pHExploration

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```
## Joining, by = "Date"
## Joining, by = "Date"
```

Exploring pH

In order to understand the variable that I want to explore, I want to look at the distribution of pH along with any patterns it may follow over time.

```
## Warning: `legend.margin` must be specified using `margin()`. For the old
## behavior use legend.spacing
```

`stat_bin()` using `bins = 30`. Pick better value with `binwidth`.

Warning: Removed 48 rows containing non-finite values (stat_bin).

Distribution of pHMEAN 80 60 20 7.4 7.6 7.8 8.0 8.2 PHMEAN

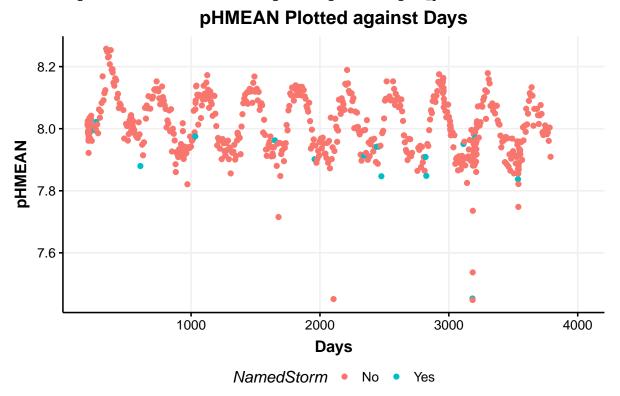
Min	Max	Mean	Median	Q1	Q3	Standard_Deviation	IQR
7.448	8.257	8.002	7.995	7.935	8.078	0.098	0.143

According to the histogram, pHMEAN appears to be bimodal and very slightly left-skewed. The average pH appears to be slightly basic, with a value of 8.002. The range of pH between the first and third quarters is

0.14. Additionally, on average, every value has about a 0.098 average distance from the mean.

```
## Warning: `legend.margin` must be specified using `margin()`. For the old
## behavior use legend.spacing
```

Warning: Removed 48 rows containing missing values (geom_point).



It is clear that the pH levels off of the coast vary throughout the year, with a higher pH in the colder months, and a lower pH value in the warmer months. Additionally, it looks as though the lowest value gets lower every year, but this will have to be examined in further detail. Values recorded during a named storm also appear to be on the smaller end, so correlations will be examined in greater detail.

```
## pHMEAN Date
## 1 7.448091 2018/09/20
```

The smallest pH value was recorded on 9/20/2018, which was about a week after Hurricane Florence hit North Carolina. Therefore, we will look into the influence of storms as well as how long these effects might last. However, is this because of the storm or just a coincidence because pH tends to lower in warmer seasons and storms happen more often in summer?

