Introduction to **Audio Content Analysis**

module 3.5: instantaneous features

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corresponding textbook section

section 3.5

- **lecture content**
  - introduction to the concept of features
  - timbre
  - spectral shape instantaneous features

- **learning objectives**
  - describe the process of feature extraction
  - list possible pre-processing option and explain potential use cases
  - describe the general impact of spectral shape on timbre perception
  - summarize features, describe their computation, and discuss their meaning

corresponding textbook section

section 3.5

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instantaneous features

introduction

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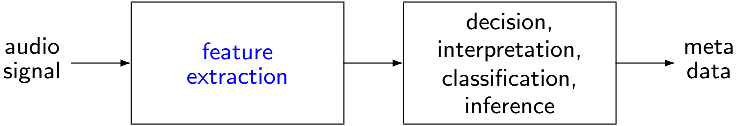
remember the flow chart of a general ACA system:



feature:

- *terminology:*
  - audio descriptor
  - instantaneous/short-term/low-level feature
- *characteristics:*
  - not necessarily musically, perceptually, or semantically meaningful
  - low-level: usually one value per block

instantaneous features

introduction

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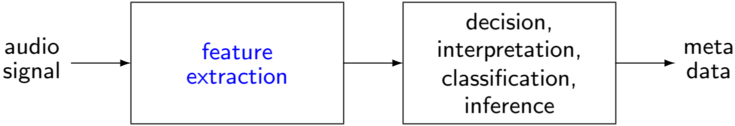

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instantaneous features
introduction

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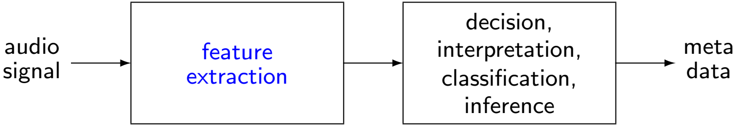

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instantaneous features

feature

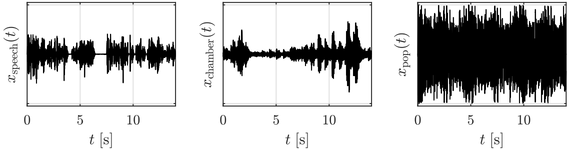
a feature ...

- is task-specific, i.e. holds descriptive power relevant to the task,
- may be custom-designed, chosen from a set of established features, or learned from data,
- can be a representation of any data (audio, meta data, other features, ...),
- is not necessarily musically, perceptually, or semantically meaningful or interpretable
- also: non-redundant, invariant to irrelevancies

instantaneous features

feature example

waveform envelope of three different signals



- envelopes of waveforms can have distinct shape

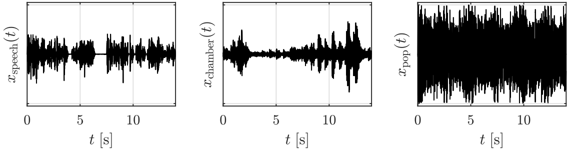
⇒ a feature describing envelope shape could help to distinguish these signal types

matlab source: plotWaveform.m

instantaneous features

feature example

waveform envelope of three different signals



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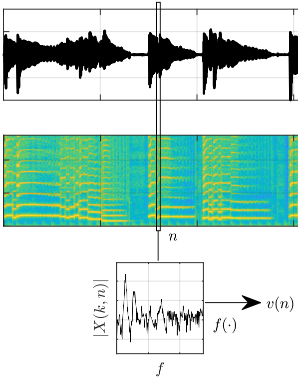
matlab source: plotWaveform.m

instantaneous features
feature extraction



- repeat for every block
- repeat for every feature: *Spectral Centroid*, *RMS*, *MFCCs*, ...

$\Rightarrow$ feature matrix per audio input

matlab source: plotFeatureExtraction.m

timbre

introduction 1/2

definition (American Standards Association)

...that attribute of sensation in terms of which a listener can judge that two sounds having the same loudness and pitch are dissimilar

What is the problem with this definition?

[1] A. S. Bregman, *Auditory Scene Analysis*. MIT Press, 1994.

