Name:			
Did.			

1. (10 points) Let $m_1, n_1, m_2, n_2 \in \mathbb{N}$, we say that $(m_1, n_1) \leq (m_2, n_2)$ iff either $m_1 < m_2$ or $m_1 = m_2$ and $n_1 < n_2$.

Let P(m,n) be some property of pairs of integers. Assume that we can prove the following statement for all $m,n\in\mathbb{N}$:

if P(x,y) is true for all $x,y \in \mathbb{N}$ such that (x,y) < (m,n), then P(m,n) is true.

Show that we can prove that P(m, n) is true for all $m, n \in \mathbb{N}$.

2. (10 points) In the subtraction game where players may subtract 1, 2 or 5 chips on their turn, identify the N- and P-positions.