

$$1) z_1 = 5 + 2i$$

$$z_1 = \sqrt{29} \left(\cos(\arctan(\frac{2}{5})) + i \sin(\arctan(\frac{2}{5})) \right)$$

$$z_1 = \sqrt{29} e^{i \arctan(\frac{2}{5})}$$

$$z_2 = -3 + i$$

$$z_2 = \sqrt{10} \left(\cos(\arctan(\frac{1}{3}) + \pi) + i \sin(\arctan(\frac{1}{3}) + \pi) \right)$$

$$z_2 = \sqrt{10} e^{i(\arctan(\frac{1}{3}) + \pi)}$$

$$z_3 = -6 - 3i$$

$$z_3 = \sqrt{45} \left(\cos(\arctan(\frac{1}{2}) + \pi) + i \sin(\arctan(\frac{1}{2}) + \pi) \right)$$

$$z_3 = \sqrt{45} e^{i(\arctan(\frac{1}{2}) + \pi)}$$

$$z_4 = 4 - 2i$$

$$z_4 = \sqrt{20} \left(\cos(\arctan(\frac{1}{2}) + 2\pi) + i \sin(\arctan(\frac{1}{2}) + 2\pi) \right)$$

$$z_4 = \sqrt{20} e^{i(\arctan(\frac{1}{2}) + 2\pi)}$$

$$2) a) z_1 = 2.5 - 1.5i$$

$$|z_1| = \sqrt{2.5^2 + 1.5^2} \approx \underline{\underline{2.92}}$$

$$z_2 = i z_1 = 1.5 + 2.5i$$

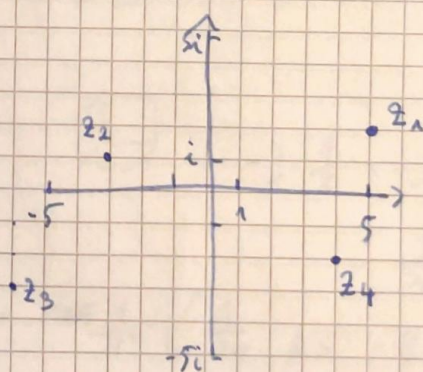
$$|z_2| = \cancel{|z_1|} |z_1| \approx \underline{\underline{2.92}}$$

$$z_3 = z_1^2 = 2.5^2 - 1.5^2$$

$$|z_3| = \cancel{|z_1|}^2 |z_1|^2 = 8.5$$

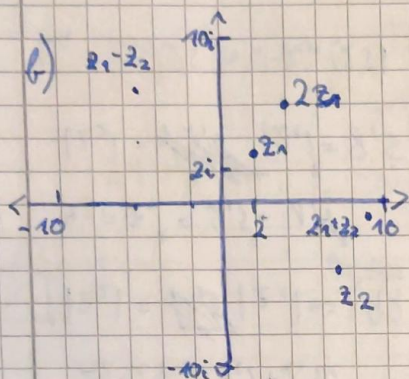
$$z_4 = \cos(25) + i \sin(25)$$

$$|z_4| = \underline{\underline{1}}$$



$$3) z_1 = 2 + 3i, \quad z_2 = 7 - 4i$$

$$a) z_1 + z_2 = \underline{9 + i} \quad z_1 - z_2 = \underline{-5 + 7i} \quad z_2 = \underline{4 + 6i}$$



$$c) z_1 z_2 = 14 + 21i - 8i - 12 = \underline{2 + 13i}$$

$$z_1 \bar{z}_2 = 14 + 21i + 8i - 12 = \underline{2 + 29i}$$

$$z_2 \bar{z}_2 = 49 + 16 = \underline{65}$$

$$z_1 / z_2 = \frac{z_1 \bar{z}_2}{z_2 \bar{z}_2} = \frac{2}{65} + \frac{29}{65}i$$

$$|z_2| = \sqrt{65} \approx \underline{8.06}$$

$$4) \frac{(4 - 5i)z - 12 + 3i}{i} = 1 - 6i \quad | \cdot i = 3i + 12$$

$$(4 - 5i)z = \frac{6 + 18 - 2i}{4 - 5i} \cdot \frac{4 + 5i}{4 + 5i}$$

$$z = \frac{8 + 12i}{41} = \underline{2 + 2i}$$

$$5) R_A = 60 \Omega \quad R_C = -50i \Omega \quad R_L = 70i \Omega$$

$$\text{Series: } R = 60 + 20i \Omega \quad |R| = \sqrt{4000} = \underline{20\sqrt{10} \approx 63.24 \Omega}$$

$$\text{Parallel: } \frac{1}{R} = \frac{1}{60} + \frac{1}{20i} - \frac{1}{30i} - \frac{1}{R} = \frac{3500i + 3000i + 4200i}{60 \cdot 70i \cdot 50i} = \underline{13i}$$

$$\frac{1}{R} = \frac{1}{60} + \frac{1}{175i} \quad \frac{35 + 12i}{2100} \Rightarrow R = \frac{2100}{35 + 12i} \approx \underline{53.68 + 18.4i}$$

$$|R| = \sqrt{35^2 + 12^2} \approx \underline{56.74 \Omega}$$

$$\text{Series: } I = \frac{220}{63.24} = \underline{3.47 A}$$

$$\text{Parallel: } I = \frac{220}{56.74} = \underline{3.87 A}$$