3D10_column_twist_v0p8_A.Flowers_Comments

July 7, 2025

1 Twisting of a column with square cross-section

1.0.1 Units

Length: mmMass: kg

• Time: s

• Force: milliNewtons

• Stress: kPa

1.0.2 Software:

• Dolfinx v0.8.0

In the collection "Example Codes for Coupled Theories in Solid Mechanics,"

By Eric M. Stewart, Shawn A. Chester, and Lallit Anand.

https://solidmechanicscoupledtheories.github.io/

2 Import modules

```
[1]: # Import FEnicSx/dolfinx
import dolfinx

# For numerical arrays
import numpy as np

# For MPI-based parallelization
from mpi4py import MPI
comm = MPI.COMM_WORLD
rank = comm.Get_rank()

# PETSc solvers
from petsc4py import PETSc

# specific functions from dolfinx modules
from dolfinx import fem, mesh, io, plot, log
```

```
from dolfinx.fem import (Constant, dirichletbc, Function, functionspace,
 ⇔Expression )
from dolfinx.fem.petsc import NonlinearProblem
from dolfinx.nls.petsc import NewtonSolver
from dolfinx.io import VTXWriter, XDMFFile
# specific functions from ufl modules
import ufl
from ufl import (TestFunctions, TrialFunction, Identity, grad, det, div, dev, u
→inv, tr, sqrt, conditional ,\
                gt, dx, inner, derivative, dot, ln, split, as matrix, dot,
⇔cos, sin)
# basix finite elements (necessary for dolfinx v0.8.0)
from basix.ufl import element, mixed_element, quadrature_element
# Matplotlib for plotting
import matplotlib.pyplot as plt
plt.close('all')
# For timing the code
from datetime import datetime
# Set level of detail for log messages (integer)
# Guide:
# CRITICAL = 50, // errors that may lead to data corruption
# ERROR = 40, // things that HAVE gone wrong
# WARNING = 30, // things that MAY go wrong later
# INFO = 20, // information of general interest (includes solver info)
# PROGRESS = 16, // what's happening (broadly)
# TRACE = 13, // what's happening (in detail)
# DBG
          = 10 // sundry
log.set_log_level(log.LogLevel.WARNING)
```

3 Define geometry

```
# This says "spatial coordinates" but is really the referential coordinates,
# since the mesh does not convect in FEniCS.
x = ufl.SpatialCoordinate(domain)
```

Identify boundaries of the domain

```
[3]: # Identify the planar boundaries of the box mesh
     # #
     # def xBot(x):
          return np.isclose(x[0], 0)
     # def xTop(x):
          return np.isclose(x[0], width)
     # def yBot(x):
          return np.isclose(x[1], 0)
     # def yTop(x):
          return np.isclose(x[1], width)
     def zBot(x):
         return np.isclose(x[2], 0)
     def zTop(x):
         return np.isclose(x[2], L)
     # Mark the sub-domains
     boundaries = [(1,zBot),(2,zTop)]
     # build collections of facets on each subdomain and mark them appropriately.
     facet_indices, facet_markers = [], [] # initalize empty collections of indices ⊔
      \rightarrow and markers.
     fdim = domain.topology.dim - 1 # qeometric dimension of the facet (mesh
      \hookrightarrow dimension - 1)
     for (marker, locator) in boundaries:
         facets = mesh.locate_entities(domain, fdim, locator) # an array of all the_
      ⇔facets in a
                                                                 # qiven subdomain_
      ⇔("locator")
         facet_indices.append(facets)
                                                                 # add these facets to ...
      \rightarrow the collection.
         facet_markers.append(np.full_like(facets, marker)) # mark them with the_
      \hookrightarrow appropriate index.
     # Format the facet indices and markers as required for use in dolfinx.
     facet_indices = np.hstack(facet_indices).astype(np.int32)
     facet_markers = np.hstack(facet_markers).astype(np.int32)
     sorted_facets = np.argsort(facet_indices)
     # Add these marked facets as "mesh tags" for later use in BCs.
     facet_tags = mesh.meshtags(domain, fdim, facet_indices[sorted_facets],_
      →facet_markers[sorted_facets])
```

Print out the unique facet index numbers

```
[4]: top_imap = domain.topology.index_map(2)  # index map of 2D entities in_
domain (facets)

values = np.zeros(top_imap.size_global)  # an array of zeros of the same_
size as number of 2D entities

values[facet_tags.indices]=facet_tags.values # populating the array with facet_
tag index numbers

print(np.unique(facet_tags.values))  # printing the unique indices

# Surface numbering:
# boundaries = [(1,zBot),(2,zTop)]
```