[2] S. McAdams and A. Bregman, "Hearing Musical Streams," *Computer Music Journal*, vol. 3, no. 4, pp. 26–60, Dec. 1979, ISSN: 0148-9267.

timbre

introduction 1/2

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timbre

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→ [timbre is] "*...the psychoacoustician's multidimensional waste-basket category for everything that cannot be labeled pitch or loudness.*"[2]

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timbre
introduction 2/2

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timbre is

- a function of **temporal envelope**
    - attack time characteristics
    - amplitude modulations
    - ...
- a function of **spectral distribution**
    - spectral envelope
    - number of partials
    - energy distribution of partials
    - ...

when dealing with complex mixtures of sound, it is very difficult (maybe impossible?) to extract detailed temporal information for individual tones

⇒ timbre features typically focus on the **spectral shape**

timbre
introduction 2/2

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timbre
introduction 2/2

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timbre

introduction 2/2

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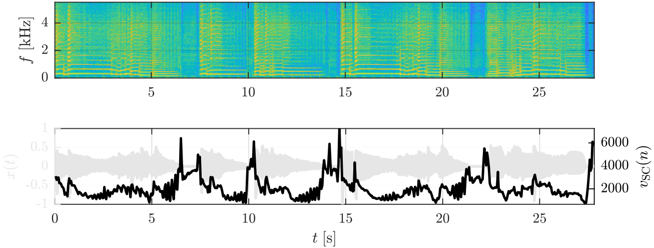
when dealing with complex mixtures of sound, it is very difficult (maybe impossible?) to extract detailed temporal information for individual tones

$\Rightarrow$ timbre features typically focus on the **spectral shape**

spectral shape features

spectral centroid

$$v_{\mathrm{SC}}(n) = \frac{\sum\limits_{k=0}^{\mathcal{K}/2} k \cdot |X(k,n)|}{\sum\limits_{k=0}^{\mathcal{K}/2} |X(k,n)|}$$



matlab source: plotFeatures.m

spectral shape features

spectral centroid

$$v_{\mathrm{SC}}(n) = \frac{\sum\limits_{k=0}^{\mathcal{K}/2} k \cdot |X(k,n)|}{\sum\limits_{k=0}^{\mathcal{K}/2} |X(k,n)|}$$

common variants:

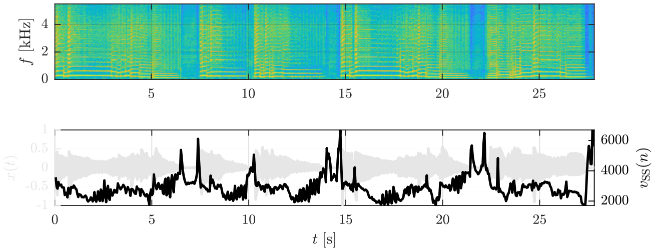
- power spectrum
- logarithmic frequency scale

$$v_{\mathrm{SC,log}}(n) = \frac{\sum\limits_{k=k(f_{\mathrm{min}})}^{\mathcal{K}/2-1} \log_2\left(\frac{f(k)}{f_{\mathrm{ref}}}\right) \cdot |X(k,n)|^2}{\sum\limits_{k=k(f_{\mathrm{min}})}^{N/2-1} |X(k,n)|^2}$$

spectral shape features

spectral spread

$$v_{\mathrm{SS}}(n) = \sqrt{\frac{\sum\limits_{k=0}^{\mathcal{K}/2} \left(k - v_{\mathrm{SC}}(n)\right)^2 \cdot |X(k,n)|}{\sum\limits_{k=0}^{\mathcal{K}/2} |X(k,n)|}}$$



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spectral shape features

spectral spread

$$v_{\mathrm{SS}}(n) = \sqrt{\frac{\sum\limits_{k=0}^{\mathcal{K}/2} \left(k - v_{\mathrm{SC}}(n)\right)^2 \cdot |X(k,n)|}{\sum\limits_{k=0}^{\mathcal{K}/2} |X(k,n)|}}$$

common variants:

