177. Stabpendel mit Kugeln

$$L=0.3 \; {
m m}; \qquad r_1=0.02 \; {
m m}; \qquad r_2=0.03 \; {
m m} \ m_0=0.1 \; {
m kg}; \qquad m_1=0.1 \; {
m kg}; \qquad m_2=0.3 \; {
m kg}$$

a)
$$I_{ges} = I_{Stab} + I_{Kugel_1} + I_{Kugel_2}$$

$$\begin{split} I_{Stab} &= \tfrac{1}{12} m_0 L^2 = 7.5 * 10^{-4} \text{ kg m}^2 \\ I_{Kugel_1} &= \tfrac{2}{5} m_1 r_1^2 + m_1 (\tfrac{L}{2} + r_1) = 2.9 * 10^{-3} \text{ kg m}^2 \\ I_{Kugel_2} &= \tfrac{2}{5} m_2 r_2^2 + m_2 (\tfrac{L}{2} + r_2) = 9.8 * 10^{-3} \text{ kg m}^2 \\ \Rightarrow I_{ges} &= \underline{1.3 * 10^{-2} \text{ kg m}^2} \end{split}$$

b)

$$\begin{split} x_{Stab_{sp}} &= 0 \text{ m} \\ x_{Kugeln_{sp}} &= \frac{m_1(-\frac{2r_1+L}{2}) + m_2(\frac{2r_2+L}{2})}{m_1+m_2} = 0.0925 \text{ m} \\ x_{sp} &= \frac{x_{Stab_{sp}} * m_0 + x_{Kugeln_{sp}} * (m_1+m_2)}{m_0 + m_1 + m_2} = \underline{0.074} \text{ m} \end{split}$$