periodogram

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Showcasing periodogram(): estimate the spectral density of a time series

The spectral density of a stationary process shows how the variance of the time series is distributed over different frequencies. As a fundamental tool of time series analysis, the periodogram function is used to estimate the spectral density of a stationary time series.

Example 1: Basic Usage of the Function

First, generate some random time series data to work with:

```
devtools::load_all()
set.seed(123)
X <- rnorm(100)</pre>
```

Next, select a numerical value from the interval $(-\pi, \pi]$, which represents the frequency at which the periodogram is evaluated:

```
lambda <- pi / 4
```

Now, calculate the periodogram for the time series with the specified frequency:

```
periodogram(X, lambda)
```

Warning in periodogram(X, lambda): Please note: This function works for stationary time series with a ## For any other time series, the results may be incorrect.

```
## [1] 1.392404
```

What is happening inside the function:

- Input Validation: The function checks whether the time series X has been passed in the correct format and lambda is a numerical value from the interval $(-\pi, \pi]$.
- Each value X_t of the time series X is multiplied by $e^{-it\lambda}$, where t is the time index.
- The sum of these products is computed.
- The absolute value of this sum is calculated and raised to the power of 2.
- The result is divided by the length of the time series n and returned as the periodogram value.

Example 2: Periodogram for a Simple Sine Curve

Create a simple sine curve sample:

```
X <- sin(2 * pi * 1:100 / 100)
```

Define the frequency of the sine curve:

```
lambda <- 2 * pi / 100
```

Compute the periodogram:

```
periodogram(X, lambda)
```

Warning in periodogram(X, lambda): Please note: This function works for stationary time series with the for any other time series, the results may be incorrect.

[1] 25

Example 3: Periodogram for a Complex Exponential Curve

Generate a complex exponential curve sample:

```
X <- exp(2 * pi * 1i * 1:100 / 100)
```

Set the frequency of the complex exponential:

```
lambda <- 2 * pi / 100
```

Compute the periodogram:

```
periodogram(X, lambda)
```

Warning in periodogram(X, lambda): Please note: This function works for stationary time series with a ## For any other time series, the results may be incorrect.

[1] 100

Example 4: Incorrect inputs

If the input do not correspond to the correct format, appropriate error messages are printed to inform the user what is wrong with their input. Here are several examples of how incorrect inputs are handled:

The time series data must be passed in an atomic vector:

```
X <- list(1, 2, 3, 4, 5)
lambda <- pi / 2
periodogram(X, lambda)</pre>
```

Error in periodogram(X, lambda): X must be an atomic vector

The values of this atomic vector must be numeric or complex:

```
X <- c(1, 2, "3", 4, "5i")
lambda <- pi / 2
periodogram(X, lambda)</pre>
```

Error in periodogram(X, lambda): The values of X must be numeric or complex

In addition, the atomic vector may not contain any NAs:

```
X <- c(1, NA, 2, 3, NA, 5)
lambda <- pi / 2
periodogram(X, lambda)</pre>
```

Error in periodogram(X, lambda): X may not contain NAs

The lambda parameter must be a numerical value:

```
X <- 1:10
lambda <- "0"
```

```
periodogram(X, lambda)

## Error in periodogram(X, lambda): lambda must be numeric

Also lambda must lie within the interval (-\pi,\pi]:

X <- 1:10

lambda <- 2 * pi

periodogram(X, lambda)

## Error in periodogram(X, lambda): lambda must be from the interval (-pi, pi]
```