

# Math 461 Notes

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# Data Analysis

**Definition.** Let  $X$  be a data set. The cumulative distribution function, or CDF, is defined as

$$F(x) = P(X \leq x)$$

That is, it measures the probability that a member of  $X$  is less than or equal to  $x$ . Thus,  $1 - F(x)$  measures the probability that a member of  $X$  is greater than  $x$ .

**Fact.** The plot of a CDF never decreases, and is bounded by  $0 \leq F(x) \leq 1$ .

**Definition.** Let  $X$  be a data set with members  $x_1, x_2, \dots, x_n$  occurring with probabilities  $p_1, p_2, \dots, p_n$ . The expected value of  $X$  is defined as

$$E[X] = \sum_{i=1}^n x_i p_i$$

That is, the expected value is the arithmetic mean of the members of  $X$ .

**Definition.** Let  $X$  be a data set, and let  $\mu = E[X]$ . Then the variance of  $X$  is defined as

$$Var(X) = E[(X - \mu)^2]$$

Informally, variance measures how spread apart the members of  $X$  are from the expected value.

**Theorem.** Let  $X$  be a data set, and let  $c$  be some real constant. Then, the following properties hold:

- (i)  $E[cX] = cE[X]$
- (ii)  $E[X + c] = E[X] + c$
- (iii)  $Var[X + c] = Var[X]$
- (iv)  $Var[cX] = c^2 Var[X]$
- (v)  $Var[X] = E[X^2] - E[X]^2$

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