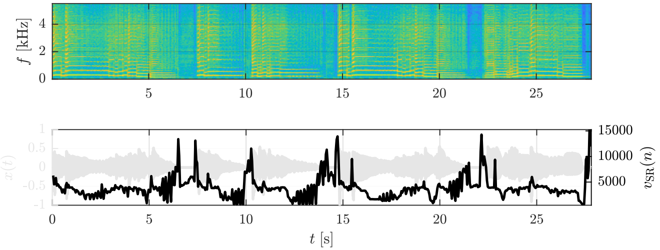
- same variants as with *Spectral Centroid*, e.g. logarithmic:

$$v_{\mathrm{SS,log}}(n) = \sqrt{\frac{\sum\limits_{k=k(f_{\mathrm{min}})}^{\mathcal{K}/2-1} \left(\log_2\left(\frac{f(k)}{1000\,\mathrm{Hz}}\right) - v_{\mathrm{SC}}(n)\right)^2 \cdot |X(k,n)|^2}{\sum\limits_{k=k(f_{\mathrm{min}})}^{\mathcal{K}/2-1} |X(k,n)|^2}}$$

spectral shape features

spectral rolloff

$$v_{\mathrm{SR}}(n) = k_{\mathrm{r}} \Bigg|_{\sum\limits_{k=0}^{k_{\mathrm{r}}} |X(k,n)| = \kappa \cdot \sum\limits_{k=0}^{\mathcal{K}/2} |X(k,n)|}$$



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spectral shape features

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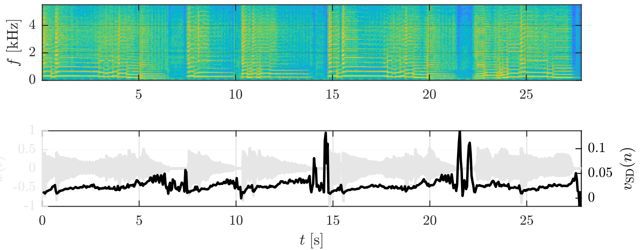
common variants:

- scaled to frequency
- power spectrum

spectral shape features

spectral decrease

$$v_{\mathrm{SD}}(n) = \frac{\sum\limits_{k=1}^{\mathcal{K}/2} \frac{1}{k} \cdot \left(|X(k,n)| - |X(0,n)|\right)}{\sum\limits_{k=1}^{\mathcal{K}/2} |X(k,n)|}$$



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spectral shape features

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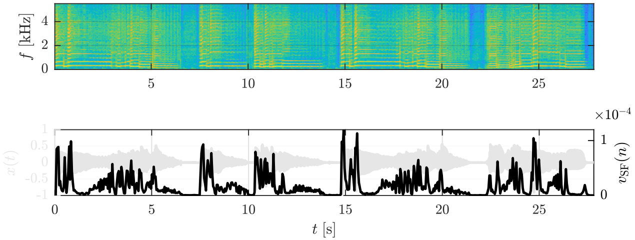
common variants:

- restricted frequency range:

$$v_{\mathrm{SD}}(n) = \frac{\sum\limits_{k=k_{\mathrm{l}}}^{k_{\mathrm{u}}} \frac{1}{k} \cdot \left(|X(k,n)| - |X(k_{\mathrm{l}}-1,n)|\right)}{\sum\limits_{k=k_{\mathrm{l}}}^{k_{\mathrm{u}}} |X(k,n)|}$$

spectral shape features
spectral flux

$$v_{\mathrm{SF}}(n) = \frac{\sqrt{\sum\limits_{k=0}^{\mathcal{K}/2} \left(|X(k,n)| - |X(k,n-1)|\right)^2}}{\mathcal{K}/2 + 1}$$



matlab source: plotFeatures.m

spectral shape features
spectral flux

$$v_{\mathrm{SF}}(n) = \frac{\sqrt{\sum\limits_{k=0}^{\mathcal{K}/2} \left(|X(k,n)| - |X(k,n-1)|\right)^2}}{\mathcal{K}/2 + 1}$$

common variants:

$$\begin{aligned}
v_{\mathrm{SF}}(n,\beta) &= \frac{\sqrt[\beta]{\sum\limits_{k=0}^{\mathcal{K}/2-1} \left(|X(k,n)| - |X(k,n-1)|\right)^\beta}}{\mathcal{K}/2} \\
v_{\mathrm{SF},\sigma}(n) &= \sqrt{\frac{2}{\mathcal{K}} \sum_{k=0}^{\mathcal{K}/2-1} \left(\Delta X(k,n) - \mu_{\Delta X}\right)^2} \\
v_{\mathrm{SF,log}}(n) &= \frac{2}{\mathcal{K}} \sum_{k=0}^{\mathcal{K}/2-1} \log_2\left(\frac{|X(k,n)|}{|X(k,n-1)|}\right)
\end{aligned}$$