```
##
##
   Welch Two Sample t-test
##
## data: pHMEAN by NamedStorm
## t = 3.4617, df = 16.507, p-value = 0.003091
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
   0.04156864 0.17207792
## sample estimates:
##
   mean in group No mean in group Yes
##
            8.004825
                              7.898002
## Warning: Removed 48 rows containing non-finite values (stat_boxplot).
```

Recorded pH With and Without Storms

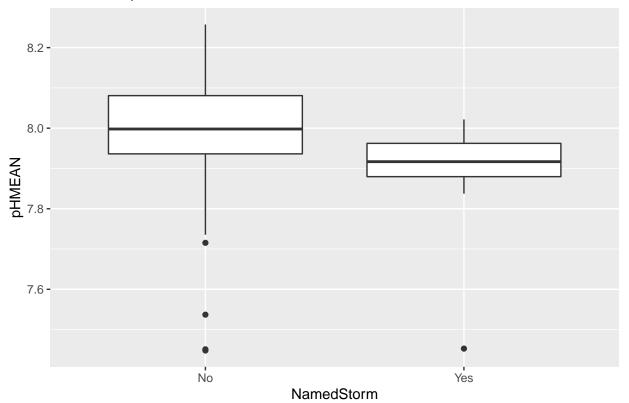
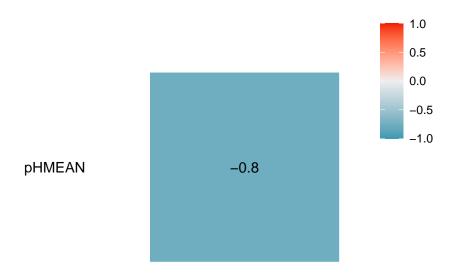


Table 2: Pairwise Wilcox Test

group1	group2	p.value
Yes	No	9e-05

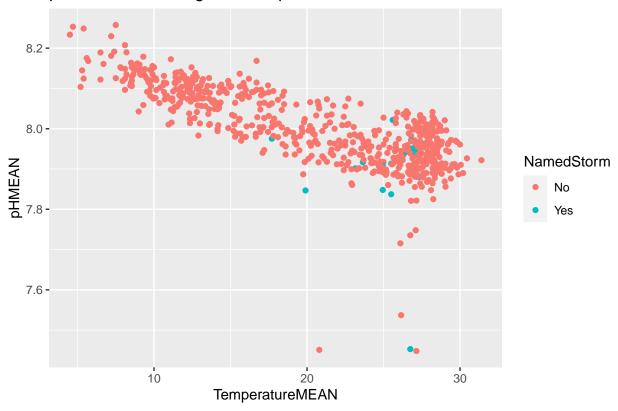
According to the boxplot and pairwise wilcox test, with a p-value of 0.00009, there is in fact a difference in the mean pH value between values recorded during a named storm and those recorded during typical weather.

TemperatureMEAN



Warning: Removed 48 rows containing missing values (geom_point).

pHMEAN Plotted against Temperature



There appears to be a somewhat negative linear relationship between temperature and pH, according to this plot. As the mean temperature increases, the mean pH decreases. This makes sense in the context of the data. Additionally, according to the correlation plot there is a relatively strong negative correlation between these two variables.

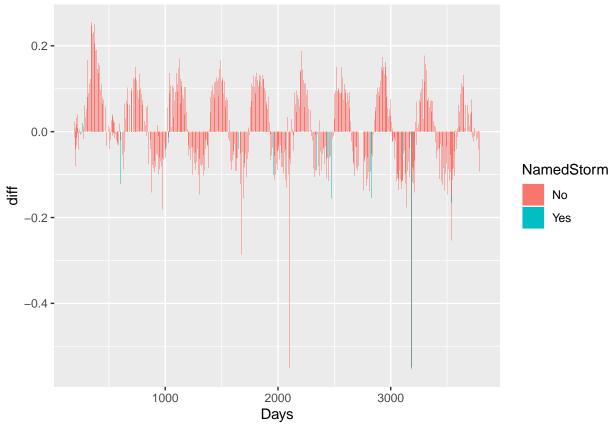
Table 3: Linear Model of pH and Temperature

term	estimate	std.error	statistic	p.value
(Intercept)	8.2140314	0.0076408	1075.01666	0
${\bf Temperature MEAN}$	-0.0104838	0.0003566	-29.40315	0

For every one degree increase in temperature, the pH is estimated to decrease by 0.0105 on average. The p-value is close to zero, meaning that there is a relationship between pH and temperature.

Warning: position_stack requires non-overlapping x intervals

Warning: position_stack requires non-overlapping x intervals



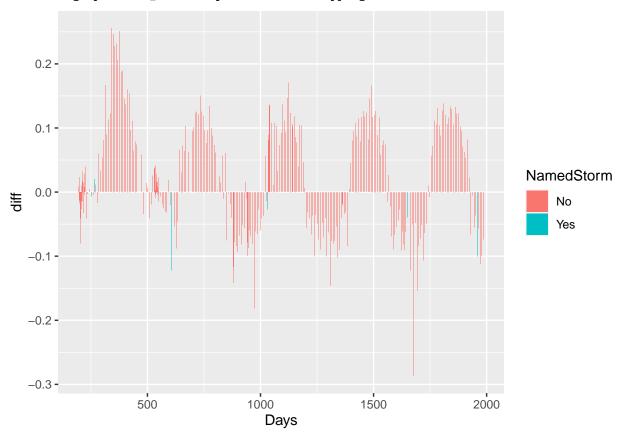
##		Date	pHMEAN	diff	NamedStorm
##	1	2010/12/08	8.257426	0.2554793	No
##	2	2010/12/15	8.248694	0.2467472	No
##	3	2010/12/22	8.229639	0.2276926	No
##	4	2010/12/29	8.233435	0.2314883	No
##	5	2011/01/05	8.207517	0.2055706	No
##	6	2011/01/12	8.253215	0.2512684	No
##	7	2011/01/19	8.189668	0.1877210	No
##	8	2011/01/26	8.191532	0.1895856	No
##	9	2011/01/27	8.180976	0.1790294	No
##	10	2016/01/20	8.189257	0.1873104	No
##	11	2019/01/16	8.178843	0.1768957	No
##		Date	pHMEAN	diff	NamedStorm
##	1	2012/08/29	7.820919	-0.1810281	No
##	2	2014/08/06	7.715420	-0.2865267	No
##	3	2014/08/20	7.847530	-0.1544166	No
##	4	2015/10/07	7.450993	-0.5509536	No
##	5	2016/10/12	7.846731	-0.1552157	Yes
##	6	2017/09/26	7.847970	-0.1539768	Yes
##	7	2018/08/08	7.825095	-0.1768513	No
##	8	2018/09/19	7.452792	-0.5491547	Yes
##	9	2018/09/20	7.448091	-0.5538559	No
##	10	2018/09/21	7.537025	-0.4649218	No
##	11	2018/09/22	7.735478	-0.2664689	No
##	12	2019/09/07	7.837277	-0.1646693	Yes
##	13	2019/09/10	7.748015	-0.2539317	No

14 2019/09/11 7.821565 -0.1803822

No

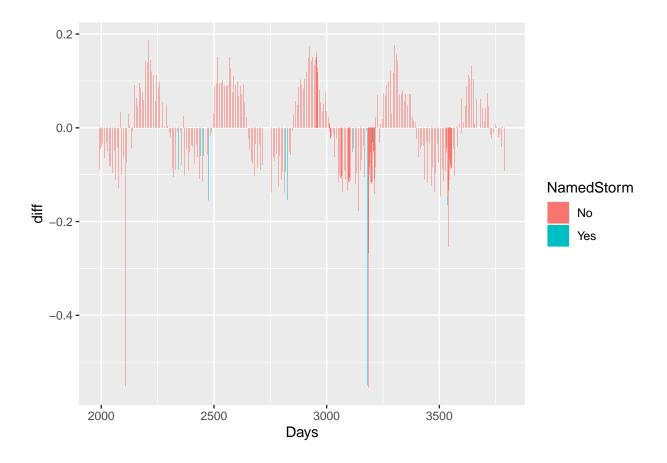
Warning: position_stack requires non-overlapping x intervals

Warning: position_stack requires non-overlapping x intervals



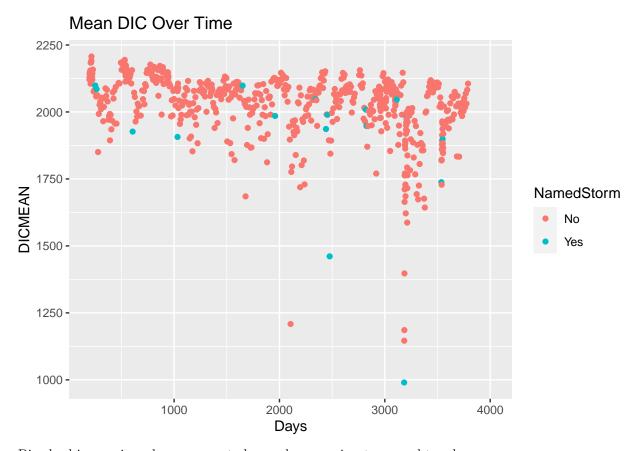
Warning: position_stack requires non-overlapping x intervals

Warning: position_stack requires non-overlapping x intervals



Dissolved Inorganic Carban

Warning: Removed 46 rows containing missing values (geom_point).

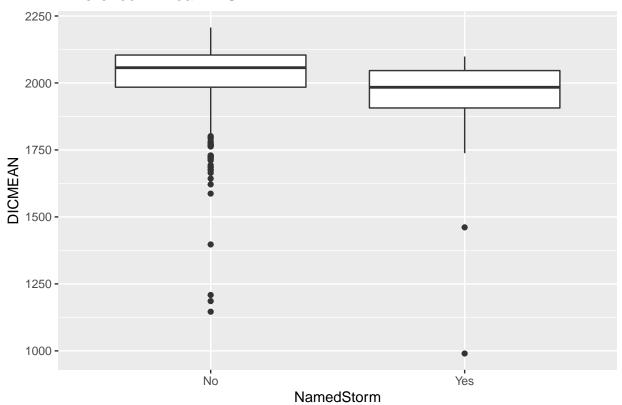


Dissolved inorganic carbon appears to have a less prominent seasonal trend

DICMEAN Date ## 1 990.2 2018/09/19

The smallest dissolved inorganic carbon recording occurred during Hurricane Florence

Difference in Mean DIC

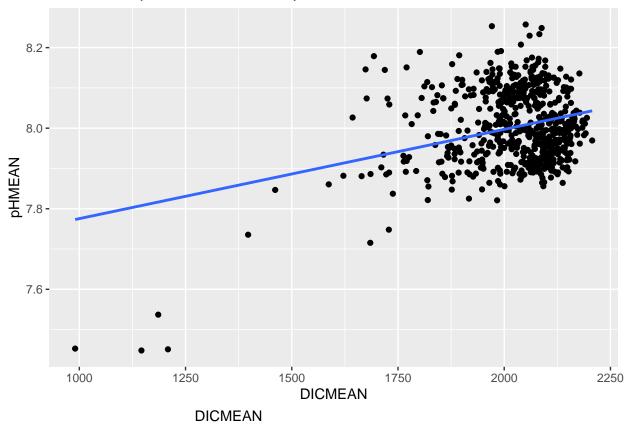


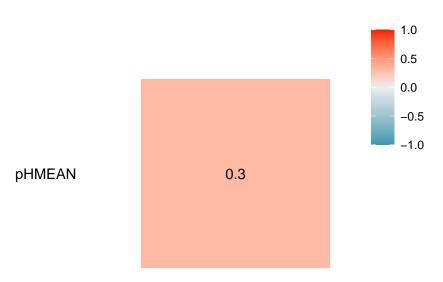
```
## # A tibble: 1 x 10
##
     estimate estimate1 estimate2 statistic p.value parameter conf.low conf.high
##
        <dbl>
                  <dbl>
                             <dbl>
                                       <dbl>
                                               <dbl>
                                                          <dbl>
                                                                   <dbl>
                                                                             <dbl>
                             1891.
                                        1.98 0.0646
                                                                   -9.16
## 1
         134.
                  2025.
                                                          16.2
                                                                              278.
## # ... with 2 more variables: method <chr>, alternative <chr>
```

While the boxplots show a difference in means between storms, the p-value is not significant, indicating that there is not a difference in the mean DIC when there is a storm.

