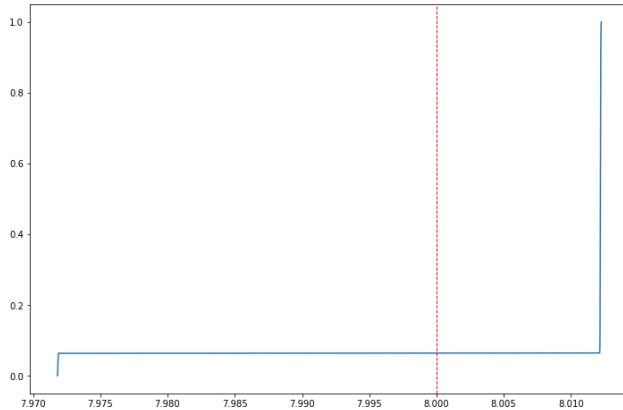


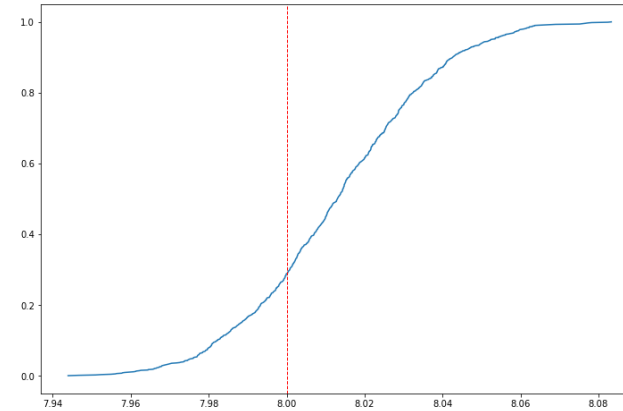
# Cumulative Posterior Distributions

Offline SHMC



$m=1/\text{cov}$ ,  $L=20$ ,  $\text{eta}=5 \cdot 10^{-12}$   
(evolution times chosen offline;  
increment=0.08)

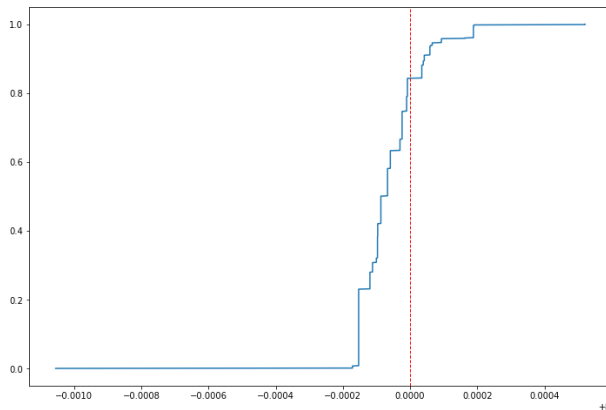
Offline SMC (SIR)



$a=0.98$ ,  $\text{ESS\_threshold}=N_{\text{particles}}/2$   
Resampling:  
 $\mu = a \cdot f_{\text{particle}} + (1 - a) \cdot \mu_{\text{current}}$   
 $\sigma = \sqrt{1 - a^2} \cdot \sigma_{\text{current}}$

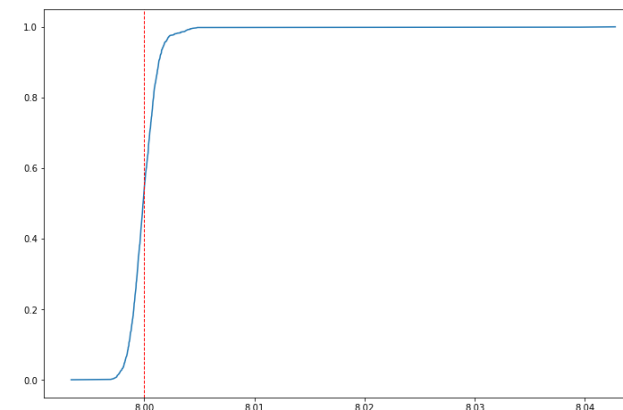
(evolution times chosen offline;  
increment=0.08)

Adaptive SHMC



$m=1/\text{cov}$ ,  $L=20$ ,  $\text{eta}=10^{-6}$   
(evolution times chosen adaptively;  
 $k=1.25$ )

Adaptive SMC (SIR)



