

Name: \_\_\_\_\_

Pid: \_\_\_\_\_

1. (10 points) Let  $S \subseteq \mathbb{N}$  be a nonempty set. Show that  $S$  is decidable iff there is a function  $f : \mathbb{N} \rightarrow \mathbb{N}$  such that  $f$  is computable,  $f$  is nondecreasing, and  $\text{Im } f = S$ .

2. (10 points) Let  $A, B \subseteq \mathbb{N}$  be enumerable sets. Show that  $A \times B$  is enumerable.