```
## `geom_smooth()` using formula 'y ~ x'
## Warning: Removed 48 rows containing non-finite values (stat_smooth).
## Warning: Removed 48 rows containing missing values (geom_point).
```

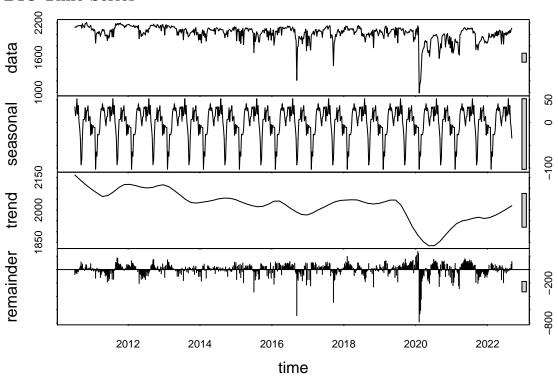
Relationship between DIC and pH





There appears to be a slight positive correlation between the two variables





Trend Mapping onto Data 2000 - 1750 - 1250 - 1000 - 1000 - 2000 3000 Days

Seasonal Cycle Mappping onto C

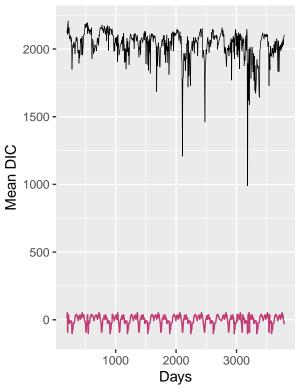
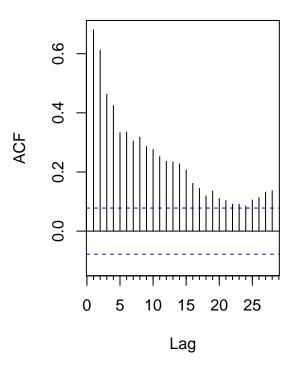


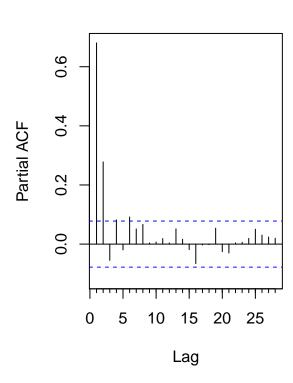
Table 4: Seasonal Mann Kendall test for pH

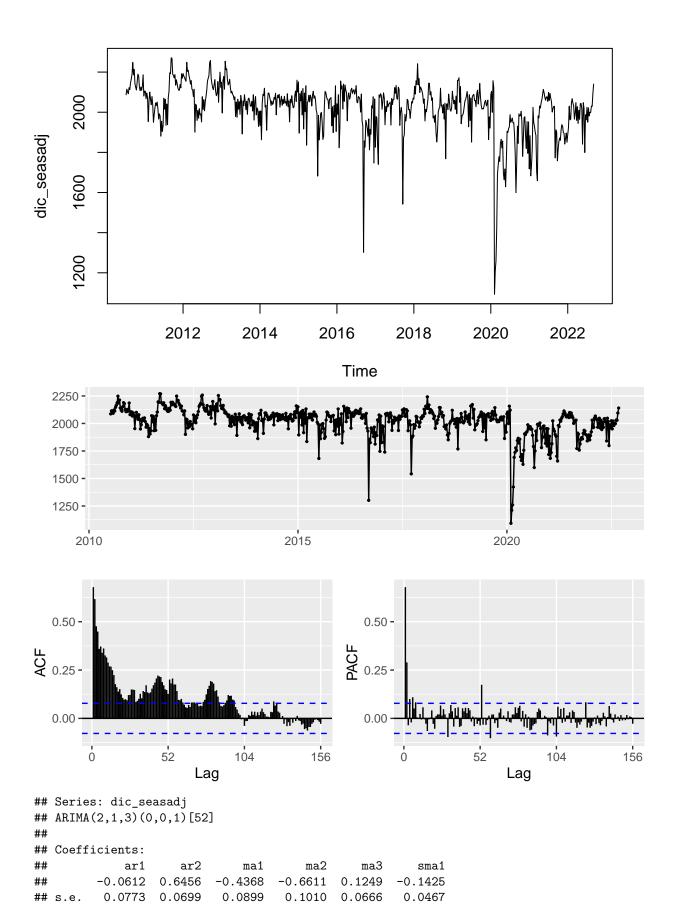
p.value	kendall_score	statistic
0	-1174	-0.3316384

```
##
## Seasonal Mann-Kendall trend test (Hirsch-Slack test)
##
## data: dic.ts
## z = -10.909, p-value < 2.2e-16
## alternative hypothesis: true S is not equal to 0
## sample estimates:
## S varS
## -1174.00 11562.67</pre>
```

Series full_DICMEAN\$DICMEAN Series full_DICMEAN\$DICMEAN

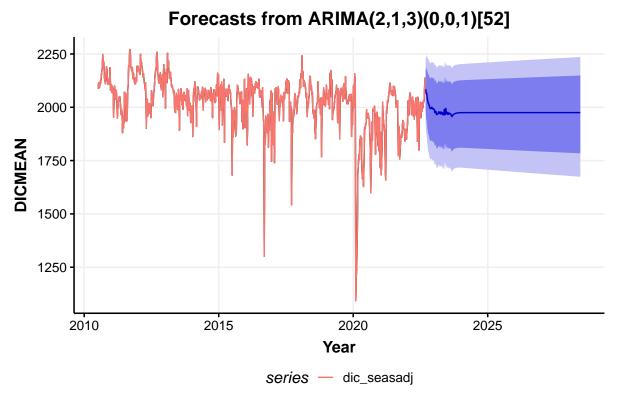