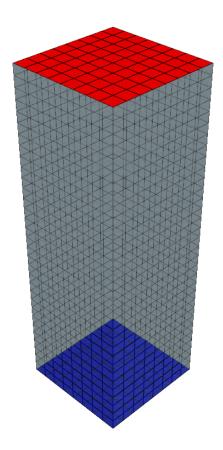
 $[1 \ 2]$

Visualize reference configuration and boundary facets

```
[18]: import pyvista
      pyvista.set_jupyter_backend('html')
      from dolfinx.plot import vtk_mesh
      pyvista.start_xvfb()
      # initialize a plotter
      plotter = pyvista.Plotter()
      # Add the mesh -- I make the 3D mesh opaque, so that 2D surfaces stand out.
      topology, cell_types, geometry = plot.vtk_mesh(domain, domain.topology.dim)
      grid = pyvista.UnstructuredGrid(topology, cell_types, geometry)
      plotter.add_mesh(grid, show_edges=True, opacity=0.5)
      # Add colored 2D surfaces for the named surfaces
      zBot_surf = pyvista.UnstructuredGrid(*vtk_mesh(domain, domain.topology.
       →dim-1,facet_tags.indices[facet_tags.values==1]) )
      zTop_surf = pyvista.UnstructuredGrid(*vtk_mesh(domain, domain.topology.

→dim-1,facet_tags.indices[facet_tags.values==2]) )
      actor = plotter.add_mesh(zBot_surf, show_edges=True,color="blue") # zBot face_
      ⇔is blue
      actor2 = plotter.add_mesh(zTop_surf, show_edges=True,color="red") # zTop is red
      labels = dict(zlabel='Z', xlabel='X', ylabel='Y')
      plotter.add_axes(**labels)
      plotter.screenshot("mesh.png")
      from IPython.display import Image
      Image(filename='mesh.png')
```

[18]:



3.1 Define boundary and volume integration measure

```
[6]: # Define the boundary integration measure "ds" using the facet tags,
# also specify the number of surface quadrature points.
ds = ufl.Measure('ds', domain=domain, subdomain_data=facet_tags,
metadata={'quadrature_degree':4})

# Define the volume integration measure "dx"
# also specify the number of volume quadrature points.
dx = ufl.Measure('dx', domain=domain, metadata={'quadrature_degree': 4})

# Define facet normal
n = ufl.FacetNormal(domain)
```

4 Material parameters

-Arruda-Boyce model

[7]:

```
Gshear_0 = Constant(domain,PETSc.ScalarType(280.0)) # Ground state_

shear modulus

lambdaL = Constant(domain,PETSc.ScalarType(5.12)) # Locking stretch

Kbulk = Constant(domain,PETSc.ScalarType(1000.0*Gshear_0))
```

5 Simulation time-control related params

```
[8]: t = 0.0  # start time (s)
thetaTot = 2 * np.pi
#
Ttot = 1
numSteps = 50
dt = Ttot/numSteps  # (fixed) step size

# Function to linearly ramp up displacement on boundary.
def thetaRamp(t):
    return thetaTot*t/Ttot
```

6 Function spaces

```
[9]: # Define function space, both vectorial and scalar
    # dolfinx v0.8.0 syntax:
    U2 = element("Lagrange", domain.basix_cell(), 2, shape=(3,)) # For displacement
    P1 = element("Lagrange", domain.basix_cell(), 1) # For pressure
    TH = mixed_element([U2, P1]) # Taylor-Hood style mixed element
    ME = functionspace(domain, TH) # Total space for all DOFs
    # Define actual functions with the required DOFs
    w = Function(ME)
    u, p = split(w) # displacement u, pressure p
    # A copy of functions to store values in the previous step
    w_old
                = Function(ME)
    u_old, p_old = split(w_old)
     # Define test functions
    u_test, p_test = TestFunctions(ME)
    # Define trial functions needed for automatic differentiation
    dw = TrialFunction(ME)
```

7 Initial conditions

- The initial conditions for degrees of freedom u and p are zero everywhere
- These are imposed automatically, since we have not specified any non-zero initial conditions.