$a=0.98$ ,  $\text{ESS\_threshold}=N_{\text{particles}}/2$   
Resampling:  
 $\mu = a \cdot f_{\text{particle}} + (1 - a) \cdot \mu_{\text{current}}$   
 $\sigma = \sqrt{1 - a^2} \cdot \sigma_{\text{current}}$

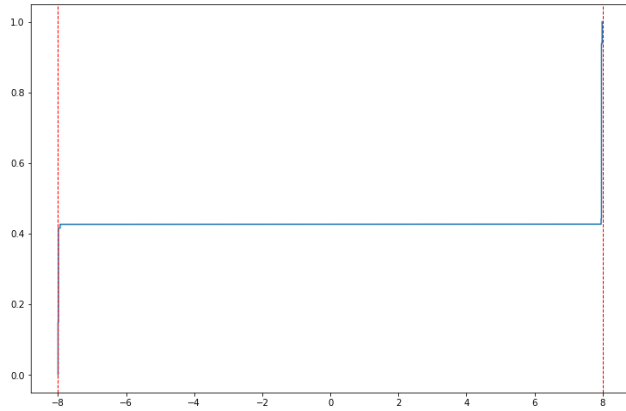
(evolution times chosen adaptively;  
 $k=1.25$ )

All:  $n=1000$ ;  $N=100$ ;  $f_{\text{max}}=10$ ;  $f_{\text{real}}=8$

# Cumulative Posterior Distributions

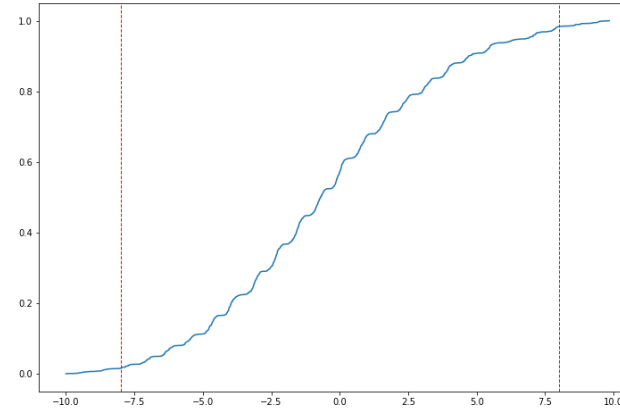
(prior with support over negative frequencies)

Offline SHMC



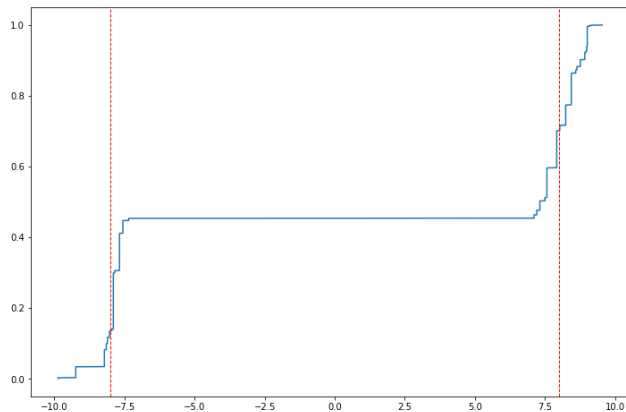
$m=1/\text{cov}$ ,  $L=20$ ,  $\text{eta}=10^{-10}$   
(evolution times chosen offline;  
increment=0.08)

Offline SMC (SIR)



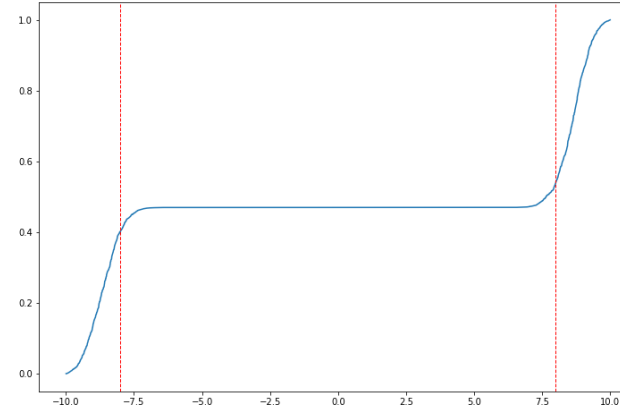
$a=0.98$ ,  $\text{ESS\_threshold}=N_{\text{particles}}/2$   
Resampling:  
 $\mu = a \cdot f_{\text{particle}} + (1 - a) \cdot \mu_{\text{current}}$   
 $\sigma = \sqrt{1 - a^2} \cdot \sigma_{\text{current}}$   
(evolution times chosen offline;  
increment=0.08)