```
##
## sigma^2 estimated as 7796: log likelihood=-3726.95
## AIC=7467.89
                AICc=7468.07
                                BIC=7499.03
## Series: dic_seasadj
## ARIMA(2,1,3)(0,0,1)[52]
## Box Cox transformation: lambda= 1.999924
##
## Coefficients:
##
             ar1
                      ar2
                               ma1
                                        ma2
                                                 ma3
                                                          sma1
         -0.0365
                  0.6653
                           -0.4766
                                    -0.6420
                                                      -0.1291
##
                                             0.1426
          0.0716 0.0653
                            0.0852
## s.e.
                                     0.0961
                                             0.0651
                                                       0.0465
##
## sigma^2 estimated as 2.645e+10: log likelihood=-8478.62
## AIC=16971.24
                  AICc=16971.42
                                   BIC=17002.38
           Residuals from ARIMA(2,1,3)(0,0,1)[52]
    500000 -
         0 -
   -500000 -
  -1000000 -
  -1500000 -
          2010
                                        2015
                                                                      2020
   0.10 -
                                                  80 -
   0.05
                                                 60 -
                                               count
   0.00
                                                 40 -
  -0.05
                                                 20 -
  -0.10 -
                                                                    ò
                              104
                    <u>5</u>2
                                         156
                                                    -1500000-1000000 -500000
                                                                                      500000
                                                                    residuals
                        Lag
##
##
    Ljung-Box test
##
## data: Residuals from ARIMA(2,1,3)(0,0,1)[52]
## Q* = 7.195, df = 6, p-value = 0.3032
##
## Model df: 6.
                  Total lags used: 12
## [1] 16971.42
## Warning: `legend.margin` must be specified using `margin()`. For the old
```

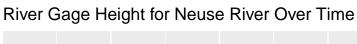
behavior use legend.spacing

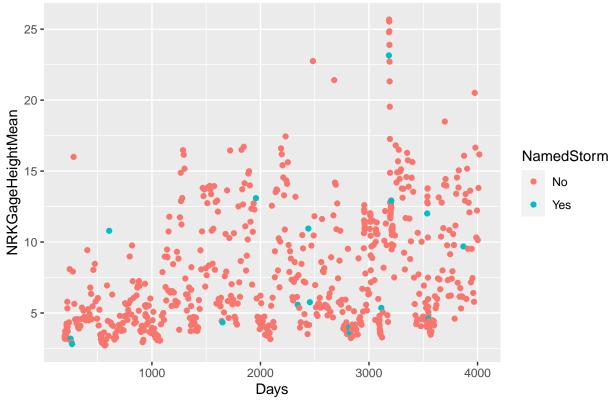


This model appears to forecast a slight decrease in dissolved inorganic carbon

River Gage

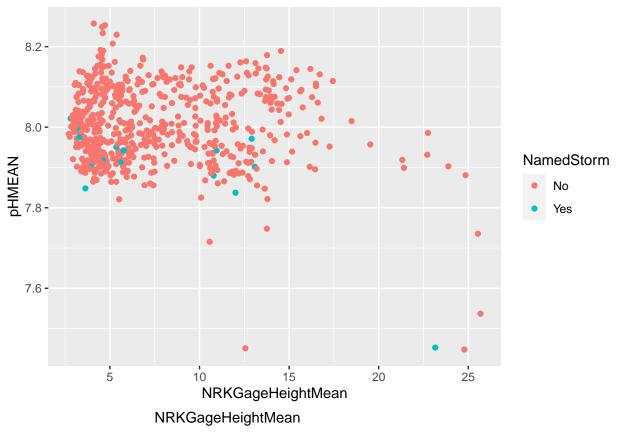
Warning: Removed 4 rows containing missing values (geom_point).

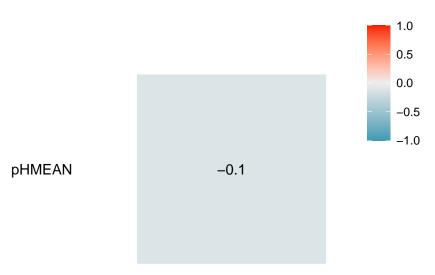




Warning: Removed 52 rows containing missing values (geom_point).



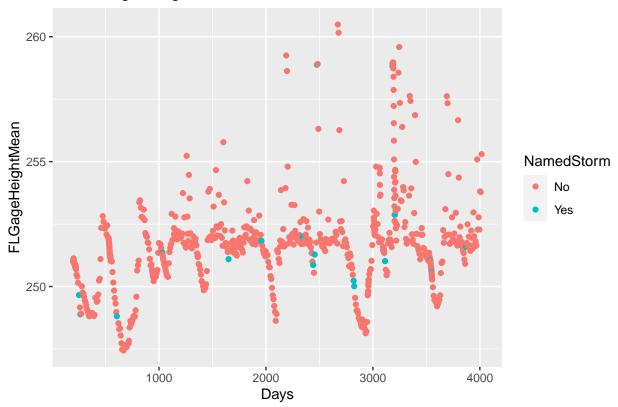




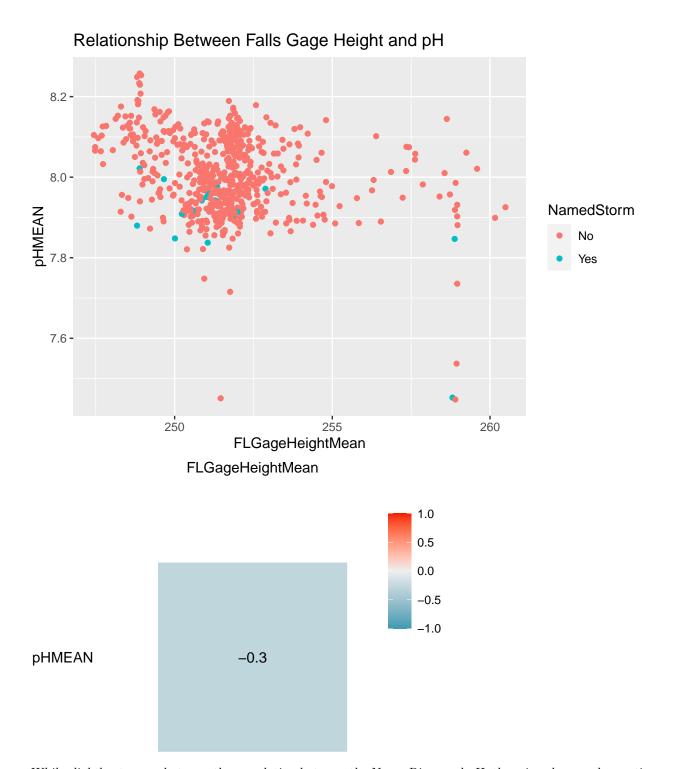
There is only a very weak negative correlation between the Neuse River gage height at Kinston, NC and the pH recorded off of Pivers Island.

Warning: Removed 3 rows containing missing values (geom_point).

River Gage Height for Falls Lake Over Time



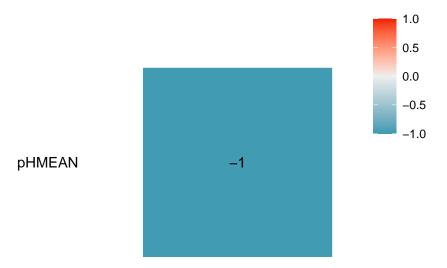
Warning: Removed 51 rows containing missing values (geom_point).



While slightly stronger between the correlation between the Neuse River and pH, there is only a weak negative correlation between the Falls Lake gage height and the pH recorded off of Pivers Island.

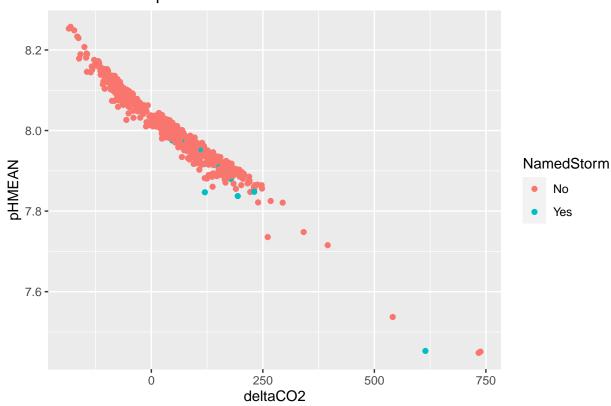
Additional Variables

deltaCO2



Warning: Removed 48 rows containing missing values (geom_point).

DeltaCO2 vs. pHMEAN



There appears to be a negative linear relationship between water-atmospheric carbon dioxide and pH. As the water-atmospheric CO2 increases, the pH decreases. Additionally, there appear to be more named storms recorded at higher values of water-atmospheric CO2 increases. According to the correlation plot, there is a strong negative correlation between these two variables.

Table 5: Linear Model of pH and DeltaCO2

term	estimate	std.error	statistic	p.value
(Intercept)	8.0413128	0.0007747	10379.7161	0
deltaCO2	-0.0008537	0.0000064	-133.6373	0

For every 100 µatm increase in water-atmospheric carbon dioxide, the pH is estimated to decrease by 0.0854 on average. The p-value is close to zero, meaning there is a relationship between the two variables.

deltaCO2 Date ## 1 737.8547 2015/10/07

The largest value for deltaCO2 occurs on a day when the second smallest pH is recorded.

Warning: Removed 48 rows containing non-finite values (stat_boxplot).

Mean DeltaCO2 for Storms and Days without Storms

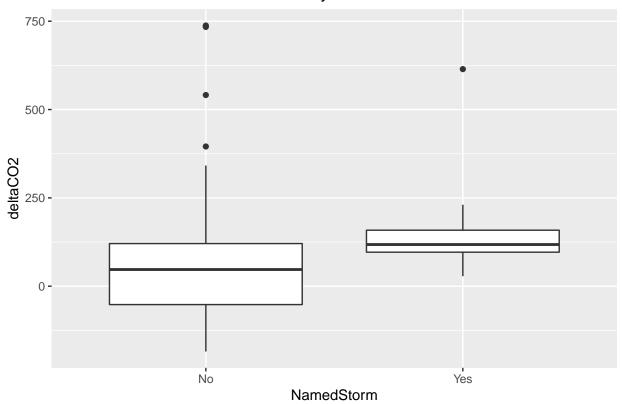
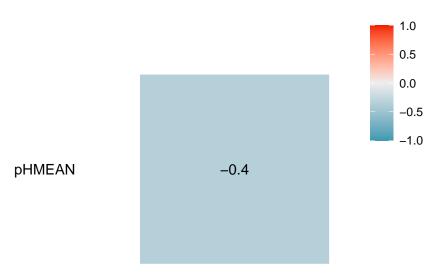


Table 6: Pairwise Wilcox Test

group1	group2	p.value
Yes	No	0.0005083

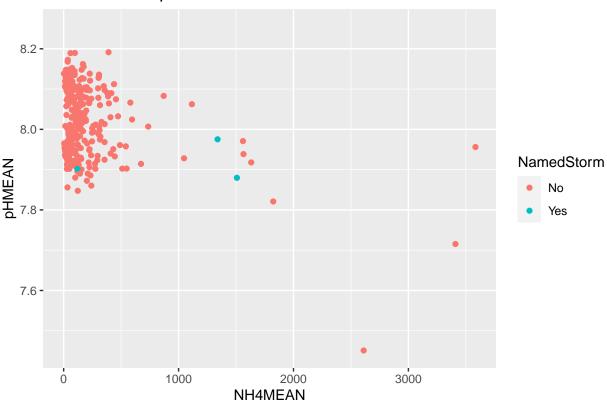
After examining the boxplot and administering a pairwise wilcox test, with a p-value of 0.0005, it is apparent that there is a difference in the mean water-atmospheric carbon dioxide for days with named stroms and days with typical weather.

NH4MEAN



Warning: Removed 382 rows containing missing values (geom_point).

NH4MEAN vs. pHMEAN



There does not appear to be a strong relationship between NH4 and pH. The correlation plot also displays a weak correlation between the two variables.

Table 7: Linear Model of pH and NH4

term	estimate	std.error	statistic	p.value
(Intercept)	8.0343996	0.0055237	1454.545014	0
NH4MEAN	-0.0000796	0.0000123	-6.454661	0

For every one nM increase in NH4, the pH decreases by -0.00008. While the small p-value suggests a relationship between the two variables, this may be a result of the influence from the outliers.

Warning: Removed 381 rows containing non-finite values (stat_boxplot).

Mean NH4MEAN For Storms and Days without Storms

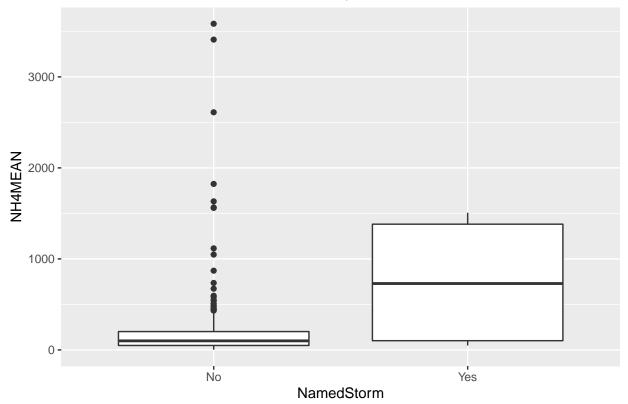


Table 8: Pairwise Wilcox Test

group1	group2	p.value
Yes	No	0.1976984

According to the boxplot there looks like there is a difference in the mean NH4 for days with a named storm, however, the pairwise wilcox test fails to reject the hypothesis that there is no difference in means.

Multiple Linear Regression

In this linear model, I will include the temperature, named storm indicator, water-atmospheric carbon dioxide, and NH4 because each variable appears to have a relationship with pH. I will also include an interaction term between the storm indicator and each of the numeric variables because there is a difference in means for values recorded during a storm.

Table 9: Multiple Linear Regression Model for pH

term	estimate	std.error	statistic	p.value
(Intercept)	8.0414305	0.0034884	2305.1744161	0.0000000
NamedStormYes	-0.0482955	0.0466487	-1.0353009	0.3013939
TemperatureMEAN	0.0002437	0.0001839	1.3253833	0.1860908
deltaCO2	-0.0008351	0.0000128	-65.3884154	0.0000000
NH4MEAN	-0.0000023	0.0000021	-1.0490303	0.2950407
NamedStormYes:TemperatureMEAN	0.0017248	0.0022417	0.7694073	0.4422800
NamedStormYes:deltaCO2	-0.0000229	0.0001669	-0.1370037	0.8911233
NamedStormYes:NH4MEAN	-0.0000070	0.0000104	-0.6755170	0.4998875

Several variables have insignificant p-values in this model, so I will perform backwards selection in order to ensure that I get the most accurate results. This test will eliminate any unnecessary predictors, which is important as any model can get a high r-squared value with a lot of variables, even if many are not considered significant.

Table 10: Reduced Model through backward Selection

term	estimate	std.error	statistic	p.value
(Intercept)	8.0397817	0.0032301	2488.996526	0.0000000
NamedStormYes	-0.0160253	0.0064739	-2.475359	0.0138757
TemperatureMEAN	0.0003153	0.0001755	1.796980	0.0733685
deltaCO2	-0.0008414	0.0000115	-72.866298	0.0000000

The reduced model only includes the named storm indicator, temperature, and water-atmospheric carbon dioxide. While temperature does not have a significant p-value, I will leave it in the model for the moment because of the results from exploratory data analysis. However, this may need to be investigated further.

Table 11: Model Selection Criteria for Full Model

Adjusted R Squared	AIC	BIC
0.9797	-1735.585	-1702.341

Table 12: Model Selection Criteria for Reduced Model

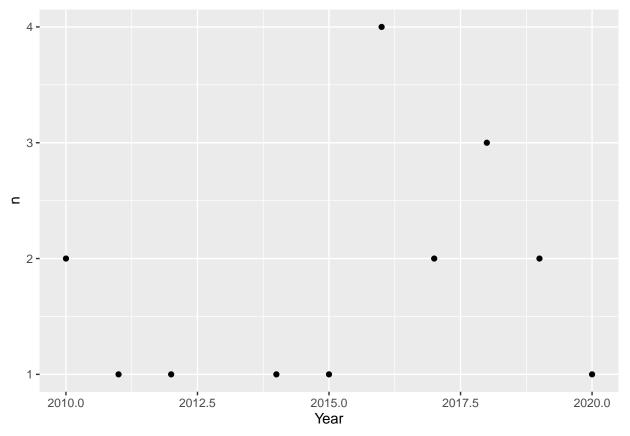
Adjusted R Squared	AIC	BIC
0.9798	-1739.935	-1721.466

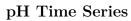
The adjusted r-squared, AIC, and BIC values are similar for the full and reduced models. However, the reduced model has a slightly higher adjusted r-squared and lower AIC and BIC values, so I will choose this as the most accurate.

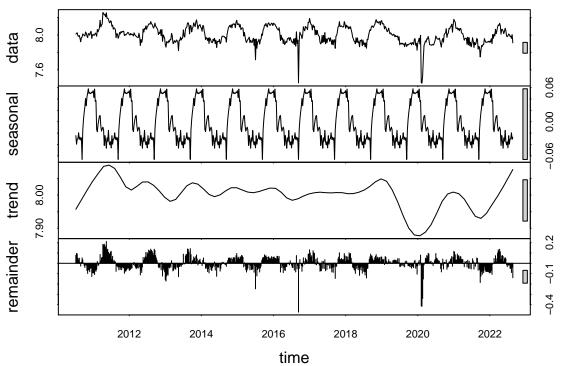
Checking Storm Frequency

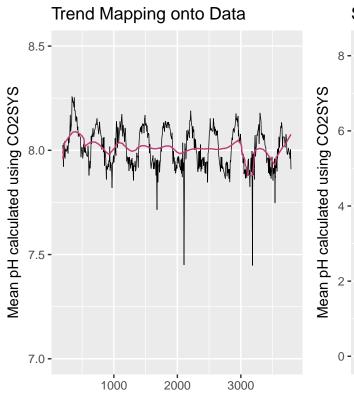
A tibble: 21 x 3
Groups: Year [11]
Year NamedStorm n