8 Subroutines for kinematics and constitutive equations

```
[10]: # Deformation gradient
     def F_calc(u):
         Id = Identity(3)
         F = Id + grad(u)
         return F
     def lambdaBar_calc(u):
         F = F_{calc}(u)
         C = F.T*F
         Cdis = J**(-2/3)*C
         I1 = tr(Cdis)
         lambdaBar = sqrt(I1/3.0)
         return lambdaBar
     def zeta_calc(u):
         lambdaBar = lambdaBar calc(u)
         # Use Pade approximation of Langevin inverse
         z = lambdaBar/lambdaL
              = conditional(gt(z,0.95), 0.95, z) # Keep simulation from blowing up
         beta = z*(3.0 - z**2.0)/(1.0 - z**2.0)
         zeta = (lambdaL/(3*lambdaBar))*beta
         return zeta
     # Generalized shear modulus for Arruda-Boyce model
     def Gshear_AB_calc(u):
         zeta = zeta_calc(u)
         Gshear = Gshear_0 * zeta
         return Gshear
     #-----
     # Subroutine for calculating the Cauchy stress
     def T calc(u,p):
         Id = Identity(3)
         F = F_{calc}(u)
         J = det(F)
         B = F*F.T
         Bdis = J**(-2/3)*B
         Gshear = Gshear_AB_calc(u)
         T = (1/J)* Gshear * dev(Bdis) - p * Id
```

```
#------
# Subroutine for calculating the Piola stress
#------
def Piola_calc(u, p):
    Id = Identity(3)
    F = F_calc(u)
    J = det(F)
    #
    T = T_calc(u,p)
    #
    Tmat = J * T * inv(F.T)
    return Tmat
```

```
[]: ##A.Flowers Comments
     # Deformation gradient
     def F_calc(u):
         Id = Identity(3)
         F = Id + grad(u)
         return F
     \#\#Calculation for deformation gradient tensor F
     def lambdaBar_calc(u):
        F = F \operatorname{calc}(u)
        C = F.T*F
         Cdis = J**(-2/3)*C
         I1 = tr(Cdis)
         lambdaBar = sqrt(I1/3.0)
         return lambdaBar
     ##Scalar stretch measure used in hyperelasticity models
     def zeta_calc(u):
         lambdaBar = lambdaBar_calc(u)
     ##Isochoric stretch from deformation
         # Use Pade approximation of Langevin inverse
         z = lambdaBar/lambdaL
     ##Normalizes stretch from polymer network
         z = conditional(gt(z, 0.95), 0.95, z) # Keep simulation from blowing up
     ##Prevents numeric instability; Langevin function because singular
         beta = z*(3.0 - z**2.0)/(1.0 - z**2.0)
     ##Pade approximation; used for stability
         zeta = (lambdaL/(3*lambdaBar))*beta
         return zeta
     ##Stress scalar from statistical mechanics model for polymers; accounts for
      finite chain extensibility. Stress tensors for nonlinear chain elasticity
```

```
# Generalized shear modulus for Arruda-Boyce model
def Gshear_AB_calc(u):
##Effective shear for nonlinear hyperelastic material
         = zeta_calc(u)
##Stretch dependent factor using inverse Langevin. Increasing of stretch-
 ⇔polymers stiffen
   Gshear = Gshear_0 * zeta
   return Gshear
##Shear module grows due to deformation
##This is important due to modeling with biological materials (i.e. tissue);
 ⇔nonlinear and stretch sensitive
#-----
# Subroutine for calculating the Cauchy stress
def T_calc(u,p):
   Id = Identity(3)
   F = F_{calc}(u)
##Deformation gradient
   J = det(F)
##Jacobian (volume change due to deformation)
   B = F*F.T
##Cauchy-Green tensor
   Bdis = J**(-2/3)*B
##Removes volumetric part to get isochoric (volume perserving aspect)
   Gshear = Gshear AB calc(u)
##Stretch dependent shear
   T = (1/J)* Gshear * dev(Bdis) - p * Id
##Cauchy stress calculation; shape change and pressure separated to obtain_
⇔deformed configuration
# Subroutine for calculating the Piola stress
#-----
def Piola_calc(u, p):
   Id = Identity(3)
   F = F_{calc}(u)
   J = det(F)
   T = T_{calc}(u,p)
   Tmat = J * T * inv(F.T)
   return Tmat
##Piola stress used in weak form of balance equation, with displacement_
 →gradient; defined in terms of reference coordinates
```