fundamentals

cepstrum 1/3

signal model:
convolution of *excitation signal* and *transfer function*

$$x(i) = e(i) * h(i)$$

$$X(\mathrm{j}\omega) = E(\mathrm{j}\omega) \cdot H(\mathrm{j}\omega)$$

$$\begin{aligned}\log\left(X(\mathrm{j}\omega)\right) &= \log\left(E(\mathrm{j}\omega) \cdot H(\mathrm{j}\omega)\right) \\ &= \log\left(E(\mathrm{j}\omega)\right) + \log\left(H(\mathrm{j}\omega)\right)\end{aligned}$$

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cepstrum 1/3

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fundamentals
cepstrum 2/3

$$
\begin{aligned}
c_x(i) &= \mathfrak{F}^{-1}\left\{\log\left(X(\mathrm{j}\omega)\right)\right\} \\
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\hat{c}_x(i_\mathrm{s}(n)\ldots i_\mathrm{e}(n)) &= \sum_{k=0}^{\mathcal{K}/2-1} \log\left(|X(k,n)|\right) e^{\mathrm{j}ki\Delta\Omega}
\end{aligned}
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fundamentals

cepstrum 2/3

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fundamentals

cepstrum 2/3

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fundamentals

cepstrum 2/3

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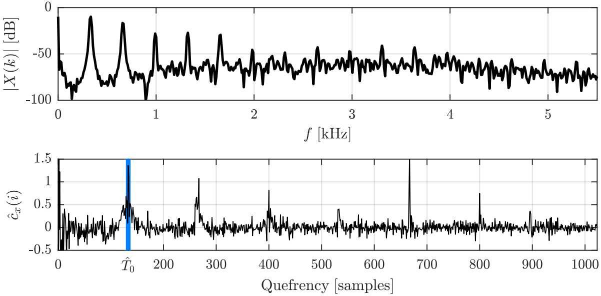

matlab source: plotF0Cepstrum.m

fundamentals

cepstrum 3/3

- **summary**:
  - cepstrum 'replaces' time domain convolution operation with addition
  - result is the *unfiltered* excitation signal *plus* the filter IR (both logarithmic)
  - can be used for, e.g., *spectral envelope extraction* or *pitch detection*

  - more naming silliness:
    cepstrum, quefrency, liftering, . . .

fundamentals

cepstrum 3/3

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spectral shape features

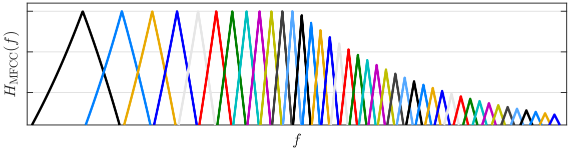
mel frequency cepstral coefficients 1/4

- typical processing steps for the mel frequency cepstral coefficients (MFCCs):
  1. compute magnitude spectrum
  2. convert linear frequency scale to logarithmic
  3. group bins into bands
  4. apply logarithm to all bands
  5. compute (inverse) cosine transform (DCT)

$$v_{\mathrm{MFCC}}^{j}(n) = \sum_{k'=1}^{\mathcal{K}'} \log\left(|X'(k', n)|\right) \cdot \cos\left(j \cdot \left(k' - \frac{1}{2}\right) \frac{\pi}{\mathcal{K}'}\right)$$

spectral shape features

mel frequency cepstral coefficients 2/4



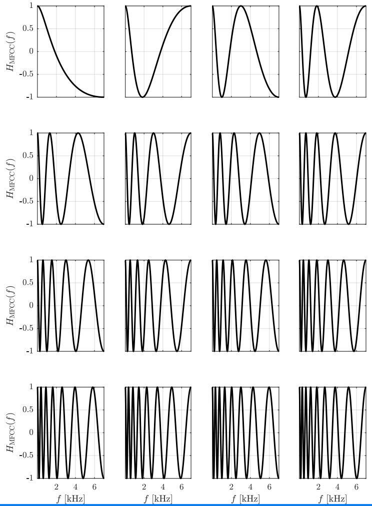
- constant Q filter spacing for higher frequencies (mel scale)
- FFT values are weighted and summed over bins for each band

