we may lose a lot of the information learnt from the first run. On BC, apart from the Cross, the most speed up is seen in solutions which inherit 1/4 from the Box and 3/4 from the Cross. The reverse is not true, and for CB there are large savings on the Cross, which it was trained on initially as well as the 1/4Box, 3/4Cross solution that BC performs well on. Figure 4 (b) and (c) shows that while BC and CB both share features of the two root patterns, they are dominated by the second trained pattern. The Cross patterns are more sparse, which could explain why it takes longer to produce a Box. In order to reduce the memory effect, it may help to use a lower learning rate. However, this simple example illustrates that dAGA is able to transfer learned structure between tasks.

6 Discussion

The results from Section 5 show that the dA can be applied to both discrete and continuous problems and regularly outperforms a GA, either in the quality of the final solution or in the number of evaluations used. The advantages over the GA are most clear on difficult combinatorial problems such as the 256-bit HIFF and MAXSAT, where the GA struggles to locate optimal solutions. On these problems, the best dAGA parameters found through a grid search displayed a

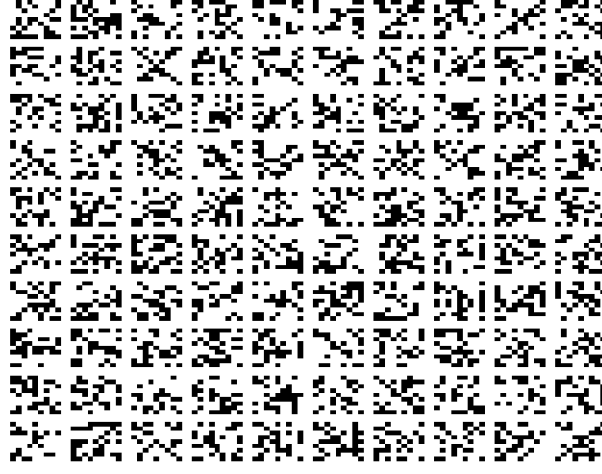


Fig. 3: Showing the difference between mean number of iterations taken to solve the image pictured on the top row without pre-learning and the mean number of iterations taken with pre learning on the two solutions pictured in the first column, averaged over 10 trials.

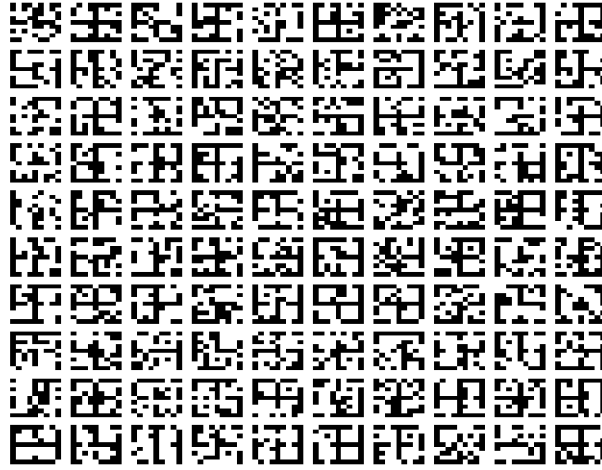
very low corruption level (0.01 for MAXSAT and 0.05 for 256-HIFF) and large population sizes (2,500 and 5,000). As seen in Fig. 1 the low corruption level maintains variance in the population, maximising the amount of information in the data pool and preventing premature convergence. Conversely, on problems such as the Knapsack and Royal Road, a large corruption level is used. This implies that on problems with more independence between input components, a high corruption level can more quickly direct search towards desired regions.

While dAGA outperformed the GA on all three parameter optimisation problems, it was outperformed by a (1+1)-ES on two. There are several improvements that could be made, one of which is the sampling method, which uses a fixed σ^2 . Using an adaptive step-size, such as the Evolutionary path length method used in population-based Evolutionary Strategies could have a positive effect on convergence. To solve the continuous problems, dAGA was found to need a large hidden layer, a factor of 2.5 or greater than the input size. Continuous search spaces are much larger than discrete ones and the dA will need a high capacity in order to effectively capture solution structure. This was also found on the 256-bit HIFF, which used 500 hidden neurons. While this could lead to overfitting on the solution set, this can be offset by the corruption applied to the inputs, which acts as a strong regulariser. There is the potential that results could be improved through deeper architectures for the dA, which could capture a hierarchical composition of features, which a shallow architecture cannot. At present we have been unable to successfully apply the algorithm to non-trivial continuous problems with more than 10 dimensions. Further work is needed to determine what architectures can support this added complexity.

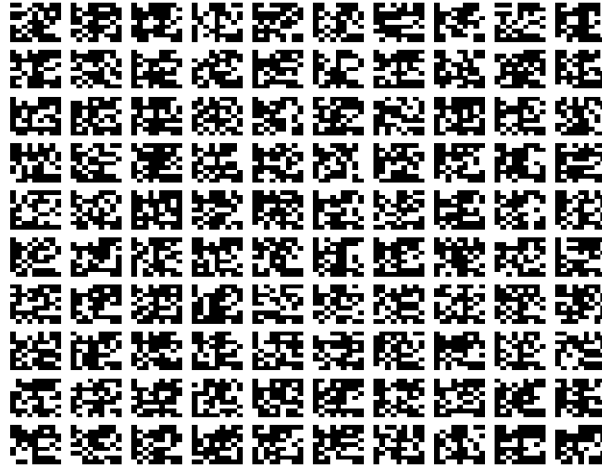
The image generation task poses an interesting question that has not been answered by the EDA community - can building a model to solve one task help improve performance on another? The results showed that using a dA, information learnt in one task can be retained and recombined with that learnt in a second task to produce an across the board speed up on the third task in the sequence. This shows the potential for using a dA, but also potentially other modelling techniques from the optimisation community, such as Restricted Boltzmann Machines or Deep Belief Networks, for transfer learning between problems of the same class. Careful experimentation is needed to discover which types of



(a)



(b)



(c)

Fig. 4: Showing the output of 100 random inputs passed through the autoencoder

problem can use machine learning techniques to transfer knowledge between unique instances and speed up optimisation as more examples are encountered.

7 Conclusion

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