9 Evaluate kinematics and constitutive relations

```
[11]: F = F_calc(u)
    J = det(F)
    lambdaBar = lambdaBar_calc(u)

# Piola stress
Tmat = Piola_calc(u, p)

[]: ##A.Flowers Comments

F = F_calc(u)
    ##F= deformation gradient tensor; u= displacement (unkown and solving for)
    J = det(F)
    ##J= Jacobian determinant. Volume change during deformation
    lambdaBar = lambdaBar_calc(u)
    ##incompressible hyperelasticity; seperates volumetric deviatoric, shapeu
    changing parts of deformation. Volume corrected stretch is calculated forulate in isochoric strain energy

# Piola stress
```

##Computes Piola stress tensor from displacement field (u) and pressure (p)

10 Weak forms

[]: ##A.Flowers Comments

Tmat = Piola_calc(u, p)

```
# Residuals:
# Res_0: Balance of forces (test fxn: u)
# Res_1: Coupling pressure (test fxn: p)

# The weak form for the balance of forces
Res_0 = inner(Tmat, grad(u_test))*dx

# The weak form for the pressure
fac_p = ln(J)/J
#
Res_1 = dot( (p/Kbulk + fac_p), p_test)*dx

# Total weak form
Res = Res_0 + Res_1

# Automatic differentiation tangent:
a = derivative(Res, w, dw)
```

The weak form for the equilibrium equation. No body force

```
Res_0 = inner(Tmat , grad(u_test) )*dx
##Mechanical residual of weak form for nonlinear elasticity; used to build the
 ⇔residual vector. Used in FE for a deforming solid
# The weak form for the pressure
fac p = ln(J)/J
##Scalar factor used for compressible / incompressible materials due to \sqcup
 ⇔pressure / energy in nonlinear elasticity
Res_1 = dot( (p/Kbulk + fac_p), p_test)*dx
##Residual defined for pressure field in FE due to incompressible materials.
 →Differentiates volumetric strain energy
# Total weak form
Res = Res_0 + Res_1
##Defines total residual of weak form; from force balance (linear momentum / \sqcup
-mechanical equillibrium) and incompressibility (pressure equation)
# Automatic differentiation tangent:
a = derivative(Res, w, dw)
##Jacobian form to solve for nonlinear PDE
```

11 Set-up output files

```
[13]: # results file name
      results_name = "3D_column_twisting"
      # Function space for projection of results
      # v0.8.0 syntax:
      U1 = element("DG", domain.basix_cell(), 1, shape=(3,)) # For displacement
      PO = element("DG", domain.basix_cell(), 1)
                                                             # For pressure
      V2 = fem.functionspace(domain, U1) #Vector function space
      V1 = fem.functionspace(domain, P0) #Scalar function space
      # fields to write to output file
      u_vis = Function(V2)
      u_vis.name = "disp"
      p_vis = Function(V1)
      p_vis.name = "p"
      J_vis = Function(V1)
      J vis.name = "J"
      J_expr = Expression(J,V1.element.interpolation_points())
```

```
lambdaBar_vis = Function(V1)
lambdaBar_vis.name = "lambdaBar"
lambdaBar_expr = Expression(lambdaBar, V1.element.interpolation_points())
P11 = Function(V1)
P11.name = "P11"
P11_expr = Expression(Tmat[0,0],V1.element.interpolation_points())
P22 = Function(V1)
P22.name = "P22"
P22_expr = Expression(Tmat[1,1],V1.element.interpolation_points())
P33 = Function(V1)
P33.name = "P33"
P33_expr = Expression(Tmat[2,2],V1.element.interpolation_points())
   = Tmat*F.T/J
T0 = T - (1/3)*tr(T)*Identity(3)
Mises = sqrt((3/2)*inner(T0, T0))
Mises_vis= Function(V1,name="Mises")
Mises_expr = Expression(Mises, V1.element.interpolation_points())
# set up the output VTX files.
file results = VTXWriter(
    MPI.COMM_WORLD,
    "results/" + results name + ".bp",
    [ # put the functions here you wish to write to output
        u_vis, p_vis, J_vis, P11, P22, P33, lambdaBar_vis,
        Mises_vis,
    ],
    engine="BP4",
)
def writeResults(t):
       # Output field interpolation
       u_vis.interpolate(w.sub(0))
       p_vis.interpolate(w.sub(1))
       J_vis.interpolate(J_expr)
       P11.interpolate(P11 expr)
       P22.interpolate(P22_expr)
       P33.interpolate(P33 expr)
       lambdaBar_vis.interpolate(lambdaBar_expr)
       Mises_vis.interpolate(Mises_expr)
       # Write output fields
       file_results.write(t)
```