```
<dbl> <fct> <int>
##
  1 2010 No
##
                      41
   2 2010 Yes
                      2
##
##
   3 2011 No
                      65
   4 2011 Yes
##
                       1
##
  5 2012 No
                       68
  6 2012 Yes
                      1
  7 2013 No
                      58
##
## 8 2014 No
                       52
## 9 2014 Yes
                      1
## 10 2015 No
## # ... with 11 more rows
```









Days

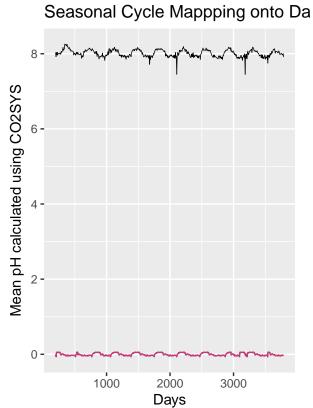


Table 13: Seasonal Mann Kendall test for pH

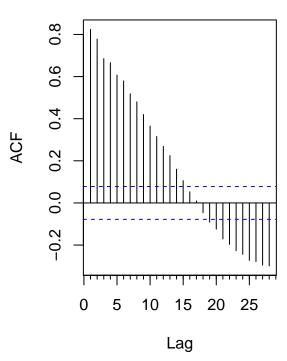
p.value	kendall_score	statistic
0.0021753	-328	-0.0932878

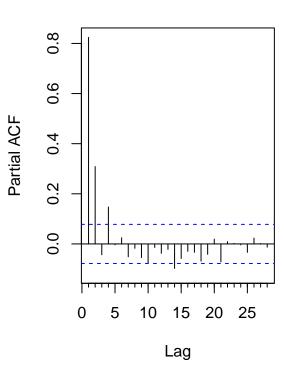
```
##
## Seasonal Mann-Kendall trend test (Hirsch-Slack test)
##
## data: pico1.ts
## z = -3.0559, p-value = 0.002244
## alternative hypothesis: true S is not equal to 0
## sample estimates:
## S varS
## -328.00 11450.67
```

p-value is less than 0.05, so we can reject the null hypothesis – There is a possible trend in the data

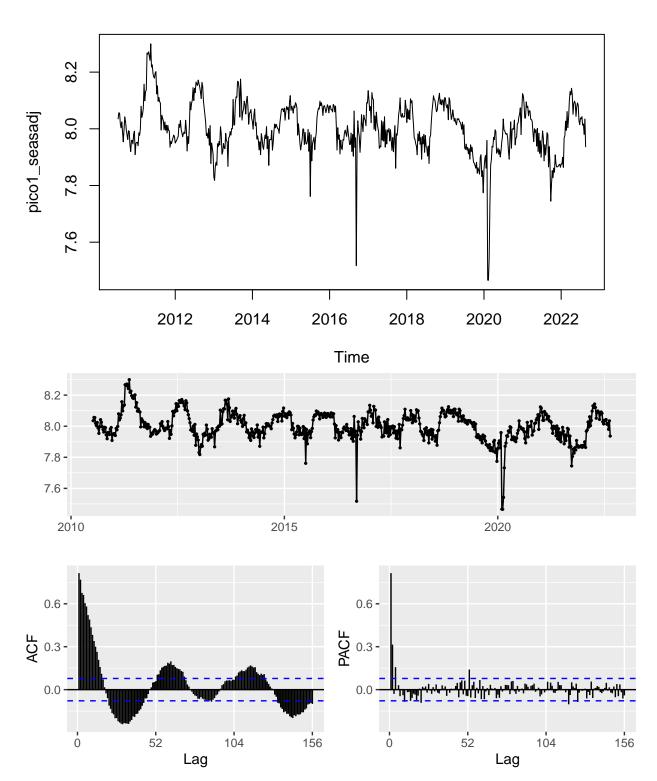
Series full_pHMEAN\$pHMEAN

Series full_pHMEAN\$pHMEAN