matlab source: plotMfccFilterbank.m

spectral shape features

mel frequency cepstral coefficients 3/4

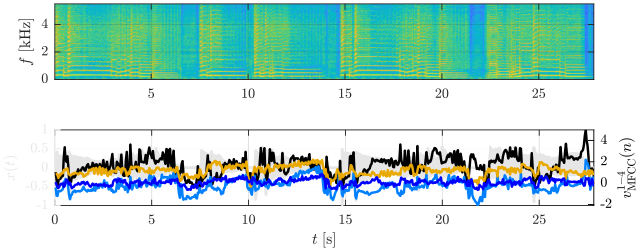
mel-warped cosine bases for DCT



spectral shape features

mel frequency cepstral coefficients 4/4

Property	DM	HTK	SAT
Num. filters	20	24	40
Mel scale	lin/log	log	lin/log
Freq. range	[100; 4000]	[100; 4000]	[200; 6400]
Normalization	Equal height	Equal height	Equal area

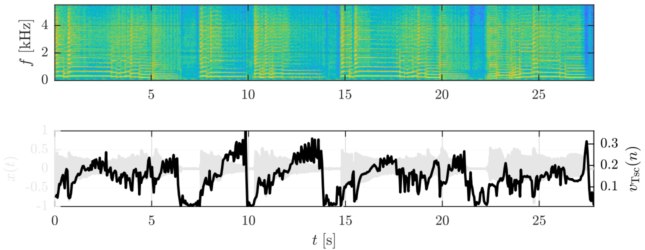


matlab source: plotFeatures.m

tonalness features

spectral crest factor

$$v_{\mathrm{Tsc}}(n) = \frac{\max\limits_{0\leq k\leq \mathcal{K}/2} |X(k,n)|}{\sum\limits_{k=0}^{\mathcal{K}/2} |X(k,n)|}$$



matlab source: plotFeatures.m

tonalness features
spectral crest factor

$$v_{\mathrm{Tsc}}(n) = \frac{\max\limits_{0\leq k\leq \mathcal{K}/2} |X(k,n)|}{\sum\limits_{k=0}^{\mathcal{K}/2} |X(k,n)|}$$

common variants:

- normalization
- power spectrum
- measure *per band* instead of whole spectrum

tonalness features

spectral flatness

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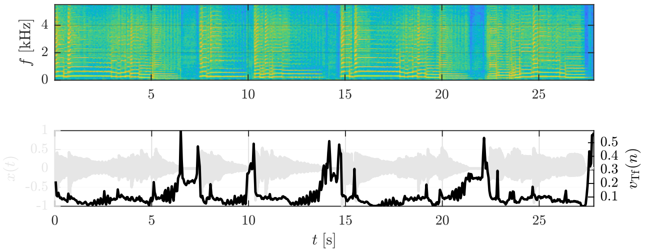
$$v_{\mathrm{Tf}}(n) = \frac{\sqrt[\mathcal{K}/2]{\prod\limits_{k=0}^{\mathcal{K}/2-1} |X(k,n)|}}{2/\mathcal{K} \cdot \sum\limits_{k=0}^{\mathcal{K}/2-1} |X(k,n)|}$$



matlab source: plotFeatures.m

tonalness features

spectral flatness

$$v_{\mathrm{Tf}}(n) = \frac{\sqrt[\mathcal{K}/2]{\prod\limits_{k=0}^{\mathcal{K}/2-1} |X(k,n)|}}{{}^{2}/_{\mathcal{K}} \cdot \sum\limits_{k=0}^{\mathcal{K}/2-1} |X(k,n)|}$$