12 Name the analysis step

```
[14]: # Give the step a descriptive name step = "Twist"
```

12.1 Boundary condtions

```
[15]: # Surface numbering:
      \# boundaries = [(1, zBot), (2, zTop)]
      # Scalar function space corresponding to dispalcement u
      V, V_to_ME = ME.sub(0).collapse()
      # Expression for applied twist
      thetaCons = Constant(domain,PETSc.ScalarType(thetaRamp(0)))
      Rot = as_matrix([[cos(thetaCons), sin(thetaCons), 0], [-sin(thetaCons), __
       \hookrightarrowcos(thetaCons), 0], [0, 0, 1]])
      rotation_displ = dot(Rot, x) - x
      # interpolate applied displacement values onto the top surface
      u top = fem.Function(V)
      rot_expr = fem.Expression(rotation_displ, V.element.interpolation_points())
      u_top.interpolate(rot_expr)
      # interpolate zero displacement onto the bottom surface
      u_bot = fem.Function(V)
      u bot.interpolate(lambda x: np.stack(( np.zeros(x.shape[1]), np.zeros(x.
       ⇒shape[1]), np.zeros(x.shape[1]))))
      # Bottom and top surface displacement degrees of freedom
      Btm_dofs = fem.locate_dofs_topological((ME.sub(0), V), facet_tags.dim,__

→facet tags.find(1))
      Top_dofs = fem.locate_dofs_topological((ME.sub(0), V), facet_tags.dim,__

¬facet_tags.find(2))
      # Build the Dirichlet BCs
      bcs 1 = dirichletbc(u bot, Btm dofs, ME.sub(0))
                                                           # fix - zBtm
      bcs_2 = dirichletbc(u_top, Top_dofs, ME.sub(0))
                                                           # twist - zTop
      # collect all BCs in one object.
      bcs = [bcs_1, bcs_2]
```

```
[]: ##A.Flowers Comments

# Surface numbering:
# boundaries = [(1,zBot),(2,zTop)]
```

```
# Scalar function space corresponding to dispalcement u
V, V_to_ME = ME.sub(0).collapse()
##ME = mixed function space (product of multiple FE function spaces); holds_{\sqcup}
→multiple fields together
##Collapse = converts subspace of mixed space to independent funtion space
##V = extracted subspace, made independent
# Expression for applied twist
thetaCons = Constant(domain,PETSc.ScalarType(thetaRamp(0)))
##thetaCons = constrant rotation angle defined
##Constant function over domain is applied; specifically used due to FEniCSxL
 ⇔expressions.Constant rotation angle defined for time step
Rot = as_matrix([[cos(thetaCons), sin(thetaCons), 0], [-sin(thetaCons),__
⇔cos(thetaCons), 0], [0, 0, 1]])
##Rot = rotation matrix that can rotate any vector by thetaCons around z-axis
rotation displ = dot(Rot, x) - x
##For each x point, computes displacement field corresponding to rigid rotation \Box
 ⇔by thetaCons around z-axis
# interpolate applied displacement values onto the top surface
u top = fem.Function(V)
##Displacement field over mesh
rot expr = fem.Expression(rotation displ, V.element.interpolation points())
##Points displaced of whole geometry, undergoing rigid rotation angle_{\sqcup}
 \hookrightarrow (thetaCons) around the z-axis
u_top.interpolate(rot_expr)
##Applies torosional deformation; twist at top of cylinder
# interpolate zero displacement onto the bottom surface
u_bot = fem.Function(V)
##Defines displacement function in FEniCSx
u_bot.interpolate(lambda x: np.stack(( np.zeros(x.shape[1]), np.zeros(x.
 ⇒shape[1]), np.zeros(x.shape[1]))))
##Set to zero displacement in domains; Defines initial / fixed ends of \Box
 \hookrightarrow displacement
# Bottom and top surface displacement degrees of freedom
Btm_dofs = fem.locate_dofs_topological((ME.sub(0), V), facet_tags.dim,__

¬facet_tags.find(1))
Top_dofs = fem.locate_dofs_topological((ME.sub(0), V), facet_tags.dim,__

¬facet_tags.find(2))
##Fixed bottom surface and applies torosional or pull displacement at the top,
\hookrightarrowsurface
# Build the Dirichlet BCs
bcs_1 = dirichletbc(u_bot, Btm_dofs, ME.sub(0))
                                                      # fix - zBtm
```

```
bcs_2 = dirichletbc(u_top, Top_dofs, ME.sub(0)) # twist - zTop

##Applies boundary conditions, fixing bottom surface and enforcing rotational

→displacement field to top surface

# collect all BCs in one object.

bcs = [bcs_1, bcs_2]

##Applies boundary conditions to the nonlinear solver
```