```
## Series: pico1.ts
## ARIMA(1,1,3)
##
  Coefficients:
##
                     ma1
                               ma2
                                        ma3
         -0.7071
                  0.3294
                          -0.2159
                                    -0.1328
##
##
          0.1300
                  0.1343
                            0.0685
                                     0.0410
## sigma^2 estimated as 0.002793: log likelihood=960.33
## AIC=-1910.66
                 AICc=-1910.57
                                   BIC=-1888.43
```



Test for Stationarity:

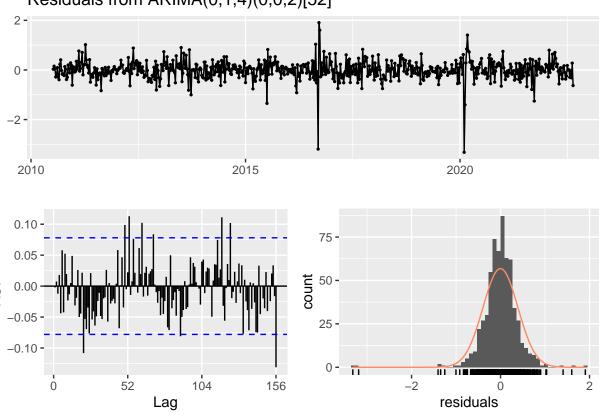
Warning in adf.test(pico1_seasadj): p-value smaller than printed p-value

##
Augmented Dickey-Fuller Test
##

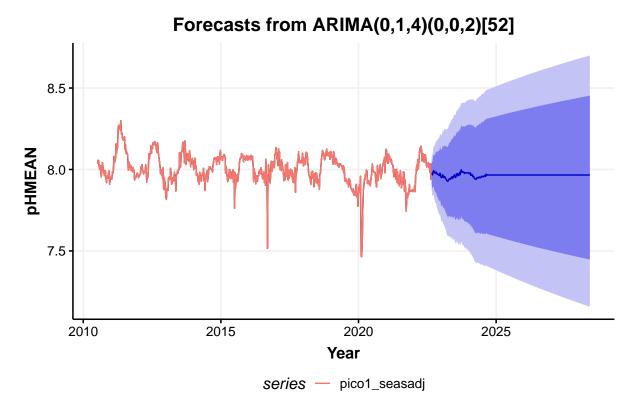
data: pico1_seasadj