Adaptive SHMC



$m=1/\text{cov}$ ,  $L=20$ ,  $\text{eta}=10^{-10}$   
(evolution times chosen adaptively;  
 $k=1.25$ )

Adaptive SMC (SIR)

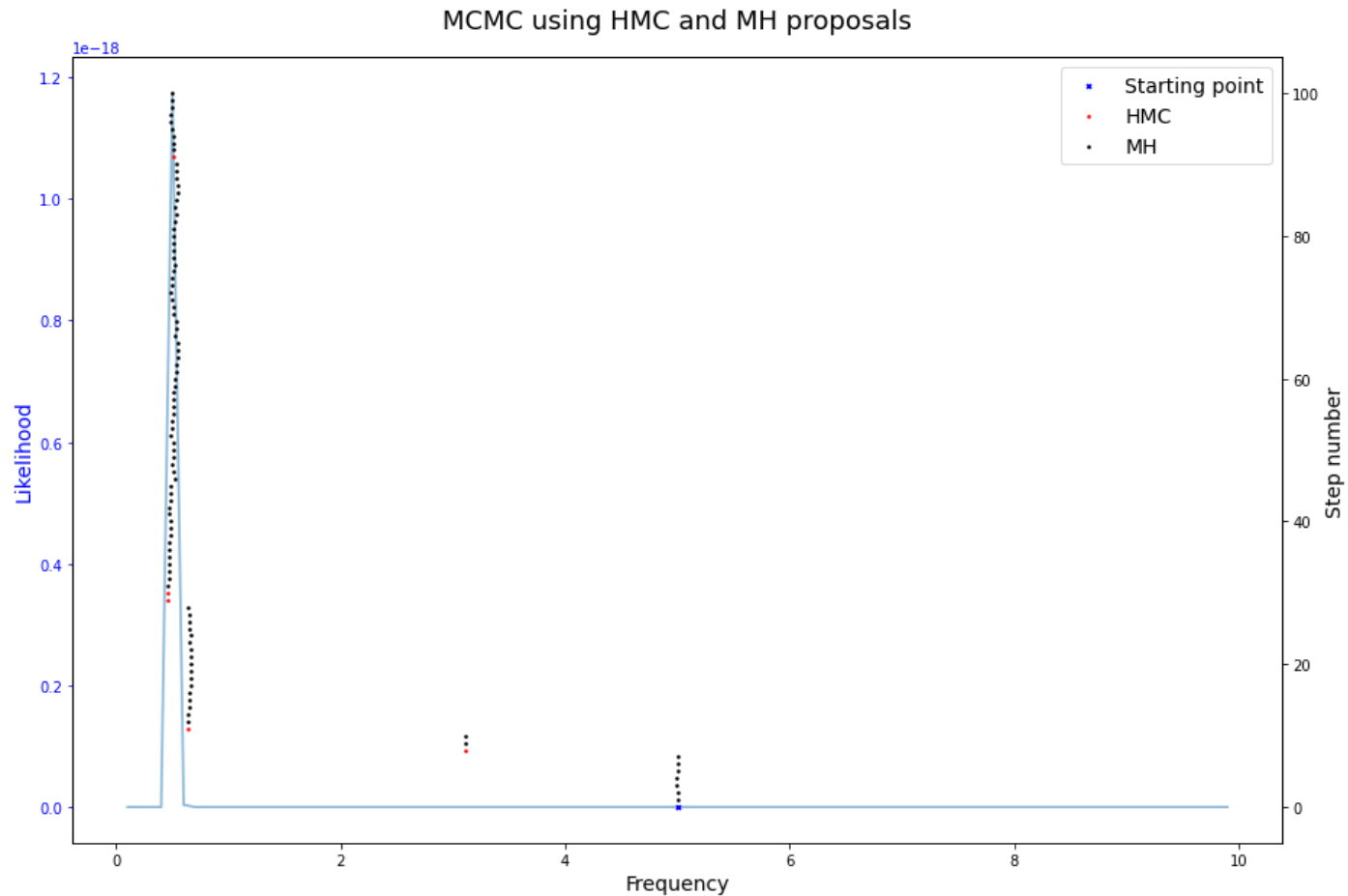


$a=0.98$ ,  $\text{ESS\_threshold}=N_{\text{particles}}/2$   
Resampling\*:  
 $\mu = a \cdot f_{\text{particle}} + (1 - a) \cdot \mu_{\text{current}}$   
 $\sigma = \sqrt{1 - a^2} \cdot \sigma_{\text{current}}$   
\*  $\sim 10\times$  less frequent than for offline  
(evolution times chosen adaptively;  
 $k=1.25$ )

