132. Freier Fall einer rotierenden Hantel

$$m_1 = 1 \text{ kg};$$

$$m_1 = 1 \text{ kg};$$
 $\vec{v}_1 = (4, 0, 0) \text{ m/s};$ $\vec{r}_1 = (0, 0, 2.5) \text{ m}$ $m_2 = 0.5 \text{ kg};$ $\vec{v}_2 = (1, 0, 0) \text{ m/s};$ $\vec{r}_2 = (0, 0, 2.2) \text{ m}$

$$\vec{r}_1 = (0, 0, 2.5)$$
 m

$$m_2 = 0.5 \text{ kg};$$

$$\vec{v}_2 = (1, 0, 0)$$
 m/s;

$$\vec{r}_2 = (0, 0, 2.2)$$
 m

$$\vec{r}_{sp} = \frac{m_1 r_1 + m_2 r_2}{m_1 + m_2} = \begin{pmatrix} 0\\0\\2.4 \text{ m} \end{pmatrix}$$

a) Im bewegten Bezugssystem, das sich mit 3 m/s mitbewegt reine Rotation

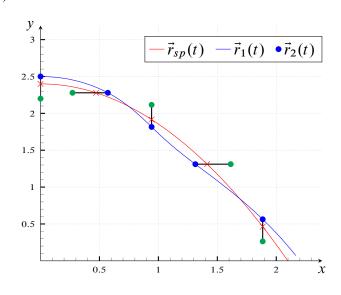
$$\Rightarrow \vec{r}_{sp}(t) = \begin{pmatrix} 0 \\ 0 \\ 2.4 \text{ m} \end{pmatrix} + \begin{pmatrix} 3 \text{ m/s} \\ 0 \\ 0 \end{pmatrix} t + \frac{1}{2} \begin{pmatrix} 0 \\ 0 \\ -9.81 \text{ m/s}^2 \end{pmatrix} t^2$$

b) Im bewegten Bezugssystem: $\vec{v}_1 = (1, 0, 0) \text{ m/s}; \ \vec{v}_1 = (-2, 0, 0) \text{ m/s}$

$$\omega = \frac{|v_1|}{r_1} = \underline{10 \text{ s}^{-1}}$$

$$T = \frac{2\pi}{\omega} = \frac{\pi}{5} = \underline{0.63 \text{ s}}$$

c)



d) Im Schwerpunktsystem:

$$\vec{r}_{1,sp}(t) = 0.1 \begin{pmatrix} \sin(\omega t) \\ 0 \\ \cos(\omega t) \end{pmatrix} \text{ m}$$

$$\vec{r}_{2,sp}(t) = -0.2 \begin{pmatrix} \sin(\omega t) \\ 0 \\ \cos(\omega t) \end{pmatrix}$$
 m

Im Laborsystem:

$$\vec{r}_{1}(t) = \vec{r}_{sp}(t) + \vec{r}_{1,sp}(t)$$

$$= \underbrace{\begin{pmatrix} 0.1\sin(\omega t) \text{ m} \\ 0 \\ 0.1\cos(\omega t) \text{ m} + 2.4 \text{ m} \end{pmatrix}}_{0} + \underbrace{\begin{pmatrix} 3 \text{ m/s} \\ 0 \\ 0 \end{pmatrix}_{t} + \frac{1}{2} \begin{pmatrix} 0 \\ 0 \\ -9.81 \text{ m/s}^{2} \end{pmatrix}_{t^{2}}$$

$$\vec{r}_{2}(t) = \vec{r}_{sp}(t) + \vec{r}_{2,sp}(t)$$

$$= \begin{pmatrix} -0.2\sin(\omega t) \text{ m} \\ 0 \\ -0.2\cos(\omega t) \text{ m} + 2.4 \text{ m} \end{pmatrix} + \begin{pmatrix} 3 \text{ m/s} \\ 0 \\ 0 \end{pmatrix}_{t} + \frac{1}{2} \begin{pmatrix} 0 \\ 0 \\ -9.81 \text{ m/s}^{2} \end{pmatrix}_{t^{2}}$$

140. International Space Station

$$R_E = 6.37 * 10^6 \text{ m}; \quad m = 4.55 * 10^5 \text{ kg}; \quad h = 3.3 * 10^5 \text{ m}$$

a)
$$h = 0 \text{ m}$$

$$F_G = mg \frac{1}{\left(1 + \frac{h}{R_E}\right)^2}$$
= $4.55 * 10^5 \text{ kg} * 9.81 \text{ m/s}^2$

$$F_G = \underline{4.46 * 10^6 \text{ kg m/s}^2}$$

b)
$$h = 3.3 * 10^5 \text{ m}$$

$$F_G = mg \frac{1}{\left(1 + \frac{h}{R_E}\right)^2}$$

$$= 4.55 * 10^5 \text{ kg} * 9.81 \text{ m/s}^2 \frac{1}{\left(1 + \frac{3*10^5 \text{ m}}{6.37*10^6 \text{ m}}\right)}$$

$$F_G = \underbrace{4.03 * 10^6 \text{ kg m/s}^2}_{g(h)}$$

$$g(h) = \frac{g}{\left(1 + \frac{h}{R_E}\right)^2}$$

$$g(3.3 * 10^5) = \underbrace{8.87 \text{ m/s}^2}_{g(h)}$$

$$v = r\omega$$
; $a = \frac{v^2}{r} = r\omega^2$; $r = R_E + h$

$$\omega = \sqrt{\frac{g(h)}{r}}$$

$$= \underline{1.2 * 10^{-3} \text{ s}^{-1}}$$

$$T = \frac{2\pi}{\omega}$$

$$= \underline{5461.58 \text{ s}}$$

$$T = \frac{2\pi}{\omega}$$
$$= \underline{5461.58 \text{ s}}$$

$$v = r\omega$$

= $\frac{7707.91 \text{ m/s}}{}$

152. Komprimierter Metallblock

$$a = h = 0.2 \text{ m}$$

$$\Delta h = 1.3 * 10^{-6} \text{ m}$$
 $m = 500 \text{ kg}$

$$m = 500 \text{ kg}$$

$$V = 8 * 10^{-3} \text{ m}^3$$

$$\Delta V = 3 * 10^{-7} \text{ m}^3$$

$$V = 8 * 10^{-3} \text{ m}^3$$
 $\Delta V = 3 * 10^{-7} \text{ m}^3$ $p = 2 * 10^6 \text{ kg/m s}^2$

a)
$$p = K \frac{\Delta V}{V}$$
; $\frac{F}{A} = E \frac{\Delta h}{a}$

$$K = p \frac{V}{\Delta V}$$

= $\frac{16}{3} * 10^{10} \text{ kg/m s}^2$

$$E = \frac{\frac{mga}{a^2 \Delta h}}{= \underbrace{1.89 * 10^{10} \text{ kg/m s}^2}}$$

b)
$$\Delta a = \mu \Delta h$$
; $K = \frac{E}{3(1-2\mu)}$

$$K = \frac{E}{3(1-2\mu)}$$
$$\frac{3K}{E} = \frac{1}{1-2\mu}$$

$$\mu = \frac{1}{2} - \frac{E}{6K}$$
$$= \underline{0.44}$$

$$\Delta a = \mu \Delta h$$
$$= \underline{5.73 * 10^{-7} \text{ m}}$$