```
## Dickey-Fuller = -4.7127, Lag order = 8, p-value = 0.01
## alternative hypothesis: stationary
## Warning in kpss.test(pico1_seasadj): p-value smaller than printed p-value
##
##
   KPSS Test for Level Stationarity
##
## data: pico1_seasadj
## KPSS Level = 0.85542, Truncation lag parameter = 6, p-value = 0.01
Conflicting conclusions for the two tests, so I will first-difference the time series to see if that will create
stationarity
## Warning in adf.test(pico1_seasadj_diff): p-value smaller than printed p-value
##
##
    Augmented Dickey-Fuller Test
## data: pico1_seasadj_diff
## Dickey-Fuller = -8.8457, Lag order = 8, p-value = 0.01
## alternative hypothesis: stationary
## Warning in kpss.test(pico1_seasadj_diff): p-value greater than printed p-value
##
##
   KPSS Test for Level Stationarity
##
## data: pico1_seasadj_diff
## KPSS Level = 0.011185, Truncation lag parameter = 6, p-value = 0.1
Because the p-value for the KPSS is larger than an alpha value of 0.05, the null hypothesis cannot be rejected.
However, we can reject the null hypothesis for the ADF test. Therefore, it can now be concluded that the
time series is stationary.
## Series: pico1_seasadj
## ARIMA(0,1,4)(0,0,2)[52]
##
## Coefficients:
##
             ma1
                     ma2
                               ma3
                                       ma4
                                                sma1
                                                          sma2
                                                      -0.1442
         -0.3853 0.0486
                          -0.1800 0.0887
##
                                             -0.1576
## s.e.
          0.0403 0.0426
                            0.0397 0.0377
                                              0.0499
##
## sigma^2 estimated as 0.002499: log likelihood=994.37
## AIC=-1974.74
                                   BIC=-1943.62
                  AICc=-1974.56
## Series: pico1_seasadj
## ARIMA(0,1,4)(0,0,2)[52]
## Box Cox transformation: lambda= 1.999924
## Coefficients:
##
                     ma2
                               ma3
                                                sma1
                                                          sma2
             ma1
                                        ma4
##
         -0.3857 0.0518 -0.1778 0.0930
                                             -0.1588
                                                      -0.1468
## s.e.
         0.0403 0.0426
                           0.0398 0.0377
                                              0.0503
                                                       0.0585
## sigma^2 estimated as 0.1555: log likelihood=-306.76
## AIC=627.53
               AICc=627.71
                               BIC=658.65
```

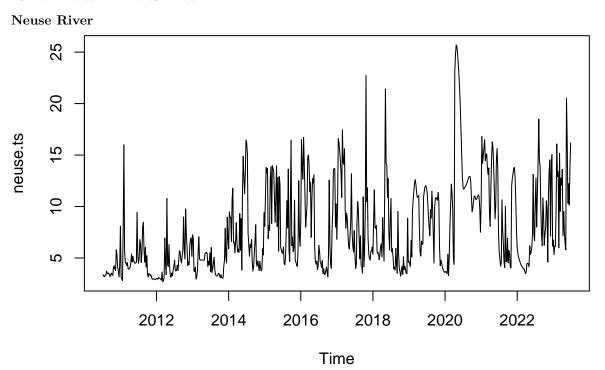
Residuals from ARIMA(0,1,4)(0,0,2)[52]

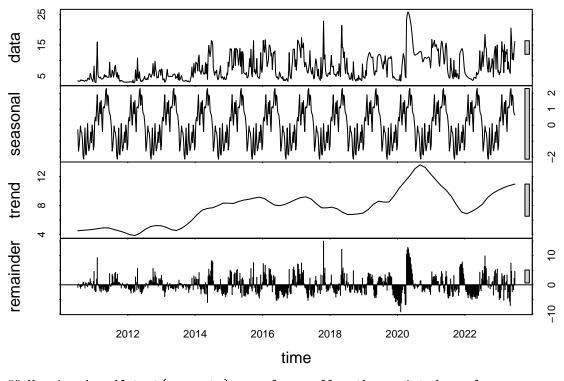


```
##
## Ljung-Box test
##
## data: Residuals from ARIMA(0,1,4)(0,0,2)[52]
## Q* = 7.3346, df = 6, p-value = 0.291
##
## Model df: 6. Total lags used: 12
## [1] 627.7082
## Warning: `legend.margin` must be specified using `margin()`. For the old
## behavior use legend.spacing
```



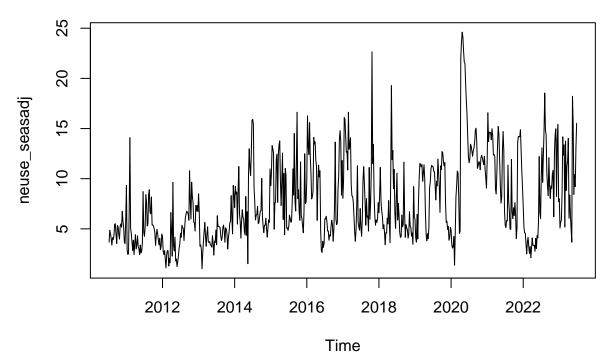
River Data Time Series



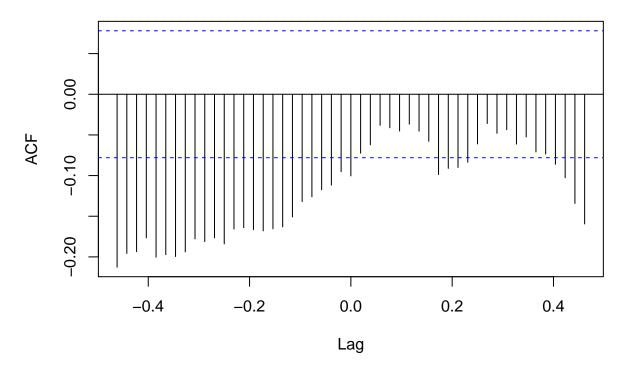