All:  $n=2000$ ;  $N=100$ ;  $f_{\text{max}}=10$ ;  $f_{\text{real}}=8$

# MCMC (single particle)

*(5% HMC steps)*



HMC:  $m=0.1$ ,  $L=10$ ,  $\eta=5 \cdot 10^{-3}$ , threshold=0.01

MH: gaussian proposals,  $\sigma=0.01$

\* Percentage of HMC steps: **5.0%**.

\* Hamiltonian Monte Carlo: 80% mean acceptance rate.

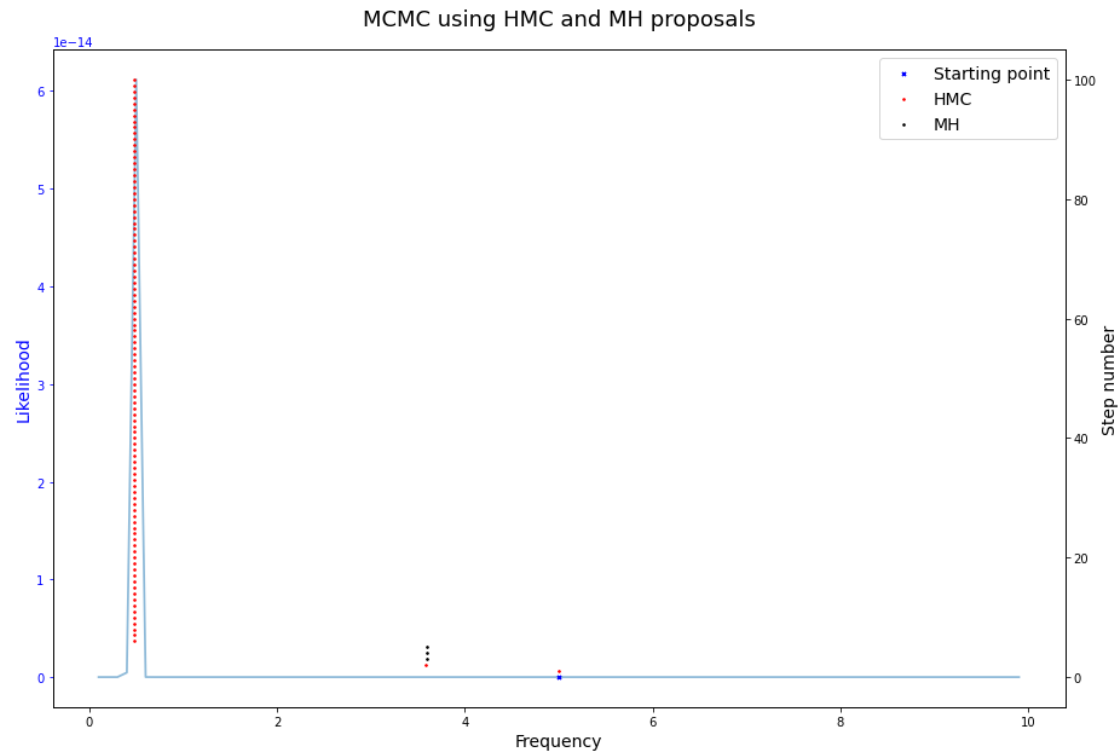
\* Metropolis-Hastings: 82% mean acceptance rate.

*(Move on product of all likelihoods, for  
evolution times chosen in advance;  
increment=0.08)*

