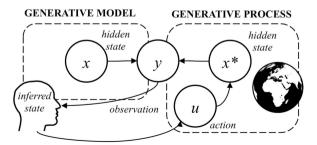
## From the Free Energy Principle to Active Inference

A Neuro-Inspired Route to (Super)Intelligent Systems

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## Active Inference: A Neuro-Inspired Blueprint for AGI

### Why this matters for AGI

Any system that *persists* must avoid disorganising ("surprising") states. Biological agents do this by building models of their world, *inferring* hidden causes of sensory data, and *acting* to make future data match their predictions.

#### Active Inference in one sentence

Agents update beliefs to explain data (perception) and select policies to make data predictable (action), jointly *minimising* expected free energy.

### Core decision objective: Expected Free Energy (EFE)

$$\begin{split} G(\pi) \; &= \; \underbrace{\mathbb{E}_{q(o,s|\pi)}[-\ln p(o)]}_{\text{pragmatic: reach preferred outcomes}} \\ &+ \underbrace{\mathbb{E}_{q(o,s|\pi)}\!\!\left[D_{\text{KL}}(q(s|o,\pi)\,\|\,q(s|\pi))\right]}_{\text{epistemic: reduce uncertainty (learn)}} \,. \end{split}$$

#### Why this matters for Superintelligence

**Unified objective:** One principle drives perception, learning, exploration, and control.

**Built-in curiosity:** Exploration emerges intrinsically.

Model-based & embodied: Learns a world model and uses it for inference, planning, and action.

**Scalable architecture:** Generalises to hierarchical, modular, self-modelled agents.

#### key:

 $G(\pi)$ : expected free energy  $\mathbb{E}[\cdot]$ : expected value (average)  $q(o,s\mid\pi)$ : predicted outcomes and states p(o): preferred outcomes  $q(s\mid o,\pi)$  vs.  $q(s\mid\pi)$ : posterior vs prior beliefs

# Why FEP/Active Inference? A biological must-do

## Core idea

Any system that *persists* - a cell, animal, robot... must keep its sensory states within viable bounds. If its encounters are too chaotic or surprising, it disintegrates. So it must *predict and control* its future sensations well enough to stay alive.

### What follows from this

The system needs an internal model of how its sensations arise from hidden causes in the world.

It must update beliefs to better explain incoming data (perception/learning).

It must **act** to make incoming data more predictable and in line with what keeps it viable (control/policy selection).

## Why it matters for AI

This gives a **single normative objective** for perception, learning and action rather than stitching separate objectives together. It also builds in **curiosity** (information-seeking) as part of staying within viable bounds.

## Free Energy Principle (FEP): inference as a survival tool

### The FEP

Under the FEP, a persisting agent behaves as if it *minimises variational free energy*: a quantity that upper-bounds how *surprising* (unlikely) its sensations are under its world model. Equation

$$F(q) = \mathbb{E}_{q(s)} \left[ \ln q(s) - \ln p(s, o) \right]$$

## Components:

o: sensory observations (what the agent senses)

s: hidden states that cause sensations (what's out there)

p(s,o): agent's generative model linking hidden states to observations

q(s): agent's approximate posterior beliefs about hidden states

 $\mathbb{E}_{q(s)}[\cdot]$ : expected value (average) over states s according to current beliefs q(s)

F(q): variational free energy; smaller F means beliefs better explain data

## Immediate consequence

Minimising F is (approximately) equivalent to Bayesian inference: improve beliefs so sensations are less surprising under the model.

## FEP: distance-to-posterior + evidence

## Equivalent decomposition

$$F(q) = D_{\mathrm{KL}}(q(s) \parallel p(s \mid o)) - \ln p(o)$$

### Interpretation:

 $D_{\mathrm{KL}}ig(q(s) \parallel p(s \mid o)ig)$ : how far the agent's beliefs q(s) are from the exact Bayesian posterior.

 $-\ln p(o)$ : (negative) model evidence for the observed sensations under the generative model.

### Mean

Minimise the gap to the true posterior while making your sensations more expected under your model. That's how a biological system avoids disorganising ("surprising") states.

## Active Inference: one objective for perception & action

### Definition

Active Inference extends FEP to include action: the agent both updates beliefs (perception/learning) to reduce free energy, and selects policies (action sequences) that are expected to reduce future free energy.

## **Embodiment**

Intelligence is *situated*: the agent's body, sensors, and effectors define the interface to the world (often framed via a *Markov blanket*). Morphology and environment constrain what the agent can sense, predict, and do; that is, *which* policies are even feasible.

## Why this helps

Unlike pipelines that glue a perception module to a control module, Active Inference uses one principle for both. That makes **exploration** (information seeking) and **goal pursuit** two sides of the same coin.

# Expected Free Energy (EFE): decisions that learn & achieve goals

Operational objective for choosing policies (fixed size, wrapped)

$$\begin{split} G(\pi) &= \underbrace{\mathbb{E}_{q(o,s|\pi)} \big[ -\ln p(o) \big]}_{\text{pragmatic value: prefer outcomes you want}} \\ &+ \underbrace{\mathbb{E}_{q(o,s|\pi)} \Big[ D_{\text{KL}} \big( q(s \,|\, o,\pi) \,\|\, q(s \,|\, \pi) \big) \Big]}_{\text{epistemic value: expected information gain}}. \end{split}$$

### Components:

```
\pi: a policy (candidate sequence of actions) p(o): preferences over outcomes (↑ when outcomes are good/viable) q(o,s|\pi): predicted outcomes and states if the agent follows \pi q(s|o,\pi) vs. q(s|\pi): posterior vs. prior beliefs about states under \pi G(\pi): expected free energy; choose policies that \min G(\pi)
```

## Meaning

Pragmatic term: "Head toward outcomes I prefer/that keep me viable."

Epistemic term: "Also choose actions that teach me most about hidden states (reduce uncertainty)"

## One-minute recap

Biological must-do: Persisting systems must avoid "surprising" (disorganising) sensory states.

**FEP**: Do approximate Bayesian inference by minimising variational free energy.

**Active Inference**: Use the same principle to *act*, not just perceive.

**EFE**: Choose policies that both reach preferred outcomes and reduce uncertainty: goal-seeking that learns.

Cover image adapted from: Pezzulo, G., Rigoli, F., Friston, K. J. (2024), \*Biological Psychology\*, 175, 108741. DOI:10.1016/j.biopsycho.2023.108741