```
## Warning in adf.test(neuse.ts): p-value smaller than printed p-value
##
## Augmented Dickey-Fuller Test
##
## data: neuse.ts
## Dickey-Fuller = -6.1267, Lag order = 8, p-value = 0.01
## alternative hypothesis: stationary
## Warning in kpss.test(neuse.ts): p-value smaller than printed p-value
##
## KPSS Test for Level Stationarity
##
## data: neuse.ts
## KPSS Level = 2.6583, Truncation lag parameter = 6, p-value = 0.01
```

Neuse River gage height is stationary. However, it appears as though there may be seasonality, so I will remove that before looking at the correlation.



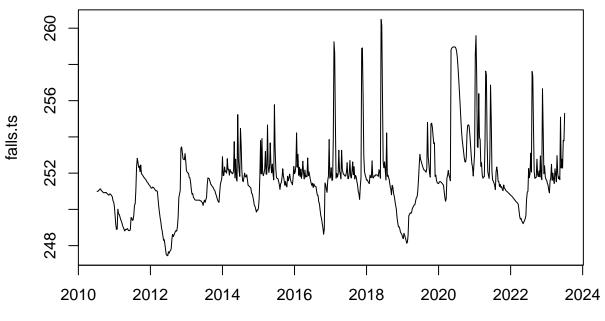
neuse_seasadj & pico1_seasadj

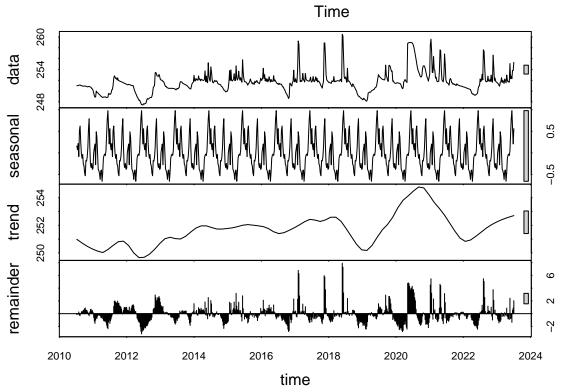


```
##
## Autocorrelations of series 'X', by lag
##
##
  -0.4615 -0.4423 -0.4231 -0.4038 -0.3846 -0.3654 -0.3462 -0.3269 -0.3077 -0.2885
   -0.213 -0.196 -0.194
                          -0.177
                                  -0.200
                                          -0.197
                                                  -0.200
                                                           -0.194
                                                                   -0.178
## -0.2692 -0.2500 -0.2308 -0.2115 -0.1923 -0.1731 -0.1538 -0.1346 -0.1154 -0.0962
                                           -0.168
   -0.177
           -0.184 -0.166 -0.164
                                   -0.166
                                                   -0.165
                                                           -0.163
                                                                   -0.151
                                                                          -0.132
## -0.0769 -0.0577 -0.0385 -0.0192 0.0000
                                           0.0192 0.0385
                                                           0.0577
                                                                   0.0769 0.0962
```

```
-0.126
            -0.117
                    -0.112
                            -0.095
                                     -0.100 -0.072
                                                     -0.062
                                                              -0.038
                                                                      -0.041
                                                                               -0.045
            0.1346
                    0.1538
                             0.1731
                                     0.1923
                                             0.2115
                                                      0.2308
                                                              0.2500
                                                                      0.2692
                                                                              0.2885
##
    0.1154
    -0.037
            -0.045
                    -0.058
                             -0.099
                                     -0.091
                                             -0.090
                                                      -0.084
                                                              -0.061
                                                                      -0.036
                                                                              -0.048
    0.3077
            0.3269
                    0.3462
                            0.3654
                                     0.3846
                                             0.4038
                                                      0.4231
                                                              0.4423
                                                                      0.4615
##
    -0.044
            -0.061
                    -0.052
                             -0.071
                                     -0.074
                                             -0.086
                                                      -0.103
                                                              -0.134
                                                                      -0.160
```

Falls Lake

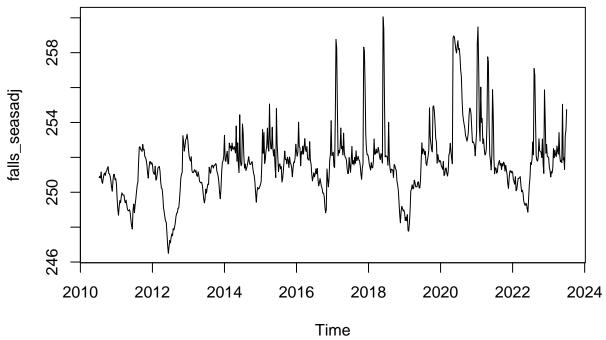




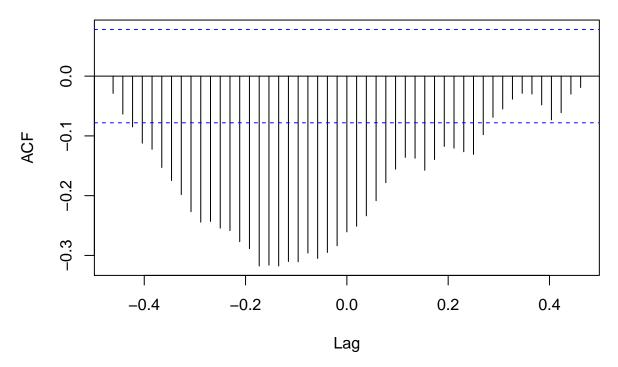
Phillips-Perron Unit Root Test

##

```
##
## data: falls.ts
## Dickey-Fuller = -7.1968, Truncation lag parameter = 6, p-value = 0.01
## Warning in kpss.test(falls.ts): p-value smaller than printed p-value
##
## KPSS Test for Level Stationarity
##
## data: falls.ts
## KPSS Level = 1.6263, Truncation lag parameter = 6, p-value = 0.01
```



falls_seasadj & pico1_seasadj



```
##
## Autocorrelations of series 'X', by lag
##
## -0.4615 -0.4423 -0.4231 -0.4038 -0.3846 -0.3654 -0.3462 -0.3269 -0.3077 -0.2885
    -0.029
           -0.064 -0.085
                           -0.112
                                   -0.122
                                            -0.153
                                                    -0.175
                                                            -0.198
                                                                    -0.227
##
                                                                            -0.244
  -0.2692 -0.2500 -0.2308 -0.2115 -0.1923 -0.1731 -0.1538 -0.1346 -0.1154 -0.0962
           -0.254 -0.258
                           -0.277
                                    -0.289
                                            -0.318
                                                    -0.316
                                                                    -0.310
    -0.243
                                                            -0.318
## -0.0769 -0.0577 -0.0385 -0.0192
                                    0.0000
                                            0.0192
                                                    0.0385
                                                            0.0577
                                                                    0.0769
                                                                             0.0962
                                            -0.251
                            -0.284
                                                    -0.234
##
    -0.296
           -0.305
                   -0.295
                                    -0.261
                                                            -0.208
                                                                    -0.178
                                                                             -0.156
    0.1154
           0.1346
                    0.1538
                            0.1731
                                    0.1923
                                            0.2115
                                                    0.2308
                                                            0.2500
                                                                    0.2692
                                                                            0.2885
##
    -0.136
            -0.137
                    -0.157
                            -0.139
                                    -0.118
                                            -0.121
                                                    -0.126
                                                            -0.131
                                                                    -0.098
                                                                            -0.069
            0.3269
                            0.3654
                                    0.3846
                                                    0.4231
    0.3077
                    0.3462
                                            0.4038
                                                            0.4423
                                                                     0.4615
           -0.039
                   -0.029
                           -0.030
                                    -0.048
                                                    -0.061
    -0.055
                                            -0.073
                                                            -0.030
                                                                    -0.019
```