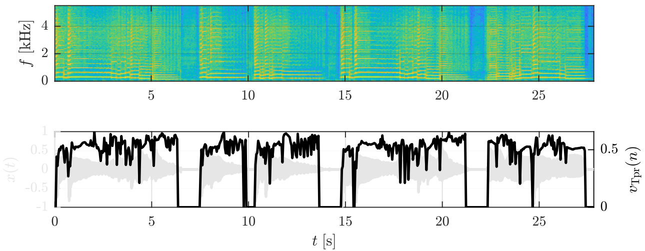
common variants:

- power vs. magnitude spectrum
- smoothed spectrum (avoid spurious 0-bins)
- measure *per band* instead of whole spectrum

tonalness features

spectral tonal power ratio

$$v_{\mathrm{Tpr}} = \frac{E_{\mathrm{T}}(n)}{\sum\limits_{i=0}^{\mathcal{K}/2} |X(k,n)|^2}$$



matlab source: plotFeatures.m

tonalness features

spectral tonal power ratio

$$v_{\mathrm{Tpr}} = \frac{E_{\mathrm{T}}(n)}{\sum\limits_{i=0}^{\mathcal{K}/2} |X(k,n)|^2}$$

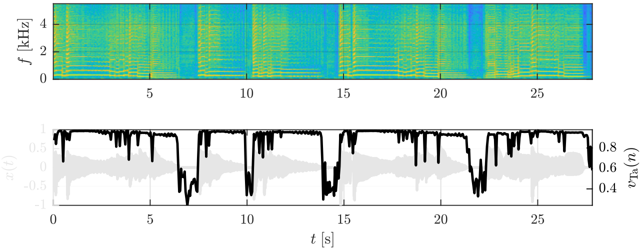
common variants:

- definition of tonal/non-tonal components
  - local maxima
  - peak salience
  - in periodic (harmonic) pattern
  - ...

tonalness features

maximum of ACF

$$v_{\mathrm{Ta}}(n) = \max_{0\leq\eta\leq\mathcal{K}-1} |r_{xx}(\eta, n)|$$

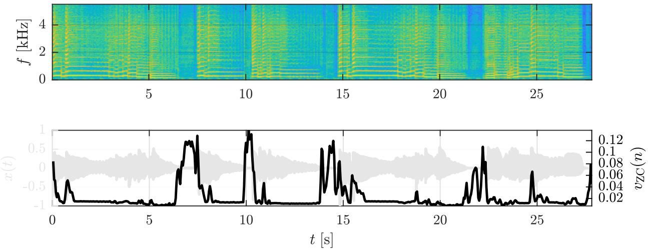


matlab source: matlab/displayFeatures.m

technical features

zero crossing rate

$$v_{\mathrm{ZC}}(n) = \frac{1}{2 \cdot \mathcal{K}} \sum_{i=i_{\mathrm{s}}(n)}^{i_{\mathrm{e}}(n)} \left| \mathrm{sign}\left[x(i)\right] - \mathrm{sign}\left[x(i-1)\right] \right|$$

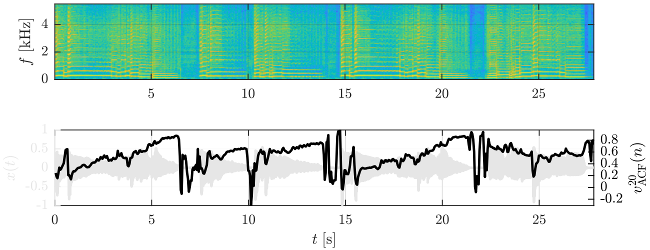


matlab source: matlab/displayFeatures.m

technical features

ACF coefficients

$$v_{\mathrm{ACF}}^{\eta}(n) = r_{xx}(\eta, n) \quad \text{with} \quad \eta = 1, 2, 3, \ldots$$



matlab source: matlab/displayFeatures.m

summary
lecture content

- **feature**
  - descriptor with condensed relevant information
  - not necessarily interpretable by humans
- **feature extraction**
  - usually extracted per short block of samples
  - many features can be extracted from audio data, resulting in feature matrix
- **timbre**
  - mostly dependent on both spectral shape and time domain envelope characteristics
  - multi-dimensional perceptual property not as clearly defined as pitch or loudness
- **instantaneous spectral shape features**
  - established set of baseline features
  - often extracted from the magnitude spectrum, describing timbre
  - condensing various properties of the spectral shape into single values
  - there exist multiple variants of “the same” feature