Millikan-Versuch

$$\eta = 18.6 \times 10^{-6} \text{ Pas}; \quad \rho_{air} = 1.16 \text{ kg/m}^3; \quad \rho_{oil} = 900 \text{ kg/m}^3$$

a)
$$v = 3.7 \times 10^{-6} \text{ m/s}$$

$$F_{\rm g} = Vg\rho_{\rm oil} = \frac{4}{3}r^3\pi g\rho_{\rm oil}$$

$$F_{\rm R} = a\eta v = 6\pi r \eta v$$

$$F_{\rm A} = Vg\rho_{\rm air} = \frac{4}{3}r^3\pi g\rho_{\rm air}$$

$$F_{\text{tot}} = F_{\text{g}} - F_{\text{A}} - F_{\text{R}} = 0$$

$$r = \sqrt{\frac{9\eta v}{2g(\rho_{\text{oil}} - \rho_{\text{air}})}} = \underline{1.88 \times 10^{-7} \text{ m}}$$

b)
$$E = 500 \text{ V/m}: v = 0 \text{ m/s}$$

$$F_{\rm el} = qE$$

$$F_{\text{tot}} = F_{\text{g}} - F_{\text{A}} - F_{\text{R}} - F_{\text{el}}$$

$$q = \frac{2\pi r \left(2gr^2(\rho_{\text{air}} - \rho_{\text{oil}}) + 9\eta v\right)}{3E} = \underline{4.86 \times 10^{-19} \text{ C}}$$

c)

Massenspektrograph - Parabelmethode

a)
$$T := \frac{l}{v_z}$$

$$F_E = qE = m \frac{dv_y}{dt}$$

$$v_y(t) = \frac{qE}{m}t$$

$$v_y(T) = \frac{qEl}{mv_z}$$

$$F_B = qv_z B = m \frac{dv_x}{dt}$$

$$v_x(t) = \frac{qB}{m}v_z t$$

$$v_x(T) = \frac{qBl}{m}$$

$$A_E = \int_0^T v_y(t) dt = \frac{qEl^2}{2mv_z^2}$$

$$A_B = \int_0^T v_x(t) dt = \frac{qBl^2}{2mv_z}$$

b)
$$\tau = \frac{D}{v_z}$$

$$y = A_E + v_y(T)\tau = \frac{qEl}{mv_z^2} \left(\frac{l}{2} + D\right)$$

$$x = A_B + v_x(T)\tau = \frac{qBl}{mv_z} \left(\frac{l}{2} + D\right)$$

$$v_z = \frac{qBl\left(\frac{l}{2} + D\right)}{mx}$$

$$y(x) = \frac{mE}{qB^2l\left(\frac{l}{2} + D\right)}x^2$$

c)
$$x = 0.05 \text{ m}$$
; $D = 0.4 \text{ m}$; $l = 0.03 \text{ m}$; $a = 1.5 \text{ mm}$; $\Delta m = 2 \text{ u}$
 $U = 15 \text{ V}$; $B = 0.1 \text{ T}$

$$\Delta y = \frac{\Delta mE}{qB^2l\left(\frac{l}{2} + D\right)}x^2 = \underline{0.004 \text{ m}}$$

Gruppengeschwindigkeit eines freien Teilchens

- a) The group velocity of a wave is the velocity of the enveloping wave, whereas the phase velocity is the speed the the inscribed wave travels through space.
- b) Dispersion relation gives the relationship between the speed and the frequency of a wave. dispersion usually happens when waves go from one medium into another and there a change in speed happens. Electromagnetic waves in vacuum don't show dispersion because it always travels in the same medium and the frequency of em-waves does not depend on its speed. Matter waves however do have a speed dependent frequency and therefore do experience dispersion.

c)

d)