12.2 Define the nonlinear variational problem

```
[16]: # Set up nonlinear problem
      problem = NonlinearProblem(Res, w, bcs, a)
      # the global newton solver and params
      solver = NewtonSolver(MPI.COMM_WORLD, problem)
      solver.convergence_criterion = "incremental"
      solver.rtol = 1e-8
      solver.atol = 1e-8
      solver.max it = 50
      solver.report = True
      # The Krylov solver parameters.
      ksp = solver.krylov solver
      opts = PETSc.Options()
      option prefix = ksp.getOptionsPrefix()
      opts[f"{option_prefix}ksp_type"] = "preonly" # "preonly" works equally well
      opts[f"{option_prefix}pc_type"] = "lu" # do not use 'gamg' pre-conditioner
      opts[f"{option_prefix}pc_factor_mat_solver_type"] = "mumps"
      opts[f"{option_prefix}ksp_max_it"] = 30
      ksp.setFromOptions()
```

12.3 Start calculation loop

```
[17]: # Variables for storing time history
totSteps = numSteps+1
timeHist0 = np.zeros(shape=[totSteps])
timeHist1 = np.zeros(shape=[totSteps])
timeHist2 = np.zeros(shape=[totSteps])

#Iinitialize a counter for reporting data
ii=0

# Write initial state to file
writeResults(t=0.0)
```

```
# Print out message for simulation start
print("----")
print("Simulation Start")
print("----")
# Store start time
startTime = datetime.now()
# Time-stepping solution procedure loop
while (round(t + dt, 9) <= Ttot):</pre>
   # increment time
   t += dt
   # increment counter
   ii += 1
   # update time variables in time-dependent BCs
   thetaCons.value = thetaRamp(t)
   # re-interpolate the applied twisting displacements
   u_top.interpolate(rot_expr)
   # Solve the problem
   try:
       (iter, converged) = solver.solve(w)
   except: # Break the loop if solver fails
       print("Ended Early")
       break
   # Collect results from MPI ghost processes
   w.x.scatter_forward()
   # Write output to file
   writeResults(t)
   # Update DOFs for next step
   w_old.x.array[:] = w.x.array
   # Print progress of calculation
   if ii%1 == 0:
       now = datetime.now()
       current time = now.strftime("%H:%M:%S")
       print("Step: {} | Increment: {}, Iterations: {}".\
             format(step, ii, iter))
       print("
                   Simulation Time: {} s of {} s".\
             format(round(t,4), Ttot))
       print()
```

```
# close the output file.
file_results.close()
# End analysis
print("----")
print("End computation")
# Report elapsed real time for the analysis
endTime = datetime.now()
elapseTime = endTime - startTime
print("----")
print("Elapsed real time: {}".format(elapseTime))
print("----")
-----
Simulation Start
_____
Step: Twist | Increment: 1, Iterations: 5
     Simulation Time: 0.02 s of 1 s
Step: Twist | Increment: 2, Iterations: 5
     Simulation Time: 0.04 s of 1 s
Step: Twist | Increment: 3, Iterations: 5
     Simulation Time: 0.06 s of 1 s
Step: Twist | Increment: 4, Iterations: 5
     Simulation Time: 0.08 s of 1 s
Step: Twist | Increment: 5, Iterations: 5
     Simulation Time: 0.1 s of 1 s
Step: Twist | Increment: 6, Iterations: 5
     Simulation Time: 0.12 s of 1 s
Step: Twist | Increment: 7, Iterations: 5
     Simulation Time: 0.14 s of 1 s
Step: Twist | Increment: 8, Iterations: 5
     Simulation Time: 0.16 s of 1 s
Step: Twist | Increment: 9, Iterations: 5
     Simulation Time: 0.18 s of 1 s
Step: Twist | Increment: 10, Iterations: 5
     Simulation Time: 0.2 s of 1 s
Step: Twist | Increment: 11, Iterations: 5
```