$n=1$ ;  $N=100$ ; measurements=100;  $f_{\max}=10$

# MCMC (single particle)

*(95%+ HMC steps)*



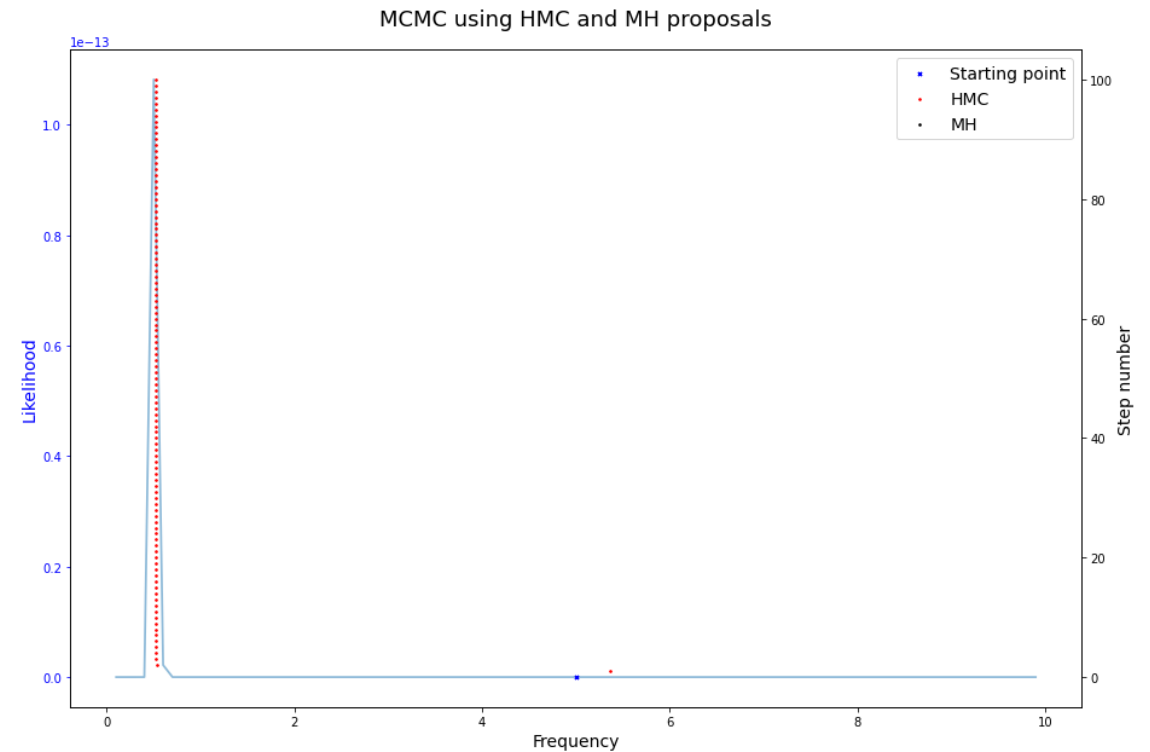
HMC:  $m=0.1$ ,  $L=20$ ,  $\eta=10^{-3}$ , threshold=0.01

MH: gaussian proposals,  $\sigma=0.01$

\* Percentage of HMC steps: **97%**.

\* Hamiltonian Monte Carlo: 99% mean acceptance rate.

\* Metropolis-Hastings: 33% mean acceptance rate.



HMC:  $m=0.1$ ,  $L=20$ ,  $\eta=10^{-3}$ , threshold=0.01

\* Percentage of HMC steps: **100%**.

\* Hamiltonian Monte Carlo: 100% mean acceptance rate

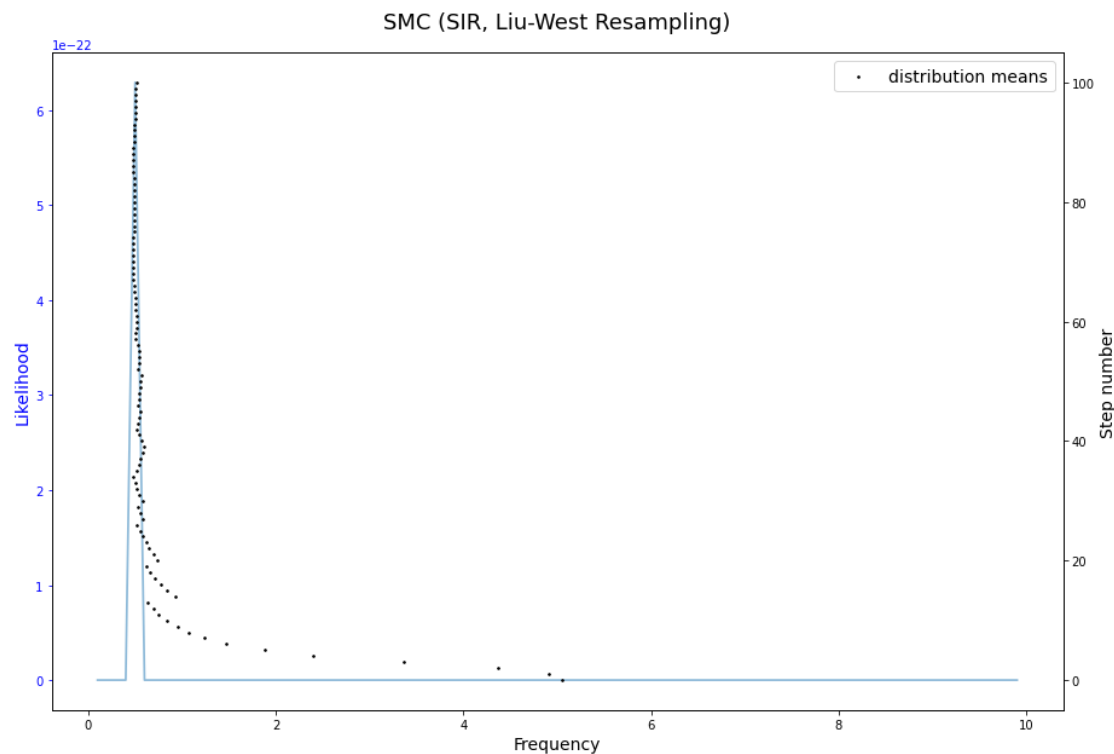
$n=1$ ;  $N=100$ ; measurements=100;  $f_{\max}=10$

