



Universität Hamburg
DER FORSCHUNG | DER LEHRE | DER BILDUNG

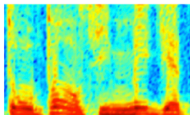
Alexander Panchenko

**FROM UNSUPERVISED INDUCTION OF
LINGUISTIC STRUCTURES FROM TEXT
TOWARDS APPLICATIONS IN DEEP
LEARNING**

Graph embeddings

Text: sparse symbolic representation

AUDIO



Audio Spectrogram

DENSE

IMAGES

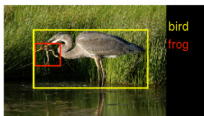


Image pixels

DENSE

TEXT

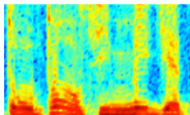
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Word, context, or
document vectors

SPARSE

Text: sparse symbolic representation

AUDIO



Audio Spectrogram

DENSE

IMAGES

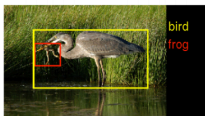


Image pixels

DENSE

TEXT

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Word, context, or document vectors

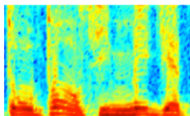
SPARSE

Image source:

<https://www.tensorflow.org/tutorials/word2vec>

Graph: sparse symbolic representation

AUDIO



Audio Spectrogram

DENSE

IMAGES

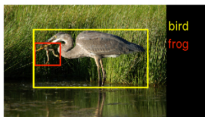
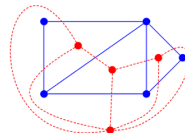


Image pixels

DENSE

GRAPH



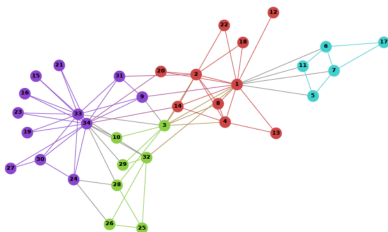
Nodes, edges, weights

SPARSE

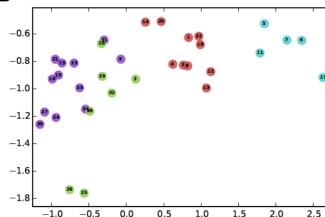
Embedding graph into a vector space

From a **survey on graph embeddings** [Hamilton et al., 2017]:

A

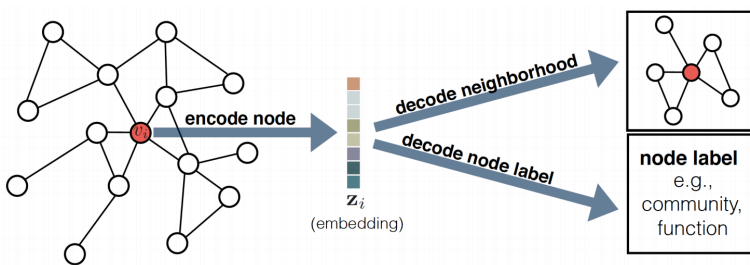


B



Learning with an “autoencoder”

From a **survey on graph embeddings** [Hamilton et al., 2017]:



Some established approaches

From a **survey on graph embeddings** [Hamilton et al., 2017]:

Type	Method	Decoder	Similarity measure	Loss function (ℓ)
Matrix factorization	Laplacian Eigenmaps [4]	$\ \mathbf{z}_i - \mathbf{z}_j\ _2^2$	general	$\text{DEC}(\mathbf{z}_i, \mathbf{z}_j) \cdot s_{\mathcal{G}}(v_i, v_j)$
	Graph Factorization [1]	$\mathbf{z}_i^\top \mathbf{z}_j$	$\mathbf{A}_{i,j}$	$\ \text{DEC}(\mathbf{z}_i, \mathbf{z}_j) - s_{\mathcal{G}}(v_i, v_j)\ _2^2$
	GraRep [9]	$\mathbf{z}_i^\top \mathbf{z}_j$	$\mathbf{A}_{i,j}, \mathbf{A}_{i,j}^2, \dots, \mathbf{A}_{i,j}^k$	$\ \text{DEC}(\mathbf{z}_i, \mathbf{z}_j) - s_{\mathcal{G}}(v_i, v_j)\ _2^2$
	HOPE [45]	$\mathbf{z}_i^\top \mathbf{z}_j$	general	$\ \text{DEC}(\mathbf{z}_i, \mathbf{z}_j) - s_{\mathcal{G}}(v_i, v_j)\ _2^2$
Random walk	DeepWalk [47]	$\frac{e^{\mathbf{z}_i^\top \mathbf{z}_j}}{\sum_{k \in \mathcal{V}} e^{\mathbf{z}_i^\top \mathbf{z}_k}}$	$p_{\mathcal{G}}(v_j v_i)$	$-s_{\mathcal{G}}(v_i, v_j) \log(\text{DEC}(\mathbf{z}_i, \mathbf{z}_j))$
	node2vec [28]	$\frac{e^{\mathbf{z}_i^\top \mathbf{z}_j}}{\sum_{k \in \mathcal{V}} e^{\mathbf{z}_i^\top \mathbf{z}_k}}$	$p_{\mathcal{G}}(v_j v_i)$ (biased)	$-s_{\mathcal{G}}(v_i, v_j) \log(\text{DEC}(\mathbf{z}_i, \mathbf{z}_j))$



Hamilton, W. L., Ying, R., & Leskovec, J. (2017).

Representation learning on graphs: Methods and applications.

arXiv preprint arXiv:1709.05584.
