1. Potentialverlauf einer geladenen Hohlkugel

$$k = \frac{1}{4\pi\epsilon_0}, V = \int\limits_{V_i}^{\infty} \vec{E} \, \mathrm{d}\vec{s}$$

1.
$$E(r) = \begin{cases} 0 & \text{for } 0 < r \le R_i, \\ \frac{kQ}{R_a^3 - R_i^3} \left(r - \frac{R_i^3}{r^2} \right) & \text{for } R_i < r < R_a, \\ kQ \frac{1}{r^2} & \text{for } R_a \le r. \end{cases}$$

For $R_a \leq r$:

$$\begin{split} E(r) &= kQ \, \frac{1}{r^2} \\ V_1(r) &= \int\limits_r^\infty \vec{E}(r) \, \mathrm{d}\vec{r} = kQ \int\limits_r^\infty \, \frac{1}{r^2} \, \mathrm{d}r = kQ \, \frac{1}{R_a} \\ V_1(r) &= kQ \, \frac{1}{r} \end{split}$$

For $R_i < r < R_a$:

$$E(r) = \frac{kQ}{R_a^3 - R_i^3} \left(r - \frac{R_i^3}{r^2} \right)$$

$$V_2(r) = \int_r^{\infty} \vec{E}(r) \, d\vec{r} = kQ \left(\int_r^{R_a} \frac{r^3 - R_i^3}{r^2 (R_a^3 - R_i^3)} \, dr + \int_{R_a}^{\infty} \frac{1}{r^2} \, dr \right) =$$

$$= kQ \left(-\frac{r^3 R_a - r R_a^3 + 2r R_i^3 + 2R_a R_i^3}{2r R_a^4 - 2r R_a R_i^3} + \frac{1}{R_a} \right)$$

$$V_2(r) = -kQ \frac{r^3 - 3rR_a^2 + 2R_i^3}{2rR_a^3 - 2rR_i^3}$$

For $r \leq R_i$:

$$E(r) = 0$$

$$V_3(r) = \int_{r}^{\infty} \vec{E}(r) \, d\vec{r} = kQ \left(\int_{r}^{R_i} 0 \, dr + \int_{R_i}^{\infty} \frac{r^3 - R_i^3}{r^2 (R_a^3 - R_i^3)} \, dr \right) = 0$$

$$V_3(r) = -kQ \frac{3(R_a + R_i)}{2(R_a^2 + R_a R_i + R_i^2)}$$

$$V(r) = \begin{cases} -kQ \frac{3(R_a + R_i)}{2(R_a^2 + R_a R_i + R_i^2)} & \text{for } 0 < r \le R_i, \\ -kQ \frac{r^3 - 3rR_a^2 + 2R_i^3}{2rR_a^3 - 2rR_i^3} & \text{for } R_i < r < R_a, \\ kQ \frac{1}{r} & \text{for } R_a \le r. \end{cases}$$

3. Elektrische Ladung zwischen Kugelladungen

$$k = \frac{1}{4\pi\epsilon_0}, V = \int_{V_i}^{\infty} \vec{E} \, d\vec{s}$$

1.

$$F = \vec{E}_2(r) * q = k \frac{qQ}{(9.5d)^2}$$