

177. Stabpendel mit Kugeln

$$\begin{array}{lll}
 L = 0.3 \text{ m}; & r_1 = 0.02 \text{ m}; & r_2 = 0.03 \text{ m} \\
 m_0 = 0.1 \text{ kg}; & m_1 = 0.1 \text{ kg}; & m_2 = 0.3 \text{ kg}
 \end{array}$$

$$\text{a) } I_{ges} = I_{Stab} + I_{Kugel1} + I_{Kugel2}$$

$$I_{Stab} = \frac{1}{12} m_0 L^2 = 7.5 * 10^{-4} \text{ kg m}^2$$

$$I_{Kugel1} = \frac{2}{5} m_1 r_1^2 + m_1 \left(\frac{L}{2} + r_1 \right)^2 = 2.9 * 10^{-3} \text{ kg m}^2$$

$$I_{Kugel2} = \frac{2}{5} m_2 r_2^2 + m_2 \left(\frac{L}{2} + r_2 \right)^2 = 9.8 * 10^{-3} \text{ kg m}^2$$

$$\Rightarrow I_{ges} = \underline{\underline{1.3 * 10^{-2} \text{ kg m}^2}}$$

b)

$$x_{Stab_{sp}} = 0 \text{ m}$$

$$x_{Kugeln_{sp}} = \frac{m_1 \left(-\frac{2r_1+L}{2} \right) + m_2 \left(\frac{2r_2+L}{2} \right)}{m_1 + m_2} = 0.0925 \text{ m}$$

$$x_{sp} = \frac{x_{Stab_{sp}} * m_0 + x_{Kugeln_{sp}} * (m_1 + m_2)}{m_0 + m_1 + m_2} = \underline{\underline{0.074 \text{ m}}}$$

$$\text{c) } T = 2\pi \sqrt{\frac{I}{Mgl}}$$

$$\begin{aligned}
 T &= 2\pi \sqrt{\frac{I}{(m_0 + m_1 + m_2) g \left(\frac{2r_2+L}{2} \right)}} \\
 &= \underline{\underline{0.77 \text{ s}}}
 \end{aligned}$$