

Ex.1

```
ClearAll["Global`*"]
```

```
T1 := UnitConvert[85 °C, "K"]
```

```
T2 := UnitConvert[20 °C, "K"]
```

```
Cv := 4.18 kJ/(kg K); m := 200 g
```

```
ΔSKaffee = UnitConvert[Integrate[m * Cv / T, {T, T1, T2}], "KJ/K"]
```

Out[11]=

-0.167424 kJ/K

```
In[ ]:= ΔSRaum = UnitConvert[Integrate[-m * Cv / T2, {T, T1, T2}], "KJ/K"]
```

Out[]= 0.185366 kJ/K

```
In[ ]:= ΔSUniversum = ΔSRaum + ΔSKaffee
```

Out[]= 0.0179422 kJ/K

```
In[ ]:= ClearAll["Global`*"]
```

```
ΔSUniversum =
```

```
Integrate[-m * Cv / T2, {T, T1, T2}] + Integrate[m * Cv / T, T] - Integrate[m * Cv / t, t] ≥ 0 /.  
{T → T1, t → T2} // FullSimplify
```

Out[]=
$$\frac{Cv m (T1 - T2 + T2 \log[T1] - T2 \log[T2])}{T2} \geq 0$$

ΔS=0, weil es reversibel ist.

Ex.2

```
In[ ]:= ClearAll["Global`*"]
S := kB * (3 n / 2 Log[e / n] + n Log[V / n] + n Log[c])
Eges = Solve[T == 1 / D[S, e], e][[1]][1]
p * V == T D[S, V] * V
μ == -T D[S, n]
```

$$\text{Out[]}= e \rightarrow \frac{3 \text{ kB } n \text{ T}}{2}$$

$$\text{Out[]}= p \text{ V} == \text{ kB } n \text{ T}$$

$$\text{Out[]}= \mu == -\text{ kB } T \left(-\frac{5}{2} + \text{Log}[c] + \frac{3}{2} \text{Log}\left[\frac{e}{n}\right] + \text{Log}\left[\frac{V}{n}\right] \right)$$

```
In[ ]:= T := 300 K
```

```
p1 := 1 bar
```

```
V1 := 1 m^3
```

```
V2 := 2 m^3
```

```
kB := k
```

```
n := p1 * V1 / (T * kB) // N
p2 = UnitConvert[n * kB * T / V2, "bar"]
e1 = UnitConvert[Eges[[2]], "eV"]
e2 = UnitConvert[Eges[[2]], "eV"]
```

$$\text{Out[]}= 0.5 \text{ bar}$$

$$\text{Out[]}= 9.36226 \times 10^{23} \text{ eV}$$

$$\text{Out[]}= 9.36226 \times 10^{23} \text{ eV}$$

```

In[ ]:=  $\mu_1 = -k_B T \left( -\frac{5}{2} + \frac{3}{2} \log\left[\frac{e_1}{n}\right] + \log\left[\frac{V_1}{n}\right] \right)$ 
 $\mu_2 = -k_B T \left( -\frac{5}{2} + \frac{3}{2} \log\left[\frac{e_2}{n}\right] + \log\left[\frac{V_2}{n}\right] \right)$ 
(*Einheiten im Log ???*)

Out[ ]:=  $\left( -\frac{5}{2} + \log[4.14195 \times 10^{-26} \text{ m}^3] + \frac{3}{2} \log[0.038778 \text{ eV}] \right) (-300 \text{ K k})$ 

Out[ ]:=  $\left( -\frac{5}{2} + \log[8.28389 \times 10^{-26} \text{ m}^3] + \frac{3}{2} \log[0.038778 \text{ eV}] \right) (-300 \text{ K k})$ 

```

Ex.3 Isotherme expansion

```

ClearAll["Global`*"]

kB :=  ☒; T1 :=  ☐ ☒; V1 :=  ☐ ☒; V2 := 2 V1

p :=  ☐ ☒; n := V1 p / (T1  ☐ ☒); Cp := 7/2  ☐ ☒

T2 := 2 T1

In[ ]:=  $\Delta U = \text{UnitConvert}[n * Cp * (T2 - T1), "J"]$ 
 $\Delta S = \text{UnitConvert}[$ 
     $\text{Integrate}[n * Cp / T, \{T, T1, T2\}] + \text{Integrate}[n  ☐ ☒ / V, \{V, V1, V2\}], "J/K"] // N$ 
 $\Delta W = \text{UnitConvert}[-\text{Integrate}[p, \{V, V1, V2\}], "J"]$ 
 $\Delta Q = \Delta U - \Delta W$ 

Out[ ]:= 350 J

Out[ ]:= 1.03972 J/K

Out[ ]:= -100 J

Out[ ]:= 450 J

```

```
In[ ]:= T2 := T1
ΔU = UnitConvert[n * Cp * (T2 - T1), "J"]
ΔS = UnitConvert[Integrate[n * R / V, {V, V1, V2}], "J/K"] // N
```

Out[]:= 0 J

Out[]:= 0.231049 J/K

```
In[ ]:= d := 1 mm ; A := 0.01 m^2 ; F := 200 N
```

ΔQ := 0

```
In[ ]:= ΔW = UnitConvert[F * d, "J"]
ΔU = ΔW + ΔQ
ΔT = UnitConvert[ΔU / (Cp * n)] // N
```

Out[]:= $\frac{1}{5}$ J

Out[]:= $\frac{1}{5}$ J

Out[]:= 0.171429 K

ΔS > 0, weil der Prozess irreversibel ist.

Ex. 4

```
In[ ]:= Na := N_A ; k := k
```

S[options_] := UnitConvert[k * Na * Log[options], "J/K/mol"] // N

```
In[ ]:= S[2]
S[6 / 4]
S[5]
```

Out[]:= 5.76315 J/(K mol)

Out[]:= 3.37122 J/(K mol)

Out[]:= 13.3816 J/(K mol)

Bonus

