177. Stabpendel mit Kugeln

$$L=0.3 \; {
m m}; \qquad r_1=0.02 \; {
m m}; \qquad r_2=0.03 \; {
m m}$$
 $m_0=0.1 \; {
m kg}; \qquad m_1=0.1 \; {
m kg}; \qquad m_2=0.3 \; {
m kg}$

a)
$$I_{ges} = I_{Stab} + I_{Kugel_1} + I_{Kugel_2}$$

$$\begin{split} I_{Stab} &= \tfrac{1}{12} m_0 L^2 = 7.5 * 10^{-4} \text{ kg m}^2 \\ I_{Kugel_1} &= \tfrac{2}{5} m_1 r_1^2 + m_1 (\tfrac{L}{2} + r_1) = 2.9 * 10^{-3} \text{ kg m}^2 \\ I_{Kugel_2} &= \tfrac{2}{5} m_2 r_2^2 + m_2 (\tfrac{L}{2} + r_2) = 9.8 * 10^{-3} \text{ kg m}^2 \\ \Rightarrow I_{ges} &= \underline{1.3 * 10^{-2} \text{ kg m}^2} \end{split}$$

b)

$$x_{Stab_{sp}} = 0 \text{ m}$$

$$x_{Kugeln_{sp}} = \frac{m_1 \left(-\frac{2r_1 + L}{2}\right) + m_2 \left(\frac{2r_2 + L}{2}\right)}{m_1 + m_2} = 0.0925 \text{ m}$$

$$x_{sp} = \frac{x_{Stab_{sp}} * m_0 + x_{Kugeln_{sp}} * (m_1 + m_2)}{m_0 + m_1 + m_2} = \underline{0.074} \text{ m}$$

c)
$$I = \sqrt{\frac{I}{(m_0 + m_1 + m_2) g\left(\frac{2r_2 + L}{2}\right)}}$$