- Simulation Time: 0.22 s of 1 s
- Step: Twist | Increment: 12, Iterations: 5 Simulation Time: 0.24 s of 1 s
- Step: Twist | Increment: 13, Iterations: 5 Simulation Time: 0.26 s of 1 s
- Step: Twist | Increment: 14, Iterations: 5 Simulation Time: 0.28 s of 1 s
- Step: Twist | Increment: 15, Iterations: 5
 Simulation Time: 0.3 s of 1 s
- Step: Twist | Increment: 16, Iterations: 5 Simulation Time: 0.32 s of 1 s
- Step: Twist | Increment: 17, Iterations: 5 Simulation Time: 0.34 s of 1 s
- Step: Twist | Increment: 18, Iterations: 5 Simulation Time: 0.36 s of 1 s
- Step: Twist | Increment: 19, Iterations: 5
 Simulation Time: 0.38 s of 1 s
- Step: Twist | Increment: 20, Iterations: 5 Simulation Time: 0.4 s of 1 s
- Step: Twist | Increment: 21, Iterations: 5 Simulation Time: 0.42 s of 1 s
- Step: Twist | Increment: 22, Iterations: 5 Simulation Time: 0.44 s of 1 s
- Step: Twist | Increment: 23, Iterations: 5 Simulation Time: 0.46 s of 1 s
- Step: Twist | Increment: 24, Iterations: 5
 Simulation Time: 0.48 s of 1 s
- Step: Twist | Increment: 25, Iterations: 5
 Simulation Time: 0.5 s of 1 s
- Step: Twist | Increment: 26, Iterations: 5 Simulation Time: 0.52 s of 1 s
- Step: Twist | Increment: 27, Iterations: 5

- Simulation Time: 0.54 s of 1 s
- Step: Twist | Increment: 28, Iterations: 5 Simulation Time: 0.56 s of 1 s
- Step: Twist | Increment: 29, Iterations: 5 Simulation Time: 0.58 s of 1 s
- Step: Twist | Increment: 30, Iterations: 5 Simulation Time: 0.6 s of 1 s
- Step: Twist | Increment: 31, Iterations: 5 Simulation Time: 0.62 s of 1 s
- Step: Twist | Increment: 32, Iterations: 5 Simulation Time: 0.64 s of 1 s
- Step: Twist | Increment: 33, Iterations: 5 Simulation Time: 0.66 s of 1 s
- Step: Twist | Increment: 34, Iterations: 5 Simulation Time: 0.68 s of 1 s
- Step: Twist | Increment: 35, Iterations: 5 Simulation Time: 0.7 s of 1 s
- Step: Twist | Increment: 36, Iterations: 5 Simulation Time: 0.72 s of 1 s
- Step: Twist | Increment: 37, Iterations: 5
 Simulation Time: 0.74 s of 1 s
- Step: Twist | Increment: 38, Iterations: 5 Simulation Time: 0.76 s of 1 s
- Step: Twist | Increment: 39, Iterations: 5 Simulation Time: 0.78 s of 1 s
- Step: Twist | Increment: 40, Iterations: 5
 Simulation Time: 0.8 s of 1 s
- Step: Twist | Increment: 41, Iterations: 5
 Simulation Time: 0.82 s of 1 s
- Step: Twist | Increment: 42, Iterations: 5 Simulation Time: 0.84 s of 1 s
- Step: Twist | Increment: 43, Iterations: 5

Simulation Time: 0.86 s of 1 s Step: Twist | Increment: 44, Iterations: 5 Simulation Time: 0.88 s of 1 s Step: Twist | Increment: 45, Iterations: 5 Simulation Time: 0.9 s of 1 s Step: Twist | Increment: 46, Iterations: 5 Simulation Time: 0.92 s of 1 s Step: Twist | Increment: 47, Iterations: 5 Simulation Time: 0.94 s of 1 s Step: Twist | Increment: 48, Iterations: 5 Simulation Time: 0.96 s of 1 s Step: Twist | Increment: 49, Iterations: 5 Simulation Time: 0.98 s of 1 s Step: Twist | Increment: 50, Iterations: 5 Simulation Time: 1.0 s of 1 s End computation -----Elapsed real time: 0:13:45.385074

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