# 100 particle SMC vs. MCMC (single particle)

*(Matched for number of measurements, measurement times, number of steps, real frequency, prior distribution, and constraints)*

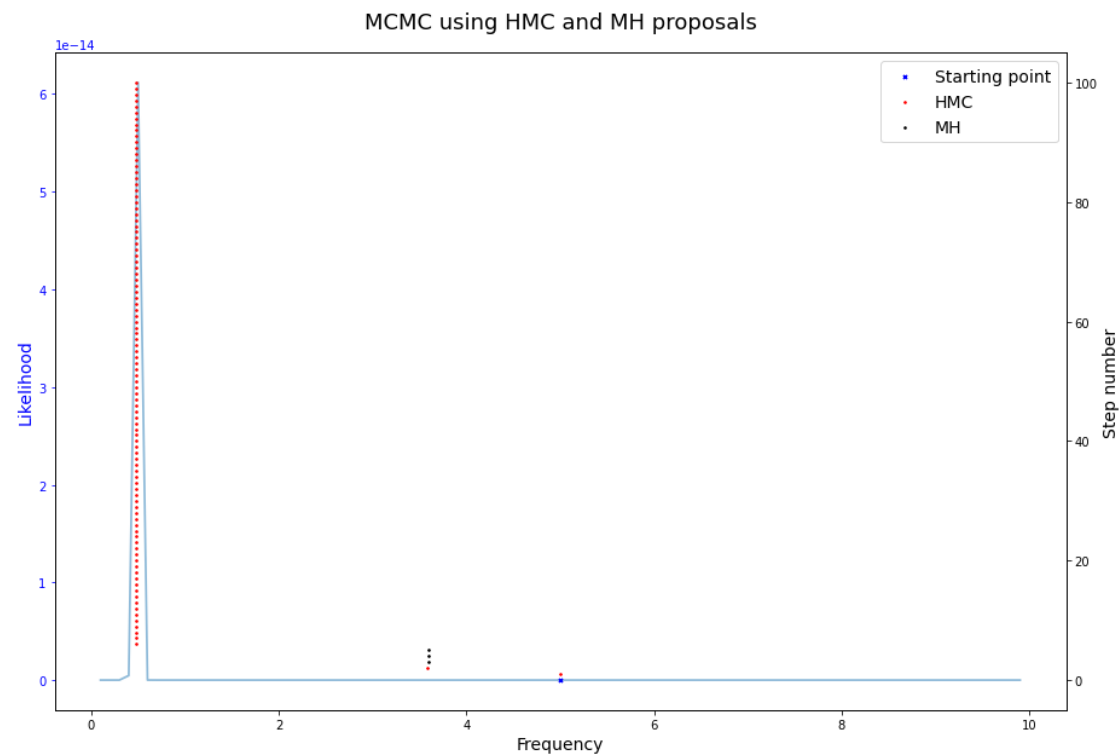
## 100 particles

*(sample from consecutive cumulative products of likelihoods)*



## 1 particle

*(sample from the product of all likelihoods)*



$n=1$  or  $100$ ;  $N=100$ ; measurements=100;  $f_{\max}=10$

*(evolution times chosen offline;  
increment=0.08)*